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# **AuE 8930: Machine Perception and Intelligence**

## **Lecture: Signal, spectrum, and vehicle sensors**

**Instructor: Bing Li, Ph.D.**  
**bli4@clemson.edu**

Assistant Professor  
Department of Automotive Engineering  
Clemson University International Center for  
Automotive Research (CU-ICAR)



# Outline

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- Introduction
- Signal and Sensor Perception
- 1D Signal and A/D
- 1D Signal Time-domain Analysis
- 1D Signal Frequency Analysis
- 1D Signal Noise Analysis
- 1D Signal Processing and Filter Design
- Electromagnetic Spectrum
- Vehicle Sensors (Perception)



# 1D Signal: Wave

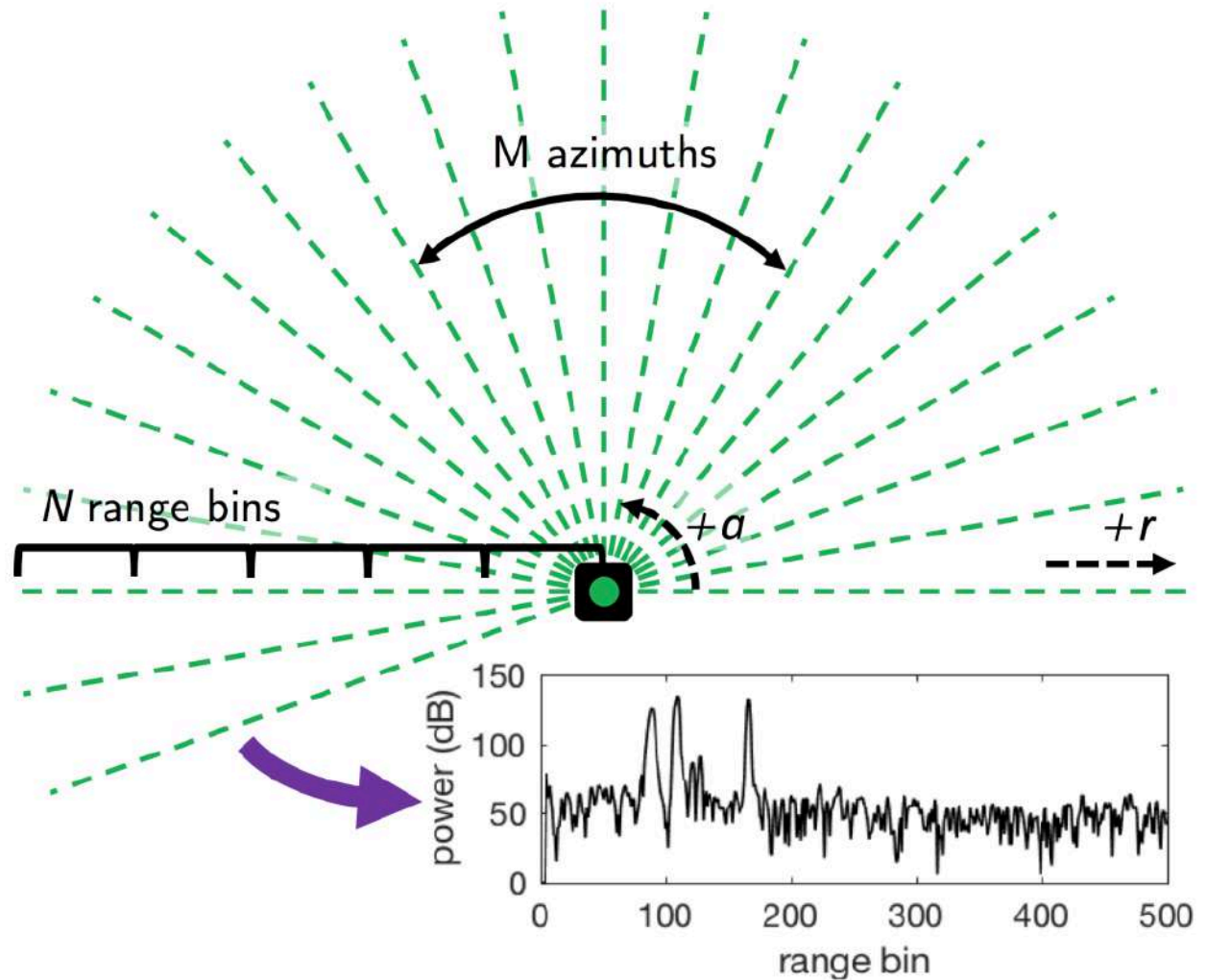
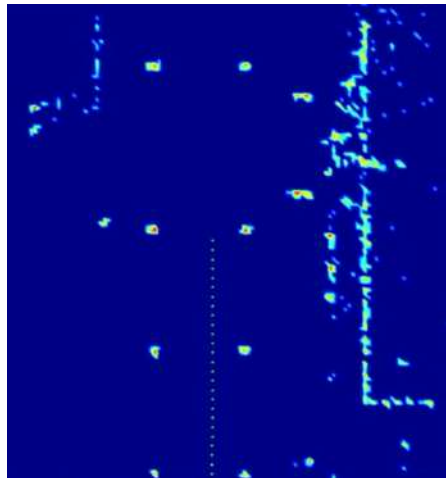
Time domain

Frequency domain

Noise filter

Patterns

...





# 2D Signal: Image

Time domain

Frequency domain

Noise filter

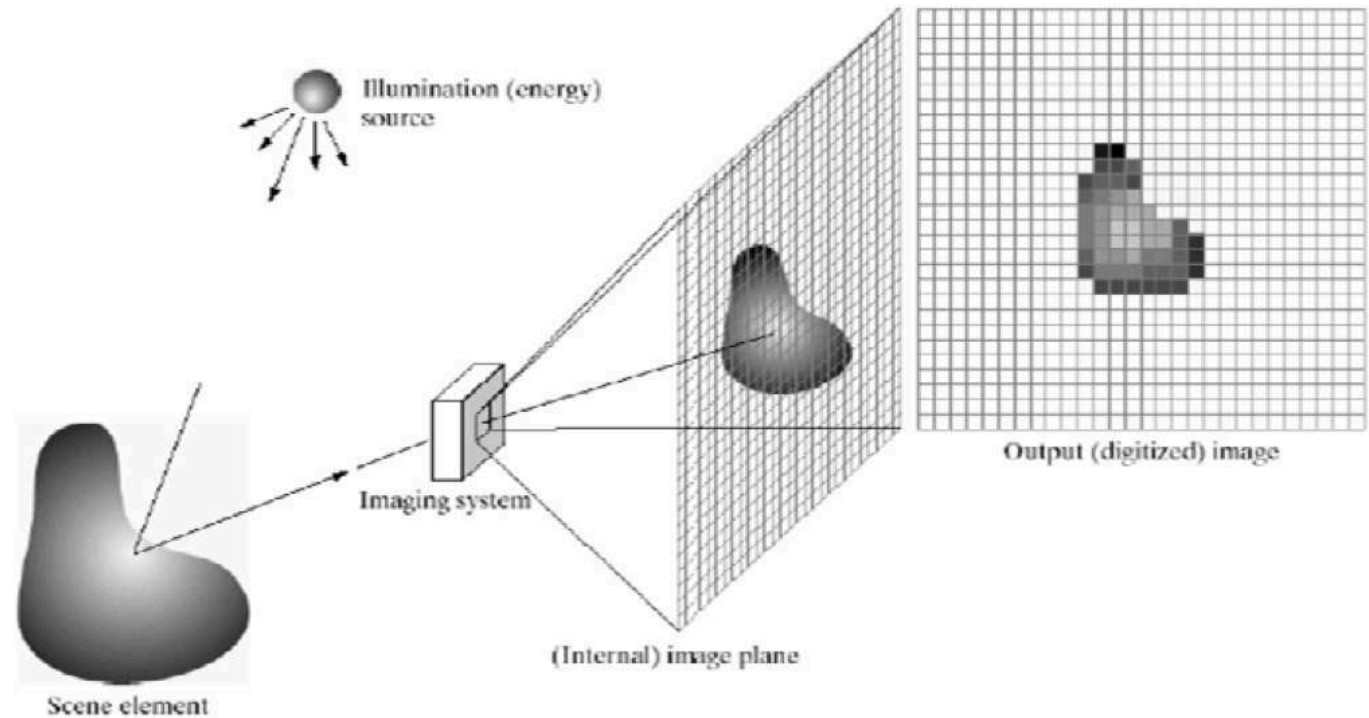
Multi-view

Features

Patterns

Understanding

...





# 3D Signal: Point Cloud

Time domain

Frequency domain

Noise filter

Geometry analysis, mapping

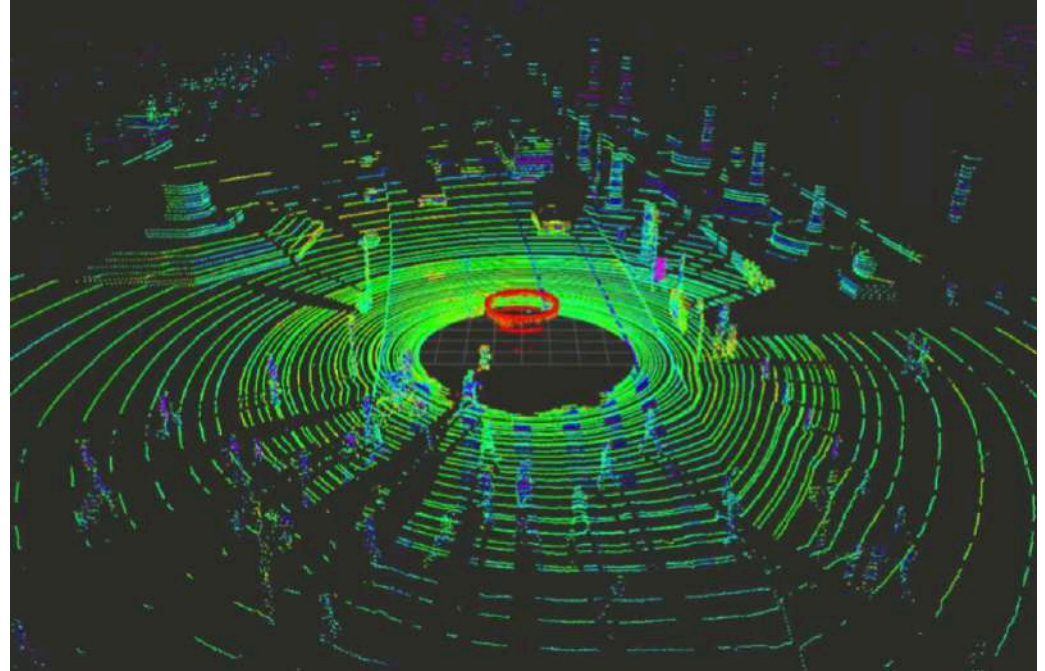
Features

Patterns

Understanding

...

Fuse with 2D vision



# Signal and Sensor Data Analysis

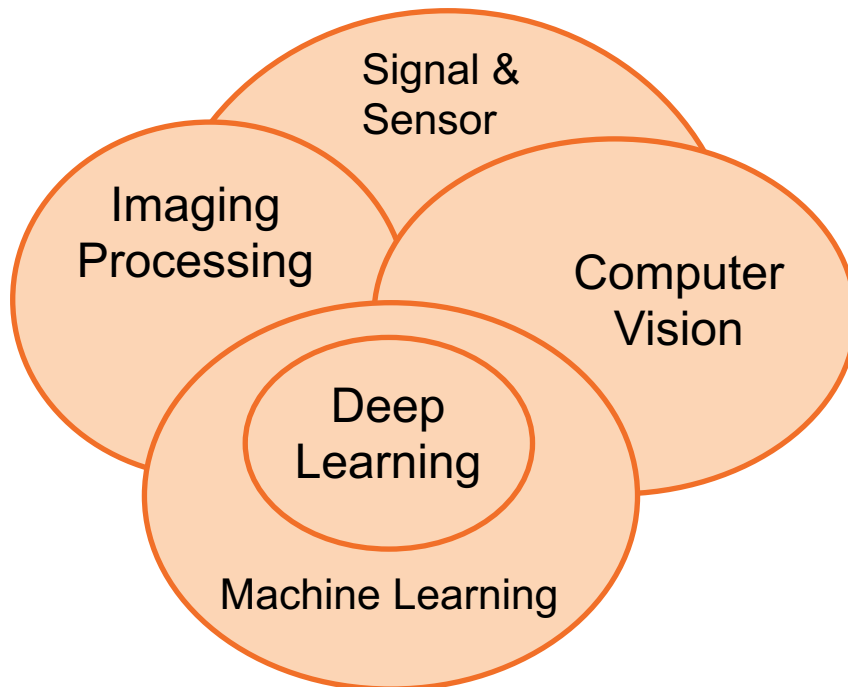
## • Applications

Vehicle perception

ADAS (Advanced driver-assistance systems)

Autonomy

## • Areas



### Space

- Space photograph enhancement
- Data compression
- Intelligent sensory analysis by remote space probes

### Medical

- Diagnostic imaging (CT, MRI, ultrasound, and others)
- Electrocardiogram analysis
- Medical image storage/retrieval

### Commercial

- Image and sound compression for multimedia presentation
- Movie special effects
- Video conference calling

### Telephone

- Voice and data compression
- Echo reduction
- Signal multiplexing
- Filtering

### Military

- Radar
- Sonar
- Ordnance guidance
- Secure communication

### Industrial

- Oil and mineral prospecting
- Process monitoring & control
- Nondestructive testing
- CAD and design tools

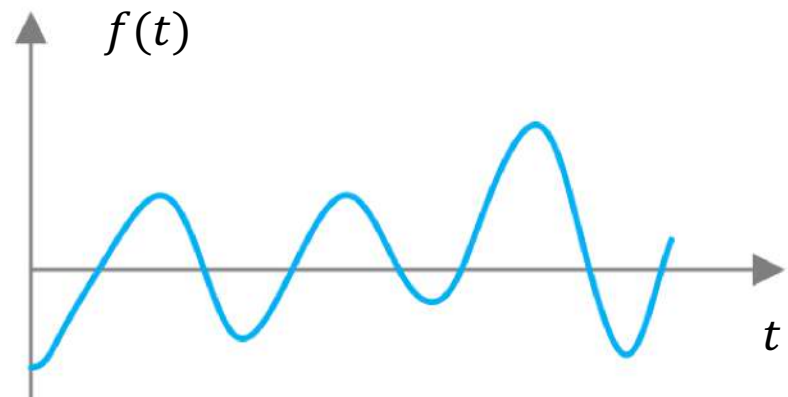
### Scientific

- Earthquake recording & analysis
- Data acquisition
- Spectral analysis
- Simulation and modeling



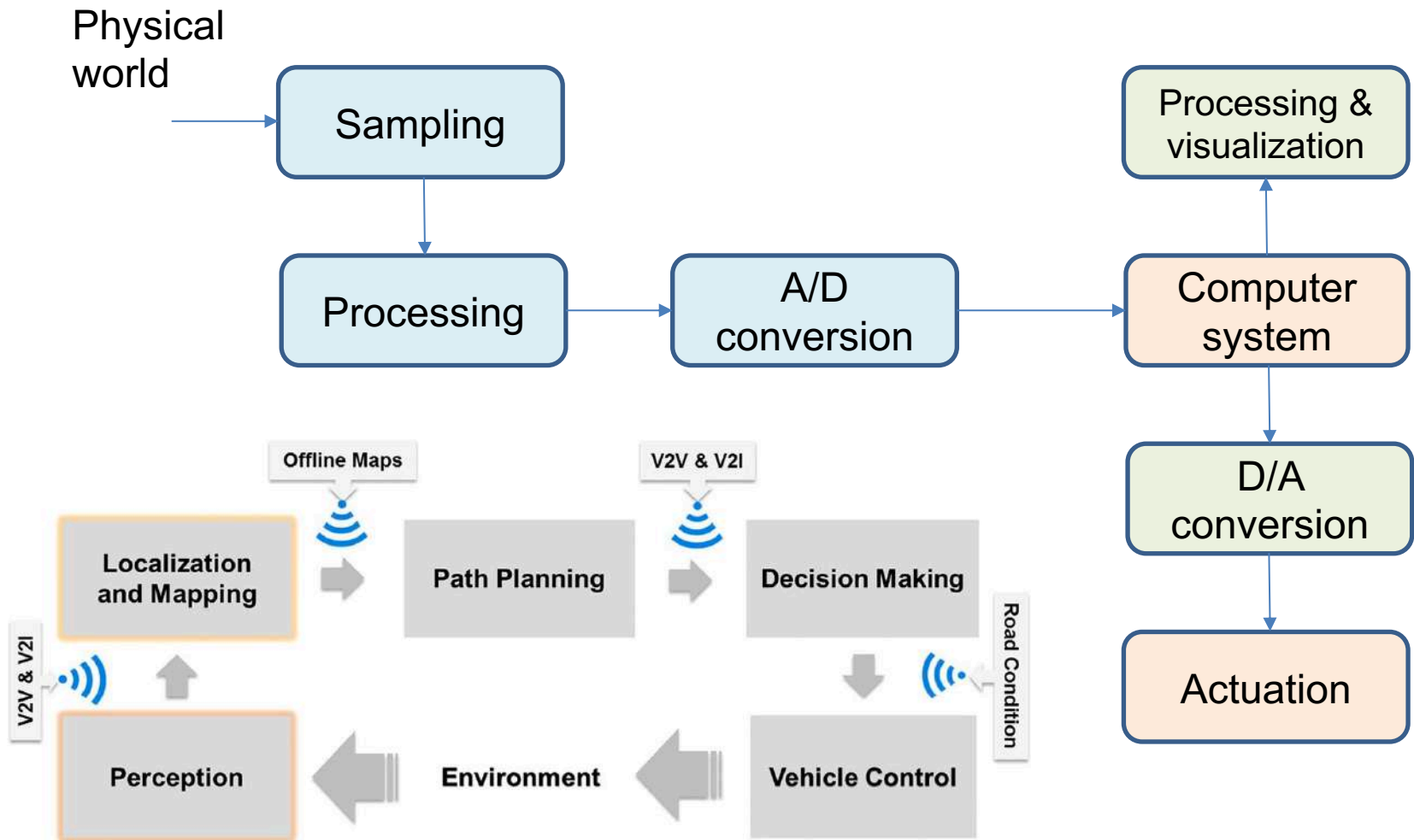
# Signal and Sensor Perception

- Perception for physical quantities  
Transduction principle - conversion of energy from one form to another
- Proprioception:  
Position, speed, acceleration, torque, battery level ...
- Exteroceptive:  
Scene, geometry, object, ...
- Analog signal  
Continuity in
  - Time domain
  - Amplitude



# Signal and Sensor Perception

- Sensor perception  $\rightarrow$  vehicle actuator control



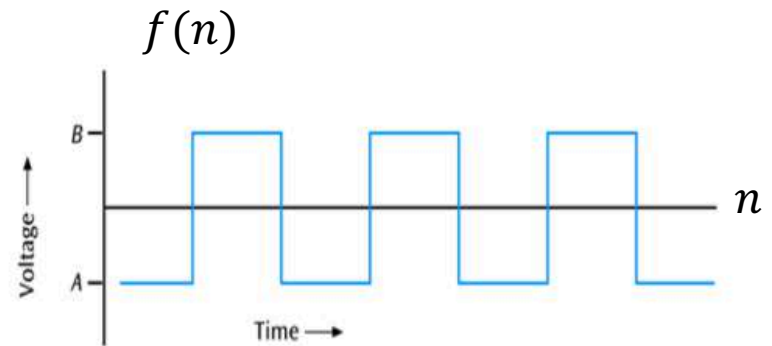
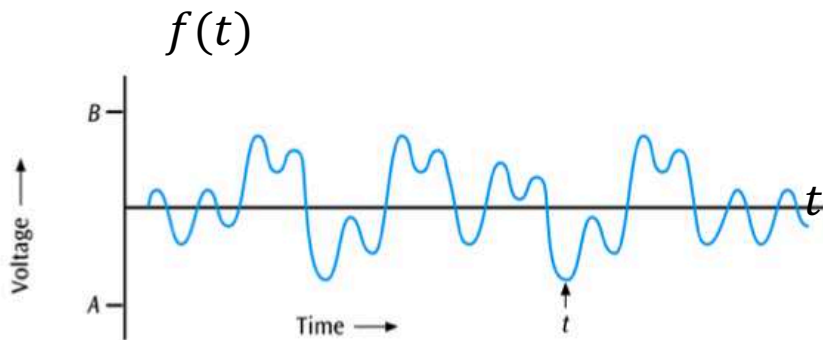




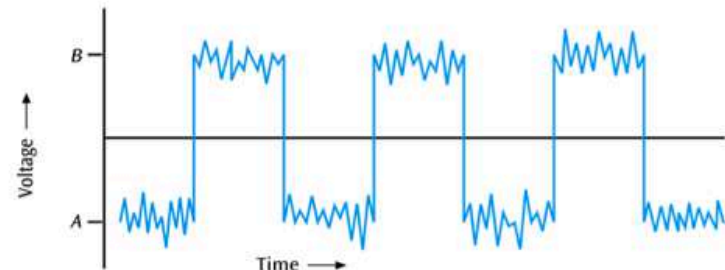
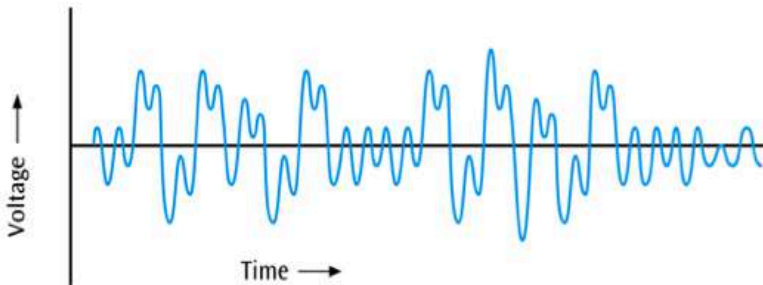
# Signal and Sensor Perception

- Analog signal VS. Digital signal

A/D (Analog-to-Digital)



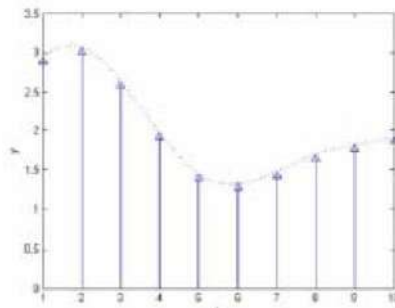
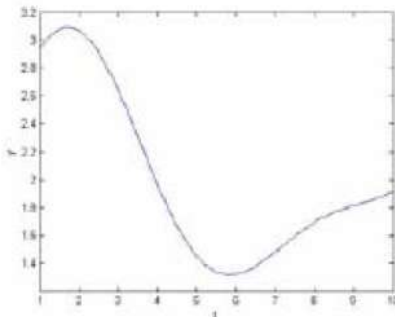
Affected by noise or EMI (Electromagnetic interference)



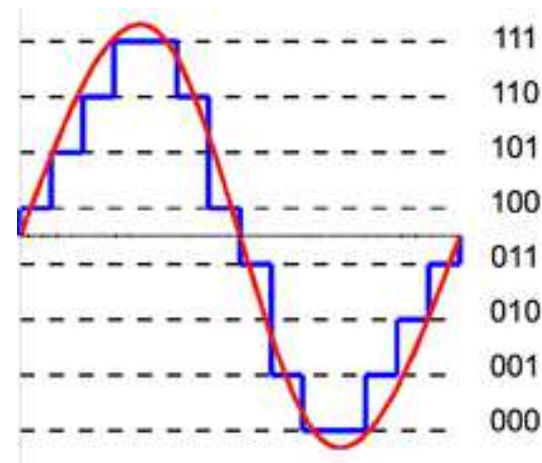


# Signal A/D (Analog-to-Digital)

- Sampling
  - From continuous signal to discrete signal
- PCM (Pulse Code Modulation)
  - Sampling  $\rightarrow$  Quantization  $\rightarrow$  Encoding



Uniform quantization

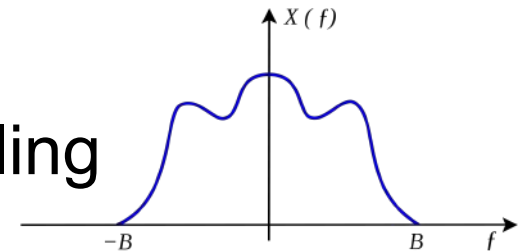


Binary encoding



# Signal A/D (Analog-to-Digital)

- Sampling
- Nyquist–Shannon sampling theorem (Harry Nyquist and Claude Shannon)
- Sufficient no-loss condition for sampling
  - Nyquist sampling rate:  $2B$
- Usage example:
  - The frequency of human voice is mostly less than 5kHz, ...
- Signal analysis
  - Time domain analysis
  - Frequency domain analysis
  - Time-Frequency domain analysis





## Time Domain Analysis

- The expectation ( $\mu_x$ ) of a signal (or called mean)

$$\mu_x = E[x(t)] = \frac{1}{T} \lim \int_0^T x(t) dt$$

- Mean square ( $A_{RMS}^2$ ) and root mean square (RMS) ( $A_{RMS}$ ) of a signal

$$A_{RMS}^2 = E[x^2(t)] = \frac{1}{T} \lim \int_0^T x^2(t) dt$$

- Variance ( $\sigma^2$ ) and standard deviation ( $\sigma$ ) of a signal

$$\sigma^2 = E[(x(t) - \mu_x)^2] = \frac{1}{T} \lim \int_0^T (x(t) - \mu_x)^2 dt$$



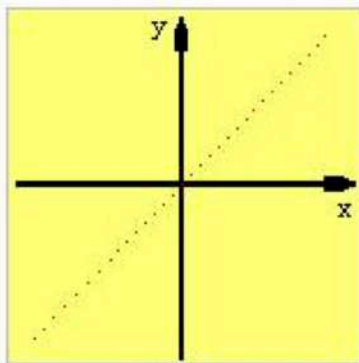
# Time Domain Analysis

- Covariance

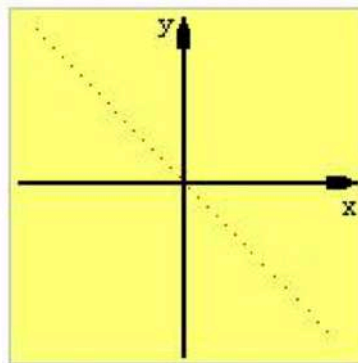
$$\text{cov}(x, y) (= E[(x(t) - \mu_x)(y(t) - \mu_y)])$$

- Statistical correlation

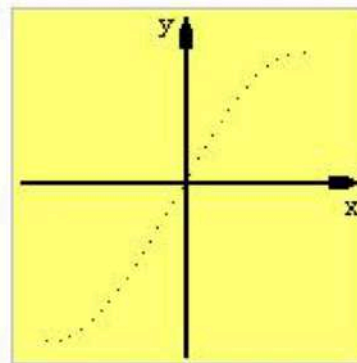
$$\rho_{xy} = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y} = \frac{E[(x(i) - \mu_x)(y(i) - \mu_y)]}{\sqrt{E[(x(i) - \mu_x)^2]E[(y(i) - \mu_y)^2]}}$$



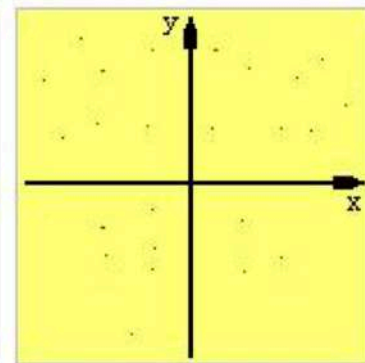
$$\rho_{xy} = 1$$



$$\rho_{xy} = -1$$



$$0 \leq \rho_{xy} \leq 1$$



$$\rho_{xy} = 0$$

Relationship?

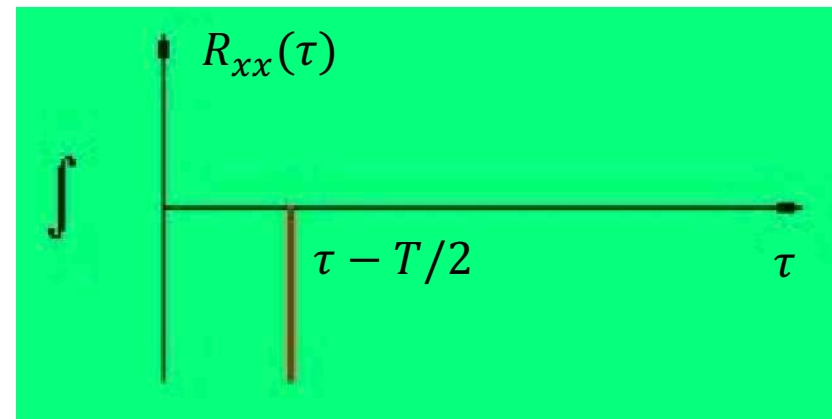
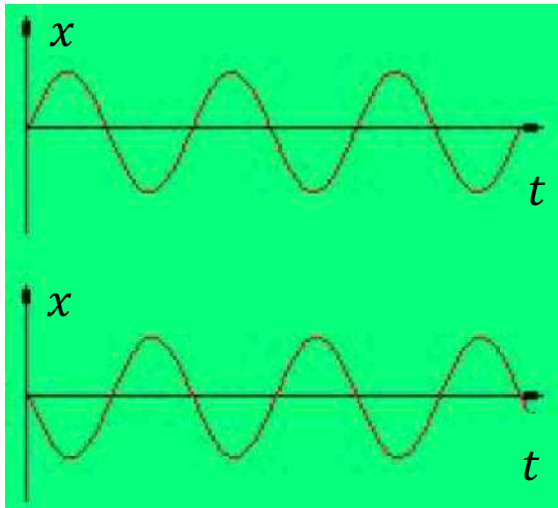


# Time Domain Analysis

- Correlation function for continuous signals

$$R_{xy}(\tau) = \lim_{T \rightarrow \infty} \int_{-T/2}^T x(t)y(t - \tau)$$

- Auto-correlation function  $R_{xx}(\tau)$



Similarity between two signals, or one signal with time shift





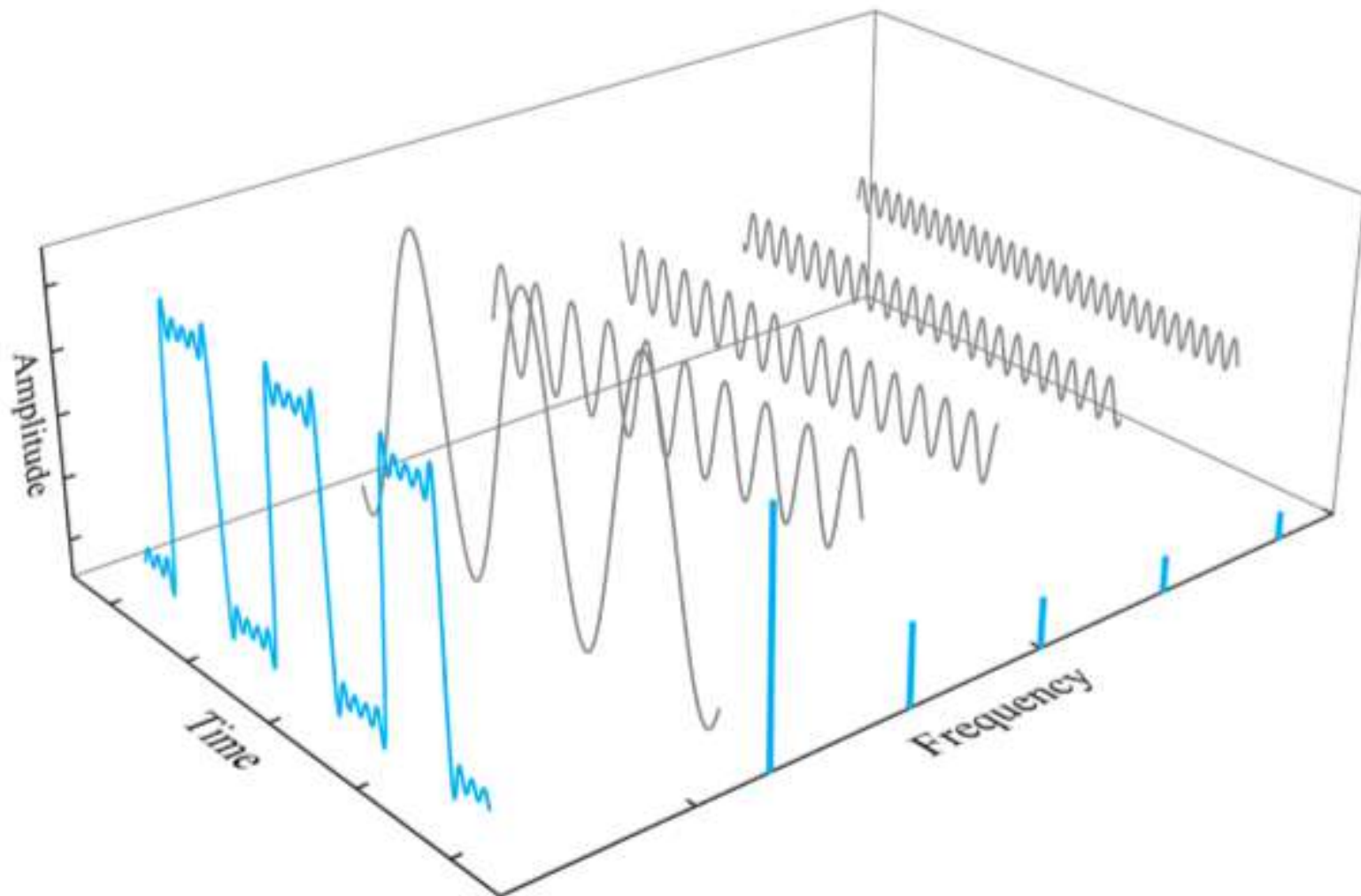
## Time Domain Analysis

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- Time-domain operations for digital signals
  - Amplitude modifications  $y[k] = a \sum x_m[k] + b$
  - Time modifications  $y[k] = x[k - m]$
  - Down-sampling  $y[k] = x[\lambda k]$
  - Up-sampling or interpolation
  - Cross-correlation ( $\otimes$ ):  $y[k] = \sum_{n=-\infty}^{\infty} x_1[n]x_2[n - k]$
  - Auto-correlation  $y[k] = \sum_{n=-\infty}^{\infty} x[n]x[n - k]$
  - Convolution ( $*$ ):  $y[k] = \sum_{n=-\infty}^{\infty} x_1[n]x_2[k - n]$



# Signal Frequency Analysis





# Signal Frequency Analysis

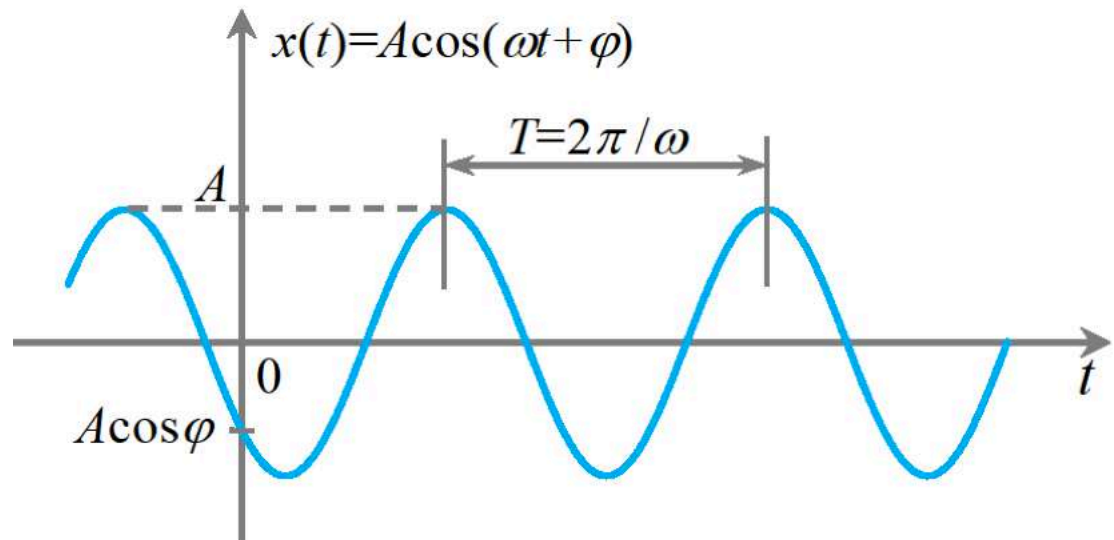
- Frequency domain
- A typical signal: *sin* wave

$$x(t) = A \cos(\omega t + \varphi)$$

Amplitude:  $A$

Frequency:  $f = \omega / 2\pi$

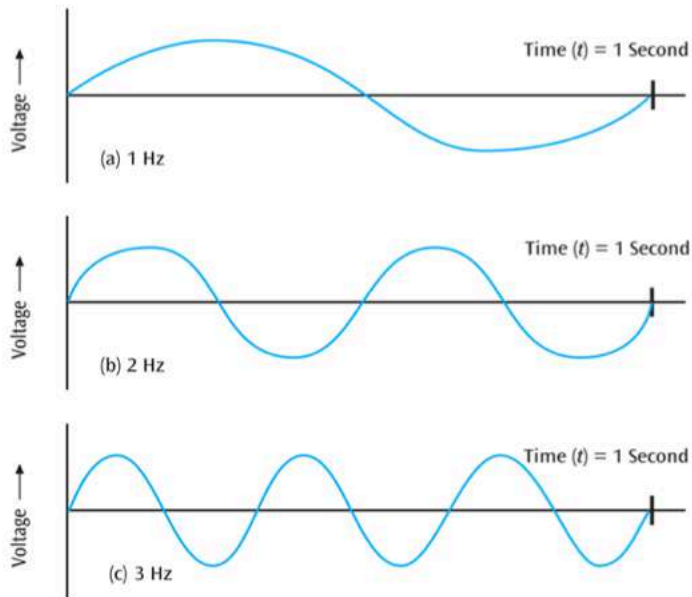
Phase:  $\varphi$





# Signal Frequency Analysis

- Frequency of a signal



Constant-amplitude signal?



Step signal?





# Signal Frequency Analysis

- Fourier transform and inverse transform  
(under Dirichlet condition of convergence)

$$X(\omega) = \int_{-\infty}^{\infty} x(t)e^{-j\omega t} dt$$
$$x(t) = \int_{-\infty}^{\infty} X(\omega)e^{j\omega t} d\omega$$

- Fourier series expansion  
DFT (Discrete-time Fourier Transform)

$$x(t) = \sum_{k=-\infty}^{\infty} A_k \cos(k\omega_0 t + \varphi_k), \omega_0 = 2\pi/T$$

Decomposes periodic complex signal to a (possibly infinite) set of simple sine waves;

Applicable for aperiodic signal, considering  $T \rightarrow \infty$



# Signal Frequency Analysis

- Given Euler's formula

$$e^{j\theta} = \cos(\theta) + j\sin(\theta), \theta = \omega t, \cos(\omega t) = \frac{e^{j\omega t} + e^{-j\omega t}}{2}$$

$$\text{Then: } A\cos(\omega t + \varphi) = \frac{A}{2} e^{j(\omega t + \varphi)} + \frac{A}{2} e^{-j(\omega t + \varphi)}$$

- Exponential form of Fourier series

$$x(t) = \sum_{k=-\infty}^{\infty} X_k e^{jk\omega_0 t}$$

where  $X_k$  are complex numbers:

$$X_k = \frac{1}{T} \int_0^T x(t) e^{-jk\omega_0 t} dt$$

- For each frequency components:

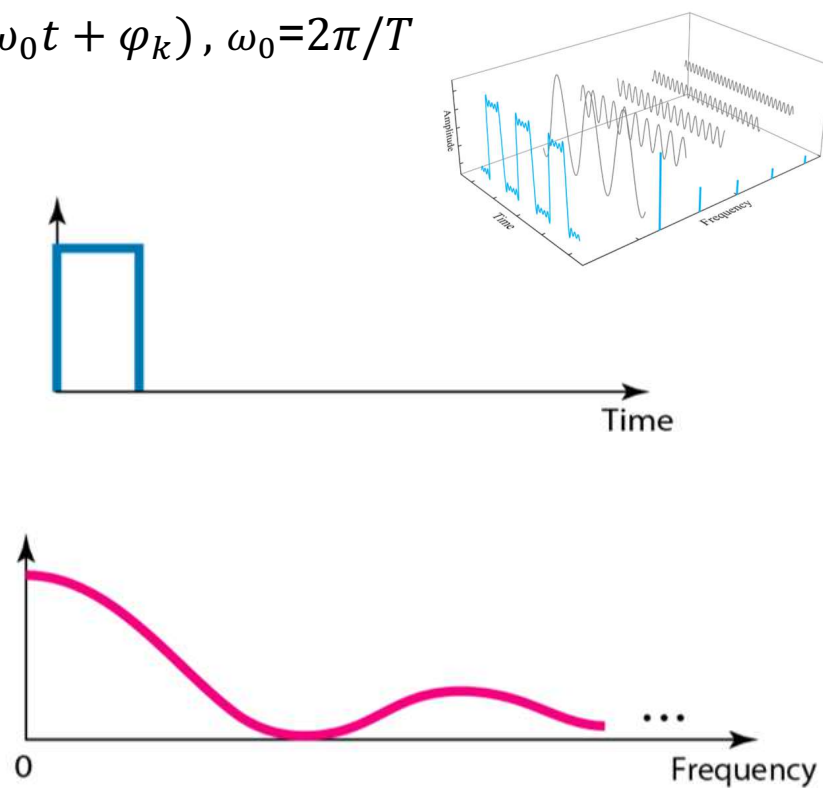
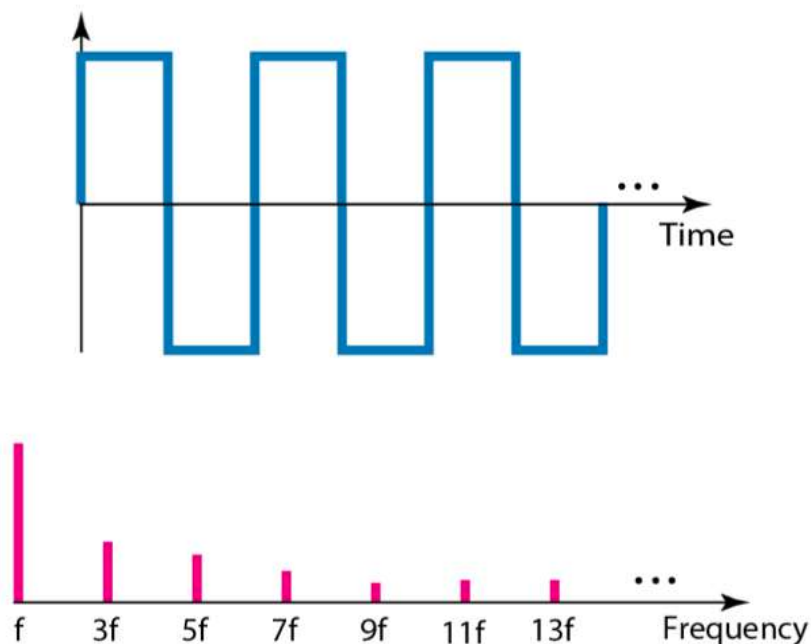
Frequencies  $k\omega_0$ ; Amplitude  $|X_k|$ ; Phase  $\arctan \frac{\text{Im}(X_k)}{\text{Re}(X_k)}$ , atan2



# Signal Frequency Analysis

- DFT difference for periodic and aperiodic signal in Trigonometric series

$$x(t) = A_0 + \sum_{k=-\infty}^{\infty} A_k \cos(k\omega_0 t + \varphi_k), \quad \omega_0 = 2\pi/T$$



# Signal noise

- Naturally, sensor data is noisy.

- Hardware filters
- Algorithm filters



- Noise

- A general term for all unwanted (probably immeasurable) modifications during signal capturing to processing process.
- Wrong measurement doesn't belong to noise.

- Noise types

- Additive noise (White noise, Gaussian noise, Cauchy noise ...)
- Multiplicative noise (multiplies or modulates the intended signal)
- Quantization error (due to conversion from continuous to discrete values)
- Phase noise (random time shifts in a signal)
- et al.



# Signal noise

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- White Gaussian noise
  - Good approximation of many real-world situations;
  - Mathematically tractable models;
- **White**: refers to "uniform power across the frequency".
- **Gaussian**: refers to "normal distribution in the time domain" with mean as zero.
- How 'big' is the noisy related to the signal?

# Signal noise

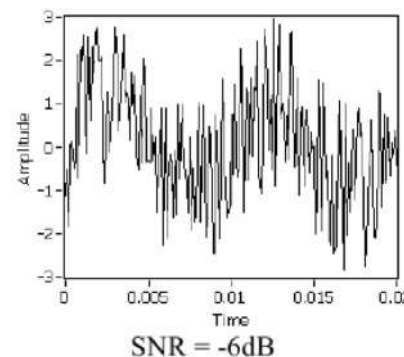
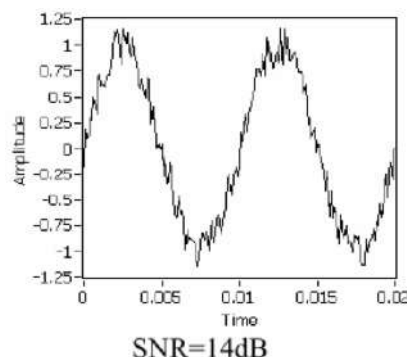
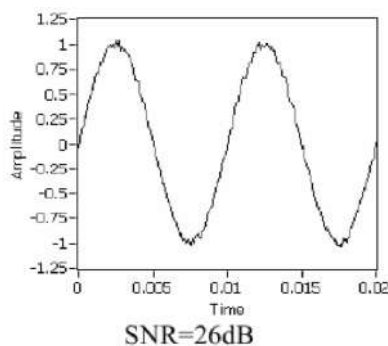
- Signal-to-noise ratio (**SNR**)

$$SNR = \frac{P_{signal}}{P_{noise}} = \left( \frac{A_{RMS,s}}{A_{RMS,n}} \right)^2$$

- Logarithmic decibel (dB) scale

$$P_{dB} = 10 \log_{10} P$$

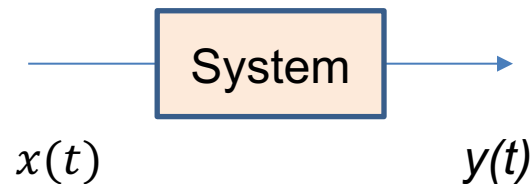
$$SNR_{dB} = 10 \log_{10} \frac{P_{signal}}{P_{noise}} = 20 \log_{10} \frac{A_{RMS,s}}{A_{RMS,n}}$$





# Digital Signal Processing Systems

- From signal to systems



examples

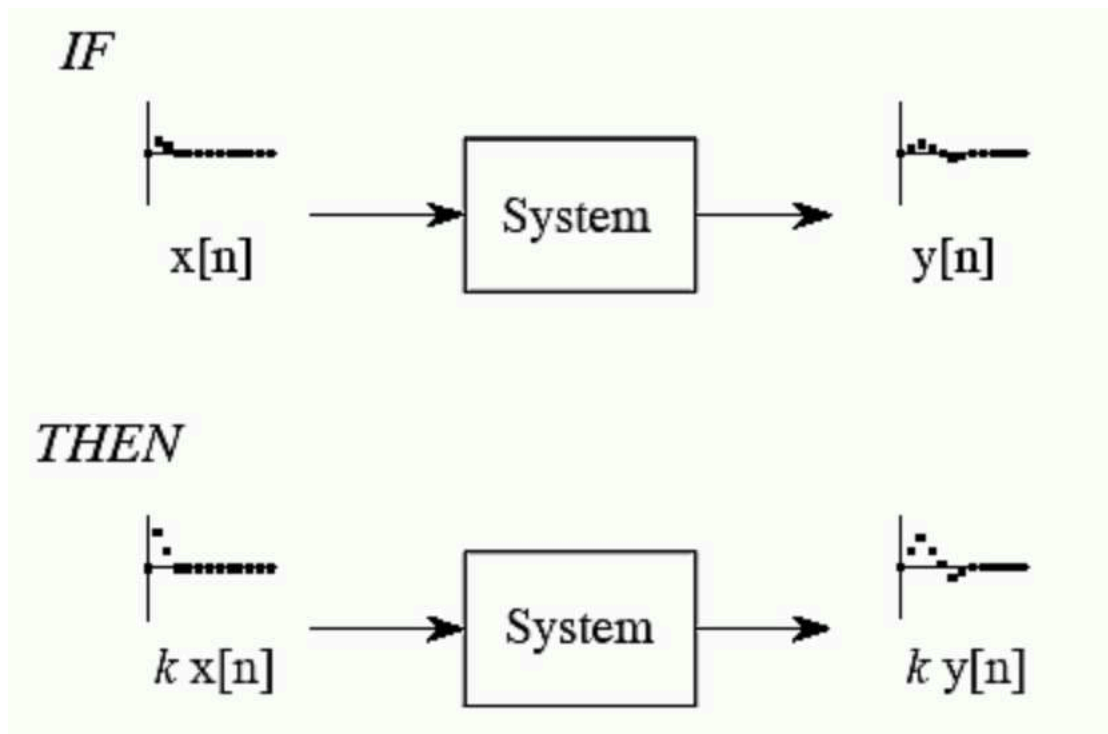
$x(t) \rightarrow \boxed{\int} \rightarrow y(t)$	$y(t)$	$\int_0^t x(\tau) d\tau$
$x(t) \rightarrow \boxed{A} \rightarrow y(t)$	$y(t)$	$Ax(t)$
$x(t) \rightarrow \boxed{\otimes} \rightarrow y(t)$	$y(t)$	$x_1(t)x_2(t)$
$x(t) \rightarrow \boxed{\oplus} \rightarrow y(t)$	$y(t)$	$x_1(t) + x_2(t)$

- Linear VS. Non-linear systems
- Characteristics of linear system
  - Homogeneity
  - Additivity
- Linear Time-invariant (LTI)



# Digital Signal Processing Systems

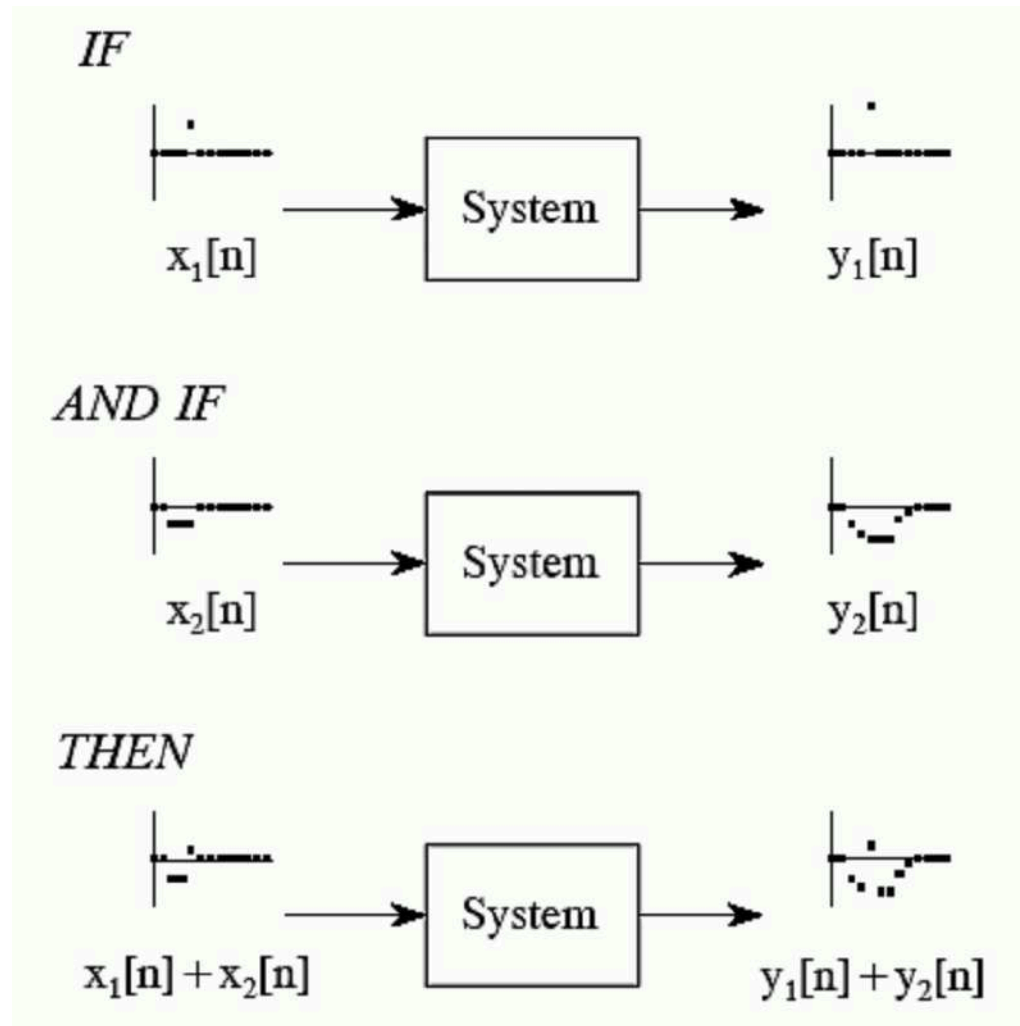
- Homogeneity of linear systems





# Digital Signal Processing Systems

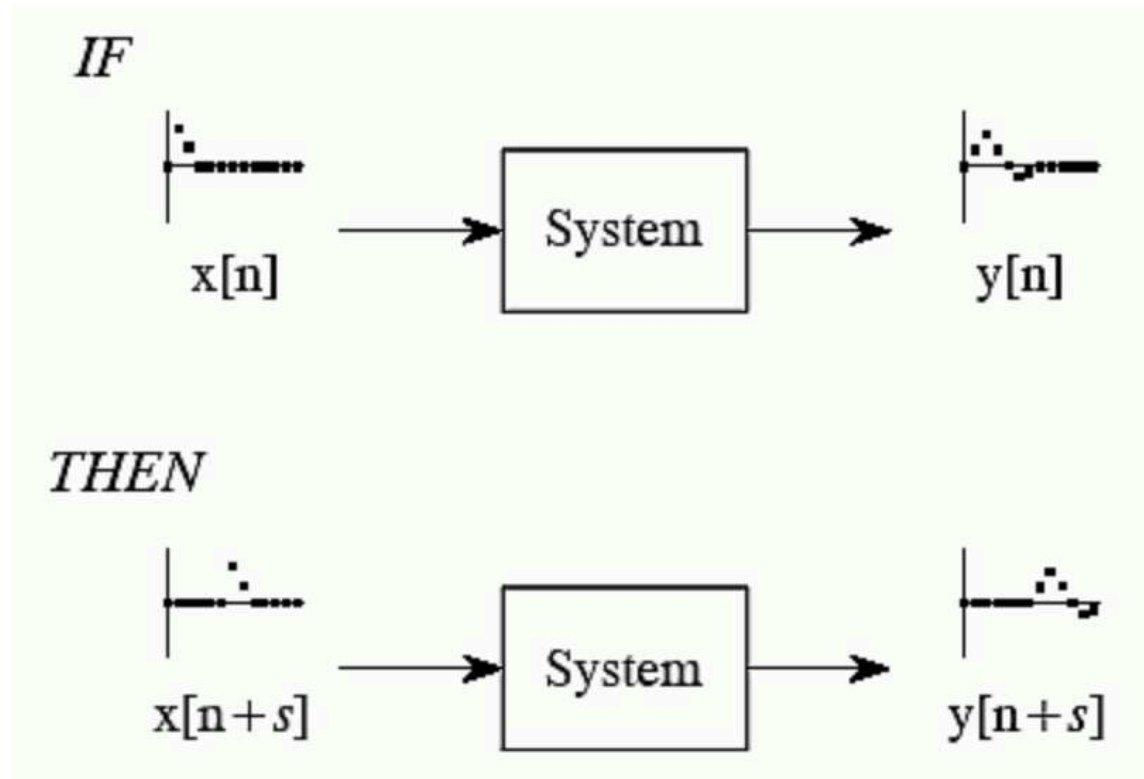
- Additivity of linear systems





# Digital Signal Processing Systems

- Time-invariant systems



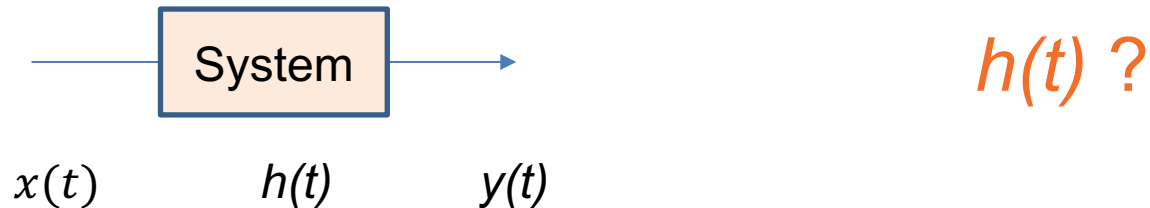
Important !

The characteristics of the system do not change with time.



# Digital Signal Processing Systems

- System analysis

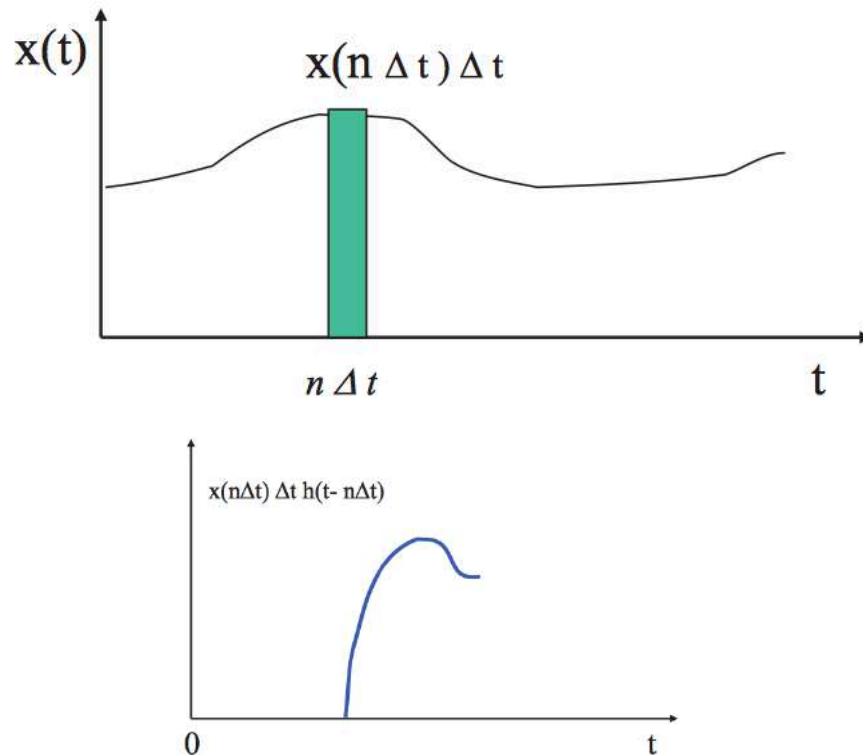


- How to mathematically describe a system?
- How to design such a system?



# Digital Signal Processing Systems

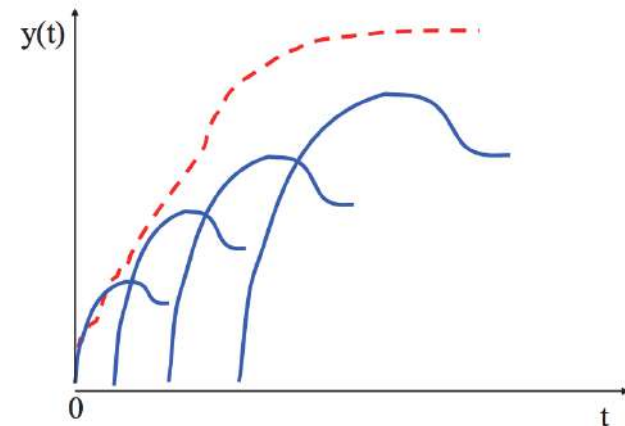
- System response



Response:

$$x(n\Delta t)\Delta t h(t - n\Delta t)$$

$$y(t) = \sum_{n=0}^{\infty} x(n\Delta t)\Delta t h(t - n\Delta t)$$



Signal convolution:

$$\begin{aligned} y(t) &= x(t) * h(t) \\ &= \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau \end{aligned}$$

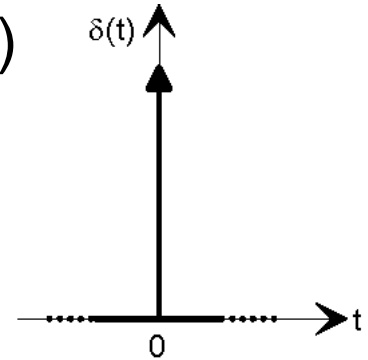


# Digital Signal Processing Systems

- (Unit) Delta function (impulse signal, Paul Dirac)

$$\delta(t - \tau_0) = 0, x \neq 0$$

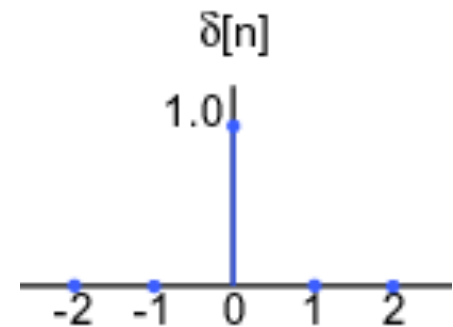
$$\lim_{\varepsilon \rightarrow 0} \int_{\tau_0 - \varepsilon}^{\tau_0 + \varepsilon} \delta(t - \tau_0) dt = 1$$



- Characteristic

$$x(\tau_0) = \int_{-\infty}^{\infty} x(t) \delta(t - \tau_0) dt$$

$$x[n] = \sum_{k=-\infty}^{\infty} x[k] \delta(n - k)$$



- $h(t)$  is defined as impulse response, which is the system response when input signal is  $\delta(t)$

# Digital Signal Processing Systems

- We have seen signal can be characterized by frequency content (pros?)
- LTI system analysis
  - Time-domain impulse response  $h(t)$
  - Frequency response ---  $H(\omega)$ ?
- For system analysis, introduce dampening factor, and Laplace transform and  $z$  transform:

$$L(\omega) = \int_{-\infty}^{\infty} x(t)e^{-(\sigma+j\omega)t} dt \rightarrow L(s) = \int_{-\infty}^{\infty} x(t)e^{-st} dt, \text{ where } s = \sigma + j\omega$$

For discrete signal:  $X(z) = \sum_{-\infty}^{\infty} x[n]z^{-n}$ ,  
 where  $z = e^{sT} = r e^{j\omega}$





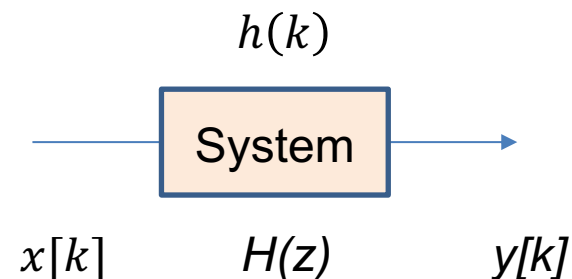
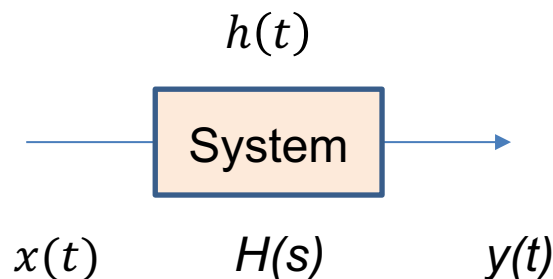
# Digital Signal Processing Systems

- All three transforms convert time-domain convolutions to polynomial equations

$$y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau$$

$$Y(\omega) = H(\omega)X(\omega), Y(s) = H(s)X(s), Y(z) = H(z)X(z)$$

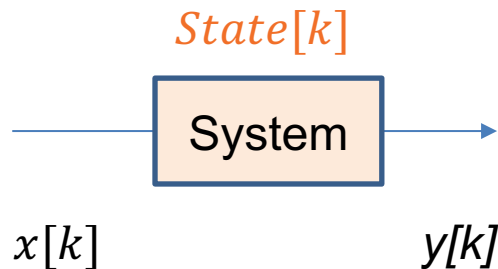
- Why Laplace transform and z transform?
  - Complex frequency-domain for Stability and Causality analysis





# Digital Filter Design

- State-space filter



Using dynamic model  
e.g.: Kalman filter

$$\bar{\mu}_t = A_t \mu_{t-1} + B_t u_t$$

$$\bar{\Sigma}_t = A_t \Sigma_{t-1} A_t^T + R_t$$

$$K_t = \bar{\Sigma}_t C_t^T (C_t \bar{\Sigma}_t C_t^T + Q_t)^{-1}$$

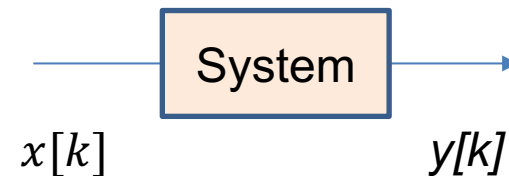
$$\mu_t = \bar{\mu}_t + K_t (z_t - C_t \bar{\mu}_t)$$

$$\Sigma_t = (I - K_t C_t) \bar{\Sigma}_t$$

- Conventional digital filters

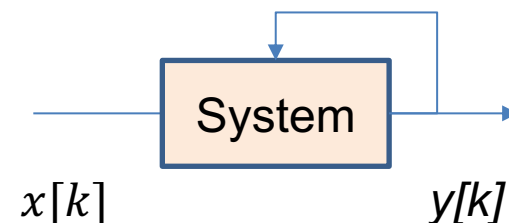
Finite Impulse Response (FIR) filters:

$$y[k] = \sum_{n=0}^N b_n x[k - n]$$



Infinite Impulse Response (IIR) filters:

$$y[k] = \sum_{n=0}^N b_n x[k - n] + \sum_{m=0}^M a_m y[k - m]$$





# Digital Filter Design

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- FIR Filters

- Pros:

- Inherently stable
    - Linear phase characteristics

- Cons:

- Need lots of memory and math terms required

- IIR Filters

- Pros:

- Very efficient in term of resources

- Cons:

- Inherently less stable

Design approaches:

Frequency sampling design

Fourier transform design

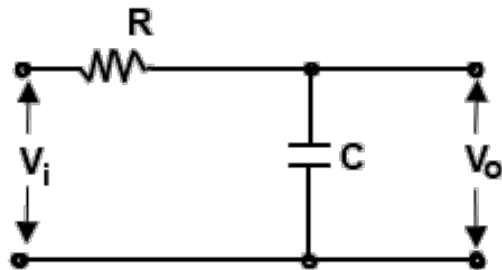
Bilinear transformation

Pole zero placement

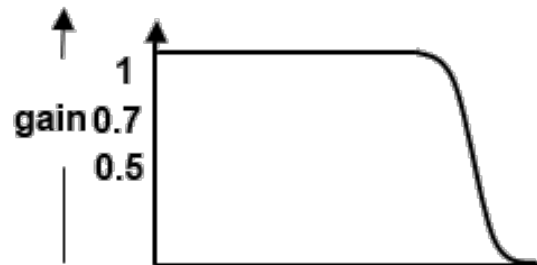


# Digital Filter Design

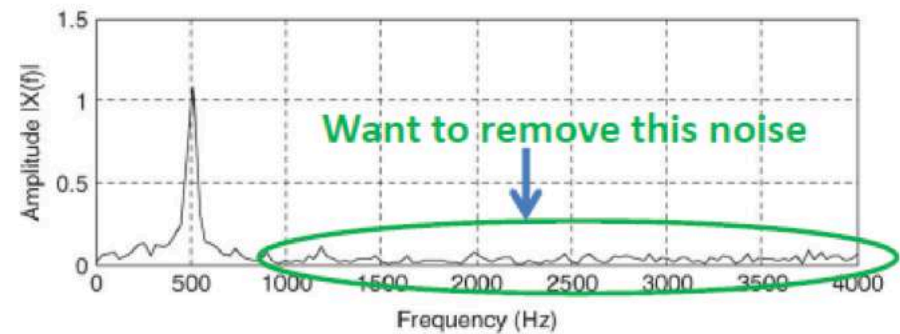
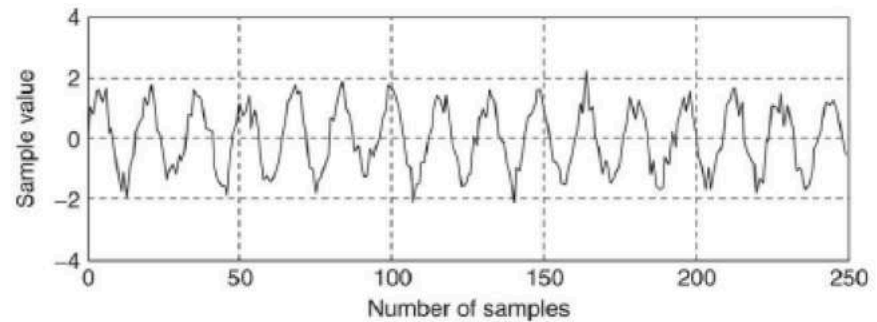
- Example: low pass filter design



(a) RC low Pass Filter Circuit



(b) Frequency Response Curve





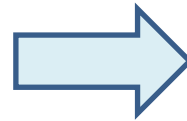
# Digital Filter Design

- A simple example of digital filter:

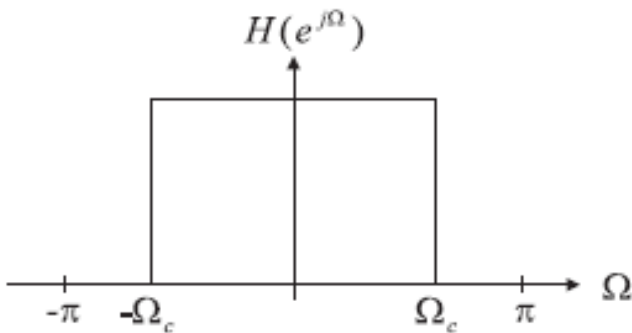
$$y[k] = \frac{1}{4} (x[k] + 2x[k-1] + x[k-2])$$

- (ideal) FIR low pass filter (LPF) design [\[1\]](#)

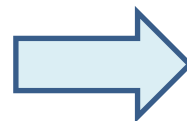
$$y[k] = \sum_{n=0}^N b_n x[k-n]$$



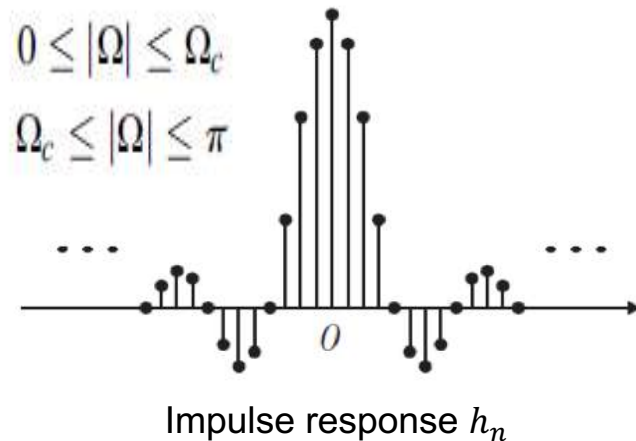
$b_n$ : filter coefficients  
(aka: kernel)



$$H(e^{j\Omega}) = \begin{cases} 1, & 0 \leq |\Omega| \leq \Omega_c \\ 0, & \Omega_c \leq |\Omega| \leq \pi \end{cases}$$



Inverse FFT

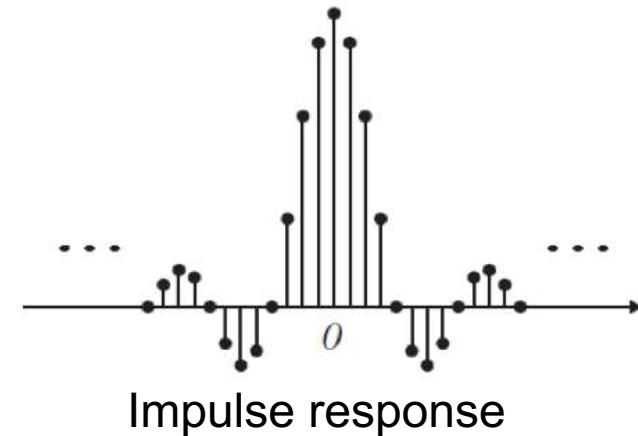




# Digital Filter Design

- (ideal) FIR low pass filter design [1]

- $h_n \rightarrow z$  transformation  $H(z)$



$$H(z) = h(M)z^M + \dots + h(1)z^1 + h(0) + h(1)z^{-1} + \dots + h(M)z^{-M}$$

Symmetric

By After truncating  $2M+1$  major components using the coefficient symmetry, where  $h_n$  is just a shift of  $b_n$  for causal design.



# Digital Filter Design

Filter	Type	Ideal Impulse Response $h(n)$ (noncausal FIR coefficients)
Lowpass:		$h(n) = \begin{cases} \frac{\Omega_c}{\pi} & \text{for } n = 0 \\ \frac{\sin(\Omega_c n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$
Highpass:		$h(n) = \begin{cases} \frac{\pi - \Omega_c}{\pi} & \text{for } n = 0 \\ -\frac{\sin(\Omega_c n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$
Bandpass:		$h(n) = \begin{cases} \frac{\Omega_H - \Omega_L}{\pi} & \text{for } n = 0 \\ \frac{\sin(\Omega_H n)}{n\pi} - \frac{\sin(\Omega_L n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$
Bandstop:		$h(n) = \begin{cases} \frac{\pi - \Omega_H + \Omega_L}{\pi} & \text{for } n = 0 \\ -\frac{\sin(\Omega_H n)}{n\pi} + \frac{\sin(\Omega_L n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$



# Digital Filter Design

- (ideal) FIR low pass filter design [1]
- **Example:** Design a 3-tap FIR LPF with cut-off frequency of 800 Hz and a sampling rate of 8,000 Hz using the Fourier transform method.

Normalized cut-off frequency ➡

$$\Omega_c = 2\pi f_c T_s = 2\pi \times 800/8,000 = 0.2\pi \text{ radians}$$

3-tap filter ➡  $2M + 1 = 3$  ➡  $M = 1$

➡  $h(n)$  for  $n$  from  $-M$  to  $M$  ➡  $n = -1, 0, 1,$





# Digital Filter Design

- (ideal) FIR low pass filter design [1]

filter coefficients  $\Rightarrow h(0) = \frac{\Omega_c}{\pi}$  for  $n = 0$   
From previous slide table

and 
$$h(n) = \frac{\sin(\Omega_c n)}{n\pi} = \frac{\sin(0.2\pi n)}{n\pi} \quad \text{for } n \neq 0$$

compute coefficients  $\Rightarrow h(0) = \frac{0.2\pi}{\pi} = 0.2$

and 
$$h(1) = \frac{\sin[0.2\pi \times 1]}{1 \times \pi} = 0.1871$$

Using symmetry  $\Rightarrow h(-1) = h(1) = 0.1871$



# Digital Filter Design

- (ideal) FIR low pass filter design [1]

Delaying  $h(n)$  by  
 $M = 1$  sample

$$\Rightarrow b_n = h(n - M)$$

for  $n = 0, 1, \dots, 2M$ .

$$\Rightarrow \begin{cases} b_0 = h(0 - 1) = h(-1) = 0.1871 \\ b_1 = h(1 - 1) = h(0) = 0.2 \\ b_2 = h(2 - 1) = h(1) = 0.1871 \end{cases}$$

FIR low pass filter: transfer function

$$H(z) = 0.1871 + 0.2z^{-1} + 0.1871z^{-2} \Rightarrow \frac{Y(z)}{X(z)} = H(z) = 0.1871 + 0.2z^{-1} + 0.1871z^{-2}$$

$$\Rightarrow Y(z) = 0.1871X(z) + 0.2z^{-1}X(z) + 0.1871z^{-2}X(z)$$

# Digital Filter Design

- (ideal) FIR low pass filter design [1]
- Further discussion
  - Undesirable Gibbs oscillations
  - Solution: window functions

1. Rectangular window:

$$w_{\text{rec}}(n) = 1, -M \leq n \leq M$$

2. Triangular (Bartlett) window:

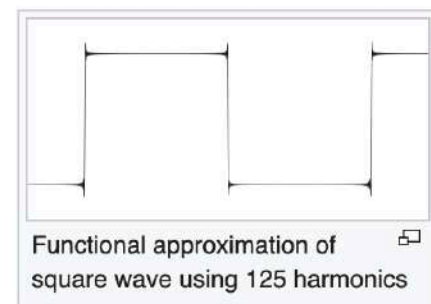
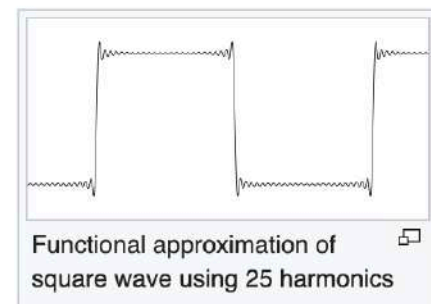
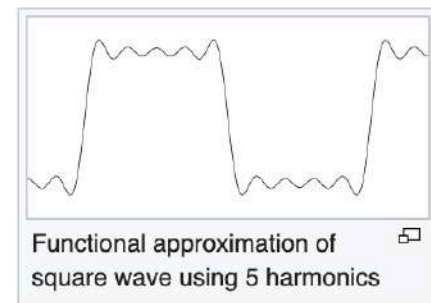
$$w_{\text{tri}}(n) = 1 - \frac{|n|}{M}, -M \leq n \leq M$$

3. Hanning window:

$$w_{\text{han}}(n) = 0.5 + 0.5 \cos\left(\frac{n\pi}{M}\right), -M \leq n \leq M$$

Applying the window sequence  $w(n)$  to the filter coefficients

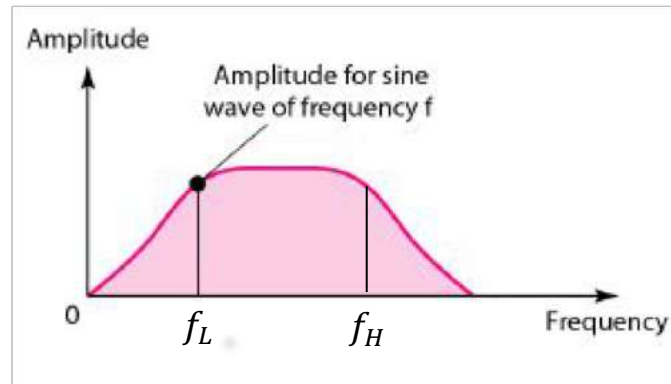
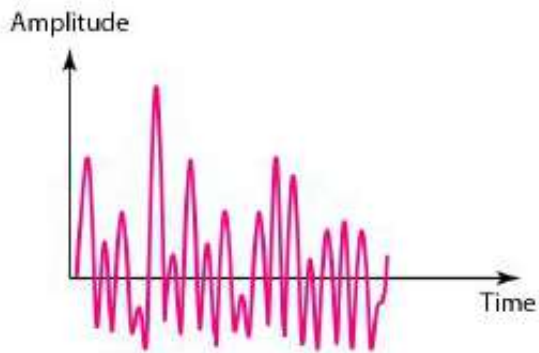
$$h_w(n) = h(n) \cdot w(n)$$





# Spectrum in Frequency Domain

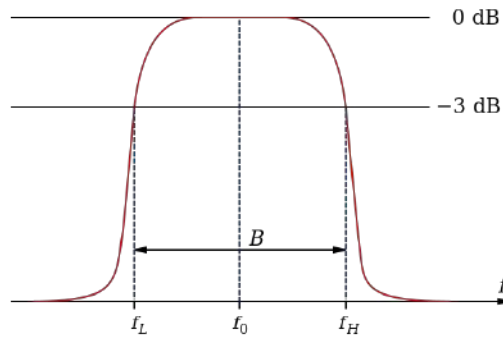
- Frequency spectrum to bandwidth



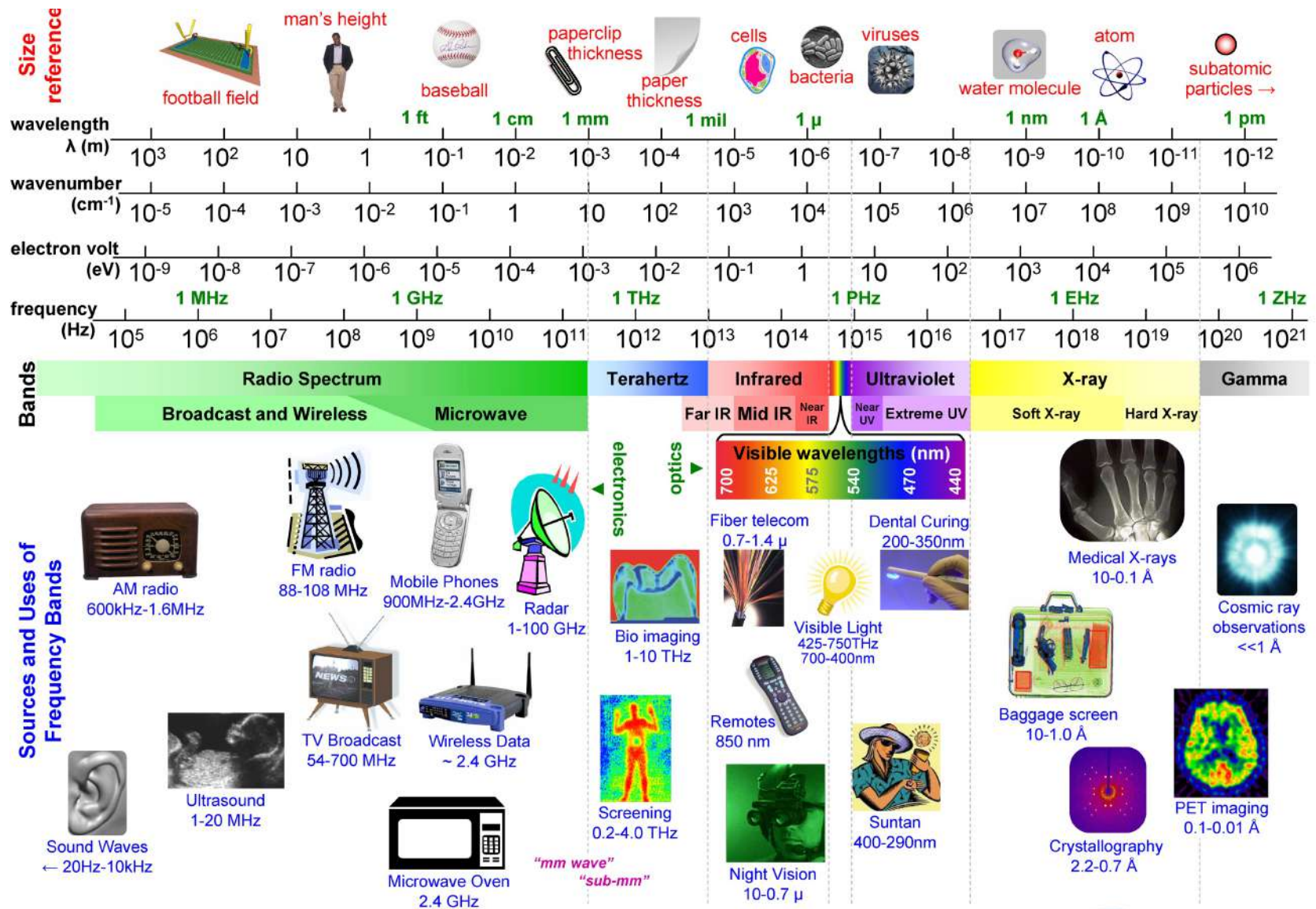
Bandwidth

Effective bandwidth

$$dB = 10 \log_{10} \frac{P_{f_L \sim H}}{P_s}$$

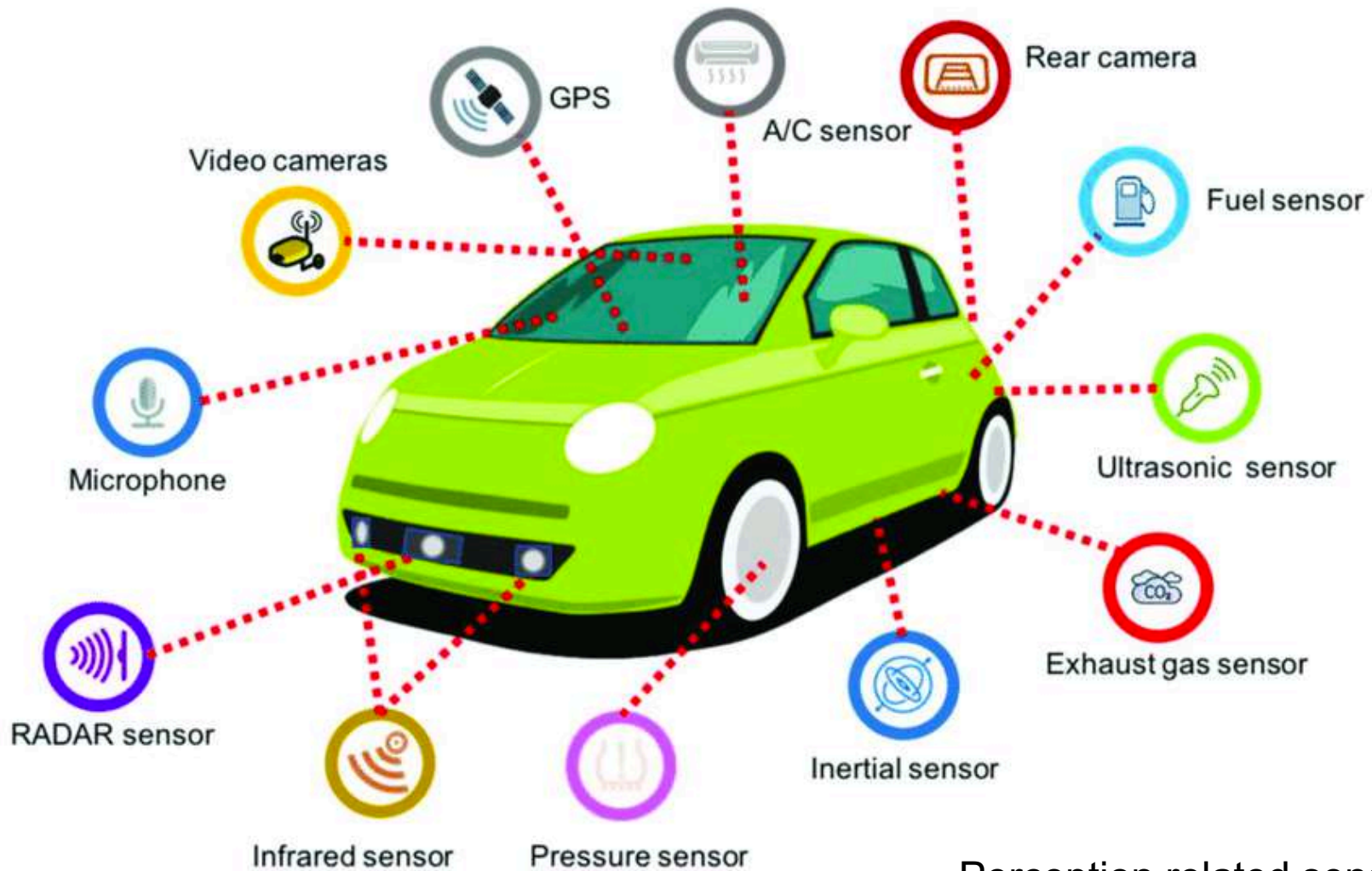


# Electromagnetic Spectrum





# Vehicle Sensors

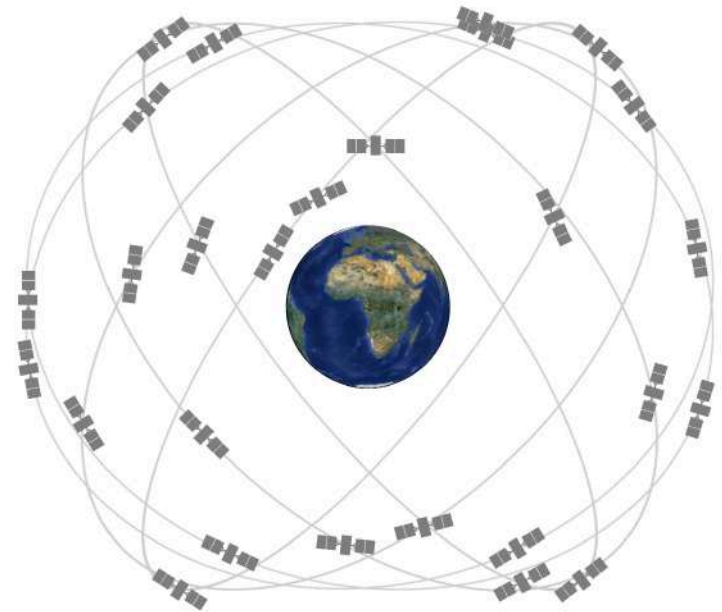


Perception related sensors



# Vehicle Sensors

- GPS (Global Positioning System)
- A constellation of 24 satellites (+several spares)
- Broadcast time; identity; orbital parameters (latitude, longitude, altitude);
- Carriers - there are two carrier radio waves:
  - L1, with frequency 1575.42 MHz
  - L2, with frequency 1227.6 MHz



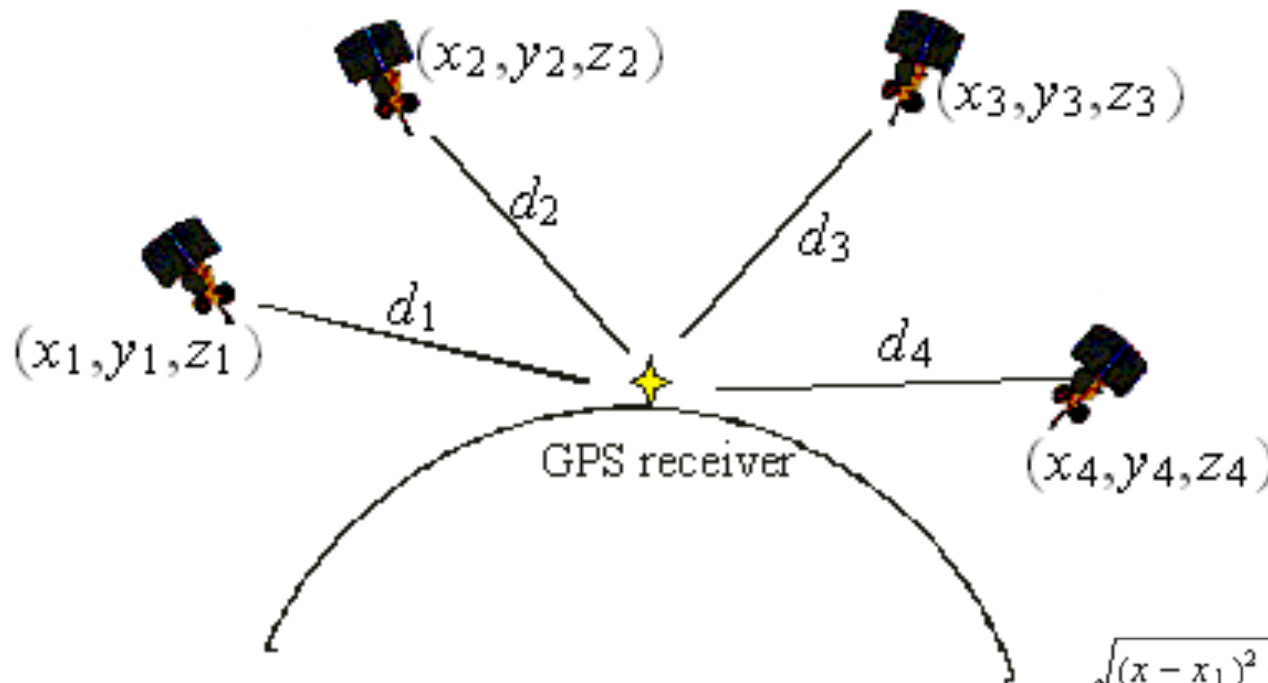
Space Segment

<https://www.gps.gov>



# Vehicle Sensors

- GPS (Global Positioning System)



Triangulation

$$\sqrt{(x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2} + ct_B = d_1$$

$$\sqrt{(x - x_2)^2 + (y - y_2)^2 + (z - z_2)^2} + ct_B = d_2$$

$$\sqrt{(x - x_3)^2 + (y - y_3)^2 + (z - z_3)^2} + ct_B = d_3$$

$$\sqrt{(x - x_4)^2 + (y - y_4)^2 + (z - z_4)^2} + ct_B = d_4$$



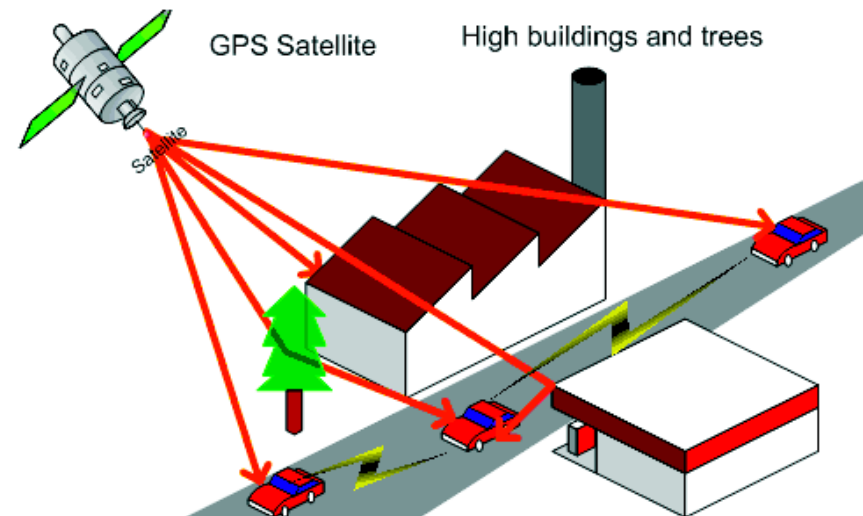


# Vehicle Sensors

- GPS (Global Positioning System)
- Spherical coordinates
  - latitude
  - longitude
  - altitude (above sea level)
- PPS - Precise Positioning Service
  - uses multiple signals
  - for military use only
- DGPS - Differential GPS
  - 2 receivers
  - 1 known fixed position

Expected errors:

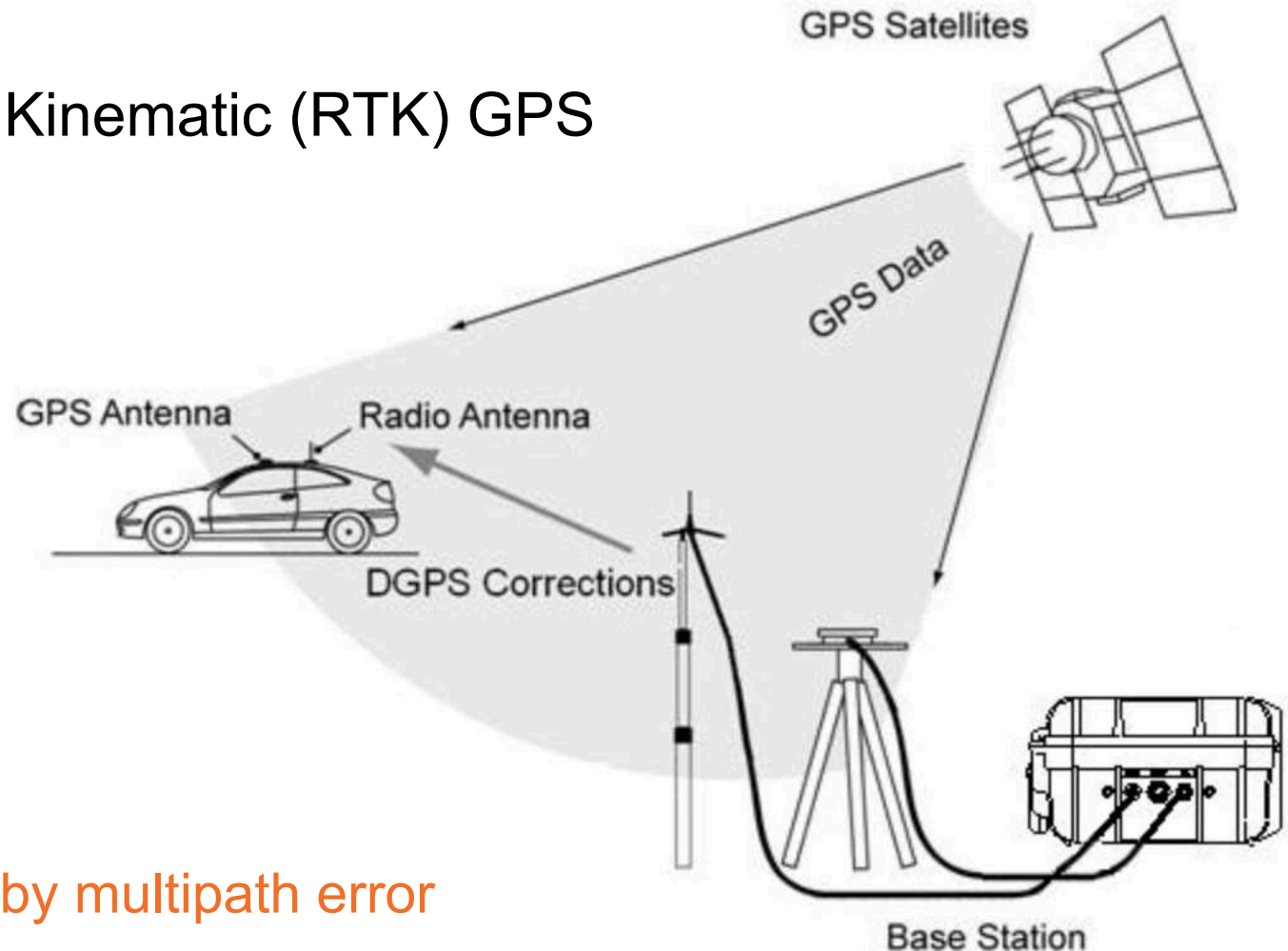
ionospheric range error  
tropospheric range error  
satellite clock range error  
receiver clock range error  
multipath error  
noise





# Vehicle Sensors

- GPS (Global Positioning System)
- Real-Time Kinematic (RTK) GPS



Still degraded by multipath error

# Vehicle Sensors

- **GNSS** global geo-spatial positioning system
  - Global Navigation Satellite System (GNSS) with global coverage.
- GNSS systems:
  - GPS, GLONASS, Galileo, Beidou and other regional systems.
- **GNSS+INS fusion**
  - Example: NovAtel SPAN-CPT GNSS-INS

**SPAN® SPAN-CPT™**



SINGLE ENCLOSURE GNSS+INS  
RECEIVER DELIVERS 3D POSITION,  
VELOCITY AND ATTITUDE



# Vehicle Sensors

- GNSS+INS
- NovAtel  
SPAN-CPT

## SPAN SYSTEM PERFORMANCE<sup>1</sup>

### Horizontal Position Accuracy (RMS)

Single point L1/L2	1.2 m
NovAtel CORRECT™	
» SBAS <sup>2</sup>	60 cm
» DGPS	40 cm
» PPP <sup>3</sup>	4 cm
» RTK	1 cm + 1 ppm

### Data Rate

GPS measurement	20 Hz
GPS position	20 Hz
IMU measurement	100 Hz
INS solution	Up to 100 Hz

**Time Accuracy<sup>4</sup>** 20 ns RMS

**Max Velocity<sup>5</sup>** 515 m/s

## IMU PERFORMANCE<sup>6</sup>

### Gyroscope Performance

Gyro technology	FOG
Output range	±375°/s
Bias	20°/hr
Bias stability	±1°/hr
Scale factor	1500 ppm
Angular random walk	0.0667°/√hr (max)

### Accelerometer Performance

Range	±10 g
Bias	50 mg
Bias stability	±0.75 mg
Scale factor	4000 ppm

## PHYSICAL AND ELECTRICAL

### Dimensions

152 x 168 x 89 mm

### Weight

2.28 kg

### Power

Power consumption	16 W max
Input voltage	+9 to +18 VDC

### Antenna Port Power Output

Output voltage	+5 VDC
Maximum current	100 mA

### Connectors

Power and I/O	MIL-DTL-38999 Series 3
Antenna Input	TNC Female

## COMMUNICATION PORTS

RS-232 UART COM	2
USB Device	1
CAN	1
Event Input Trigger	1
Configurable PPS	1

## ENVIRONMENTAL

### Temperature

Operating	-40°C to +65°C
Storage	-50°C to +80°C

**Humidity** 95% non-condensing

### Waterproof

MIL-STD-810F, 506.4, Procedure I

## INCLUDED ACCESSORIES

- Combined I/O and power cable

## OPTIONAL ACCESSORIES

- GPS-700 series antennas (dual-frequency required)
- ANT series antennas (dual-frequency required)
- RF cables—5, 10 and 30 m lengths
- Inertial Explorer post-processing software

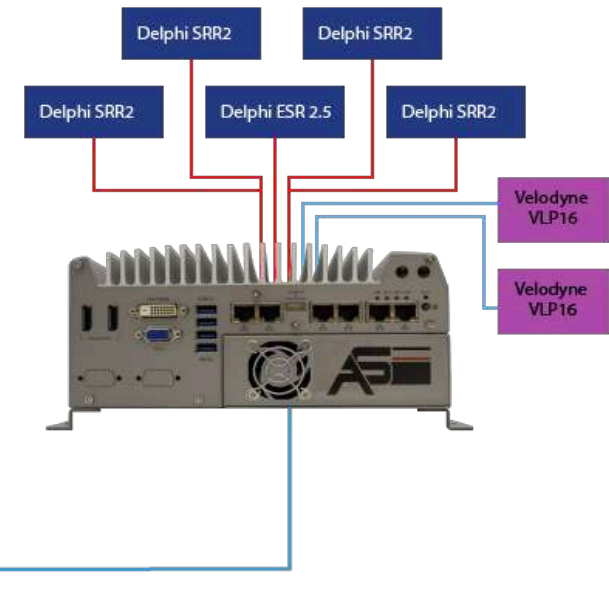
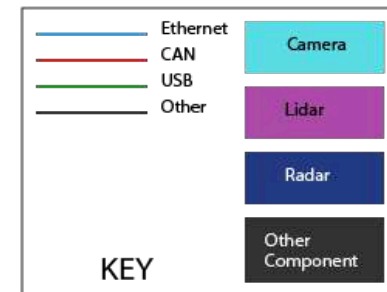
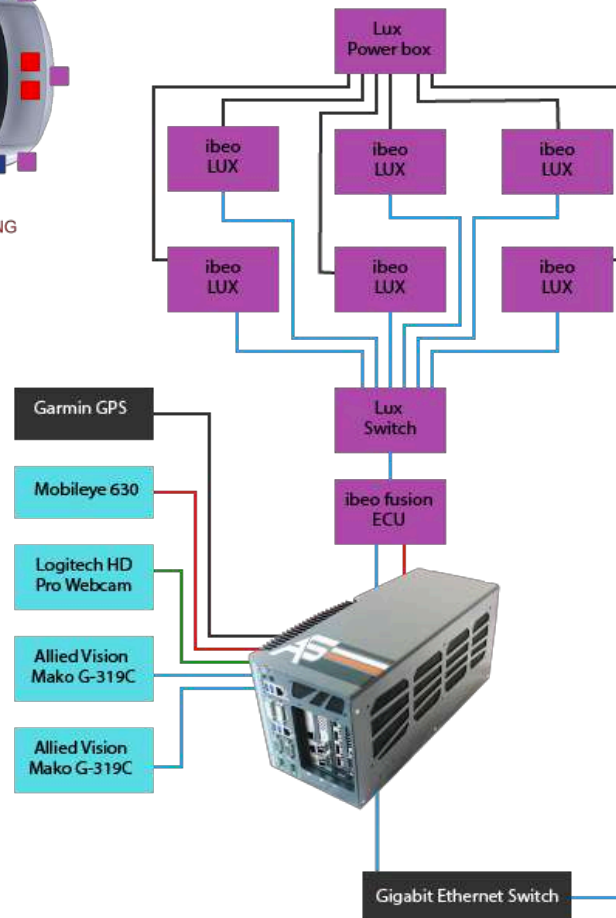
### Optional Dual Antenna<sup>7</sup>

Baseline	Accuracy
0.5 m	0.4°
1.0 m	0.2°
2.0 m	0.1°



# Vehicle Sensors

- Perception kit configuration example



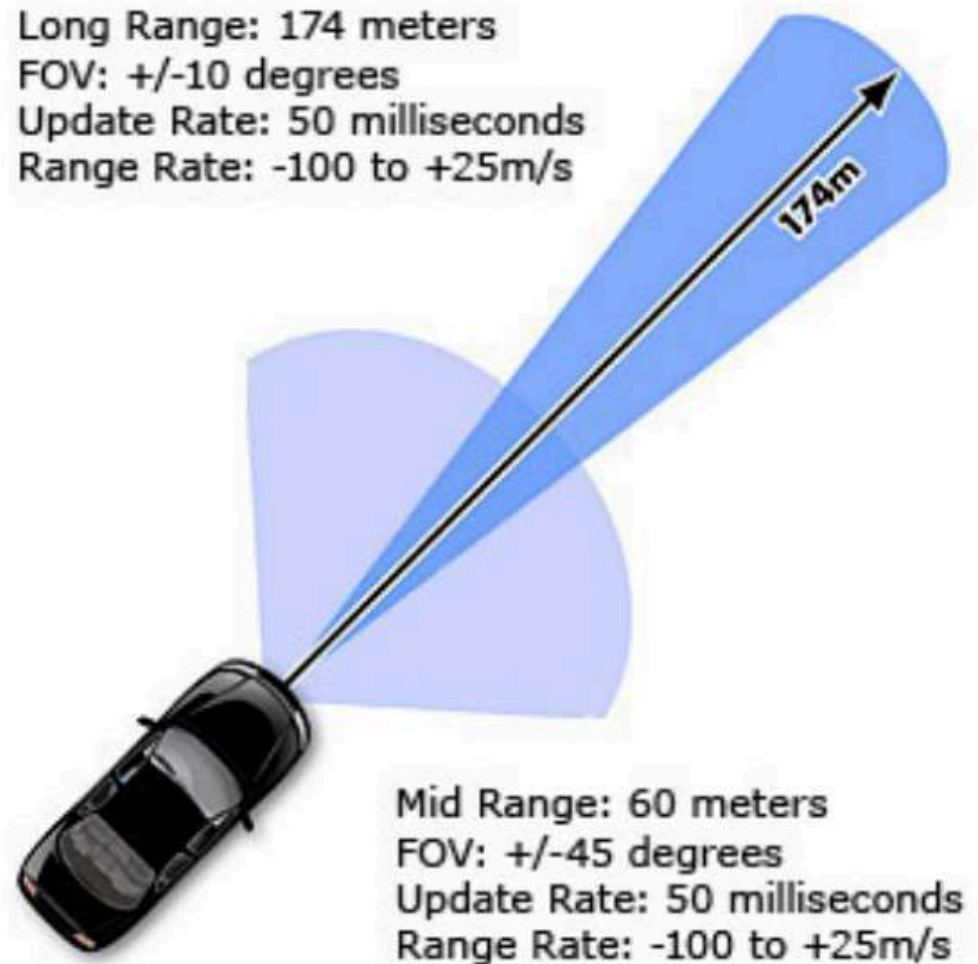


# Vehicle Sensors

- Delphi ESR 2.5 Radar

- DEL-ESR-2.5  
-24VDC+

- Delphi's multimode  
Electronically  
Scanning  
RADAR (ESR)

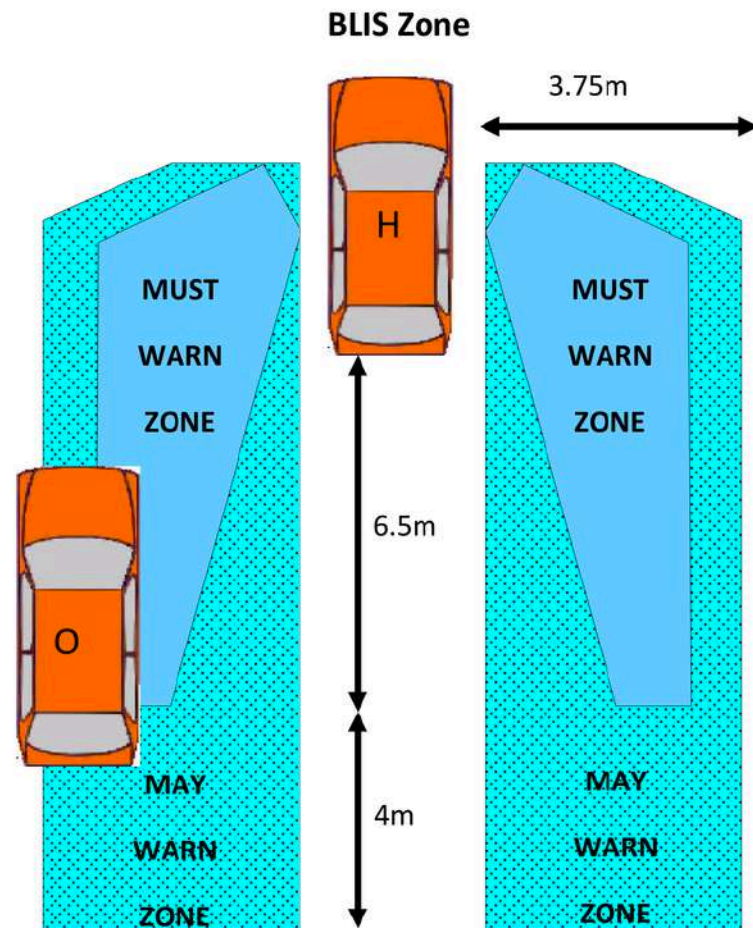
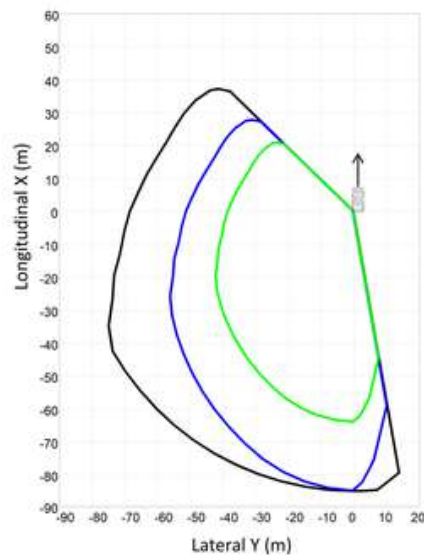
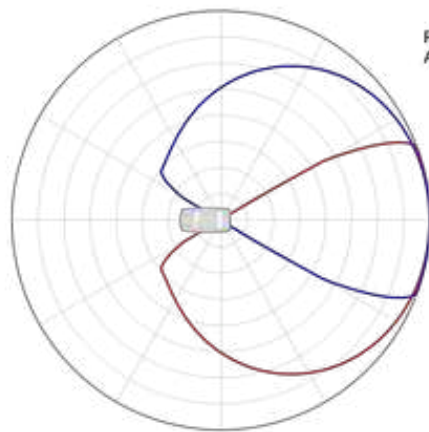






# Vehicle Sensors

- Delphi SRR2 Rear & Side Radar



# Vehicle Sensors

- ibeo "IBE-1000003-LUX+" LiDAR
- Range up to 200m/650ft
- Object tracking (up to 65 objects)

LASER / OPTICAL	ibeo LUX 4L	ibeo LUX 8L	ibeo LUX HD
Laser class:	Class 1		
Wave length:	905 nm		
Technology:	Time of flight, Output of distance and echo pulse width		
Range:	50 m / 164 ft @ 10% remission	50 m / 164 ft @ 10% remission	30 m / 98 ft @ 10% remission
Horizontal field of view:	110° (50° to -60°)		
Vertical field of view:	3.2°	6.4°	3.2°
Multi-layer:	4 parallel scanning layers	8 layers (2 pairs of 4 layers)	4 parallel scanning layers
Multi echo:	Up to 3 distance measurements per shot (allow measurements through atmospheric clutter like rain and dust)		
Data update rate:	25.0 Hz		









# Vehicle Sensors

- Mobileye "MBL-630-CAM-KIT+"
  - EyeQ2® Image Processing SOC
  - EyeWatch® display
  - 2 seconds ahead warning:
    - Forward Collision
    - Pedestrian & Cyclist Collision

Item	Description	Value
Signals Cables	Car inputs	BAT+, GND, Ignition, High Beam, CAN-Bus (High/Low)
Voltages	Input	12 - 36VDC
	Current Load (full operation)	12v > 360mA, 24v > 180mA**
	Stand-by Current Load (Ignition off)	12v > 10µA, 24v > 10µA
	Power consumption	Nominal 5.2W



-  Forward Collision Warning
-  Pedestrian and Cyclist Collision Warnings
-  Lane Departure Warning
-  Headway Monitoring and Warning
-  Intelligent High-Beam Control \*
-  Speed Limit Indication



# Vehicle Sensors

- Allied Vision "AVT-MAKO-G-319C+" Camera

- Mono and Color modes

- Global Shutter

V.S. rolling shutter?

- Auto exposure

- Gamma correction

Interface	IEEE 802.3 1000BASE-T, IEEE 802.3af (PoE)
Resolution	2064 (H) × 1544 (V)
Sensor	Sony IMX265
Sensor type	CMOS
Sensor Size	Type 1/1.8
Cell size	3.45 μm x 3.45 μm
Lens mount	C-Mount
Frame rate	37.5 fps
ADC	12 Bit
Image buffer (RAM)	64

# Vehicle Sensors - Perception

- Velodyne "VEL-VLP-16+" LiDAR

- 16 Channels
  - Measurement Range: 100 m
  - Range Accuracy: Up to  $\pm 3$  cm (Typical) 1
  - Field of View (Vertical):  $+15.0^\circ$  to  $-15.0^\circ$  ( $30^\circ$ )
  - Angular Resolution (Vertical):  $2.0^\circ$
  - Field-of-View (Horizontal):  $360^\circ$
  - Angular Resolution (Horizontal/Azimuth):  $0.1^\circ - 0.4^\circ$
  - Rotation Rate: 5 Hz – 20 Hz
- 
- 3D LiDAR Data Points Generated:
    - - Single Return Mode: ~300,000 points per second
    - - Dual Return Mode: ~600,000 points per second





# Summary

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- Signal
- Noise
- Time-domain Analysis
- Frequency-domain Analysis
- Signal processing filter design
- Electromagnetic spectrum
- Vehicle sensors (perception)

END, Thank you



# Reference

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- Smith, Steven W. "The scientist and engineer's guide to digital signal processing." (1997): 35.
- Digital Signal Processing and Analysis, Lecture Notes, The University of Michigan, Jeffrey A. Fessler.
- Introduction to Electronics, Signals, and Measurement, Lecture Notes, Massachusetts Institute of Technology, Manos Chaniotakis and David Cory.



# Appendix Related Resource

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- [The Scientist and Engineer's Guide to DSP](#)
- [Vehicle Environment Sensing \(Perception\)](#)
- [Signals & Systems Series](#) (Video)
- [Fourier Transform - A visual introduction](#) (Video)
- [Signal Processing and Machine Learning Techniques for Sensor Data Analytics in Matlab](#) (Video)
- [Signal Processing - create A Digital Filter in Python](#) (Video)
- [Automotive Sensors](#) (Video)