Modeling ice-shelf cavities using Lagrangian elements

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Key Points:

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4 Abstract.

Iceberg calving is an important feature of the Antarctic environment, and accounts for approximately half of Antarctic ice-shelf decay. However, despite its importance, the current generation of ocean models are unable to represent iceberg calving in a physically realistic way. This is because curent models of ice-shelf cavities represent the ice shelf on an static Eularian grid, which does not lend itself to modeling drifting icebergs. In this study we develop a new ice-shelf cavity model where the ice shelf is represented on 11 a 'Lagrangian grid'. In this model, the ice shelf is constructed out of Lagrangian elements which are bonded together by numerical bonds. This Lagrangian 13 framework allows for large pieces of the ice shelf to break away and become tabular icebergs. We test the model by simulating the circulation within a (static) idealized ice-shelf cavity, which was developed as part of the Marine Ice Ocean Modeling Inter-comparison Project (MISOMIP). We then com-17 pare the results to a second simulation that uses an Eularian ice shelf with an otherwise identical configuration. Results show that the Lagrangian and Eularian models are almost indistinguishable. The similarly between the Eularian and Lagrangian models provides a proof of concept for the Lagrangian model, and means that we can confidently use this model to extend the capabilities of the Eularian model.

1. Introduction

Floating ice shelves cover vast regions of the Antarctic polar oceans. These massive platforms of ice extend deep into the water column, applying large pressures to surface of the ocean, which is often hundreds of meters below global sea level. Beneath the ice shelves, both the bottom topography and the ice-shelf geometry play a role in steering ocean currents [Nicholls , 1996; Jenkins et al , 2010; Stern et al , 2014]. The topographic constraint imposed by the ice shelf at the ocean's upper boundary significantly affects the circulation within the ice-shelf cavities, and gives the ocean in this region a unique character.

Satellite observations suggest that ice-shelf decay occurs via two main processes: melting
and breaking [Depoorter et al , 2013; Rignot et al , 2013]. Each of these is responsible for
approximately half of the ice-shelf decay, and each influences the surrounding ocean (and
ice-shelf geometry) in a distinct way. Melting at the base of ice shelves causes freshwater
fluxes into the ice-shelf cavity. The input of buoyant meltwater creates rising density
plumes, which are guided along the ice-shelf base, and help drive ocean circulation beneath
the ice shelves [MacAyeal , 1984; Holland and Feltham , 2006]. Over time, melting at the
ice-shelf base can erode the ice shelf, gradually altering the ice-shelf geometry. In contrast,
ice-shelf breaking causes sudden changes to the ice-shelf geometry, and releases giant
icebergs into the ocean. After calving, these tabular icebergs can travel large distances
and impact ocean hydrography [Martin and Adcroft , 2010; Stern et al , 2015], sea-ice
formation [Robinson et al , 2012; Stern et al , 2016] and ocean biology [Smith et al , 2007;
Vernet et al , 2012; Biddle et al , 2015] many miles away.

In recent years society's need for improved projections of future sea level has lead to
an increased focus on the Antarctic mass balance, and hence, on modeling Antarctic subice-shelf cavities [Asay-Davis et al , 2016]. Modeling the ocean beneath the ice shelves
presents a unique set of challenges, since (i) the presence of ice shelves provides a rigid
upper boundary for the ocean model which is not encountered elsewhere in the ocean, and
(ii) melting and breaking ice shelves imply a changing ocean boundary conditions which
present numerous numerical difficulties.

The earliest models of ocean ice-shelf cavities were developed using static ice shelves with a fixed shape [Hellmer and Olbers , 1989; Determan and Gerdes , 1994; Grosfeld et al , 1997; Holland and Jenkins , 2001; Losch , 2008]. In these models, ice-shelf melting was represented through salinity and temperature fluxes, while the ice-shelf geometry remained unchanged. Later models of ice-shelf cavities allowed the ice-shelf geometry to evolve as the ice shelf melted, permitting the study of coupled ocean-ice phenomena [Gladish et al , 2012; Sergienko , 2013]. More recently, dynamic ice-shelf models have been coupled the ocean cavity, allowing the study of grounding line migration, which is of key importance for sea level rise projections [Grosfeld and Sandhger , 2004; Goldberg et al , 2012; De Rydt and Gudmundsson , 2016].

As far as we know, all models of ice-shelf cavities to date have omitted ice-shelf breaking
and iceberg detachment. This is because (i) there is much uncertainty of the physics that
govern ice-shelf breaking [Benn et all , 2007; Alley et al , 2008; Levermann et al , 2012;
Bassis and Jacobs , 2013], and (ii) current models of ice-shelf cavities represent the ice
shelves on a static Eularian grids, which do not lend themselves to modeling drifting
icebergs. In contrast, existing *iceberg* models represent icebergs as Lagrangian particles,

since this is a convenient way to model discrete objects traveling over large distances [Bigg et al , 1997; Gladstone et al , 2001; Martin and Adcroft , 2010; Marsh et al , 2015]. To date there has been no real effort to synthesize these two approaches (i.e.: to combine ice shelf and iceberg models).

In this study we develop a new ice-shelf cavity model where the ice shelf is represented 72 on a 'Lagrangian grid'. In this model, the ice shelf is constructed out of Lagrangian 73 elements which are bonded together by numerical bonds. This Lagrangian framework allows for large pieces of the ice shelf to break away and become tabular icebergs. Figures 1 and 2, which show a tabular iceberg drifting away an idealized ice shelf, demonstrate the enhanced capabilities of this Lagrangian model (see Stern et al [2017] for more details). 77 However, before analyzing the improved capabilities of the Lagrangian ice-shelf model, it is necessary to thoroughly test and benchmark the Lagrangian model in a more familiar configuration. To do this we compare the Lagrangian ice-shelf-cavity model to existing Eularian model in a static ice-shelf configuration. For this comparison, we use the model configuration developed as part of the Marine Ice Ocean Modeling Inter-comparison Project 82 (MISOMIP). The goals of this study are (i) to introduce and describe the Lagrangian ice-shelf model, and (ii) to prove that the Lagrangian model can replicate the behavior of an Eularian ice-shelf model when modeling static ice shelves. Demonstrating this is a prerequisite for moving beyond the capabilities of the Eularian model, and increases our confidence in more complex simulations involving calving icebergs.

2. Lagrangian model description

This section provides a brief description of the Lagrangian Tabular Iceberg Model (LTAM), which is used to construct the Lagrangian ice shelf used in this study. A detailed

description of the LTAM, including many of the technical details involved in constructing
the model, can be found in Stern et al [2017].

2.1. Lagrangian grid

The LTAM is a discrete element model (DEM) in that the objects of the model are
Lagrangian elements. Each Lagrangian element represents a mass of ice which is floating
in the ocean. The elements each have their own position, velocity, mass, and a set of
dimensions, which can evolve in time. Each element moves according to its own momentum equation which is solved in the (Lagrangian) reference frame of the element. The
elements are forced by oceanic, sea ice and atmospheric drag forces, as well as a force
due to sea surface height gradients and the Coriolis force. As the elements drift, they
decay according to melt parametrization. The elements can also be 'bonded' together
by numerical bonds, which hold the elements together and allow many elements to move
together as a unit. By bonding many ice elements together, the LTAM model is able to
form larger structures, such as tabular icebergs or (non-dynamic) ice shelves.

When constructing ice shelves using the LTAM model, the collection of elements can
be thought of as being a 'Lagrangian grid' for the ice shelf. In this Lagrangian grid, the
nodes (elements) can move at every time step, altering the shape of the ice shelf. This
is in contrast to the more traditional approach of modeling ice shelves on an Eularian
grid, where the grid is fixed in time. The major advantage of modeling ice shelves using a
Lagrangian grid is that the grid is not static, which means that we can simulate pieces of
ice breaking away from the ice shelf to form icebergs that drift in the open ocean (Figures
1, 2). One consequence of using Lagrangian elements for the ice-shelf grid is all variables

need to be interpolated from the 'Lagrangian grid' onto the Eularian ocean grid in order to be passed to the ocean model. The details of this interpolation are discussed below.

2.2. Interaction with the ocean

Since the LTAM model uses a Lagrangian grid, all of the ice shelf information is stored with the elements. At every time step, this information has to be interpolated from the Lagrangian grid to (Eularian) ocean grid, so that it can be passed to the ocean model. The interpolation from the Lagrangian grid to the Eularian ocean grid is done by assuming that the elements have surface areas that are shaped as regular hexagons. Element's properties are 'spread' from the Lagrangian grid to the Eularian grid by exactly calculating fraction of an elements surface area that is contained in each ocean grid cell, and dividing the element's properties between the ocean grid cell in proportion to that fraction.

Five fields are 'spread' from the Lagrangian to Eularian grids at each time step: mass, surface area, temperature flux, salinity flux and mass flux. Once these five fields are in hand, the LTAM mode interacts with the ocean model in exactly the same way the Eularian model does. As in Eularian ice-shelf models, these fields are passed to the ocean model and are used to: (i) apply a pressure to the ocean surface, (ii) alter the upper-ocean boundary condition to reflect that the ocean is covered by ice, and (iii) apply salt, temperature and mass fluxes associated with ice-shelf melting and freezing.

The ocean is sensitive to small changes to the ocean surface pressure, which can trigger
barotropic ocean waves. This means that accurately interpolating fields from the Lagrangian to Eularian grids is the key to making the Lagrangian ice-shelf model behave
like the Eularian ice-shelf model for using static ice-shelf simulations. Ocean mixed layer
properties are passed from ocean model to the LTAM model, and are interpolated onto

the elements using a bilinear interpolation. The model is less sensitive to the details of this interpolation.

3. Experiment Setup

The LTAM model is used to simulate the flow within an idealized ice-shelf cavity.

The simulations are repeated using an Eularian ice shelf with an identical configuration.

The details of the experimental setup for both the Lagrangian and Eularian models are

3.1. Domain configuration

presented here.

- In order for our simulations to be easily comparable to previous models of ice-shelf cavities, we use an experimental setup based on the configuration created for the Marine Ice Ocean Modeling Inter-comparison Project (MISOMIP) [Asay-Davis et al , 2016]. The MISOMIP configuration was developed as a standardized configuration to allow for a comparison between various ocean-ice coupled models. The configuration consists of an idealized ice shelf in a rectangular domain $L_x = 80 \text{km}$ long and $L_y = 480 \text{km}$ wide. The ice shelf is grounded on the southern side of the domain with the ice-shelf front at y=650km. The ice thickness and bottom topography of this setup are shown in Figure 3a and 3b respectively, with the grounding line position drawn in for reference. The configuration is the same as that of the Ocean0 setup in the MISOMIP, with three changes made:
- 1. The 'calving criteria' used in the MISOMIP study (which states that all points in the ice shelf with thickness less than 100m are set to zero thickness) has not been used.
- 2. The ice shelf has been thickened on the flanks of the domain, so that the latitude of the grounding line increases away from the center of the ice shelf.

3. The ice shelf is configured to be symmetric about its meridional center line $(x = \frac{L_x}{2})$.

This was achieved by using the average of the left and right flanks of the ice-shelf thickness.

These three changes were made in order to make the circulation beneath the ice shelf easier to interpret.

3.2. Ocean Model

The Lagrangian and Eularian ice shelves are coupled to the MOM6 ocean model [Hall-157 berg et al, 2013. The ocean model is run in using vertical coordinate system which is 158 a hybrid between a sigma-level and a z-level coordinate, achieved using ALE regridding-159 remapping scheme [White et al., 2009]. In this vertical coordinate, model layers bend underneath surface topography (i.e.: the ice shelf), as they would in a sigma coordinate 161 model, and intersect the bottom topography, as they would in a z-coordinate model. The model has 72 vertical layers and has a horizontal resolution of $\Delta x = 2$ km. The numerical 163 simulations were all repeated using an isopycnal coordinate (without ALE regrinding-164 remapping). The results were qualitatively similar to the ALE results. All results pre-165 sented below are from the ALE simulations, unless specified otherwise. 166 Ocean parameters are shown in Table 1 and are specified in the MISOMIP configuration 167

[Asay-Davis et al , 2016]. The simulation is initialized from rest, with horizontally uniform initial ocean temperature and salinity profiles which vary linearly between specified surface and bottom values: $T_{top} = -1.9^{\circ}\text{C}$, $T_{bottom} = 1.0^{\circ}\text{C}$, $S_{top} = 33.8$ psu, $S_{bottom} = 34.7$. The maximum ocean depth is $H_{ocean} = 720$ m. A sponge layer is used on the northern boundary, which relaxes back to the initial temperature and salinity with a relaxation time scale of $T_{sponge} = 0.1$ days. Melting is set to zero for ocean cells where the ocean column thickness is less than 10m.

3.3. Lagrangian ice-shelf simulations:

The Lagrangian ice shelf is created using 10882 Lagrangian hexagonal elements with sides of length S=0.98 km. The positions of the hexagonal elements are initialized by packing them together in a space-filling staggered lattice. Gaps along the boundaries are filled in using smaller elements so that the total ice-shelf area is preserved. The initial mass of the ice elements is determined by a preprocessing inversion step, which is the inverse of the 'mass-spreading' interpolation procedure discussed in Section 2.2.

3.4. Eularian ice-shelf simulations:

The Eularian ice-shelf simulation is performed using an existing Eulerian ice-shelf cavity model [Goldberg et al, 2012], which is an optional module of the MOM6 ocean model.

The ice shelf is initialized on the same grid as the ocean model with a horizontal resolution of $\Delta x = 2$ km. The ice-shelf thickness field is using the same ice-shelf draft used for the Lagrangian model (Figure 3b).

3.5. ice-shelf motion and decay

The melt rates in both the Lagrangian and Eularian ice-shelf simulations are calculated using the 3 equation model for ice-shelf decay [Holland and Jenkins, 1999]. In both experiments the ice shelf is held stationary. In the Eularian code, this is achieved by setting the ice-shelf velocity to zero, while in Lagrangian ice shelf, the element velocities are set to zero. In both simulations, the ice shelf is thermodynamically active and is able to 'melt' but has a constant thickness (as specified in the Ocean0 experiment in the MISOMIP [Asay-Davis et al., 2016]). In this setup, ice-shelves melting generate temperature and salinity fluxes into the ocean, but do not change the thickness of the ice

shelf / ice elements. This can be thought to represent an ice shelf in dynamic equilibrium
where the melt is exactly balanced ice-shelf advection. The models are spun up for 5
years, and results are considered after the spinup period.

4. Results

4.1. Results from the Lagrangian ice-shelf simulation

The results from the Lagrangian ice-shelf simulation fit within the current understanding 197 of ice-shelf cavity circulations based on ice-shelf observations [MacAyeal, 1984; Lewis and 198 Perkin, 1986; Jacobs et al., 2011] and previous modeling efforts [Determan and Gerdes 199 1994; Holland and Feltham, 2006; Losch, 2008]. The initial water temperatures inside 200 the domain are warmer than the in-situ freezing point, and cause melting at the ice-shelf 201 base. The melt water entering the domain is more buoyant than the water around it, 202 and rises along the ice shelf as a cool fresh plume (Figure 4b, c). As the plume rises, it entrains ambient water causing a warming of the upper ocean (Figure 4b). This injection 204 of positive buoyancy at depth drives a clockwise circulation outside of the ice-shelf cavity (Figure 6a), providing the ice-shelf cavity with a continuous supply of warm water, which 206 provides the thermal energy required for continuous ice-shelf melt. The highest melt rates are observed within 100km of the grounding line (Figure 5a). 208 These elevated melt rates are caused by the presence of warm water (Figure 5d) and 209 increased ocean velocities (Figure 5c) near the grounding line, as well as the fact that

freezing point of ice decreases with increasing pressure. Elevated melt rates are also seen

February 24, 2017, 2:57pm

near the ice front, caused by strong currents running along the ice-shelf front.

211

4.2. Comparison of Lagrangian and Eularian ice-shelf models

The LTAM results from the static ice-shelf experiment are qualitatively similar to most 213 of the simulations from the MISOMIP experiment [Asay-Davis et al., 2016], which use 214 a similar configuration. To get a quantitative comparison, we compare the Lagrangian ice-shelf model results to a simulation using an Eulerian ice-shelf model with an identical 216 configuration. The results show that two simulations are almost indistinguishable. This 217 is the case both for simulations using the ALE-hybrid vertical coordinate system and the isopycnal vertical coordinate. The Lagrangian and Eularian models are have very similar 219 circulations (Figures 6), melt rates (Figures 7) temperature/salinity profiles (Figures 8). The differences between the barotropic stream functions of the two simulations (for exam-221 ple), are two orders of magnitude smaller than the differences between two simulations using the same Eularian ice shelf with different vertical coordinate systems (Figures 6 and 223 9). 224 The good agreement between the Eularian and Lagrangian simulations is not too sur-225 prising since the two models are coupled to the same ocean model in exactly the same 226 configuration. Recall that the role of the ice-shelf model in these simulations is to (i) apply a pressure to the ocean surface, (ii) provide melt fluxes to the ocean, and (iii) alter 228

prising since the two models are coupled to the same ocean model in exactly the same configuration. Recall that the role of the ice-shelf model in these simulations is to (i) apply a pressure to the ocean surface, (ii) provide melt fluxes to the ocean, and (iii) alter the upper ocean boundary condition below the ice shelf. The agreement between the Eularian and Lagrangian simulations is a confirmation that these three tasks are being done correctly within the LTAM model, and that the LTAM is able to model sub-ice-shelf cavities as well as the Eularian model does. This is a good starting point for moving beyond the capabilities of the Eularian model.

5. Conclusion

This study presents a new Lagrangian framework for modeling sub-ice-shelf cavities.

In this framework, the ice shelf is constructed out of many Lagrangian elements, which
are bonded together by numerical bonds. The collection of Lagrangian elements can
be thought of as being a Lagrangian grid, which stores the ice-shelf properties. Unlike
Eularian grids, the nodes (elements) can move at every time step, altering the shape of
the ice shelf. This allows us to use the Lagrangian ice-shelf model to large pieces of the
ice-shelf breaking away from the ice shelf to becoming tabular icebergs that are fully
embedded in the ocean (Figures 1 and 2). This capability is currently not possible using
more traditional Eularian models [Stern et al , 2017].

The present study focuses on using the Lagrangian ice shelf to model static ice shelves.

The model is demonstrated by modeling the circulation beneath a (static) idealized ice

shelf, which was developed as part of the MISOMIP inter-comparison project. The re
sults from the Lagrangian ice-shelf model fit within our paradigm of understanding for

circulation within ice-shelf cavities: buoyant meltwater that enters the ice-shelf cavity

drives freshwater plumes at the ice-shelf base, which drives the circulation within the

cavity. The circulation, melt rates and ocean hydrography achieved using the Lagrangian

ice shelf compare well with other simulations in the MISOMIP experiments.

A direct comparison comparison between one Lagrangian and Eularian ice-shelf models
showed that the results are extremely similar, and differences between the Lagrangian
and Eularian ice shelves models (resulting from interpolation errors) are much smaller
than the differences observed when changing the ocean vertical coordinate system (for
example). Achieving similarity between when using a Lagrangian and Eularian ice-shelf

- $_{256}$ model in the same static ice-shelf configuration is a prerequisite developing more advanced
- Lagrangian ice-shelf models and represents a good benchmark test for new Lagrangian
- ice-shelf models.

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6. New Figure ideas:

- 1) Combine Figure 1 and Figure 2 into a new figure (so that this paper uses different figures to the tabular iceberg paper)
- 2) Figure showing the layout of hexagons, which is different to the tabular iceberg paper perhaps have hexagons directly over ice shelf draft?
- 3) Combine the barotropic stream function figure for layered into one figure.

7. Things to think about:

1) The dynamics of the ice elements are not related to ice shelf dynamics. This needs to be explained somehow/somewhere.

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411

414

DRAFT

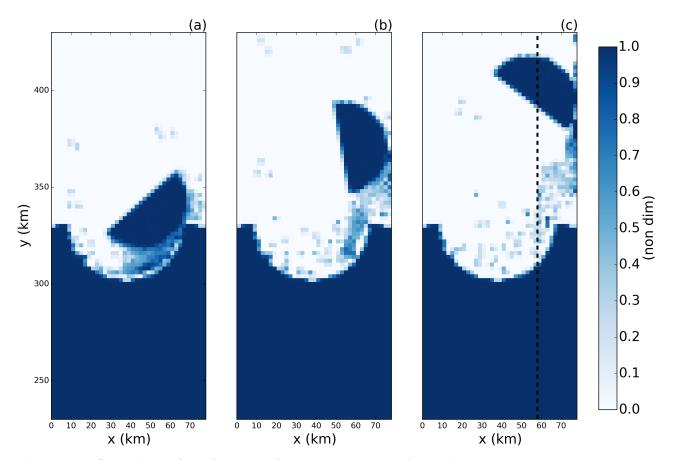


Figure 1. Snapshots of the fraction of ice cover in the LTAM tabular iceberg calving simulation. Snapshots are taken (a) 7, (b) 15, and (c) 30 days after calving. The dashed line in panel (c) shows the location of the vertical transects shown in Figure 2.

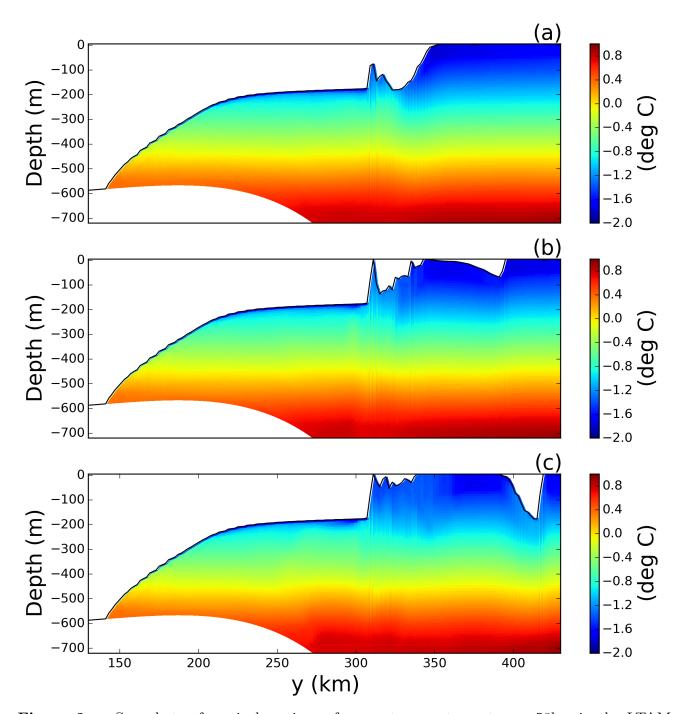


Figure 2. Snapshots of vertical sections of ocean temperature at x = 58km in the LTAM tabular iceberg calving experiment. Snapshots are taken (a) 7, (b) 15, and (c) 30 days after calving. The position of the vertical transects is shown by the dashed lines in Figure 1c.

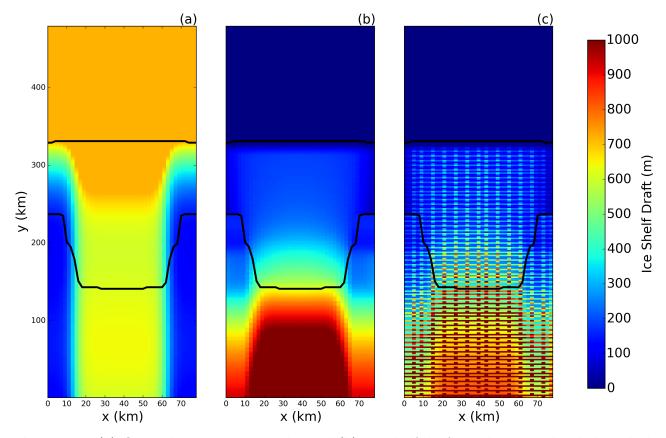


Figure 3. (a) Ocean bottom topography and (b) ice-shelf draft used to initialized the tabular iceberg calving simulation. The ice draft is calculated from the total mass in an ocean grid cell after the mass-spreading interpolation has been applied (as explained in Section 2.2). (c) Initial ice draft that would be calculated if the mass-spreading interpolation were not used (i.e.: elements treated as point masses).

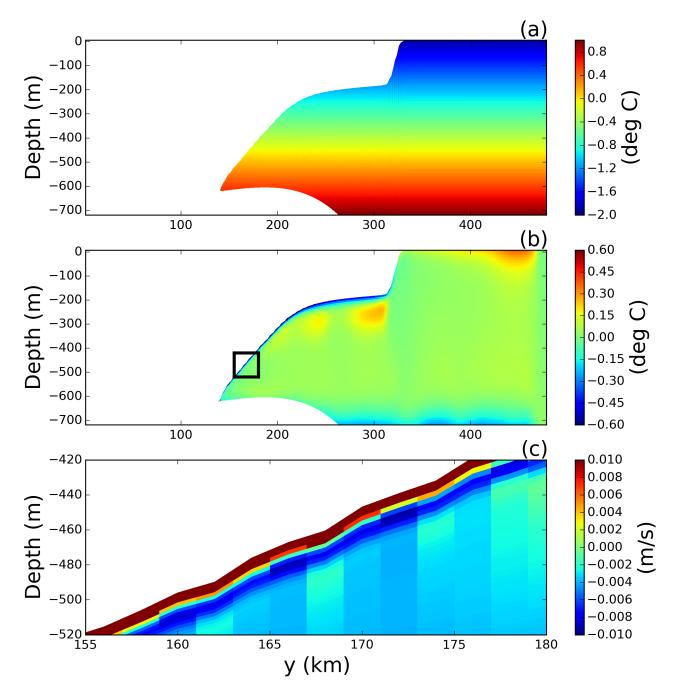


Figure 4. Results of the static ice-shelf experiment using the LIISM model coupled to MOM6. Panels show cross sections of the (a) initial temperature field, (b) temperature anomaly after 5-years (relative the the initial field), and (c) meridional velocity near the ice-shelf base after 5 years of simulation. The region shown in panel (c) is indicated by the black box on panel (b),

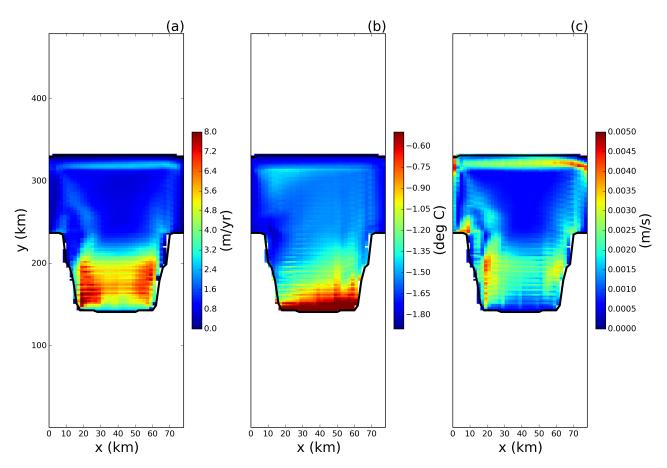


Figure 5. Results of the static ice-shelf experiment using the LIISM model coupled to MOM6. The three panels show 5 year time average of the (a) melt rate, (b) top-of-ocean and (c) frictional velocity, u^* , at the base of the ice shelf. Fields are only shown in regions where the ice area fraction is ≥ 0.8 .

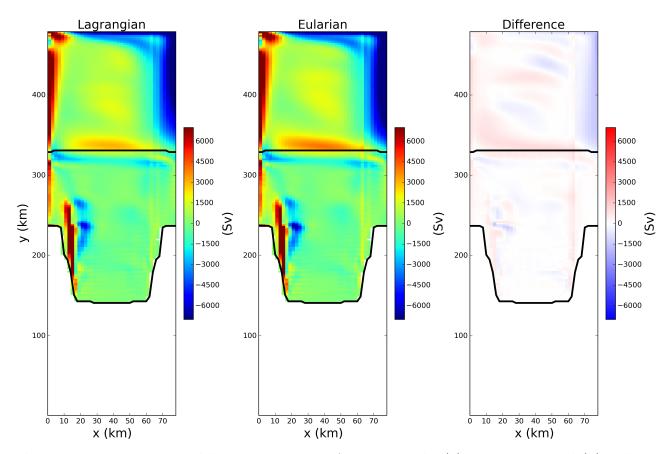


Figure 6. Time-averaged barotropic stream function in the (a) Lagrangian and (b) Eularian simulations in the static ice-shelf configuration. Panel (c) shows the difference between panels (a) and (b). The time averages are taken over 5 years of model time, beginning at the end of the 5 year spin up period.

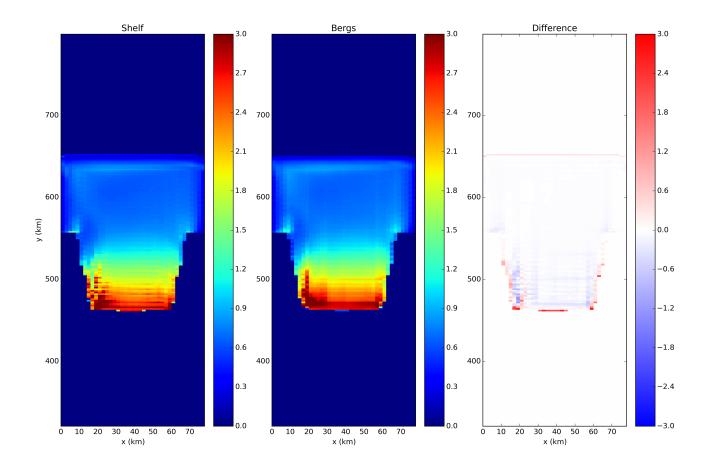


Figure 7. Comparison of Eulerian ice-shelf model and Lagrangian Ice shelf model melt fields.

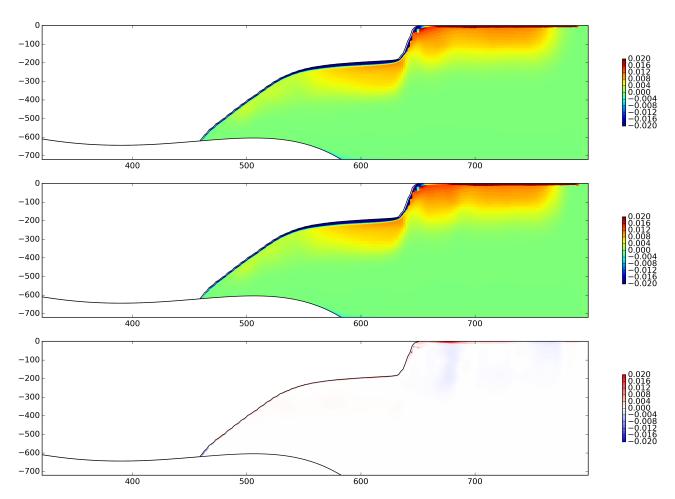


Figure 8. Comparison of Eulerian ice-shelf model and Lagrangian ice-shelf model salinity fields.

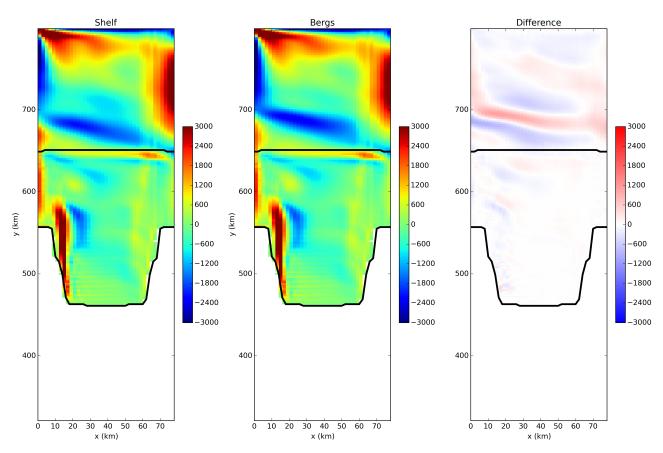


Figure 9. Layer: Comparison of Eulerian ice-shelf model and Lagrangian ice-shelf model barotropic stream function

Parameter	Symbol	Value	Unit
Domain Length	L_x	80	km
Domain Width	L_y	480	km
Horizontal Resolution	Δx	2	km
Number of vertical layers	N_l	72	non-dim
Horizontal Viscosity	$ u_H$	6.0	$\frac{m^2}{s}$
Diapycnal Viscosity	$ u_V$	10^{-3}	$\frac{m^2}{s}$
Horizontal Diffusivity	ϵ_H	1.0	$\frac{\frac{m^2}{m^2}}{\frac{m^2}{s}}$ $\frac{m^2}{\frac{m^2}{s}}$ oC
Diapycnal Diffusivity	ϵ_V	5×10^{-5}	$\frac{m^2}{s}$
Initial Surface Temperature	T_t	-1.9	${}^o\!C$
Initial Bottom Temperature	T_b	1.0	^{o}C
Initial Surface Salinity	S_t	33.8	psu
Initial Bottom Salinity	S_b	34.7	psu
Maximum Ocean depth	H_{ocean}	720	\mathbf{m}
Relaxation Time of Sponge Layer	T_{sponge}	0.1	days
Time Step for Static Shelf Experiment	dt_{Static}	1000	S
Time Step for Iceberg Calving Experiment	$dt_{Calving}$	10	S

8. Supplementary Figures