**User Manual for the  
Discrete Dipole Approximation Code  
ADDA** **1.4.0-alpha**

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Abstract

This manual describes the open-source code ADDA, which simulates elastic light scattering from finite 3D objects of arbitrary shape and composition, either in free space or near the plane surface. Besides standard sequential execution, ADDA can run on a multiprocessor system, using MPI (message passing interface), parallelizing a *single* DDA calculation. Hence the size parameter of the scatterer, which can be accurately simulated, is limited only by the available size of the supercomputer. However, if the refractive index is large compared to 1, computational requirements significantly increase. Moreover, ADDA can effectively employ modern GPUs (video cards) to accelerate computations.

ADDA is written in C99 (using routines in Fortran and C++) and is highly portable. It provides full control over the scattering geometry (particle morphology and orientation, incident beam) and allows one to calculate a wide variety of integral and angle-resolved scattering quantities (cross sections, the Mueller matrix, dipole decay rate enhancement, etc.). Moreover, ADDA incorporates a range of state-of-the-art DDA improvements, aimed at increasing the accuracy and computational speed of the method. This manual explains in details how to perform electromagnetic scattering calculations using ADDA, discussing both physical and computational aspects.

This manual can be cited as:

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The source of this manual in Microsoft Word format is available at

<https://github.com/adda-team/adda/raw/v1.4.0/doc/manual.docx> (NOT YET)

Parts of this manual were published in [1]. Please consider citing it instead of the manual.

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# Introduction

The discrete dipole approximation (DDA) is a general method to calculate scattering and absorption of electromagnetic waves by particles of arbitrary geometry. In this method the volume of the scatterer is divided into small cubical subvolumes (“dipoles”). Dipole interactions are approximated based on the integral equation for the electric field [2]. Initially the DDA (sometimes referred to as the “coupled dipole approximation”) was proposed by Purcell and Pennypacker [3] replacing the scatterer by a set of point dipoles (hence the name of the technique). Although the final equations are essentially the same, derivations based on the integral equations give more mathematical insight into the approximation, while the model of point dipoles is physically clearer. For an extensive review of the DDA, including both theoretical and computational aspects, the reader is referred to [2]and references therein.

ADDA is a C implementation of the DDA. The development was conducted by Hoekstra and coworkers [4–7] since 1990 at the University of Amsterdam. From the very beginning the code was intended to run on a multiprocessor system or a multicore processor (parallelizing a *single* DDA simulation).[[1]](#footnote-1) The code was significantly rewritten and improved by Yurkin [8], also at the University of Amsterdam, and publicly released in 2006. Since then ADDA is the open-source code developed by an international team.[[2]](#footnote-2) Originally coined “Amsterdam DDA”, the code name has been officially abbreviated to reflect this change.

ADDA is intended to be a versatile tool, suitable for a wide variety of applications ranging from interstellar dust and atmospheric aerosols to biological cells and nanoparticles; its applicability is limited only by available computer resources (§4). As provided, ADDA should be usable for many applications without modification, but the program is written in a modular form, so that modifications, if required, should be fairly straightforward.[[3]](#footnote-3)

This code is openly available to others in the hope that it will prove a useful tool. We ask only that:

* If you publish results obtained using ADDA, you should acknowledge the source of the code. A general reference [1] is recommended for that.[[4]](#footnote-4)
* If you discover any errors in the code or documentation, please submit it to the ADDA issue tracker.[[5]](#footnote-5)
* You comply with the “copyleft” agreement (more formally, the GNU General Public License v.3[[6]](#footnote-6)) of the Free Software Foundation: you may copy, distribute, and/or modify the software identified as coming under this agreement. If you distribute copies of this software, you must give the recipients all the rights which you have. See the file LICENSE distributed with the ADDA software.

We strongly encourage you to identify yourself as a user of ADDA by subscribing to adda-announce Google group;[[7]](#footnote-7) this will enable the developers to notify you of any bugs, corrections, or improvements in ADDA. If you have a question about ADDA, which you think is common, please look into the FAQ[[8]](#footnote-8) before searching for the answer in this manual. If neither of these helps, direct your questions to adda-discuss Google group.[[9]](#footnote-9) The archive of this group is available,[[10]](#footnote-10) so you may try to find an answer to your question before posting it. However, this also means that you should *not* include (potentially) confidential information in your message; in that case contact one of the developers directly. We also advise users, interested in different aspects of ADDA usage, to join this group and to participate in discussions initiated by other people.[[11]](#footnote-11)

# Using the Manual

This manual is intended to cover the computational and physical aspects of ADDA, i.e. choosing proper values for input parameters, performing the simulations, and analyzing the results. In particular, the succeeding sections contain instructions for:

* running a sample simulation (§3);
* defining a scatterer (§6) and its orientation (§8);
* specifying the type and propagation direction of the incident beam (§9);
* specifying the DDA formulation (§10);
* specifying what scattering quantities should be calculated (§11);
* understanding the computational aspects (§12) and timing of the code (§13);
* understanding the command line options (§A) and formats of input (§B) and output (§C) files.

A lot of technical aspects are covered by online wiki pages, which are extensively referred to throughout the manual. This manual assumes that you have already obtained the executable for ADDA. You can either download the full source code and compile it yourself,[[12]](#footnote-12) or download precompiled executables for Windows.[[13]](#footnote-13) Both source and executable packages of the recent release can be downloaded from <https://github.com/adda-team/adda/releases>.

If you want to use the latest features or track the development progress, you may download the recent source directly from the ADDA repository using web browser[[14]](#footnote-14) or any git client.[[15]](#footnote-15) Please mind, however, that the latest between-releases version may be unstable. If you decide to try it and discover any problems, comment on this in the issue tracker.5

Everywhere in this manual, as well as in input and output files, it is assumed that all angles are in degrees (unless explicitly stated differently). The unit of length is assumed µm; however, it is clear that it can be any other unit, if all dimensional values are scaled accordingly. However, scaling of units of radiation forces is more subtle (§11.6).

# Running ADDA

## Sequential mode

The simplest way to run ADDA is to type

adda[[16]](#footnote-16)

while positioned in a directory, where the executable is located. ADDA will perform a sample simulation (sphere with size parameter 3.367, refractive index 1.5, discretized into 16 dipoles in each direction) and produce basic output (§11, §C). The output directory and terminal output (stdout) should look like examples that are included in the distribution: sample/run000\_sphere\_g16\_m1.5 and sample/stdout respectively. ADDA takes most information specifying what and how to calculate from the command line, so the general way to call ADDA is

adda -<par1> <args1> -<par2> <args2> …

where <par> is an option name (starting with a letter), and <args> is none, one, or several arguments (depending on the option), separated by spaces. <args> can be both text or numerical. How to control ADDA by proper command line options is thoroughly described in the following sections; the full reference list is given in §A. If you prefer a quick hands-on start with ADDA before looking at all possible options, you are welcome to a tutorial.[[17]](#footnote-17) Quick help is available by typing

adda -h

For some options input files are required, they are described in §B. It is recommended to copy the contents of the directory input/ of the package (examples of all input files that are silently used) to the directory where ADDA is executed. All the output produced by ADDA is described in §C. Version of ADDA, compiler used to build it,[[18]](#footnote-18) width of memory access registers (32 or 64 bits), build options,12 and copyright information are available by typing

adda –V

## Parallel mode

On different systems MPI is used differently, you should consult someone familiar with MPI usage on your system. However, running on a multi-core PC is simple, just type

mpiexec –n <N> ./adda\_mpi …

where all ADDA command line options are specified in the end of the line, and <N> stands for the number of cores. Actually, <N> is the number of threads created by MPI implementation, and it should not necessarily be equal to the number of cores. However, this choice is recommended. MPICH2 allows one to force local execution of all threads by additionally specifying command line option ‑localonly after <N>. However, this may be different for other MPI implementations.

Running on a cluster is usually not that trivial. For example, on many parallel computers, PBS (portable batch system)[[19]](#footnote-19) is used to schedule jobs. To schedule a job one should first write a shell script and then submit it. An example of such PBS script is included in the distribution (sample/test.pbs). It is important to note that usually output of the batch job (both stdout and stderr) is saved to file. The name of the file usually contains the job id number given by the system. The same number appears in the directory name (§C.3).

Another batch system is SGE (Sun grid engine).[[20]](#footnote-20) We do not give a description of it here, but provide a sample script to run ADDA using SGE (sample/test.sge). One can easily modify it for a particular task.

## OpenCL (GPU) mode

This mode is very similar to the sequential mode, except ADDA executable is named adda\_ocl and part of the calculations is carried on the GPU [9]. Therefore a GPU, supporting double precision calculations, is required as well as recent drivers for it. Currently, ADDA can use only a single GPU, and will choose the first (default) one, if several GPUs are available. To use another GPU, specify its index (starting from zero) through the command line option

-gpu <index>

Therefore, several instances of adda\_ocl can be run in parallel, each using one CPU core and one GPU.

More details about the OpenCL implementation, including existing limitations are described in the corresponding wiki page.[[21]](#footnote-21) While the developers do their best to ensure reliability of OpenCL mode, it is a good idea to perform selected tests of this mode against the sequential mode on your specific hardware before performing a large set of simulations.

# Applicability of the DDA

## General applicability

The principal advantage of the DDA is that it is completely flexible regarding the geometry of the scatterer, being limited only by the need to use a dipole size *d* small compared to both any structural length in the scatterer and the wavelength *λ*. A large number of studies devoted to the accuracy of DDA results exist, e.g. [8,10–19]. Most of them are reviewed in [2]; here we only give a brief overview. The DDA is a “numerically exact” method, i.e. it can reach any required accuracy given sufficient computational resources. However, the required resources are not necessarily practically acceptable.

The rule of thumb for particles in free space with size comparable to the wavelength is: “10 dipoles per wavelength inside the scatterer”, i.e. size of one dipole is

|  |  |  |  |
| --- | --- | --- | --- |
| |  |  | | --- | --- | | , | (1) | |  |

where *m* is refractive index of the scatterer. That is the default for ADDA (§6.2). The expected accuracy of cross sections is then several percent (for moderate *m*, see below). With increasing *m* the number of dipoles that is used to discretize the particle increases; moreover, the convergence of the iterative solver (§12.1) becomes slower. Additionally, the accuracy of the simulation with default dipole size deteriorates, and smaller, hence more dipoles must be used to improve it. Therefore, it is accepted that the refractive index should satisfy

|  |  |
| --- | --- |
| . | (2) |

Larger *m* *can* also be simulated accurately. In that case, however, the required computer resources rapidly increase with *m*. Fortunately, state-of-the-art DDA formulations (§10) can alleviate this problem and render larger refractive indices accessible to DDA simulations. Note however that the application of the DDA in this large-*m* regime is investigated much less thoroughly than for moderate refractive indices, and therefore warrants further studies.

When considering larger scatterers (volume-equivalent size parameter *x* > 10) the rule of thumb still applies. However, it does not describe well the dependence on *m*. When employing the rule of thumb, errors do not significantly depend on *x*, but do significantly increase with *m* [8]. However, simulation data for large scatterers is also limited; therefore, it is hard to propose any simple method to set dipole size. The maximum reachable *x* and *m* are mostly determined by the available computer resources (§5).

The DDA is also applicable to particles smaller than the wavelength, e.g. nanoparticles. In some respects, it is even simpler than for larger particles, since many convergence problem for large *m* are not present for small scatterers. However, in this regime there is an additional requirement for *d* – it should allow for an adequate description of the shape of the particle. Although this requirement is relevant for any scatterers, it is usually automatically satisfied for larger scatterers by Eq. (1). For instance, for a sphere (or similar compact shape) it is recommended to use at least 10 dipoles along the smallest dimension, no matter how small is the particle. Smaller dipoles are required for irregularly shaped particles and/or large refractive index. The accuracy of the DDA for gold nanoparticles was studied in [20].

To conclude, it is hard to estimate *a priori* the accuracy of DDA simulation for a particular particle shape, size, and refractive index, although the papers cited above do give a hint. If one runs a single DDA simulation, there is no better alternative than to use rule of thumb and hope that the accuracy will be similar to that of the spheres, which can be found in one of the benchmark papers (e.g. [8,13,18]). However, if one plans a series of simulations for similar particles, especially outside of the usual DDA application domain [Eq. (2)], it is highly recommended to perform an accuracy study. For that one should choose a single test particle and perform DDA simulations with different *d*, both smaller and larger than proposed by the rule of thumb. The estimate of *d* required for a particular accuracy can be obtained from a variation of results with decreasing *d*. You may also make the estimation much more rigorous by using an extrapolation technique, as proposed by Yurkin *et al.* [21] and applied in [20,22,23].

Finally, it is important to note that the price paid for versatility of the DDA is its large computational costs, even for “simple” scatterers. Thus, in certain cases other (more specialized) methods will clearly be superior to the DDA. A review of relevant comparative studies is given in [2]. Additionally, it was recently shown that the DDA performs exceptionally well for large index-matching particles (e.g. biological cells in a liquid medium). In this regime the DDA is 10 to 100 times faster than a (general-purpose) finite-difference time-domain method when required to reach the same accuracy [22], and is comparable in speed to the discrete sources method for red blood cells [24], where the latter method explicitly employs the axisymmetry of the problem.

## Extensions of the DDA

In its original form the DDA is derived for finite particles (or a set of several finite particles) in vacuum. However, it is also applicable to finite particles embedded in a homogeneous non-absorbing dielectric medium (refractive index *m*0). To account for the medium one should replace the particle (and environment) refractive index *m* by the relative refractive index *m*/*m*0, and the wavelength in the vacuum *λ* by the wavelength in the medium *λ*/*m*0. All the scattering quantities produced by DDA simulations with such modified *m* and *λ* are then the correct ones for the initial scattering problem. The only exception is the radiative force per each dipole which should be additionally scaled in the presence of the medium (see §11.6).

While ADDA can handle particles near an infinite surface (§7), it is not directly applicable to other infinite environments, such as multi-layer substrates, waveguides, or particles crossing the infinite surface. However, a number of approximate methods are still available:

* One could consider the environment only by its influence on the incident field; let us denote the modified incident field as . This may be accurate enough if the particle is far from the elements of the environment (e.g., boundary of the substrate) and/or the refractive index of the environment is close to unity. Field  need then to be given to ADDA through a file (§9.2).
* Another approach is to take a large computational box around the particle, and explicitly discretize the environment that falls into it [25]. This is rigorous in the limit of infinite size of computational box, but requires much larger computer resources than that for the initial problem. It also requires one to specify the shape files for all different sizes of the computational box.

The problem with the latter approach is the diffraction of the plane wave on the edges of the computational domain. It can be alleviated by using a Gaussian beam with a width smaller than the computational domain but larger than all structural features of the problem (e.g., particles above or inside the multi-layered substrate) [26].

A combination of these two approaches was proposed by D’Agostino *et al.* [27] to decrease spurious boundary effects for infinite plane substrate, but can be generalized to arbitrary environment. The total near- of far-field **E**(**r**) is replaced by an adjusted field **E**adj(**r**)

|  |  |
| --- | --- |
| , | (3) |

where **E**env(**r**) is the result of a DDA simulation for the truncated environment alone (without particles) with the free-space incident field. It is expected that **E**adj(**r**) will converge to the correct solution with increasing computational domain faster than **E**(**r**).

Another useful extension of the DDA is introduction of periodic boundary conditions [28,29], which is relevant to photonic crystals and similar applications. This requires relatively simple modification of the algorithm and it was recently implemented in the DDSCAT 7 [30]. However, ADDA does *not* yet support this feature.

# System Requirements

Computational requirements of DDA primarily depend on the size of the computational grid, which in turn depends on the size parameter *x* and refractive index *m* of the scatterer (§6.2). This section addresses requirements of standard (FFT) mode of ADDA, while sparse mode is discussed separately (§12.3). The memory requirements of ADDA depend both on the total number of dipoles in a computational box (*N*) and the number of real (non-void) dipoles (*N*real); it also depends on the number of dipoles along the *x*‑axis (*nx*) and number of processors or cores used (*n*p). The total memory requirement *M*tot (for all processors) in the free-space mode is approximately

|  |  |
| --- | --- |
| , | (4) |

where additional memory proportional to *N* is required only in parallel mode (see §12.2 for details). Coefficient before *N*real depends on the chosen iterative solver, as 31 + 48(*n*vec + 1), where *n*vec is the number of vectors used by the solver (§12.1, Table 3). In the surface mode (§7) the following additional memory is required

|  |  |
| --- | --- |
| , | (5) |

which is usually insignificant. The memory requirements of each processor depends on the partition of the computational grid over the processors that is generally not uniform (see §6.6). Total memory used by ADDA and maximum per one processor are shown in log (see §C.4). It is important to note that *double* precision is used everywhere in ADDA. This requires more memory as compared to single precision, but it helps when convergence of the iterative solver is very slow and machine precision becomes relevant, as is the case for large simulations, or when very accurate results are desired, as in [21].

There is a maximum number of processors, which ADDA can effectively employ (§6.6), equal to *nz* if the latter is a “round” number (§12.2). This determines the largest problem size solvable on a given supercomputer with very large number of processors but with a limited amount of memory per processor *M*pp. For a given problem, setting *n*p = *nz* leads to the following maximum memory requirements per processor (in the free-space mode):[[22]](#footnote-22)

|  |  |
| --- | --- |
| , | (6) |

where *n*slice ≤ *nxny* is the maximum number of real dipoles in a slice parallel to the *yz*‑plane.

To have a quick estimate of maximum achievable discretization on a given hardware, one may consider a cube and less-memory-consuming iterative solvers. Then, Eqs. (4) and (6) lead to maximum *nx* equal to 113[*M*tot(GB)]1/3 and 1067[*M*pp(GB)]1/2 for single-core PC and very large cluster respectively.

In OpenCL mode the memory proportional to *N* in Eq. (4) is moved to the GPU thus reducing the used amount of main (CPU) memory. In this case additional 8*N*real bytes of CPU memory is required for CGNR and Bi-CGStab iterative solvers. Moreover, ADDA may additionally allocate up to 768*N*∙min(1,16/*nx*) bytes (double that in the surface mode) on the GPU, if available, to improve simulation speed (when –opt speed is enabled, see below).

ADDA may optimize itself during runtime for either maximum speed or minimum memory usage. It is controlled by a command line option

-opt {speed|mem}

By default, speed optimization is used. A command line option

-prognosis

can be used to estimate the memory requirements without actually performing the allocation of memory and simulation.[[23]](#footnote-23) It also implies ‑test option (§C.3). By default, this estimate is based on the upper limit of memory that ADDA can use (especially, for OpenCL memory). To get the minimum required memory combine –prognosis with –opt mem.

 

Fig. 1. Capabilities of ADDA 0.76 for spheres with different *x* and *m*. (a) Applicability region – the lower-left region corresponds to full convergence and gray region – to incomplete convergence. The dashed lines show two levels of memory requirements for the simulation. (b) Total simulation wall clock time on 64 processors in logarithmic scale. Horizontal dotted lines corresponding to a minute, an hour, a day, and a week are shown for convenience. Adapted from [8].

Simulation time (see §12 for details) consists of two major parts: solution of the linear system of equations and calculation of the scattered fields. The first one depends on the number of iterations to reach convergence, which mainly depends on the size parameter, shape and refractive index of the scatterer, and time of one iteration, which depends only on *N* as 𝒪(*N*ln*N*) (see §12.2). Execution time for calculation of scattered fields is proportional to *N*real, and is usually relatively small if scattering is only calculated in one plane. However, it may be significant when a large grid of scattering angles is used (§11.2, §11.4). In the surface mode (§7) significant time is additionally required for initialization (building up the interaction matrix, §12.7). Employing multiple processors brings the simulation time down almost proportional to the number of processors (see §12.4). To facilitate very long simulations checkpoints can be used to break a single simulation into smaller parts (§12.5).

For example, on a desktop computer (P4-3.2 GHz, 2 Gb RAM) it was possible to simulate light scattering by spheres[[24]](#footnote-24) up to *x* = 35 and 20 for *m* = 1.313 and 2.0 respectively (simulation times are 20 and 148 hours respectively). The capabilities of ADDA 0.76 for simulation of light scattering by spheres using 64 3.4 GHz cores were reported in [8]. Here we present only Fig. 1, showing the maximum reachable *x* versus *m* and simulation time versus *x* and *m*. In particular, light scattering by a homogenous sphere with *x* = 160 and *m* = 1.05 was simulated in only 1.5 hours, although the runtime steeply increased with refractive index. Examples of more recent and even larger simulations are gathered on a special wiki page.[[25]](#footnote-25)

# Defining a Scatterer

## Reference frames

Three different reference frames are used by ADDA: laboratory, particle, and incident wave reference frames. The laboratory reference frame is the default one, and all input parameters and other reference frames are specified relative to it. ADDA simulates light scattering in the particle reference frame, which naturally corresponds to particle geometry and symmetries, to minimize the size of the computational grid (§6.2), especially for elongated or oblate particles. In this reference frame the computational grid is built along the coordinate axes. The incident wave reference frame is defined by setting the *z*‑axis along the propagation direction (more precisely, the argument of ‑prop option, §9.1). In some cases it is used for definition of scattering plane and angles (§11.1).

The origins of all reference frames coincide with the center of the computational grid (§6.2). By default, both particle and incident wave reference frames coincide with the laboratory frame. However, they can be made different by rotating the particle (§8) or by ‑prop option (§9.1) respectively. If you are unsure about the dipole coordinates or the position of the reference frame relative to the particle, try saving the incident beam to the file (§9). Then, the resulting file (§C.9) will contain dipole coordinates in the particle reference frame.

## The computational grid

ADDA embeds a scatterer in a rectangular computational box, which is divided into identical cubes (as required for the FFT acceleration, §12.2). Each cube is called a “dipole”; its size should be much smaller than a wavelength. The flexibility of the DDA method lies in its ability to naturally simulate any arbitrarily shaped and/or inhomogeneous scatterer, because the optical properties (refractive index, §6.3) of each dipole can be set independently. There are a few parameters describing the computational grid: size of one dipole (cube) *d*, number of dipoles along each axis *nx*, *ny*, *nz*, total size (in µm) of the grid along each axis *Dx*, *Dy*, *Dz*, volume-equivalent radius *r*eq, and incident wavelength *λ*. However, they are not independent. ADDA allows one to specify all three grid dimensions *nx*, *ny*, *nz* as arguments to the command line option

-grid <nx> [<ny> <nz>]

If omitted *ny* and *nz* are automatically determined by *nx* based on the proportions of the scatterer (§6.4). When particle geometry is read from a file (§6.3) all grid dimensions are initialized automatically.[[26]](#footnote-26) Because of the internal structure of the ADDA all the dimensions are currently limited to be even. If odd grid dimension is specified by any input method, it is automatically incremented. In this case ADDA produces a warning to avoid possible ambiguity. If the ‑jagged option is used the grid dimension is effectively multiplied by the specified number (§6.3).

One can also specify the size parameter of the entire grid *kDx* (*k* is the free space wave vector) or *x* = *kr*ef, using three command line options:

-lambda <arg>

-size <arg>

-eq\_rad <arg>

which specify (in µm) *λ*, *Dx*, and *r*ef respectively. By default *λ* = 2*π* µm, then ‑size determines *kDx* and ‑eq\_rad sets *x*. The last two are related by

|  |  |
| --- | --- |
| , | (7) |

where *f*vol is ratio of particle to computational grid volumes, which is known analytically for many shapes available in ADDA (§6.4). It is important to note that *Dx* denotes the size of *possibly adjusted* computational grid. Although ADDA will warn user of possible ambiguities, it is not recommended to use ‑ size command line option for shapes read from file, when inherent *nx* of this shape is not guaranteed to be even. It may cause a modeled scatterer to be slightly smaller than originally intended. Some shapes define the absolute particle size themselves (§6.4). However, the size given in the command line (by either ‑size or ‑eq\_rad) overrides the internal specification and the shape is scaled accordingly.

The size parameter of the dipole is specified by the parameter “dipoles per lambda” (dpl)

|  |  |
| --- | --- |
| , | (8) |

which is given to the command line option

-dpl <arg>

dpl does not need to be an integer; any real number can be specified.

ADDA will accept at most two parameters from: dpl, *nx*, *kDx*, and *x* since they depend on each other by Eq. (7) and

|  |  |
| --- | --- |
| . | (9) |

Moreover, specifying a pair of *kD*x and *x* is also not possible. If any other pair from these four parameters is given on the command line (*nx* is also defined if particle geometry is read from file) the other two are automatically determined from the Eqs. (7) and (9). If the latter is *nx*, dpl is slightly increased (if needed) so that *nx* exactly equals an even integer. There is one exception: a pair of *x* and dpl can only be used for shapes, for which *f*vol can be determined analytically (§6.4), because numerical evaluation of *f*vol is only possible when particle is already discretized with a certain *nx*. If less than two parameters are defined dpl or/and grid dimension are set by default.[[27]](#footnote-27) The default for dpl is 10|*m*| [cf. Eq. (1)], where *m* is the maximum (by absolute value) refractive index specified by the ‑m option (or the default one, §6.3). The default for *nx* is 16 (possibly multiplied by ‑jagged value). Hence, if only ‑size or ‑eq\_rad is specified, ADDA will automatically discretize the particle, using the default dpl (with the exception discussed above for *x*). This procedure may lead to very small *nx*, e.g. for nanoparticles, hence ADDA ensures that *nx* is at least 16, when it is auto-set from default dpl. However, if dpl is specified in the command line, ADDA puts absolute trust in it and leaves all the consequences to the user.

## Construction of a dipole set

After defining the computational grid (§6.2) each dipole of the grid should be assigned a refractive index (a void dipole is equivalent to a dipole with refractive index equal to 1). This can be done automatically for a number of predefined shapes or in a very flexible way by specifying scatterer geometry in a separate input file. For predefined shapes (§6.4) the dipole is assigned to the scatterer if and only if its center falls inside the shape, see Fig. 2(a) for an example. When the scatterer consists of several domains, e.g. a coated sphere, the same rule applies to each domain. By default, ADDA slightly corrects the dipole size (or equivalently dpl) to ensure that the volume of the dipole representation of the particle is exactly correct [Fig. 2(b)], i.e. exactly corresponds to *x*. This is believed to increase the accuracy of the DDA, especially for small scatterers [10]. However, it introduces a minor inconvenience that the size of the computational grid is not exactly equal to the size of the particle. The volume correction can be turned off by command line option

-no\_vol\_cor

fig1

Fig. 2. An example of dipole assignment for a sphere (2D projection). Assigned dipoles are gray and void dipoles are white. (a) initial assignment; (b) after volume correction; (c) with “‑jagged” option enabled (*J* = 2) and the same total grid dimension. Adapted from [1].

In this case ADDA tries to match the size of the particle using specified *kDx* or calculating it from specified *x* (if shape permits). Moreover, ADDA then determines the “real” value of *x* numerically from the volume of the dipole representation. Its value is shown in log file (§C.4) and is further used in ADDA, e.g. for normalization of cross sections (§11.4), although it may slightly differ from specified or analytically derived *x*.

To read particle geometry from a file, specify the file name as an argument to the command line option

-shape read <filename>

This file specifies all the dipoles in the simulation grid that belongs to the particle (possibly several domains with different refractive indices). Supported formats include ADDA text formats and DDSCAT 6 and 7 shape formats (see §B.5 for details). Dimensions of the computational grid are then initialized automatically. Packages misc/pip and misc/hyperfun allow one to transform a variety of common 3D shape formats to one readable by ADDA. It is also possible to add support for new shape format directly into ADDA.[[28]](#footnote-28)

Sometimes it is useful to describe particle geometry in a coarse way by larger dipoles (cubes), but then use smaller dipoles for the simulation itself.[[29]](#footnote-29) ADDA enables this by the command line option

-jagged <arg>

that specifies a multiplier *J*. Large cubes (*J*×*J*×*J* dipoles) are used [Fig. 2(c)] for construction of the dipole set. Cube centers are tested for belonging to a particle’s domain. All grid dimensions are multiplied by *J*. When particle geometry is read from file it is considered to be a configuration of big cubes, each of them is further subdivided into *J*3 dipoles.

ADDA includes a granule generator, which can randomly fill any specified domain with granules of a predefined size. It is described in details in §6.5.

The last parameter to completely specify a scatterer is its refractive index. Refractive indices are given on the command line

-m {<m1Re> <m1Im> […]|<m1xxRe> <m1xxIm> <m1yyRe> <m1yyIm> <m1zzRe> <m1zzIm> […]}

Each pair of arguments specifies the real and imaginary part[[30]](#footnote-30) of the refractive index of the corresponding domain (first pair corresponds to domain number 1, etc.). Command line option

-anisotr

can be used to specify that a refractive index is anisotropic. In that case three refractive indices correspond to one domain. They are the diagonal elements of the refractive index tensor in the particle reference frame (§6.1). Currently ADDA supports only diagonal refractive index tensors; moreover, the refractive index must change discretely. Anisotropy cannot be used with either CLDR polarizability (§10.1) or SO formulations (§10.1, §10.2, §10.4), since they are derived assuming isotropic refractive index, and cannot be easily generalized. Use of anisotropic refractive index cancels the rotation symmetry if its *x* and *y*‑components differ. Limited testing of this option was performed for Rayleigh anisotropic spheres.

The maximum number of different refractive indices (particle domains) is defined at compilation time by the parameter MAX\_NMAT in the file const.h. By default it is set to 15. The number of the domain in the geometry file (§B.5) exactly corresponds to the number of the refractive index. Numbering of domains for the predefined shapes is described in §6.4. If no refractive index is specified, it is set to 1.5, but this default option works only for single-domain isotropic scatterers. Currently ADDA produces an error if any of the given refractive index equals to 1. It is planned to improve this behavior to accept such refractive index and automatically make corresponding domain void. This can be used, for instance, to generate spherical shell shape using standard option –shape coated. For now, one may set refractive index to the value very close to 1 for this purpose, e.g. equal to 1.00001.

ADDA saves the constructed dipole set to a file if the command line option

-save\_geom [<filename>]

is specified, where <filename> is an optional argument. If it is not specified, ADDA names the output file <type>.<ext>. <type> is shape name – a first argument to the ‑shape command line option, see above and §6.4, possibly with addition of \_gran (§6.5). <ext> is determined by the format (geom for ADDA and dat for DDSCAT formats), which itself is determined by the command line option

-sg\_format {text|text\_ext|ddscat6|ddscat7}

First two are ADDA default formats for single- and multi-domain particles respectively. DDSCAT 6 and 7 format, which differ by a single line, are described in §B.5. text is automatically changed to text\_ext for multi-domain particles. Output formats are compatible with the input ones (see §C.11 for details). The values of refractive indices are not saved (only domain numbers). This option can be combined with ‑prognosis, then no DDA simulation is performed but the geometry file is generated.

## Predefined shapes

Predefined shapes are initialized by the command line option

-shape <type> [<args>]

where <type> is a name of the predefined shape. The size of the scatterer is determined by the size of the computational grid (*Dx*, §6.2); <args> specify different dimensionless aspect ratios or other proportions of the particle shape. However, some shapes define the absolute size themselves, which can be overridden (§6.2). In the following we describe the supported predefined shapes in alphabetic order:

* axisymmetric – axisymmetric homogeneous shape, defined by its contour in *ρz*-plane of the cylindrical coordinate system, which is read from file (format described in §B.6).
* bicoated – two identical concentric coated spheres with outer diameter *d* (first domain), inner diameter *d*in, and center-to-center distance *R*cc (along the *z*‑axis). It describes both separate and sintered coated spheres. In the latter case sintering is considered symmetrically for cores and shells.
* biellipsoid – two general ellipsoids in default orientations with centers on the *z*‑axis, touching each other. Their semi-axes are *x*1, *y*1, *z*1 (lower one, first domain) and *x*2, *y*2, *z*2 (upper one, second domain).
* bisphere – two identical spheres with outer diameter *d* and center-to-center distance *R*cc (along the *z*‑axis). It describes both separate and sintered spheres.
* box – a homogenous cube (if no arguments are given) or a rectangular parallelepiped with edge sizes *x*, *y*, *z*.
* capsule – cylinder with height (length) *h* and diameter *d* with half-spherical caps on both ends. Total height of the capsule is *h* + *d*.
* chebyshev – axisymmetric Chebyshev particle of amplitude *ε* (|*ε*| ≤ 1) and order *n* (natural number). Its formula in spherical coordinates (*r*, *θ*) is

|  |  |
| --- | --- |
| , | (10) |

where *r*0 is determined by the particle size.

* coated – sphere with a spherical inclusion; outer sphere has a diameter *d* (first domain). The included sphere has a diameter *d*in (optional position of the center: *x*, *y*, *z*).
* cylinder – homogenous cylinder with height (length) *h* and diameter *d*.
* egg – axisymmetric biconcave homogenous particle, which surface is given as

|  |  |
| --- | --- |
| , | (11) |

where *r* is the radius in spherical coordinates and *a* is scaling factor, which can be derived from egg diameter (maximum width perpendicular to the *z*‑ axis) or volume [31]. Center of the reference frame in Eq. (11) is shifted along the *z*‑axis relative to the center of the computational grid to ensure that North and South Poles of the egg are symmetric over the latter center.

* ellipsoid – homogenous general ellipsoid with semi-axes *x*, *y*, *z*.
* line – line along the *x*‑axis with the width of one dipole.
* plate – homogeneous plate (cylinder, which sides are rounded by adding half-torus) with height (thickness) *h* and full diameter *d* (i.e. the diameter of the constituent cylinder is *d* − *h*).
* prism – homogeneous right prism with height (length along the *z*‑axis) *h* based on a regular polygon with *n* sides of size *a*. The polygon is oriented so that the positive *x*‑axis is a middle perpendicular for one of its sides. *Dx* equals 2*R*i and *R*c + *R*i for even and odd *n* respectively. *R*c = *a*/[2sin(*π*/*n*)] and *R*i = *R*ccos(*π*/*n*) are radii of circumscribed and inscribed circles respectively.
* rbc – red blood cell, an axisymmetric biconcave homogenous particle, which is characterized by diameter *d*, maximum and minimum width *h*, *b*, and diameter at the position of the maximum width *c*. Its surface is defined as

|  |  |
| --- | --- |
| , | (12) |

where *ρ* is the radius in cylindrical coordinates (*ρ*2 = *x*2 + *y*2). *P*, *Q*, *R*, and *S* are determined from the values of the parameters given in the command line (see [32] for specific expressions). This formula is based on [33], and is qualitatively similar to the RBC shape used in [34].

* sphere – homogenous sphere (used by default).
* spherebox – sphere (diameter *d*sph) in a cube (size *Dx*, first domain).

Table 1. Brief description of arguments, symmetries (§6.7), and availability of analytical value of *f*vol for predefined shapes. Shapes and their arguments are described in the text. “±” means that it depends on the arguments.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| <type> | <args> | dom.a | symYb | symRc | *f*vol | sized |
| axisymmetric | filename | 1 | + | + | − | + |
| bicoated | *R*cc/*d*, *d*in/*d* | 2 | + | + | + | − |
| biellipsoid | *y*1/*x*1, *z*1/*x*1, *x*2/*x*1, *y*2/*x*2, *z*2/*x*2 | 2 | + | ± | + | − |
| bisphere | *R*cc/*d* | 1 | + | + | + | − |
| box | [*y*/*x*, *z*/*x*] | 1 | + | ± | + | − |
| capsule | *h*/*d* | 1 | + | + | + | − |
| chebyshev | *ε*, *n* | 1 | + | + | + | − |
| coated | *d*in/*d*, [*x*/*d*, *y*/*d*, *z*/*d*] | 2 | ± | ± | + | − |
| cylinder | *h*/*d* | 1 | + | + | + | − |
| egg | *ε*, *ν* | 1 | + | + | + | − |
| ellipsoid | *y*/*x*, *z*/*x* | 1 | + | ± | + | − |
| line | – | 1 | − | − | − | − |
| plate | *h/d* | 1 | + | + | + | − |
| prism | *n*, *h*/*Dx* | 1 | ± | ± | + | − |
| rbc | *h*/*d*, *b*/*d*, *c*/*d* | 1 | + | + | − | − |
| sphere | – | 1 | + | + | + | − |
| spherebox | *d*sph/*Dx* | 2 | + | + | + | − |

a number of domains.

b symmetry with respect to reflection over the *xz*‑plane.

c symmetry with respect to rotation by 90° over the *z*‑axis.

d whether a shape defines absolute size of the particle.

For all axisymmetric shapes, symmetry axis coincides with the z‑axis. The order of domains is important to assign refractive indices specified in the command line (§6.3). Brief reference information is summarized in Table 1, while examples are provided in Fig. 3. For multi-domain shapes *f*vol is based on the total volume of the particle. Adding a new shape is straightforward for anyone who is familiar with C programming language.[[31]](#footnote-31)

## Granule generator

Granule generator is enabled by the command line option

-granul <vol\_frac> <diam> [<dom\_number>]

which specifies that one particle domain should be randomly filled with spherical granules with specified diameter <diam> and volume fraction <vol\_frac>. The domain number to fill is given by the last optional argument (default is the first domain). Total number of domains is then increased by one; the last is assigned to the granules. Suffix “\_gran” is added to the shape name and all particle symmetries (§6.7) are cancelled.

shapes

Fig. 3. Examples of predefined shapes. Most shapes are depicted by projections on the *xz*‑plane. A blue arrow around the z‑axis denotes axisymmetry.

A simplest algorithm is used: to place randomly a sphere and see whether it fits in the given domain together with all previously placed granules. The only information that is used about some of the previously place granules is dipoles occupied by them, therefore intersection of two granules is checked through the dipoles, which is not exact, especially for small granules. However it should not introduce errors larger than those caused by the discretization of granules. Moreover, it allows considering arbitrary complex domains, which is described only by a set of occupied dipoles. This algorithm is unsuitable for high volume fractions, it becomes very slow and for some volume fractions may fail at all (depending on the size of the granules critical volume fractions is 30–50%). Moreover, statistical properties of the obtained granules distribution may be not perfect; however, it seems good enough for most applications. To generate random numbers ADDA uses the Mersenne twister,[[32]](#footnote-32) which combines high speed with good statistical properties [35]. The granule generator was used to simulate light scattering by granulated spheres by Yurkin *et al.* [36].

If volume correction (§6.3) is used, the diameter of the granules is slightly adjusted to give exact *a priori* volume fraction. *A posteriori* volume fraction is determined based on the total number of dipoles occupied by granules and is saved to log (§C.4). It is not recommended to use granule diameter smaller than the size of the dipole, since then the dipole grid cannot adequately represent the granules, even statistically. ADDA will show a warning in that case; however, it will perform simulation for any granule size.

Currently the granule generator does not take into account ‑jagged option, which is planned to be fixed in the future.[[33]](#footnote-33) For now one may save a geometry file for a particle model scaled to *J* = 1 and then load it using any desired *J*. The same trick can be used to fill different particle domains and/or using different sizes of granules. To do it the complete operation should be decomposed into elementary granule fills, which should be interweaved with saving and loading of geometry files.

Coordinates of the granules (its centers) can be saved to a file granules (§C.12) specifying command line option

-store\_grans

This provides more accurate information about the granulated particle than its dipole representation, which can be used e.g. to refine discretization.

## Partition over processors in parallel mode

To understand the parallel performance of ADDA it is important to realize how a scattering problem is distributed among different processors. Both the computational grid and the scatterer are partitioned in slices parallel to the *xy‑*plane (in another words, partition is performed over the *z*‑axis); each processor contains several consecutive slices. For the FFT-based task the computational grid is partitioned both along the *x*- and *z*‑axes, and the partial *xz*‑blocks are exchanged between processors during the 3D FFT. The partition of the computational grid is optimal if both *nz* and 2*nx* divides the number of processors *n*p (at least approximately, §12.2). One can also control optimality *a posteriori* by studying the log file (§C.4) – the dimensions for the FFT-grid should be twice larger than the computational grid (“box dimensions”).

The partition of the scatterer itself also benefits from *nz* being multiple of *n*p, however it is still not optimal for most of the geometries,[[34]](#footnote-34) i.e. the number of non-void dipoles is different for different processors (Fig. 4). This partition is relevant for the computation of the scattered fields; hence its non-optimality should not be an issue in most cases. However, if large grid of scattering angles is used (§11.2, §11.4), the parallel performance of the ADDA may be relatively low (the total simulation time will be determined by the maximum number of real dipoles per processor).[[35]](#footnote-35)



Fig. 4. Same as Fig. 2(a) but partitioned over 4 processors (shown in different shades of gray).

The conclusion of this section is that careful choice of *nz* and number of the processors (so that the former divides the latter) may significantly improve the parallel performance. ADDA will work fine with any input parameters, so this optimization is left to the user. Consider also some limitations imposed on the grid dimensions by the implemented FFT routines (§12.2).

If the particle is prolate or oblate, parallel efficiency of ADDA depends on orientation of the former in the particle reference frame. First, it is recommended to set the *y*‑axis along the smallest particle dimension. Second, positioning the longest scatterer dimension along the *x*‑axis minimizes the memory requirements for a fixed (and relatively small) *n*p [Eq. (4)], while position along the *z*‑axis is optimal for the maximum *n*p [Eq. (6)]. Unfortunately, currently ADDA cannot rearrange the axes with respect to the particle,[[36]](#footnote-36) so the only way to implement the above recommendations is to prepare input shape files (§6.3) accordingly. For predefined shapes (§6.4) one needs to export geometry to a shape file, rotate it in the shape file by a separate routine, and import it back into the ADDA.[[37]](#footnote-37) Direction of propagation of the incident radiation should also be adjusted (§9.1), if axes of the particle reference frames are rearranged, to keep the scattering problem equivalent to the original one.

Finally, this section is not relevant for the sparse mode (§12.3), since then only the non-void dipoles are considered. Those dipoles are uniformly distributed among the processors irrespective of their position in the computational grid. In particular, there is no limitation of a slice to belong to a single processor.

## Particle symmetries

Symmetries of a light-scattering problem are used in ADDA to reduce simulation time. All the symmetries are defined for the default incident beam (§9). If the particle is symmetric with respect to reflection over the *xz*‑plane (*yz*‑plane), only half of the scattering *yz*‑plane (*xz*‑plane) is considered (scattering angle from 0° to 180°, §11.1). If the particle is symmetric with respect to rotation by 90° over the *z*‑axis, the Mueller matrix in the *yz*‑plane (§11.1) can be calculated from the calculation of the internal fields for just one incident polarization (*y*‑polarization is used). The second polarization is then equivalent to the first one but with scattering in the *xz*‑plane (in negative direction of *x*‑axis). Analogous scheme is used for another scattering plane (§11.1). The symmetries are automatically determined for all the predefined shapes (§6.4). Some or all of them are automatically cancelled if not default beam type and/or direction (§9), anisotropic refractive index (§6.3), or granule generator (§6.5) are used.

Use of symmetry can be controlled by the command line option:

-sym {auto|no|enf}

First option corresponds to the default behavior described before, while no and enf specify to never use or enforce symmetry respectively. Use the latter with caution, as it may lead to erroneous results. It may be useful if the scattering problem is symmetric, but ADDA do not recognize it automatically, e.g. for particles that are read from file or when non-default incident beam is used, which does not spoil the symmetry of the problem (e.g. plane wave propagating along the *x*‑axis for a cubical scatterer). It is important to note that not the scatterer but its dipole representation should be symmetric;[[38]](#footnote-38) otherwise the accuracy of the result will generally be slightly worse than that when symmetry is not enforced. The final symmetries determined by ADDA are saved to log (§C.4), where X, Y, Z denote symmetries along the corresponding axes (i.e. with respect to reflection over the *xy*-, *xz*-, and *yz*‑planes respectively) and R denotes symmetry with respect to rotation by 90° over the *z*‑axis. Alternatively, ADDA specifies that symmetries are either cancelled or enforced by user.

Particle symmetries can also be used to decrease the range of orientation/scattering angles for different averagings/integrations. However, it is user’s responsibility to decide how a particular symmetry can be employed. This is described in the descriptions of corresponding input parameters files (§B.2, §B.3, §B.4).

# Surface Mode

Apart from the default free-space mode, ADDA is applicable to particles (finite systems of scatterers) located above the plane surface parallel to the *xy*‑plane [37]. This is enabled by command line option:

-surf <h> {<mre> <mim>|inf}

where *h* is the distance from surface to the particle center (in μm). Following argument(s) specify the refractive index of the substrate (below the surface), assuming that the vacuum is above the surface. It is done either by two values (real and imaginary parts of the complex value) or as effectively infinite inf which corresponds to perfectly reflective surface (§7). The case of particle fully submerged into the *non-absorbing* substrate can also be handled by rescaling all refractive indices (including the vacuum above the substrate) by *m*s (§4.2) and rotating the reference frame appropriately.

Details of the implementation are described in other sections of the manual. There are, however, a number of important caveats:

* Significant additional time for initialization is required (§5, §12.7);
* The surface mode is incompatible with radiation forces (§11.6), Gaussian incident beam (§9.2), WKB initial field for the iterative solver (§12.1), and rotation of particle (§8).
* DDA accuracy, including required discretization (§4.1), in the surface mode is poorly studied and may strongly depend on the refractive index and location of substrate.
* Definitions of common light-scattering quantities, like Mueller scattering matrices or cross sections, are somewhat ambiguous when beam is incoming from or scattered into the substrate. See corresponding sections for specific definitions employed by ADDA (§10.4, §11). It is even more ambiguous for absorbing substrate. Still, above-the-substrate quantities are well-defined in all cases.

# Orientation of the Scatterer

## Single orientation

Any particle orientation with respect to the laboratory reference frame can be specified by three Euler angles (*α*,*β*,*γ*). ADDA uses a notation based on [38], which is also called “*zyz*‑notation” or “*y*‑convention”. In short, coordinate axes attached to the particle are first rotated by the angle *α* over the *z*‑axis, then by the angle *β* over the current position of the *y*‑axis (the line of nodes), and finally by the angle *γ* over the new position of the *z*‑axis (Fig. 5). These angles are specified in degrees as three arguments to the command line option

-orient <alpha> <beta> <gamma>

ADDA simulates light scattering in the particle reference frame (§6.1), therefore rotation of the particle is equivalently represented as an inverse rotation of the incident wave propagation direction and polarization (§9.1), position of the beam center (if relevant, §9.2), and scattering plane (angles, §11.1). The information about the orientation of a scatterer is saved to the log (§C.4). Particle rotation cannot be used in the surface mode.[[39]](#footnote-39)

## Orientation averaging



Fig. 5. Transformation of the laboratory reference system *xyz* into the particle reference frame *x′y′z′* through consecutive rotation by angles *α*, *β*, and *γ*. Adapted from [1].

Orientation averaging is performed over three Euler angles (*α*,*β*,*γ*). Rotating over *α* is equivalent to rotating the scattering plane without changing the orientation of the scatterer relative to the incident radiation. Therefore, averaging over this orientation angle is done with a single computation of internal fields; additional computational time for each scattering plane is comparably small. Averaging over other two Euler angles is done by independent DDA simulations (defining the orientation of the scatterer as described in §8.1). The averaging itself is performed using the Romberg integration (§12.6), parameters of the averaging are stored by default in file avg\_params.dat (§B.2). Orientation averaging is enabled by the command line option

-orient avg [<filename>]

where <filename> is an optional argument that specifies a different file with parameters of the averaging. Integration points for *β* are spaced uniformly in values of cos*β* [39]. Currently only the Mueller matrix in one scattering plane (§11.2), *C*ext, and *C*abs (§11.4) are calculated when doing orientation averaging.

It also cannot be used in combination with saving incident beam (§9), internal fields or dipole polarizations (§11.7), or radiation forces (§8.2), nor with calculating scattering for a grid of angles (§11.2).

# Incident Beam

This section describes how to specify the incident electric field. This field, calculated for each dipole, can be saved to file IncBeam (§C.9). To enable this functionality, specify command line option

-store\_beam

## Propagation direction

The direction of propagation of the incident radiation is specified by the command line option

-prop <x> <y> <z>

where arguments are *x*, *y*, and *z* components of the propagation vector. Normalization (to the unity vector **a**) is performed automatically by ADDA. By default vector **e***z* = (0,0,1) is used.

The option ‑prop is cumulative with rotation of the particle (§8.1) because the latter is equivalent to the inverse rotation of incident wave and scattering angles. If after all transformations the propagation vector is not equal to the default (0,0,1), all the symmetries of the scatterer are cancelled (§6.7).

The default (above) meaning of ‑prop option is used for directed beams, like plane or Gaussian beams. However, it has a very different meaning for dipole incident field (determines dipole orientation), and may also be not relevant for incident beams read from file (§9.2). Still, in all cases it (the vector **a**) determines the incident-wave reference frame (§6.1).

## Beam type

Additionally to the default plane wave ADDA supports several types of finite size incident beams, specified by the command line option

-beam <type> [<args]

Table 2. Incident beam types. All numeric arguments are in μm, the coordinates are specified in the laboratory reference frame (§6.1) except for read.

|  |  |  |
| --- | --- | --- |
| <type> | <args> | Description |
| barton5 | *w*0, [*x*, *y*, *z*] | Fifth-order approximation of Gaussian beam |
| davis3 | *w*0, [*x*, *y*, *z*] | Third-order approximation of Gaussian beam |
| dipole | *x*, *y*, *z* | Point dipole |
| lminus | *w*0, [*x*, *y*, *z*] | First-order approximation of Gaussian beam |
| plane |  | Plane wave |
| read | filenameY, [filenameX] | Arbitrary beam from file |

where available types are listed in Table 2 and are discussed in details below. The default is the plane wave, while lminus [40], davis3 [41], and barton5 [42]are approximations of the Gaussian beam up to the 1st, 3rd, and 5th order of the beam confinement factor (*s* = 1/*kw*0), respectively. Four arguments specified in the command line specify width (*w*0) and *x*, *y*, *z* coordinates of the center of the beam (in laboratory reference frame, §6.1) respectively. barton5 is recommended for all calculations involving Gaussian beams; others are left mainly for comparison purposes. However, for tightly focused beams even barton5 may be not accurate enough.[[40]](#footnote-40)

For a plane wave incidence

|  |  |
| --- | --- |
| , | (13) |

where **k** = *k***a** and |**e**0| = 1. For all beam types ADDA assumes unity amplitude of the electric field in the focal point of the beam (in Gaussian-CGS system of units, i.e. 1 statV/cm), which implies time-averaged irradiance in the beam focal point *I*0 = *c*/(8*π*). Total power of the beam for barton5 is [42]

|  |  |
| --- | --- |
| , | (14) |

For lower-order approximations (lminus and davis3) corresponding small terms in the parentheses in Eq. (14) should be omitted. Some of the particle symmetries (§6.7) may be cancelled according to the coordinates of the beam center.

In the surface mode (§7) the incident beam consists of three parts: incoming (), reflected () and transmitted (). Incoming plane wave far from particle and surface is given by Eq. (13), but with **k** replaced by **k**in = min*k***a**, where *m*in is the refractive index of the “incoming” medium – either 1 (above surface) or *m*s (below surface). In particular, the incoming field has unity amplitude and zero phase in the particle center. This may lead to counterintuitive very large amplitudes of the incoming field at the surface, if it propagates from the highly absorbing substrate and particle is far from the substrate. Reflected and transmitted counterparts are calculated using standard Fresnel formulae [43]:

|  |  |
| --- | --- |
| , | (15) |
| , | (16) |

where **e***s*, **e***p* are unit vector for *s*- (parallel to the surface) and *p*‑polarizations respectively; *rs*, *rp*, *ts*, *tp* are (complex) amplitude reflection and transmission coefficients for both polarizations, **k***r* = *k*(*ax*,*ay*,−*az*) and

|  |  |
| --- | --- |
| , | (17) |

where the complex square root is considered with branch cut along the negative real axis. Generally, **k***t* is a complex (bi-)vector, which corresponds to inhomogeneous wave.[[41]](#footnote-41) Moreover, in some cases ℑ(*kt*,*z*) < 0, which may seem counterintuitive, but is physically correct, given the scale of beam amplitude as exp(i**k***t*∙**r**) in Eq. (16) and infinite lateral extent of the plane wave.[[42]](#footnote-42) Vectors **e***p* depend on particular part of the incident wave (specified by the superscript *X* below), but conform to the following general definition:

|  |  |
| --- | --- |
| . | (18) |

For homogeneous **k***X* (always the case for incoming and reflected parts)  is a real unit vector (as is also the case for **e***s*), but for inhomogeneous (general-case) **k***t*  is a complex vector, satisfying . The second term in exponents in Eqs. (15), (16) is due to the shift of surface relative to the origin.

The total *incident* field (acting on the particle) in the surface mode is  or , when field propagates from above (*az* < 0) or below (*az* > 0) the surface respectively. Unfortunately, Gaussian beams are currently not supported in the surface mode.40 Irradiance of the incoming plane wave at the particle center is *I*0 = ℜ(*m*in)*c*/(8*π*), which may be different from that in the free-space case. Here and further ℜ and ℑ denote real and imaginary part of the complex number, respectively.

Another option is the point-dipole incident field (dipole). Location of the dipole **r**0 is given by the argument to ‑beam, while its orientation (direction) is **a** (given by ‑prop, §9.1), both in laboratory reference frame (§6.1). The dipole polarization (dipole moment) is assumed equal to unit electric field, integrated over the cube with size 1/*k*, i.e. **p**0 = *k*−3**a** statV/cm. Then

|  |  |
| --- | --- |
| , | (19) |

where **G̅** is defined in §10.2, and |**E**inc| is comparable to 1 at distance 1/*k* from **r**0. The main purpose of such incident field is to calculate decay rate enhancement (§11.5), however all other scattering quantities may also be calculated with certain caveats. The normalization of the field is different from the standard one, described above, so most of the results will be scaled. In other words, definition of *I*0 is ambiguous in this case, but ADDA still assumes *I*0 = *c*/(8*π*). Also, only the single incident polarization should be simulated (§9.3). Since the dipole field is singular, its position must not coincide with any of the dipoles of the particle (otherwise NAN will be produced in the output). Moreover, the physical problem corresponding to dipole placed inside the particle (between the discretization dipoles) is ambiguous, and applicability of existing algorithms to such problem is unclear. However, placing a dipole into the cavity inside the particle is perfectly valid. Point-dipole incident field can also be used in the surface mode, then **G̅** is replaced by **G̅** + **R̅** (§10.3) in Eq. (19). However, the dipole must be located above the surface and absorption in the substrate is not fully accounted for calculation of decay rate enhancement (§11.5).

Adding of a new beam is straightforward for anyone who is familiar with C programming language.[[43]](#footnote-43) Moreover, arbitrary beam can be read from file, using

-beam read <filenameY> [<filenameX>]

Normally two files are required for *y*‑ and *x*‑polarizations respectively (§9.1), but a single filename is sufficient if only *y*‑polarization is used (§9.3). For that “‑sym enf” should be explicitly specified, since “‑beam read” breaks the symmetry by itself. In contrast to other beam options, read incident field should be specified in a *particle* reference frame, see §B.7 for file format. ADDA cannot determine amplitude or whereabouts of the beam read from file, so it always assumes unity amplitude of the incoming field in its center (focus) and (in the surface mode) *m*in = 1. If not correct, this will introduce the scaling of the scattering quantities (§11).

## Incident polarization

Usually, ADDA performs simulation for two incident polarizations **e**0 (§11.1), which are then used to compute amplitude and Mueller scattering matrices (§11.2, §11.3). The latter can then be used to calculate the result for any incident polarization. Symmetry can sometimes be used to effectively avoid a second simulation (§6.7).

However, in certain applications one needs only the result for a single specific incident polarization, or the incident beam (e.g. point-dipole one) does not have a clear meaning of polarization at all. Currently, ADDA cannot handle such cases in a proper way,[[44]](#footnote-44) but one can use “‑sym enf” to perform a single run for *y*‑polarization (§6.7). Then the scattering quantities that are produced for each incident polarization independently (they have Y in the filename) will be correct. But the scattering matrices albeit computed by ADDA are expected to be wrong, and can be turned off by "‑scat\_matr none" (§11.3). Still, one can obtain the scattered intensity from the amplitude matrix, but the particular formulae depend on the scattering direction (§11.1, §11.3). For example, for default propagation direction and scattering in the *yz*‑plane *S*2 and *S*4 correspond to parallel and perpendicular components of the scattered fields (with respect to the scattering plane).

# DDA Formulation

Since its introduction by Purcell and Pennypacker [3] the DDA has been constantly developed; therefore a number of different DDA formulations exist [2]. Here we only provide a short summary, focusing on those that are implemented in ADDA. All formulations are equivalent to the solution of the linear system to determine unknown dipole polarizations **P***i*

|  |  |
| --- | --- |
| , | (20) |

where  is the incident electric field (§9.2),  is the dipole polarizability (self-term), **H̅***ij* is the total interaction term (Green’s tensor of the environment), and indices *i* and *j* enumerate the dipoles. In the free-space mode **H̅***ij* = **G̅***ij* (direct interaction), while in the surface mode (§7) it additionally contains reflection term **R̅***ij* (**H̅***ij* = **G̅***ij* +**R̅***ij*). Moreover, we postulate  (but not ), i.e. the proper treatment of the corresponding self-action singularity is traditionally included in the expression for  (§10.1). The (total) internal electric field **E***i* is the one present in a homogenous particle modeled by an array of dipoles, also known as macroscopic field [44]. It should be distinguished from the exciting electric field  that is a sum of  and the field due to all other dipoles (and substrate, if present), but excluding the field of the dipole *i* itself. Both total and exciting electric field can be determined once the polarizations are known:

|  |  |
| --- | --- |
| , | (21) |

where *V*d = *d*3 is the volume of a dipole and *χi* = (*εi* − 1)/4*π* is the susceptibility of the medium at the location of the dipole **(***εi* – relative permittivity**)**. In the following we will also refer to **E** as internal fields (those inside the particle) in contrast to near- and far-fields, which are calculated from **E** or **P** together with other scattering quantities. Below we discuss different formulations for the polarizability prescription (§10.1), direct interaction (§10.2) and reflection terms (§10.3), and formulae to calculate scattering quantities (§10.4). In addition to the published ones, ADDA contains options to use new theoretical improvements under development. We do not discuss them here, since they are still in the early research phase. However, you may try them at your own risk.

## Polarizability prescription

A number of expressions for the polarizability are known [2]. ADDA implements the following: the Clausius–Mossotti (CM), the radiative reaction correction (RR, [45]), formulation by Lakhtakia (LAK, [46]), digitized Green’s function (DGF, [46]), approximate integration of Green’s tensor over the dipole (IGTSO, [47]), the lattice dispersion relation (LDR, [11]), corrected LDR (CLDR, [48]), and the Filtered Coupled Dipoles (FCD). There are also a few prescriptions under development: non-local (NLOC and NLOCav) and second order (SO). The CM polarizability is the basic one, given by

|  |  |
| --- | --- |
| , | (22) |

where **I̅** is the identity tensor. Other polarizability formulations can be expressed through it, using the correction term **M̅** associated with finite size of the dipoles [47]:

|  |
| --- |
| , |

in particular, **M̅**CM = 0. RR is a third-order (in *kd*) correction to the CM [45]:

|  |  |
| --- | --- |
| . | (23) |

Following formulations add second-order corrections. LAK is based on replacing the cubical dipole by an equi-volume sphere with radius *a*d = *d*(3/4*π*)1/3 and integrating Green’s tensor over it [49]:

|  |  |
| --- | --- |
| . | (24) |

DGF is an approximation of LAK up to the third order of *kd* [46]:

|  |  |
| --- | --- |
| , , | (25) |

while IGTSO is the same-order approximation applied to the original cubical dipole [47]

|  |  |
| --- | --- |
| , . | (26) |

LDR is based on consideration of infinite grid of point dipoles [11]:

|  |  |
| --- | --- |
| , | (27) |
| , , , , | (28) |

where *µ* denotes vector components. The LDR prescription can be averaged over all possible incident polarizations [11], resulting in

|  |  |
| --- | --- |
| . | (29) |

Corrected LDR is independent on the incident polarization but leads to the diagonal polarizability tensor instead of scalar [48]

|  |  |
| --- | --- |
| , | (30) |

where *δµν* is the Kronecker symbol. The FCD polarizability is obtained from the value of filtered Green’s tensor [Eq. (34)] for zero argument, leading to [23]

|  |  |
| --- | --- |
| . | (31) |

Naturally, Eq. (31) is applicable only when *kd* < *π*, i.e. dpl > 2.

All polarizability formulations, except CLDR and SO, can be used together with anisotropic electric permittivity, given by a *diagonal* tensor . Polarizability is then also a diagonal tensor, calculated by the same formulae [Eqs. (22)–(31)] but separately for each component:

|  |  |
| --- | --- |
| . | (32) |

The choice of the polarizability prescription is performed by command line option

-pol <type> [<arg>]

where <type> is one of the cldr, cm, dgf, fcd, igt\_so, lak, ldr, nloc, nloc\_av, rrc, so. <arg> is optional flag that can be only avgpol and only for LDR specifying that the LDR polarizability should be averaged over incident polarizations. Default is LDR without averaging. It is important to note that this is not the best option for all cases. Our experience shows that LDR may perform particularly badly (as compared to CM or RR) for very large refractive indices, and FCD (together with its interaction term, §10.2) becomes the best option [23].

Finally, other DDA improvements are known, which modify the polarizability (or permittivity) of the dipoles near the boundary. These improvements include weighted discretization [50] and spectral filtering of the permittivity that was proposed in combination with the FCD [19]. These ideas have not yet been implemented in ADDA.[[45]](#footnote-45) However, adding new options is straightforward for anyone who is familiar with C programming language.[[46]](#footnote-46)

## Interaction term

A few formulations for the direct interaction term are known [2]. Currently, ADDA can use the simplest one (interaction of point dipoles), the FCD (in other words, filtered Green’s tensor [19]), quasistatic version of the FCD, the Integrated Green’s Tensor (IGT, [14]), approximation of IGT (IGTSO). There are also a few prescriptions under development: non-local (NLOC and NLOCav) and second order (SO). The interaction of point dipoles is described by the Green’s tensor of the free space:

|  |  |
| --- | --- |
| , | (33) |

where **r***i* is the radius-vector of the dipole center, **R** = **r***j* − **r***i*, *R* = |**R**|, and *R̂R̂* is a tensor defined as *R̂R̂µν* = *RµRν*. The filtered Green’s tensor is defined [19] as

|  |  |
| --- | --- |
| , | (34) |

where *hr* is filter impulse response:

|  |  |
| --- | --- |
| , | (35) |

*k*F = *π*/*d* – the wavenumber corresponding to the grid, and *g*F is the filtered scalar Green’s function:

|  |  |
| --- | --- |
|  | (36) |

To apply this formulation *k*F must be larger than *k*, i.e. dpl > 2. Quasistatic FCD is obtained in the limit *kR* → 0, which leads to a simpler expression [51]:

|  |  |
| --- | --- |
| . | (37) |

Although it is just a special case of full FCD, it is implemented in ADDA as a separate option for testing and research purposes. Since FCD was originally designed for high refractive indices, we recommend using it especially in this regime. However, it also works fine for moderate refractive index, generally not worse than the standard approach of point dipoles [23].

The IGT directly accounts for the finiteness of the cubical dipole, by integrating over its volume *Vj* [14]:

|  |  |
| --- | --- |
| . | (38) |

Implementation of the IGT in ADDA is based on the Fortran code kindly provided by IGT’s original authors [14]. IGTSO is based on approximate evaluation of Eq. (38), up to second order of *kd*, using tabulated integrals. Thus it is almost as fast as Eq. (33) and almost as accurate as IGT. Both IGT and IGTSO are known to perform very good for small scatterers with large and almost real refractive indices.

The choice of the interaction term is performed by the command line option

-int <type> [<arg1> [<arg2>]]

where <type> is one of the fcd, fcd\_st, igt, igt\_so, nloc, nloc\_av, poi, so. Two optional arguments are relevant only for igt. <arg1> is the maximum distance (in dipole sizes), for which integration is performed. For larger distances simpler Eq. (33) is used. Using value of this parameter from 1 to 3 is recommended – then extra computational time for the IGT is rather small, while most of the accuracy gain is achieved (compared to the default IGT without distance limit). <arg2> specifies the relative error of the integration (minus its decimal logarithm). By default the same value as argument of ‑eps command line option (§12.1) is used. For IGTSO and SO formulation tables of precalculated integrals are used, they are automatically read from files in tables/ (§D.1).

The default formulation for interaction term is that of point dipoles (poi); however, it is expected to be inferior to fcd or igt in many cases. However, the latter have been studied in much less details. Moreover, counterparts of those advanced formulations are still lacking for the reflection term (§10.3), so predicting accuracy in the surface mode (§7) is even more problematic. Therefore, we recommend testing different formulations for a particular class of scattering problems of interest. Moreover, adding a new option to calculate the interaction term is straightforward for anyone who is familiar with C programming language.[[47]](#footnote-47)

## Reflection term

In contrast to **G̅** the reflection term **R̅** does not have full translational symmetry, but only the one parallel to the surface. In particular, **R̅** is a function of distance between evaluation point and the image of source:

|  |  |
| --- | --- |
| , | (39) |

where **ρ** is the distance along the surface. Also, it satisfies . The simplest option to calculate the reflection term is based on a single image dipole

|  |  |
| --- | --- |
| , | (40) |

where  is a projector on the *z*‑axis, and . This approach is exact for perfectly conducting substrate (§7), and can be considered a fast approximation otherwise. The accuracy of the approximation improves with increasing *Z* and/or |*ε*s|.

The general rigorous approach to calculate **R̅** is based on Sommerfeld integrals [52]

|  |  |
| --- | --- |
| , | (41) |

where the scaling (factor of *k*2) is the same as that used for **G̅** in Eq. (33), and the integrals , , , and  depend on *ρ*, *Z*, and *ε*s. Particular expressions for these integrals and computational aspects are discussed in §12.7.

The choice of the reflection term is performed by the command line option

-int\_surf {img|som}

where img and som correspond to single image and Sommerfeld integrals. By default, som is used, unless the substrate is perfectly conducting (then img). Adding a new option to calculate the reflection term is straightforward for anyone who is familiar with C programming language.[[48]](#footnote-48)

## How to calculate scattering quantities

The simplest way to calculate scattering quantities is to consider a set of point dipoles with known polarizations, as summarized by Draine [45]. The scattering amplitude **F**(**n**) is defined through the asymptotic expansion of the electric field:

|  |  |
| --- | --- |
| , | (42) |

where *k*sca is the wave vector for the scattering direction. The original definition of Eq. (42) was given in [53] for the free-space scattering, when *k*sca = *k* and the scattering amplitude is

|  |  |
| --- | --- |
| . | (43) |

We generalize this definition to the surface mode (§7) by defining *k*sca = *m*sca*k*, where *m*sca is the refractive index at the scattering direction – either 1 (above surface, *nz* ≥ 0) or *m*s (below surface, *nz* < 0). For the scattering amplitude in Eq. (42) we have two separate cases. Above the surface the result is a combination of directly scattered [Eq. (43)] and the following reflected wave

|  |  |
| --- | --- |
| , | (44) |

while below the surface (*nz* < 0) – the scattering amplitude is

|  |  |
| --- | --- |
| , | (45) |

The definitions are the same as used in Eqs. (15), (16) but for a wave propagating back from the scattering direction, i.e. **a** = −**n** (or **k**in = −*k*sca**n**) and . In particular, the transmission coefficients in Eq. (45) are for transmission of wave from the substrate into the vacuum. Eqs. (44), (45) are based on the reciprocity principle [54], but can also be obtained from the far-field limit of surface Green’s tensor (see Appendix D of [55]). Factor *m*s in Eq. (45) comes from *k*sca in Eq. (42).

Note that consideration of specific scattering angle (and wavenumber) in Eq. (42) implies that we completely ignore the surface plasmon polaritons, which can, in principle, be considered as scattering at 90°.

The amplitude and Mueller scattering matrices for direction **n** are determined from **F**(**n**) calculated for two incident polarizations (§11.2, §11.3). Time-averaged Poynting vector of the scattered field **S**sca is a second-order function of **F**(**n**):

|  |  |
| --- | --- |
| , | (46) |

where *m*sca is a step function of **n** (relevant in the surface mode), and the exponent is relevant only for scattering into the absorbing substrate. Scattering cross section *C*sca and asymmetry vector **g** are determined by integration of **S**sca(**r**) over the whole solid angle [53]:

|  |  |
| --- | --- |
| , | (47) |
| , | (48) |

where *I*0 is the incident irradiance (§9.2) and the rightmost parts are obtained by neglecting the exponent, depending on *r*. The latter are actually used by ADDA.[[49]](#footnote-49) The definition of **g** is generalized to the surface mode, but this quantity has a clear physical meaning related to the momentum of the scattered field only in the free-space mode (§11.6). Extinction and absorption cross section (*C*ext and *C*abs) [53] are determined directly from **P***i*:

|  |  |
| --- | --- |
| , | (49) |
| . | (50) |

Variations of Eq. (50) (which is used by default) are possible, for instance [14]:

|  |  |
| --- | --- |
| , | (51) |

which is based on considering radiation correction of a *finite* dipole instead of a *point* dipole used in Eq. (50). The difference between these two expressions is subtle and depends on polarizability formulation (§10.1). In particular, it is zero if and only if **M̅** − (2/3)i(*kd*)3 is a Hermitian tensor. For LDR, CLDR, and SO the difference is 𝒪((*kd*)2), but only when ℑ(*m*) ≠ 0. For CM and LAK the difference is 𝒪((*kd*)3) and 𝒪((*kd*)5) respectively for any *m*. For all other formulations the difference is always zero.

Corrections to the above expressions are possible, considering the far-field limit of IGT interaction term (§10.2), in particular [47]

|  |  |
| --- | --- |
| , | (52) |
| , | (53) |

IGTSO is based on truncating Taylor expansion in Eq. (53) and applying the result [1 − (*kd*)2/24] as a multiplicative factor in Eqs.(43) and (49). Other expressions are unchanged, although *C*sca is effectively multiplied by the square of this factor.

The choice between different ways to calculate scattering quantities is performed by command line option

-scat <type>

where <type> is dr, fin, igt\_so, or so. Draine’s classical formulation (dr) corresponds to Eqs. (43), (49), and (50). Finite dipole correction (fin) uses Eq. (51) to calculate *C*abs. A few quick tests showed that finite dipole correction do *not* improve the accuracy, so using the default dr is recommended in most cases. However, igt\_so is recommended, when the same formulation (or IGT) is used for interaction term (§10.2).

*C*sca can be determined as *C*ext − *C*abs (in free-space mode or for non-absorbing substrate), which is faster than Eq. (47). However, this issue needs further clarifying. Draine noted [45] that *C*sca calculated by integration over the solid angle can be more accurate than *C*ext − *C*abs, due to loss of significant digits when the latter two cross sections have close to equal values. Moreover, it has been suggested [56] that the difference between *C*sca calculated by these two methods can be used as an internal measure of DDA accuracy. However, we stress that this difference is a measure of convergence of the iterative solver and accuracy of the integration over the solid angle, but not of the physical approximation itself (in the default mode “‑scat dr”). In other words, the difference may be very small, while the values themselves are very inaccurate (compared to the exact solution). To prove this, one may consider a supplementary disconnected particle consisting of a set of point dipoles with the same positions and polarizabilities as dipoles representing the original (connected) particle. For this supplementary particle DDA equations (20) involve no approximations, since they directly follow from the constitutive equations of a point dipole.[[50]](#footnote-50) Therefore, their exact solution will satisfy the optical theorem, which can be formulated as *C*sca = *C*ext − *C*abs. Hence, the only possible reasons for the latter to be violated are inaccurate solution of Eq. (20) or inaccurate calculation of Eq. (47). And the difference between the original and supplementary particles, which is the error of the DDA itself, is not relevant. The simulations comply with this conclusion (data not shown, but see parts 12 and 13 of the tutorial17).

Similar conclusions are valid for other symmetry-based tests. For instance, recently a reciprocity condition, i.e. the invariance of the simulation results when incident and scattered directions are exchanged, was studied in the framework of the DDA [57]. It was shown that reciprocity condition is automatically satisfied for the DDA results, whenever polarizability formulation (§10.1) is independent of the incident direction (or at least the same for two reciprocal configurations). In other words, the difference of results between two reciprocal configurations can be very small (on the order of the threshold of the iterative solver, §12.1), while the results themselves are completely wrong. And even for the LDR or CLDR polarizability the level of fulfillment of the reciprocity condition (while not trivial) is still not an adequate measure of the overall DDA accuracy.

# What Scattering Quantities Are Calculated

## Definition of scattering plane and angles

Currently two definitions for scattering plane and angles are employed in ADDA. In the free-space mode all scattering angles (polar *θ* and azimuthal *φ*, the latter is counted from the *x*‑axis) are specified in the incident-wave reference frame (§6.1). For default propagation direction (**a** = **e***z*, §9.1) this reference frame coincides with the laboratory reference frame. Two incident polarizations are used: along the *x*‑ and *y*‑axes. Those are perpendicular (⊥) and parallel (||) polarizations [53] respectively with respect to the default scattering plane (*yz*). If the beam propagates along non-default direction, these polarizations are transformed simultaneously with the propagation vector – all three vectors, defining the incident-wave reference frame, are rotated by two spherical angles (first *θ*‑rotation around the *y*‑axis, then *φ*‑rotation around the original *z*‑axis) so that **e***z* is transformed into **a**.[[51]](#footnote-51) Those rotated vectors are shown in the log (§C.4).

By contrast, in the surface mode (§7) the scattering angles *θ* and *φ* are defined with respect to the laboratory reference frame, which is in turn aligned with the surface.[[52]](#footnote-52) The default scattering plane is the one passing through **a** and **e***z*, i.e. the one with *φ* equal to that of vector **a**. Scattering angle *θ* coincides with the corresponding spherical angle, i.e. it is counted from **e***z* (*not* from **a**) in the direction of **a**. For propagation directions **a** = ±**e***z* the scattering plane is the *xz*‑plane (*φ* = 0°), in contrast to *yz*‑plane (*φ* = 90°) above. So the two definitions of the default scattering plane and incident polarizations differ even for **a** = **e***z*.Moreover, *y*- and *x*‑polarizations are then perpendicular (⊥, *s*) and parallel (||, *p*) to the scattering plane.

While the definition of scattering angles is fully determined by the mode (free-space or surface), the default scattering plane can be chosen by command lines

-yz

-scat\_plane

which corresponds to the *yz*‑plane or through-**e***z* plane, respectively, and overrides the default setting. Only one of these two options can be used at a time. Moreover, when a grid of scattering angles is calculated (either for saving or integrating over *φ*, §11.2) the scattering in the scattering plane is by default *not* calculated. However, ADDA may be forced to calculate it by specifying one of the above options.

The range of [0°,180°] in the scattering plane is equally divided into *Nθ* intervals, the latter is defined through the command line option

-ntheta <arg>

By default *Nθ* is from 90 to 720 depending on the size of the computational grid (§6.2). If the particle is not symmetric (§6.7) and orientation averaging (§8.2) is not used, the range is extended to 360°. Totally *Nθ* + 1 or 2*Nθ* + 1 points are calculated.

## Mueller matrix and its derivatives

ADDA calculates the complete Mueller scattering matrix [53] for a set of scattering angles. The Mueller matrix is 4×4 real matrix, which relates the Stokes vector of scattered and incoming waves (the latter is different from incident field in the surface mode, §9.2):

|  |  |
| --- | --- |
| , | (54) |

where the exponent is non-trivial only for scattering into the absorbing substrate. The definitions of the Stokes vector through the electric fields can be found in textbooks [53,58]. In particular, this definition contains the refractive index of the medium *m* as factor ℜ(*m*) [58]. The Mueller matrix can be obtained from the amplitude matrix (§11.3) using the well-known formulae [53]. However, in the surface mode (§7) the result of this formulae need to additionally multiplied by ℜ(*m*sca)/ℜ(*m*in) due to the corresponding factors discussed above – see, e.g., Eq. (56) below. In other words, the Mueller matrix relates the irradiances of the waves, not just squared norms of the electric fields.

Note also that the Mueller matrix is dimensionless and not normalized.[[53]](#footnote-53) Moreover, it is defined with respect to the scattering reference frame opposed to the laboratory reference frame used in definition of the Stokes phase matrix [58].

By default scattering in a single scattering plane (§11.1) is calculated and the result is saved in file mueller (§C.5). To calculate the Mueller matrix in one scattering plane ADDA simulates two incident polarizations, except when the particle is symmetric with respect to the rotation by 90° over the propagation vector of incident radiation (§6.7). In the latter case one incident polarization and two scattering planes are used instead.

More advanced options are available to calculate scattering at any set of angles. If any of the two command line options

-store\_scat\_grid

-phi\_integr <arg>

is specified, the Mueller matrix is calculated for a set of angles, specified, by default, in file scat\_params.dat (§B.4). The first flag indicates that values of the Mueller matrix for all calculated angles should be saved to file mueller\_scatgrid (§C.5), while the second flag turns on the integration of Mueller matrix over *φ* with different multipliers. The latter is defined by <arg>, an integer from 1 to 31, each bit of which, from lowest to highest, corresponds to multipliers 1, cos(2*φ*), sin(2*φ*), cos(4*φ*), and sin(4*φ*) respectively.[[54]](#footnote-54) Integration results are saved to files mueller\_integr, mueller\_integr\_c2, mueller\_integr\_s2, mueller\_integr\_c4, and mueller\_integr\_s4 respectively (§C.5). It is important to note that the results of the integration are divided by the width of the *φ* interval (2*π* by default), i.e. actually averaging over *φ* takes place. If both above-mentioned command line options are specified, both complete-grid and integrated results are saved to hard disk.

The format of the input file is very flexible (see §B.4 for details) allowing one to use either values uniformly spaced in some interval or any set of values, which is explicitly specified, for *θ* and *φ* independently. Even an arbitrary set of (*θ*,*φ*) pairs can be used. However, if integration over *φ* is used, a set of *φ* values must comply with the Romberg integration (§12.6). A different file describing a set of angles can be used if specified as an argument to the command line option

-scat\_grid\_inp <filename>

When a grid of scattering angles is calculated (either for saving or integrating over *φ*) the scattering in a single scattering plane is by default *not* calculated. However, ADDA may be forced to calculate it by specifying command line option ‑yz or ‑scat\_plane (§11.1).

The Mueller matrix contains the complete intensity-based information about angle-resolved scattering for any incident polarization, but other quantities are also commonly used, e.g. differential scattering cross section. Depending on the incident polarization it can be calculated as [cf. Eq. (47)]:

|  |  |
| --- | --- |
| , | (55) |

where plus and minus correspond to incident polarization along the *x*- and *y*‑axis respectively, and *φ* is the azimuthal angle of the scattering direction (relative to the *x*‑axis), and |…| is used since *k*sca is generally complex. “unpol” denotes unpolarized incident light. Eq. (55) is derived from formulae given in [53].

In other applications, the following scattering intensities are of interest:

|  |  |
| --- | --- |
|  | (56) |

where ||‖ and ⊥ denote respectively parallel and perpendicular components (relative to the scattering frame) of the incident and scattered fields. *S*1–*S*4 are elements of the amplitude matrix (§11.3). Corresponding differential cross sections can be obtained from scattering intensities through division by  [cf. Eq. (55)]. We generalized Eq. (56) and others below to the surface mode, but we are not aware of such non-free-space uses.

In applications involving preferential direction it is customary to denote two components of the incident and scattered fields as vertical (v) and horizontal (h). The correspondence between those and ||, ⊥ depends on a particular application. For instance, if all considered scattering planes contain the *z*‑axis, || and ⊥ correspond to v and h respectively [60].

Another related quantity is (radar) backscattering cross section. The name itself is somewhat misleading, since it denotes not the integral quantity (as in §11.4) but the differential scattering cross section at exact backscattering direction multiplied by 4*π* [53]. It can be decomposed into different components, as in Eq. (56), , where *α* and *β* can be replaced by ||, ⊥, v, h, *x* or *y* (see, e.g., [61]). Moreover, the expressions can be simplified using the symmetry fact *S*12 = *S*21 for *θ* = 180° [62]. Therefore, one can obtain the following cross section using the values in file mueller for *θ* = 180°, usually in the last line:

|  |  |
| --- | --- |
| , | (57) |

where the alternating signs before *S*12 are for *yz* (*φ* = 90°) and *xz* (*φ* = 0°) scattering planes respectively. Linear depolarization ratio (at backscattering) is defined through these cross-sections [61], while circular polarization ratio *μ*c can be defined as [63] (for any *φ*):

|  |  |
| --- | --- |
| . | (58) |

## Amplitude matrix

An alternative approach to characterize the scattering process is by 2×2 dimensionless complex matrix, the amplitude scattering matrix, which relates scattered and incoming electric fields (the latter is different from incident field in the surface mode, §9.2):

|  |  |
| --- | --- |
| , | (59) |

where ⊥ and || denote perpendicular and parallel components of the field, respectively, with respect to the scattering plane (§11.1). The definition for the free space corresponds to that in [53],[[55]](#footnote-55) while the generalization to the surface mode is in line with that used previously for 2D case [64]. Thus, the elements of the amplitude scattering matrix are closely related to **F**(**n**) – cf. Eq. (42). Compared to the intensity-based Mueller matrix the amplitude matrix contains also the phase of the field, but it can be measured only by limited number of experimental set-ups, mainly in microwave frequency domain.

ADDA can calculate the amplitude matrix when enabled by the command line option

-scat\_matr {muel|ampl|both|none}

which allows one to specify whether the Mueller matrix (muel, the default choice), the amplitude matrix (ampl), both, or none should be calculated and saved to file.

The set of angles to calculate the amplitude matrix are determined the same way as for the Mueller matrix (§11.2). In particular, by default a uniform grid in the scattering plane (§11.1) is used and the result is saved into file ampl (§C.6). When ‑store\_scat\_grid is used, the amplitude matrix for a grid of scattering angles is saved to file ampl\_scatgrid (§C.6). However, there is one important difference – no averaging of the amplitude matrix is performed neither over orientation (–orient avg) nor over the azimuthal scattering angle (–phi\_integr).[[56]](#footnote-56)

## Integral scattering quantities

All scattering quantities described in this section are saved to several files (§C.7), corresponding to each of two incident polarizations (CrossSec‑X and CrossSec‑Y) and to orientation-averaged results (CrossSec). For the latter the result is calculated for unpolarized incident light. However, it is equal to that for any incident polarization, if the full range of Euler angle *α* is used for averaging (§8.2). ADDA always calculates *C*ext and *C*abs (together with corresponding efficiencies *Q*ext, *Q*abs).[[57]](#footnote-57) Optionally, it can calculate scattering cross section *C*sca (and efficiency *Q*sca) and normalized and non-normalized asymmetry vectors – **g** and **g***C*sca respectively. *C*sca and **g** are defined by Eqs. (47) and (48) respectively, the *z*‑component of **g** is the usual asymmetry parameter <cos*θ*>. Values of cross sections are in units of µm2. All the efficiencies are calculated by dividing the corresponding cross section over the area of the geometrical cross section of the sphere with volume equal to that of dipole representation of the particle, .[[58]](#footnote-58) Optional calculation of *C*sca, **g***C*sca and **g** can be enabled, respectively, by command line options

-Csca

-vec

-asym

If **g** is calculated *C*sca and **g***C*sca are also calculated automatically.[[59]](#footnote-59) The calculation of **g** and *C*sca is performed by integration over the whole solid angle, using a grid of scattering angles. The grid is specified by default in file alldir\_params.dat (see §B.3 for format) in a form suitable for the Romberg integration (§12.6). Integration points for *θ* are spaced uniformly in values of cos*θ*. Different grid file can be specified through the command line option

-alldir\_inp <filename>

In most cases *C*sca can be accurately calculated as *C*ext − *C*abs, without using ‑Csca option. As discussed in §10.4 accuracy of this method can be improved when *C*sca << *C*abs by using smaller *ε* (§12.1). Whether this is more computationally effective than using ‑Csca or not depends on the particular problem. For instance, *C*ext and *C*abs may coincide in (almost) all digits saved to file for particles much smaller than the wavelength, leaving integration of scattered fields over the solid angle as the only viable option. However, in this case the integration can be done analytically (in the free-space mode), using formulae for the Rayleigh regime. For a general non-symmetric particle formulae are cumbersome. However, if total particle polarizability is a diagonal tensor in the laboratory reference frame (e.g. general ellipsoid with axes along coordinate axes), then starting from chapter 5.7 of [53] one can derive:

|  |  |
| --- | --- |
| , | (60) |

where plus and minus correspond to incident polarization along the *y*- and *x*‑axis respectively. Mueller matrix elements are considered at the forward direction in the *yz*‑plane (§11.1), i.e. they can be found in the second line of the mueller file (§11.2).

When absorbing substrate is present (§7) the default definition of *C*sca is unphysical (§10.4). A more adequate approach may be to integrate the scattered field only in the upper hemisphere, which can be done by changing the range of *θ* to [0°,90°] in alldir\_params.dat (§B.3).

Currently ADDA provides no built-in functionality for automatically scanning over a wavelength spectrum. However, a simple workaround is to execute ADDA for each wavelength independently, using a script, and then collect the output data.[[60]](#footnote-60)

## Decay rate enhancement

These quantities are calculated if and only if the point-dipole incident field is used (§9.2). A dipole with polarization **p**0 at position **r**0 has a certain decay rate in free-space, which is enhanced in the presence of nanoparticle. The emitted energy is, in general, partly absorbed by the particle (nonradiative part) and partly scattered to the infinity (radiative part). The relevant formulae are given in [65,66]. Here we present them in terms of effective cross sections (proportional to decay rates) to reuse quantities described in §11.4. Free-space decay cross section *C*0 is given as

|  |  |
| --- | --- |
| . | (61) |

In the presence of the nanoparticle, the total decay cross section *C*tot is also given by Eq. (61) but with the modified Green’s tensor (accounting for particle):

|  |  |
| --- | --- |
| , | (62) |
| , | (63) |

where symmetry (reciprocity) relation

|  |  |
| --- | --- |
|  | (64) |

has been used. *C*enh corresponds to decay rate enhancement due to particle and its simplified expression (assuming real **p**0) is very similar (but not equal) to *C*ext in Eq. (49).

The part absorbed by the particle (nonradiative, NR) is given by *C*abs (§11.4), while radiative part *C*rad = *С*tot – *C*abs, which is not equal to *C*sca since incident dipole field interferes with the scattered field. In other words, *C*rad is the scattering cross section of the whole set of dipoles, including both exciting one and those from discretization of the particle. The enhancements of decay rates are obtained by normalizing corresponding cross sections to *C*0:

|  |  |
| --- | --- |
| . | (65) |

These three enhancement factors are calculated and saved into file CrossSec (§C.7). Note also that these factors are independent of the particular magnitude (or units) of **p**0 used for simulation.

In the surface mode (§7) the decay rate is changed by the surface itself even when no particle is present. Corresponding cross section *C*surf is obtained by replacing **G̅** by **G̅** + **R̅** (§10.3) in Eq. (61). ADDA still calculates the enhancement factors using Eq. (65), i.e. normalizing to *C*0, but also saves *C*surf/*C*0 into file CrossSec (§C.7), so ratios with respect to *C*surf can be easily obtained manually. The important limitation exists for absorbing substrate, since *C*abs does not include the absorption in the substrate. Then the total enhancement factor is correct, but its division into radiative and not radiative parts is not. The possible (complicated) workaround is to integrate the total far-field (sum of exciting and scattered fields) over the upper hemisphere.[[61]](#footnote-61)

## Radiation forces

Radiation force for the whole scatterer and for each dipole can also be calculated by ADDA. If the command line option

-Cpr

is specified, the radiation force (pressure) cross section **C**pr and efficiency **Q**pr (vectors) are calculated and saved into file CrossSec (§C.7). Total time-averaged force **F**rad acting on the particle is proportional to **C**pr [67,68]:

|  |  |
| --- | --- |
| , | (66) |

where *w*rad is time-averaged energy density (or pressure) of the electric field, **E**0 and *I*0 are the electric field amplitude (complex vector) and the time-averaged irradiance of the incident beam. For non-plane beams (§9.2), **E**0 and *I*0 are considered in the focal point of a beam. The formula connecting *w*rad and **E**0 is given for Gaussian-CGS system of units, which is used throughout ADDA. In SI “1/8*π*” should be replaced by “*ε*0/2”. However, the relation between *w*rad and *I*0 is the same for both systems. It is important to note, that Eq. (66) explicitly contains the refractive index of the surrounding medium *m*0. Hence, **C**pr calculated for equivalent scattering problem of particle in the vacuum (§4) is the correct one, but **F**rad should be additionally multiplied by *m*0 (for the same *I*0). Relation between *I*0 and the total beam power is discussed in §9.2.

To save the radiation forces on each dipole into file RadForce (§C.8) use

-store\_force

This option implies ‑Cpr and can be used, e.g., to study internal stress inside the particle or forces and/or torques acting on separate parts of a multi-particle system. Unfortunately, currently there is no automatic way to calculate optical torque on the particle (or on each dipole separately). However, there exist a workaround.[[62]](#footnote-62) It is important to note that these dipole-wise radiation forces are given in the particle reference frame, while integral quantities, saved in CrossSec, are given in either laboratory or incident-wave reference frame (§11.1).

The calculation of optical force on each dipole implicitly assumes unity amplitude of the incident beam (|**E**0| = 1 statV/cm). Hence, the unit of force in file RadForce is 10−8 dyne when all lengths are measured in µm (see §2). For other value of |**E**0|, the result should be multiplied by |**E**0|2. For instance, if |**E**0| = 1 V/m the unit of force is 1.11×10−22 N. Moreover, to account for surrounding medium one should multiply the result of the “scaled” problem by  and *m*0 for the same **E**0 and *I*0 respectively.

For a plane incident wave **C**pr can also be calculated from momentum conservation [67]:

|  |  |
| --- | --- |
| , | (67) |

where the two terms correspond to momentum extracted from the incident wave and contained in the scattered wave, respectively. The same distinction also applies to force on each dipole [7], and they are calculated separately by ADDA. For convenience, these two resulting vectors are also saved to file CrossSec, when ‑Cpr is used. They can be directly compared to the values, obtained by the default approach (§11.4). Unfortunately, Eq. (67) holds neither for non-plane beams nor for the surface mode, in particular, momentum extracted from the incident wave is no more directly proportional to *C*ext (extracted energy).

It is important to note that calculation of radiation forces is still under development. There are three major drawbacks of the current implementation:

* It cannot be used in combination with non-plane beams (§9.2), due to more complex expressions for “extinction” force.[[63]](#footnote-63)
* It is computationally inefficient with speed , also it occupies 𝒪(*N*real) extra memory in parallel mode.[[64]](#footnote-64) It is planned to rewrite this implementation according to Hoekstra *et al.* [7], which will make it 𝒪(*N*ln*N*) – usually even faster than calculation of **g***C*sca by integration of the scattered field (§11.4). However, currently the fastest ways to obtain **C**pr for a *plane* incident wave is through Eq. (67) without calculating the radiation forces at all.
* It is not compatible with the surface mode (§7).[[65]](#footnote-65)

## Internal fields and dipole polarizations

ADDA can save internal electric fields **E***i* and/or dipole polarizations **P***i* at each dipole (§10) to files IntField and DipPol respectively (§C.9), using command line options

-store\_int\_field

-store\_dip\_pol

These options allow one to study in details the accuracy of the DDA (see e.g. [17]) or the physics behind it. To save internal fields for future use by ADDA consider using checkpoints of type “always” (§12.5).

## Near-field

Near-field is the electric field near the particle, i.e. neither in the particle itself nor far enough to be considered a scattered field. Currently, ADDA cannot calculate the near-field in a completely convenient manner. However, Fabio Della Sala and Stefania D'Agostino [27] have contributed a package near\_field, which adds this functionality using the dipole polarizations calculated by ADDA. This package is distributed in the misc/ folder, and is accompanied by all necessary instructions.

While the above option is recommended one, there exist another workaround that may be preferential in some special cases. One may include all the points, where near-field need to be calculated, in the particle geometry, but set their refractive index to a value very close to 1 (e.g. 1.00001). Then the scattering problem is identical to the initial one. Saving the internal fields (§11.7) will directly produce the required near-field together with the field inside the particle, even in the surface mode [37]. The drawback of this workaround is increase of computational time, which depends on the size of the box containing the extended particle geometry. Moreover, a user is required to specify a shape file, except for the simplest cases. For instance, predefined shapes “coated” or “spherebox” (§6.4) can be used to calculate near-field in a sphere or cube around the homogenous sphere, respectively. However, this method can be much faster when full 3D picture of the near field is required, because it implicitly uses FFT-acceleration of the simulations. This idea was further developed for even more efficient calculation of the near-field [69], but this approach has not been yet implemented in ADDA.

# Computational Issues

## Iterative solver

The main computation of a DDA simulation, usually taking the major part the execution time, is finding a solution of a large system of linear equations. ADDA uses an alternative form of Eq. (20):

|  |  |
| --- | --- |
| . | (68) |

Decomposition of  is possible if and only if it is complex-symmetric. This is sufficient for the current version of ADDA, which supports only diagonal polarizability tensors. Since , the interaction matrix **A** is complex–symmetric and Jacobi-preconditioned (has unity diagonal). ADDA incorporates several different iterative methods for solution of Eq. (68): Bi-conjugate gradient (Bi-CG) [70,71], Bi-CG stabilized (Bi-CGStab) [72], enhanced Bi-CGStab(2) [73], conjugate gradient applied to normalized equations with minimization of the residual norm (CGNR) [72], CSYM [74], quasi minimal residual (QMR) [70] and its modification based on 2-term recurrence (QMR2) [75]. Adding of a new iterative solver is straightforward for anyone who is familiar with C programming language.[[66]](#footnote-66)

Comparison of the iterative solvers in terms of matrix–vector products (MVPs) per iteration and required number of vectors (memory, see §5) is presented in Table 3. Some solvers employ the complex symmetric property of **A** to calculate only one MVP per iteration [70]. Our experience suggests that QMR is usually the fastest iterative solver, however in some cases Bi-CGStab may be faster (also their modern variants, namely QMR2 and Bi-CGStab(2) respectively, may be preferred – see below). Performance of Bi-CG is comparable to that of QMR, but convergence behavior of the former is erratic, similar to that of Bi-CGStab. Still, Bi-CG may be preferred when memory is sparse. While being the slowest, CGNR is very simple and its convergence is guaranteed to be monotonic [72]. CSYM has the same properties, and is expected to be faster than CGNR, in terms of MVPs [74]. QMR2 is expected to be faster than QMR in finite-precision arithmetic [75] and requires slightly less memory. Bi-CGStab(2) is expected to be faster than Bi-CGStab [73] in terms of MVPs, but requires slightly more memory.

The iterative solver is chosen by the command line option

-iter <type>

where <type> is one of the values specified in Table 3. By default QMR is used. There are several options to choose the initial field, set by the command line option

-init\_field {auto|inc|read <filenameY> [<filenameX>]|wkb|zero}

where zero vector is a general approach and inc (derived from the incident field, more precisely – equal to the right-hand-side of the linear system) may be closer to the exact solution for small index-matching particles. wkb is derived from the incident field corrected for phase shift during propagation in the particle (Wentzel–Kramers–Brillouin approximation [76]). It can be considered as an extension of inc, but currently it works only for default incident beam – plane wave propagating along the *z*‑axis in particle reference frame (§9) and not in the surface mode (§7).[[67]](#footnote-67) By default (auto) ADDA automatically choses from zero and inc the one with lesser residual norm.[[68]](#footnote-68) Finally, the starting field can also be read from files. Normally two files are required for *y*‑ and *x*‑polarizations respectively (§9.1), but a single filename is sufficient if only *y*‑polarization is used (e.g. due to symmetry). Incident field should be specified in a *particle* reference frame, see §B.7 for file format. The choice of initial field is shown in the log (§C.4).

Table 3. Iterative solvers.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| <type> | Name | Syma | MVPs per iteration | # of vectorsb | Max stagnation |
| bcgs2 | Bi-CGStab(2) | − | 4 | 8 | 15 000 |
| bicg | Bi-CG | + | 1 | 4 | 50 000 |
| bicgstab | Bi-CGStab | − | 2 | 7 | 30 000 |
| cgnr | CGNR | − | 2 | 4 | 10 |
| csym | CSYM | + | 1 | 6 | 10 |
| qmr | QMR | + | 1 | 7 | 50 000 |
| qmr2 | QMR2 | + | 1 | 6 | 50 000 |

a whether complex symmetric property of the matrix is explicitly used.

b includes input residual and output solution, but does not include incident beam.

It is important to note, that initial field inc corresponds to , i.e. it sets exciting field, while both wkb and read define internal field **E**(0), cf. Eq. (68). In particular, “‑beam read fY fX –init\_field inc” is not completely equivalent to “‑init\_field read fY fX” in terms of the starting vector. The connection between the two fields depends on the polarizability formulation (§10.1), but can be approximately described as  (this equation is exact for CM polarizability).

The stopping criterion for iterative solvers is the relative norm of the residual. The process stops when this norm is less than *ε*, which can be specified by the command line option

-eps <arg>

where *ε* = 10−<arg>. By default, *ε* = 10−5. It is important to note that the residual is updated iteratively along the execution of the iterative solver, which may cause substantial round-off errors for large number of iterations. True residual at the end of the iterative solver can be calculated by ADDA through additional MVP. For that specify

-recalc\_resid

in the command line. The maximum number of iterations can be specified as <arg> to the command line option

-maxiter <arg>

If this number is reached before convergence (to *ε* level) ADDA will produce a warning, but will continue to calculate the (potentially less accurate) scattering quantities. So –maxiter can be used to softly limit the simulation time. By default the maximum number of iterations is set to a very high value, which is not expected to be ever reached.[[69]](#footnote-69) Also, ADDA will terminate execution with an error if the iterative solver stagnates for a long time, i.e. residual norm do not decrease during a number of last iterations. Corresponding numbers are specified in Table 3.[[70]](#footnote-70)

All iterative solvers except CGNR and CSYM are susceptible to breakdowns. Although such situations are very improbable, they may happen in specific cases. For instance, simulation of light scattering by cube with edge length that is exactly a multiple of the wavelength results in breakdowns of QMR, QMR2, and Bi-CG. ADDA should detect almost any breakdown and produce a meaningful error message; however, it is possible that some breakdown is not detected. It then results in the stagnation of the residual norm or its oscillations without any further progress. On contrary, ADDA may claim breakdown when the convergence is slow but still satisfactory. The behavior of breakdown detection may be modified,[[71]](#footnote-71) but it requires recompilation of the code.

If you notice any error of the breakdown detection, both false-negative and false-positive, please communicate it to the developers. If the breakdown does appear, the solution is either to try different iterative solver or adjust input parameters a little bit. Usually changing particle size (or wavelength) by only 0.01% completely eliminates the breakdown.

In general, it is hard to estimate the required number of iterations *a priori*. However, for the case of particles much smaller than the wavelength (e.g., nanoparticles) in free space a simple formula is available [47]:

|  |  |
| --- | --- |
| , | (69) |

which depends on neither particle shape nor size (as long as the latter is sufficiently small) and is expected to be accurate within a factor of two for QMR and Bi-CG.

## Fast Fourier transform

The iterative method only needs the interaction matrix for calculating matrix–vector products. This can be done in 𝒪(*N*ln*N*) operations (where *N* is the total number of dipoles) using the FFT [77]. In ADDA 3D (parallel) FFT is explicitly decomposed into a set of 1D FFTs, reducing calculations (see [6] for details). In the surface mode (§7) the 3D FFT acceleration is also used for the reflected part simultaneously with the direct interaction part.[[72]](#footnote-72) Overall, the time of one iteration in the surface mode is approximately 50% longer than that in the free-space mode.[[73]](#footnote-73)

1D FFTs are performed using standard libraries – two are implemented in ADDA: a routine by Temperton (CFFT99, [79]), or the more advanced package FFTW3 [80]. The latter is generally significantly faster, but requires separate installation of the package.[[74]](#footnote-74) The FFT routine to use is chosen at compile time: default is FFTW3, and another one is turned on by compilation option FFT\_TEMPERTON.12

FFT is performed on the grid that is doubled in each dimension compared to the computational grid. Temperton’s FFT requires that the dimensions of this grid be of the form 2*p*3*q*5*r* (all exponents are integers), FFTW3 works with any grid dimensions but is most effective for dimensions of the form 2*p*3*q*5*r*7*s*11*u*13*v* (*u* + *v* ≤ 1). It should not be a limitation for the sequential mode, since ADDA automatically increases the FFT-grid dimensions to the first number of the required form.[[75]](#footnote-75) But in parallel mode these dimensions along the *x*- and *z*‑axes must also divide *n*p and 2*n*p respectively. Therefore the increase of the dimensions (and hence simulation time) may be substantial, and not possible at all if the number of processors divide any prime number larger than 5 for Temperton FFT or has more than one divisor of either 11 or 13 (or at least one larger than 13) for FFTW3. Therefore it is strongly recommended *not* to use such “weird” number of processors.[[76]](#footnote-76) It is the user’s responsibility to optimize the combination of computational grid dimensions and number of processors, although ADDA will work, but probably not efficiently, for most of the combinations (see also §6.6).

In OpenCL mode ADDA employs one of the two FFT implementations. The default one is clAmdFft, which works for sizes of the form 2*p*3*q*5*r*, but requires separate package installation[[77]](#footnote-77) and may have problems when run on Nvidia GPUs.[[78]](#footnote-78) Recent source already uses its predecessor – clFFT. Alternative implementation (by Apple) is turned on by compilation option CLFFT\_APPLE.12 It is limited to power-of-two sizes and is significantly slower than clAmdFft. For both implementations ADDA will automatically adjust the FFT-grid dimensions to the minimum supported size.

Symmetry of the DDA interaction matrix is used in ADDA to reduce the storage space for the Fourier-transformed matrix, except when SO formulae to calculate interaction term are used (§10.2). This option can be disabled (mainly for debugging purposes) by specifying

-no\_reduced\_fft

in the command line.

## Sparse mode

For cases when *N* >> *N*real, e.g. for very sparse (porous) aggregates, FFT may not provide desired acceleration. Specially for such cases there is a compilation mode of ADDA, named “sparse mode”. It is a direct implementation of matrix–vector product in the DDA without FFT. Its main advantage is that the empty dipoles are not included at all in the data model, which decreases required computer memory and simplifies MPI parallelization. The effect on computational speed depends on the porosity (sparseness) of the particle: the standard (FFT) mode is faster for moderately porous particles, while the sparse mode is faster for extremely porous ones. In particular, the sparse ADDA was used for simulations of radar backscattering by snowflakes [81].

In general, usage of sparse mode is very similar to the FFT mode, discarding all FFT-related aspects. However there are certain limitations (incompatibilities with some of other ADDA features), which are discussed at the corresponding wiki page,[[79]](#footnote-79) together with compilation and usage instructions.

System requirements for sparse mode are significantly different from the standard mode (§5). Memory requirements are

|  |  |
| --- | --- |
| , | (70) |

where definitions of §5 are used and range of numbers correspond to different iterative solvers. A term proportional to *n*p indicates poor parallel scaling of the memory for the current implementation.[[80]](#footnote-80) The surface mode (§7) requires additional memory

|  |  |
| --- | --- |
| , | (71) |

which also badly scales in MPI mode.[[81]](#footnote-81) Computational time (more specifically, time of one iteration) scales as , and this time almost perfectly divides by *n*p during parallel execution.

While the developers do their best to ensure reliability of sparse mode, it is a good idea to perform selected tests of this mode against the standard mode on a few sample problems before performing a large set of simulations.

## Parallel performance

ADDA is capable of running on a multiprocessor system, parallelizing a single DDA simulation. It uses MPI for communication routines. This feature can be used both to accelerate the computations and to circumvent the single-computer limit of the available memory, thus enabling simulations with a huge number of dipoles. We do not discuss the parallel efficiency of ADDA in detail, since it largely depends on the hardware. However, in our experience it was usually larger than 70–90% on a modern computer clusters (if the FFT grid is optimally partitioned among the processors, §6.6), and close to 100% in sparse mode (§12.3). It is also important to note that the MPI interface may occupy significant amount of RAM on each node, thereby decreasing the RAM available for ADDA itself (see also §5 and §6.6).

## Checkpoints

To facilitate very long simulations ADDA incorporates a checkpoint system, which can be used to break a single simulation into smaller parts. All the intermediate vectors of the iterative solver (§12.1) are saved, which allows restarting the iterative solver exactly at the position, where the checkpoint was created. Time of a checkpoint is specified by command line option

-chpoint <time>

where <time> is in format “#d#h#m#s”.[[82]](#footnote-82) There are 3 possible strategies for checkpoints, chosen through the command line option

-chp\_type <type>

where <type> is one of normal, regular, always. “Normal” means that after the checkpoint time elapsed, the checkpoint is saved as soon as possible (it waits for the finishing of the current iteration) and ADDA finishes execution without any further actions. This type is useful when one need ADDA to run not longer than certain time. “Regular” checkpoints are saved after every specified time interval but do not influence the normal execution of ADDA – it runs until simulation is fully completed. Use this option when abrupt termination of ADDA may occur (e.g. system crash or the system resources are urgently needed for other tasks). “Always” type is similar to “normal” if checkpoint time elapsed during the execution, however it will also save a checkpoint (after the last iteration) when ADDA finishes normally earlier. That is the only checkpoint type, for which time may be not specified (then it is equivalent to infinite time). It may be useful if the simulation is valuable by itself but may be extended in the future, e.g. to obtain better convergence (lower *ε*, §12.1) or to calculate different scattering quantities (§11).

To restart the simulation from a checkpoint

-chp\_load

should be specified in the command line. The user should take care that the simulation is restarted with the same parameters that were used when saving the checkpoint. Although some parameters can indeed be different (e.g. those determining the output of ADDA), the consistency of the results is user’s responsibility. By default all the checkpoint data is saved in the directory chpoint (§D.2), however a different directory (the same for saving and loading of checkpoints) can be specified through the command line option

-chp\_dir <dirname>

The total size of the checkpoint files is approximately half of the RAM used, therefore 1) enough space on the hard disk should be available; 2) saving of a checkpoint may take considerable time. Both issues are especially relevant for large simulations on multiprocessor systems. If the simulation time is strictly limited (e.g. by a batch system of a supercomputer with shared usage) checkpoint time should be set slightly smaller, so that ADDA would have enough time to finish the iteration and save a checkpoint (and possibly to calculate the scattering quantities if the iterative solver will converge just before the checkpoint time). User should estimate the needed time reserve himself. When loading a checkpoint, ADDA initializes anew, this takes some time. However, this time is usually small compared to the time used for the iterations.

It is also important to note that by default the same checkpoint directory is used for all the simulations on the current system that are run from the same path, therefore new checkpoints overwrite the old ones.[[83]](#footnote-83) To avoid it specify a different checkpoint directory for each instance of ADDA; it is obligatory when several instances of ADDA run in parallel. For now, ADDA *always* saves checkpoints into the same directory where it loads it from.

Currently only the state of the iterative solver is saved at a checkpoint, therefore it is suitable only for simulations for a single incident polarization.

## Romberg integration

Integration is performed in several parts of ADDA: orientation averaging (§8.2), integration of the Mueller matrix over the azimuthal angle (§11.2), and integration of the scattered field over the whole solid angle (§11.4). The same routine is used for all these purposes, which is based on the one- or two-dimensional Romberg integration [82]. This is a high-order technique that may be used in adaptive mode, automatically performing only the necessary number of function evaluations to reach a prescribed accuracy. The latter is relevant for orientation averaging, where each function evaluation is a complete DDA simulation, but not for integration over scattering angles, for which all values are precalculated. Romberg integration also provides an estimate of the integration error, which is reliable for “sufficiently nice” functions [82]. When 2D integration is performed ADDA integrates an error estimate obtained in the inner integration loop simultaneously with the function values, resulting in a reliable estimate of the final error in the outer loop. The information about the integration together with errors is saved to separate log files (§C.10): log\_orient\_avg, log\_int\_Csca‑X, log\_int\_asym\_x‑X, log\_int\_asym\_y‑X, log\_int\_asym\_z‑X for orientation averaging, calculation of *C*sca and each component of **g** respectively (the last 4 file names have different suffixes – X or Y – for different incident polarizations). For orientation averaging some information is saved to the main log (§C.4). For integration of the Mueller matrix over the azimuthal angle only the averaged errors are saved together with the values directly to mueller\_integr files (§C.5)

The drawback of the Romberg integration is that argument values must be uniformly spaced and their total number is limited to be 2*n* + 1 (*n* is any integer). The set of integration points is specified by minimum and maximum values and minimum and maximum number of subdivisions (refinements) *J*min and *J*max (the latter is equal to *n*). The required accuracy to reach is also a parameter. In some cases minimum and maximum values of some arguments are equivalent (e.g. 0° and 360° for *φ*), ADDA accounts for it to slightly decrease simulation time.

If the function is “nice” and periodic over the interval of integration, then it is not beneficial and may be even harmful to use higher order integration scheme. For such cases the simplest trapezoid rule (or equivalently midpoint rule) is the most efficient [82]. The same is true, when e.g. the function is integrated over the half of its period and is symmetric with respect to both borders of the integration interval. ADDA’s behavior is determined by the flag periodic in the input files. If it is true then trapezoid rule is used as a special case of the general Romberg scheme. This keeps the limitation on the number of integration points, but provides adaptability and reliable error estimates. All the integration parameters are specified in input files: avg\_params.dat (§B.2), scat\_params.dat (§B.4), alldir\_params.dat (§B.3) corresponding to different integration tasks.

## Sommerfeld integrals

The four Sommerfeld integrals used by ADDA to calculate reflection term (§10.3) are expressed through two essential integrals *V*22 and *U*22 [52,83]:

|  |  |
| --- | --- |
| , | (72) |

which, in turn, can be evaluated by integration of either Bessel or Hankel functions with appropriate deformation of complex path:

|  |  |
| --- | --- |
|  | (73) |

ADDA calculates Sommerfeld integrals using slightly modified routine from NEC2C,[[84]](#footnote-84) which is a Fortran-to-C translation of [52]. This routine contains internal error control, and has been tested to produce consistent (within 0.1%) results in comparison with other codes [84,85]. Still, it should be regarded as a black box. While the accuracy is expected to be sufficient for most applications, it is hard to confidently put any numbers on it.

To accelerate computations ADDA first computes a table of Sommerfeld integrals for all unique values of *ρ* and *Z* required for dipoles on the computational grid, which takes time comparable to 200 iterations of the iterative solver[[85]](#footnote-85). Moreover, such table requires additional memory (§5).

# Timing

## Basic timing

The basic timing of ADDA execution on a single processor is performed using standard ANSI C functions clock and time, which are completely portable. The drawbacks are low precision (1 s) of wall-time and low precision (0.01–0.1 s on most systems) and possible overflows (after 1 hour on some systems) of the processor timer. However, ADDA will use precise wall-timers (precision of order µs) when available, including both Windows and POSIX operating systems. Wall-time is used only for the total execution time and timing of checkpoints (§12.5), and for the rest processor time is measured. It makes timing more precise especially on desktop computers that are partly occupied by other tasks; however, for long simulations some timing results may become meaningless because of the timer overflow. The problem with clock overflows should not be relevant in 64-bit environment because of larger size of clock\_t type (system dependent). This timing may also be inaccurate in OpenCL mode, since the standard doesn’t defines whether clock includes the time of GPU calculations. This can be assessed by comparing total processor and wall times, given in log (§C.4).[[86]](#footnote-86)

In parallel mode all the times are wall-times measured by the high-precision MPI\_Wtime function, which is a part of MPI standard. This solves above-mentioned problems of the ANSI C timers.

Timing results are presented in the end of the log (§C.4) together with some statistics (total number of iterations, total number of planes where the scattered field is calculated). It covers all major parts of ADDA execution: initialization (including initialization of FFT, §12.2, building the interaction matrix, and constructing a dipole representation of the particle, §6.3), solution for the internal fields (including generation of incident beam, §9, and iterative solver, §12.1), calculation of the scattering quantities (scattered electric field and others, §11), input/output (including checkpoint loading/saving, §12.5), integration (§12.6). Some are divided into subsections. If ‑prognosis option is used, only the time for constructing a particle is shown.

In parallel mode communication time (between different processors) is shown separately for some tasks, which can be used to estimate the parallel efficiency. To measure this time accurately synchronization is done before the communication takes place. Our experience shows that this should not decrease the performance of ADDA, except for the small effect in the granule generator (§6.5).

## Precise timing

This feature of ADDA is used to perform the thorough timing of the most computationally intensive parts: initialization of interaction matrix and FFT (especially FFTW3, §12.2) and matrix–vector product. It gives the detailed information both on FFT and algebraic parts, which can be used for deep optimization or performance studies. However, this regime is incompatible with the normal ADDA execution – it terminates after the first matrix–vector product. Only the stdout (§C.2) and log (§C.4) are produced. Precision of the precise timing routines are of order µs, however they measure wall-time[[87]](#footnote-87) and are operating-system-dependent (see §13.1). To enable precise timing recompile ADDA with option PRECISE\_TIMING.12

Behavior in OpenCL mode.

# Miscellanea

Additional files contributed by users will be located in the directory misc/. These files should be considered to be supported (to some extent) by their respective authors. They should be accompanied by enough information to explain their use. A brief description of the available tools is given together with description of ADDA package.13 Moreover, being a command line tool ADDA easily lends itself to scripting and automatization. In particular, there is a wrapper in language R with several usage examples[[88]](#footnote-88) – it can be easily generalized to other scripting languages and applications.

# Finale

This manual is somewhat inelegant, but we hope that it will prove useful. The structure of the input files is intended to be simple and suggestive so that, after reading the above notes once, the users may not have to refer to them again. Command line help system (‑h option, §3.1) is intended to provide quick reference on different command line options. If that is not enough, thorough description of all command line options can be found in this manual (§A). A lot of other information about ADDA can be found in corresponding wiki-pages,[[89]](#footnote-89) ranging from compiling instructions to description of how to add new predefined shapes. In particular, an up-to-date list of acknowledgements is available,[[90]](#footnote-90) including contributors and funding sources.

Users are encouraged to subscribe to adda-announce Google group7; bug reports and any new releases of ADDA will be made known to those who do. All known bugs are available at issue tracker,5 it also lists the future plan for ADDA development. Users may upvote issues, which they consider important, to influence their priorities (GitHub account is required for that). Specific suggestions for improving ADDA and this manual are welcomed. You may either submit it directly to the issue tracker5 or discuss it in the ADDA discussion group.9 A list of frequently asked questions is also available.8

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1. Command Line Options

Most of the parameters are specified to ADDA in the command line. ADDA will automatically detect most inconsistencies in input parameters, and produce an error or warning if necessary (§C.1). If you notice that particular command line option causes abrupt termination or any erroneous behavior of ADDA, please communicate it to the developers. Command line option ‑h can be used to get both general help and detailed description of other command line options.

Below is the full list of command line options in alphabetical order. “<…>” denotes an argument, “[…]” denotes an optional part, and “{…|…}” denotes different possibilities. “Default:” and “Example:” fields specify the values of parameters excluding the command line option itself. Default value for all flags (those that can be used without arguments) is false, i.e. if the flag is not specified, the corresponding option is not enabled.

-alldir\_inp <filename>

Specifies a file with parameters of the grid of scattering angles for calculating integral scattering quantities (§11.4). Input format is described in §B.3.

Default: alldir\_params.dat

-anisotr

Specifies that refractive index is anisotropic (§6.3). Option ‑m then accepts 6 arguments per each domain. Cannot be used with CLDR polarizability (§10.1) and all SO formulations (§10.1, §10.2, §10.4).

-asym

Calculate the asymmetry vector (§11.4). Implies ‑Csca and ‑vec.

-beam <type> [<args>]

Sets incident beam, either predefined or “read” from file (§9.2). All parameters of predefined beam types are floats.

Default: plane

-chp\_dir <dirname>

Sets directory for the checkpoint (both for saving and loading, §12.5).

Default: chpoint

-chp\_load

Restart a simulation from a checkpoint (§12.5).

-chp\_type {normal|regular|always}

Sets type of the checkpoint (§12.5). All types, except always, require ‑chpoint.

Default: normal

-chpoint <time>

Specifies the time for checkpoints (§12.5) in format “#d#h#m#s”. All fields are optional, numbers are integers, “s” can be omitted, the format is not case sensitive.

Examples: 12h30M, 1D10s, 3600

-Cpr

Calculate the total radiation force, expressed as cross section (§11.6).

-Csca

Calculate scattering cross section (by integrating the scattered field, §11.4).

-dir <dirname>

Sets directory for output files.

Default: constructed automatically, see §C.3.

-dpl <arg>

Sets parameter “dipoles per lambda” (§6.2), float.

Default: 10|*m*|, where *m* is the maximum (by absolute value) refractive index specified by the ‑m option (§6.3).

-eps <arg>

Specifies the stopping criterion for the iterative solver (§12.1) by setting the relative norm of the residual *ε* to reach. <arg> is an exponent of base 10 (float), i.e. *ε* = 10−<arg>.

Default: 5 (*ε* = 10−5)

-eq\_rad <arg>

Sets volume-equivalent radius of the particle in µm (§6.2), float. If default wavelength is used, this option specifies the volume-equivalent size parameter. Cannot be used together with ‑size. Size is defined by some shapes themselves, then this option can be used to override the internal specification and scale the shape.

Default: determined by the value of –size or by ‑grid, ‑dpl, and –lambda.

-gpu <index>

Specifies index of GPU that should be used (starting from 0). Relevant only for OpenCL version of ADDA, running on a system with several GPUs (§3.3).

Default: 0

-granul <vol\_frac> <diam> [<dom\_number>]

Specifies that one particle domain should be randomly filled with spherical granules with specified diameter <diam> and volume fraction <vol\_frac> (§6.5). Domain number to fill is given by the last optional argument.

Default <dom\_number>: 1

-grid <nx> [<ny> <nz>]

Sets dimensions of the computation grid (§6.2). Arguments should be even integers (otherwise corrected automatically by ADDA). In most cases <ny> and <nz> can be omitted (they are automatically determined by <nx> based on the proportions of the scatterer). This command line option is not relevant when particle geometry is read from a file (‑shape read, §6.3). If ‑jagged option is used the grid dimension is effectively multiplied by the specified number (§6.3).

Default: 16 (if neither ‑size nor ‑eq\_rad are specified) or defined by –size or ‑eq\_rad, ‑lambda, and ‑dpl.

-h [<opt> [<subopt>]]

Shows help. If used without arguments, ADDA shows a list of all available command line options. If first argument is specified, help on specific command line option <opt> is shown (only the name of the option should be given without preceding dash). For some options (e.g. ‑beam or ‑shape) specific help on a particular suboption <subopt> may be shown.

Example: shape coated

-init\_field {auto|inc|read <filenameY> [<filenameX>]|wkb|zero}

Sets prescription to calculate initial (starting) field for the iterative solver (§12.1). auto – automatically choose from zero and inc based on the lower residual value, inc – derived from the incident field, wkb – from WKB approximation, read – defined by separate files, which names are given as arguments, zero – a zero vector. Format of the files for option read is described in §B.7.

Default: auto

-int {fcd|fcd\_st|igt [<lim> [<prec>]]|igt\_so|nloc <Rp>|nloc\_av <Rp>|poi|so}

Sets prescription to calculate interaction term (§10.2). The SO formulation cannot be used with ‑anisotr (§6.3). fcd requires dpl to be larger than 2. Parameters of igt are: <lim> – maximum distance (in dipole sizes), for which integration is performed, (default: ∞); <prec> – minus decimal logarithm of relative error of the integration, i.e. *ε* = 10-<prec> (default: same as argument of ‑eps command line option). <Rp> is the width of the Gaussian density (in μm) for non-local formulations.

Default: poi

-int\_surf {img|som}

Sets prescription to calculate the reflection term (§10.3).

Default: som (but img if surface is perfectly reflecting)

-iter {bcgs2|bicg|bicgstab|cgnr|csym|qmr|qmr2}

Sets the iterative solver (§12.1).

Default: qmr

-jagged <arg>

Sets a size of a big dipole in units of small dipoles (§6.3), integer. It is used to improve the discretization of the particle without changing the shape.

Default: 1

-lambda <arg>

Sets incident wavelength in µm (§6.2), float.

Default: 2*π*

-m {<m1Re> <m1Im> […]|  
<m1xxRe> <m1xxIm> <m1yyRe> <m1yyIm> <m1zzRe> <m1zzIm> […]}

Sets refractive indices (§6.3), float. Each pair of arguments specifies real and imaginary parts of the refractive index of one of the domains. If ‑anisotr is specified, three refractive indices correspond to one domain (diagonal elements of the refractive index tensor in particle reference frame). None of the given refractive indices may be equal to 1.

Default: 1.5 0

-maxiter <arg>

Sets the maximum number of iterations of the iterative solver, integer.

Default: very large, not realistic value (§12.1).

-no\_reduced\_fft

Do not use symmetry of the interaction matrix to reduce the storage space for the Fourier-transformed matrix (§12.2).

-no\_vol\_cor

Do not use “dpl (volume) correction” (§6.3). If this option is given, ADDA will try to match size of the dipole grid along the *x*‑axis to that of the particle, either given by ‑size or calculated analytically from ‑eq\_rad. Otherwise (by default) ADDA will try to match the volumes, using either ‑eq\_rad or the value calculated analytically from ‑size.

-ntheta <arg>

Sets the number of intervals into which range of scattering angles [0°,180°] in the scattering plane is equally divided (§11.1), integer. If particle is not symmetric (§6.7) and orientation averaging (§8.2) is not used, the range is extended to 360 degrees (with the same length of elementary interval).

Default: from 90 to 720 depending on the size of the computational grid (§6.2).

-opt {speed|mem}

Sets whether ADDA should optimize itself for maximum speed or for minimum memory usage (§5).

Default: speed

-orient {<alpha> <beta> <gamma>|avg [<filename>]}

Either sets an orientation of the particle by three Euler angles *α*, *β*, *γ* (§8.1) or specifies that orientation averaging should be performed (§8.2). <filename> sets a file with parameters for orientation averaging (input format is described in §B.2).

Default orientation: 0 0 0

Default <filename>: avg\_params.dat

-phi\_integr <arg>

Turns on and specifies the type of Mueller matrix integration over azimuthal angle *φ* (§11.2). <arg> is an integer from 1 to 31, each bit of which, from lowest to highest, indicates whether the integration should be performed with multipliers 1, cos(2*φ*), sin(2*φ*), cos(4*φ*), and sin(4*φ*) respectively.

Examples: 1 (one integration with no multipliers), 6 (two integrations with cos(2*φ*) and sin(2*φ*) multipliers).

-pol {cldr|cm|dgf|fcd|igt\_so|lak|ldr [avgpol]|nloc <Rp>|nloc\_av <Rp>|rrc|so}

Type of polarizability prescription (§10.1). An optional flag avgpol can be added for LDR – it specifies that LDR polarizability should be averaged over incident polarizations. CLDR and SO cannot be used with ‑anisotr (§6.3). fcd requires dpl to be larger than 2. <Rp> is the width of the Gaussian density (in μm) for non-local formulations.

Default: ldr (without averaging).

-prognosis

Do not actually perform simulation (not even memory allocation) but only estimate the required RAM (§5). Implies ‑test.

-prop <x> <y> <z>

Sets propagation direction of incident radiation (§9.1), float. Normalization (to the unity vector) is performed automatically by ADDA.

Default: 0 0 1

-recalc\_resid

Recalculate residual at the end of iterative solver (§12.1).

-save\_geom [<filename>]

Saves dipole configuration to a file <filename> (a path relative to the output directory, §6.3). Output format is determined by –sg\_format and described in §C.11. This option can be used with ‑prognosis.

Default: <type>.geom

(<type> is shape name, to which \_gran is added if –granul is used; file extension can differ depending on argument of ‑sg\_format)

-scat {dr|fin|igt\_so|so}

Sets prescription to calculate scattering quantities (§10.4). The SO formulation cannot be used with ‑anisotr (§6.3).

Default: dr

-scat\_grid\_inp <filename>

Specifies a file with parameters of the grid of scattering angles for calculating the Mueller or the amplitude matrix. The Mueller matrix can be integrated over *φ* (§11.2). Input format is described in §B.4.

Default: scat\_params.dat

-scat\_matr {muel|ampl|both|none}

Specifies which scattering matrices, the Mueller (§11.2) and/or the amplitude (§11.3), should be saved to file. Amplitude matrix is never integrated, i.e. the effect of the corresponding option does not combine with that of ‑orient avg or ‑phi\_integr.

Default: muel

-scat\_plane

Explicitly enables calculation of the scattering in the plane through **e***z* and **a** (in laboratory reference frame). For default incidence this is the *xz*‑plane. It can also be implicitly enabled by other options (§11.1).

-sg\_format {text|text\_ext|ddscat6|ddscat7}

Specifies format for saving geometry files (§6.3). First two are ADDA default formats for single- and multi-domain particles respectively. DDSCAT 6 and 7 formats are described in §C.11.

Default: text

-shape <type> [<args>]

Sets shape of the particle, either predefined or “read” from file (§6.3). All the parameters of predefined shapes are floats described in detail in §6.4, except for file names.

Default: sphere

-size <arg>

Sets the size of the computational grid along the *x*‑axis in µm (§6.2), float. If default wavelength is used, this option specifies the “size parameter” of the computational grid.

Default: determined by the value of ‑eq\_rad or by ‑grid, ‑dpl, and ‑lambda. Size is defined by some shapes themselves, then this option can be used to override the internal specification and scale the shape.

-store\_beam

Save incident electric fields to a file (§9). Output format is described in §C.9

-store\_dip\_pol

Save dipole polarizations to a file (§11.7). Output format is described in §C.9.

-store\_force

Calculate the radiation force on each dipole (§11.6). Output format is described in §C.9. Implies ‑Cpr.

-store\_grans

Save granule coordinates to a file, if ‑granul option is used (§6.5). Output format is described in §C.12.

-store\_int\_field

Save internal fields to a file (§11.7). Output format is described in §C.9.

-store\_scat\_grid

Calculate Mueller matrix for a grid of scattering angles and save it to a file (§11.2). Output format is described in §C.5.

-surf <h> {<mre> <mim>|inf}

Specifies that scatterer is located above the plane surface, parallel to the *xy*‑plane and located at *h* μm below the particle center. Following argument(s) specify the refractive index of the substrate: either as real and imaginary parts or as inf, which corresponds to perfectly reflective surface (§7).

-sym {auto|no|enf}

Automatically determine particle symmetries (auto), do not take them into account (no) or enforce them (enf, §6.7).

Default: auto

-test

Begin name of the output directory with test instead of run (§C.3)

-V

Show ADDA version, compiler used to build this executable, build options, and copyright information (§3.1).

-vec

Calculate the not-normalized asymmetry vector (§11.4).

-yz

Explicitly enables calculation of the scattering in the *yz*‑plane (in incident-wave reference frame). It can also be implicitly enabled by other options (§11.1).

1. Input Files

All the input files should be located in the directory, in which ADDA is executed. Exceptions are the files specified in the command line – they may be located in a different directory. Some auxiliary files that may be required for ADDA execution (but which should not be modified by user) are described in §D. Comments can be used in most of the input files, they are defined as lines that start with # character. In most cases ADDA will detect incompatible format and terminate with an error message, consistency checks are also performed (producing error messages if necessary, §C.1). If you notice that particular input files cause abrupt termination or any erroneous behavior of ADDA, please communicate it to the developers. All files in this section are in ASCII format to ensure portability.

* 1. ExpCount

This is a very simple file, consisting of a single number (“run number”). In the beginning of its execution ADDA reads this number, increments it and saves back to the file. The read number appears in the name of the output directory (§C.3). The name of the ExpCount file cannot be changed, however this file is not required. If it does not exist ADDA creates the ExpCount file and saves “1” in it. The purpose of the run number is two-fold: to provide convenience in sorting and analysis of output directories and guaranteeing that the name of the output directory is unique, so that ADDA will not overwrite any valuable data by its output. The first task (convenience) can be influenced by the user, who may change the number in ExpCount manually or delete this file to restart numbering.

The uniqueness of the directory name is a bit tricky, when several instances of ADDA run in parallel (each instance may be in sequential or parallel mode). It is possible albeit improbable that one instance of ADDA will read ExpCount between the other instance reads and updates the file. Then both instances will read the same run number. It may lead, though not necessarily, to the same name of output directories of these instances. On systems employing PBS or SGE (see §3.2) this problem is alleviated by adding a job id (which is unique) to the directory name (§C.3). Another option is used for all systems to guarantee the uniqueness of the run number – a file locking. Before reading ExpCount ADDA creates a file ExpCount.lck and removes it after updating ExpCount. All other ADDA instances wait until ExpCount.lck is removed. On POSIX systems ExpCount.lck is additionally locked to ensure robustness when working over the network file system, e.g. on parallel supercomputer.

Though highly improbable, permanent lock may occur under certain circumstances. That is when ExpCount.lck permanently exists (e.g. if ADDA is abruptly terminated between creating and removing this file). ADDA detects the permanent lock, using timeout, specified by parameters LOCK\_WAIT (length of one wait cycles in seconds) and MAX\_LOCK\_WAIT\_CYCLES (maximum number of wait cycles, after which timeout is declared), defined in the beginning of io.c. By default, values 1 and 60 are used for these parameters respectively, i.e. if ExpCount.lck exists for one minute, ADDA exits with an error message. To solve the permanent-lock problem remove ExpCount.lck manually.

The other potential problem of file locking is that its implementation is operating-system-dependent. ADDA should perform locking of ExpCount through lock file correctly on any POSIX-compliant or Windows operating system. However, it will produce an error during compilation if an operation system is not supported. If you experience this problem or unexplainable permanent locks occur, turn off file locking completely by recompiling with option NOT\_USE\_LOCK.12 Some POSIX file systems do not support or do not allow (advanced) locking of files. ADDA should detect this, produce a warning, and continue without using this feature. However, the detection may take some time (up to 1 min). Therefore, if you get such warning from ADDA you are advised to turn off advanced file locking by recompiling with option LOCKFILE\_ONLY.12

* 1. avg\_params.dat

This file specifies parameters for orientation averaging (§8.2). It consists of three sections, each specifying the parameters for each of the Euler angles: *α*, *β*, and *γ* (using “*zyz*-notation”). The first section looks like

alpha:  
min=0  
max=360  
Jmin=2  
Jmax=4  
eps=0  
equiv=true  
periodic=true

specifying minimum and maximum angles, minimum and maximum number of refinements, required accuracy, whether the minimum and maximum angles are equivalent, and whether the function is periodic on the given interval (see §12.6 to understand the meaning of these parameters). Sections for other Euler angles contain the same parameters, but start with “beta:” and “gamma:” respectively. Specified eps and Jmin are relevant for *β* and *γ*, but they are not actually used for *α*, because values for integration over this angle are precalculated. If min and max are the same for some angle all other parameters are ignored for it and averaging over this angle is not performed. Values of *β* are spaced uniformly in values of cos*β* inside the specified interval. Currently the error of the integration of *C*ext is used as a stopping criterion (it is compared to the specified eps). Thus the error of integration of other computed quantities may significantly differ from eps.

Particle symmetries may be considered by the user to decrease the ranges of Euler angles used for averaging. For example, if particle is axisymmetric (over the *z*‑axis), *γ* is not relevant and user should set

gamma:  
min=0  
max=0

This will dramatically increase the speed of the orientation averaging. However even if particle is axisymmetric, its dipole representation has only 90° rotation symmetry. Hence, to be more precise, user should set max=45;equiv=false and decrease Jmax by 3. If a particle is symmetric with respect to the *xy*‑plane, then the *β* range may be limited to [0°,90°], reducing corresponding Jmax by 1. Most of the particle symmetries can be employed, but that is user’s responsibility to carefully account for them.

When *β* = 0° or 180°, *γ* and *α* are not relevant independently but only as a combination *α* ± *γ*. If *α* is varied in a full range [0°,360°), ADDA simulates only one *γ* value for these specific values of *β*, saving a few evaluations of internal fields. Therefore, do *not* change the default (full) range of *α*, unless you have a good reason for it. It will cause all *γ* values to be honestly simulated. However, if you do have such a reason, please communicate it to the developers, motivating implementation of special optimizations for such “exotic” case. Moreover, a range of *α* is completely irrelevant (and ignored by ADDA) if only the cross sections need to be averaged (‑scat\_matr none), since the latter are calculated for unpolarized incident light (§11.4).

The example of the parameter file is included in the distribution (input/avg\_params.dat), it is commented to facilitate its editing. The order of all the parameters is important, however comments can be inserted anywhere. A file with a different name can be used if specified in the command line (see §8.2).

* 1. alldir\_params.dat

This file specifies parameters for averaging over the scattering angles for calculating integral scattering quantities (§11.4). It consists of two sections, specifying parameters for two scattering angles *θ* and *φ*. Each section is completely the same as in the avg\_params.dat (§B.2), but starts with “theta:” or “phi:” respectively. A specified eps does not decrease the computational time, since all the integrated values are precalculated, but may decrease accuracy. If min and max are the same for some angle all other parameters are ignored for it and averaging over this angle is not performed. Values of *θ* are spaced uniformly in values of cos*θ* inside the specified interval. Scattering angles are defined in §11.1.

Particle symmetries may be considered by the user to decrease the ranges of scattering angles used for averaging. For example, if a particle is axisymmetric (over the *z*‑axis), range of *φ* can be decreased and user should set

phi:  
min=0  
max=90  
equiv=false

and decrease Jmax by 2. It will significantly increase the speed of the averaging. Many of the particle symmetries can be employed, but that is user’s responsibility to carefully account for them.

The example of the parameter file is included in the distribution (input/alldir\_params.dat), it is commented to facilitate its editing. The order of all the parameters is important, however comments can be inserted anywhere. A file with a different name can be used if specified in the command line (see §11.4).

* 1. scat\_params.dat

This file specifies parameters to calculate Mueller matrix on a grid of scattering angles (*θ* and *φ*), and possibly integrate result over the azimuthal angle *φ* (§11.2). It consists of one “global” section, two sections specifying the set of values for *θ* and *φ*, and one section for parameters of integration over *φ*. The first section looks like

global\_type=grid  
N=2  
pairs=  
0 0  
30 90  
…

First argument can be either grid or pairs. Grid is constructed as a Cartesian product of two sets of angles (described below). Pairs are specified by total number N and list of (*θ*,*φ*) values separated by space (each pair comes on a separate line). No comments can be inserted between “pairs=” and the end of the pairs list. pairs option is not compatible with integration over *φ*. The second section looks like

theta:  
type=range  
N=91  
min=0  
max=180  
values=  
0  
10  
…

type can be either range or values. Range is determined by min and max values, in which N points (including boundary points) are uniformly distributed. Values are specified by the total number N and a list (each value comes on a separate line). No comments can be inserted between “values=” and the end of the values list. A set of *φ* angles is defined by the similar section that starts with “phi:”, however if integration over *φ* is enabled a range of *φ* is initialized based on the last section. This section is completely the same as in the avg\_params.dat (§B.2), but starts with “phi\_integr:”. Specified eps and Jmin are not actually used, since all the integrated values are precalculated. All options that are not relevant for current configuration (e.g. number and list of pairs when grid of scattering angles is used) are ignored by ADDA, so one doesn’t need to remove them from the file. Scattering angles are defined in §11.1.

Particle symmetries may be considered by the user to decrease e.g. the range of *φ* used for integration. For example, if particle is symmetric with respect to the *xz*‑plane, then *φ* range may be limited to [0°,180°], reducing corresponding Jmax by 1, for integration of the block-diagonal Mueller matrix elements (*S*11, *S*12, *S*21, *S*22, *S*33, *S*34, *S*43, *S*44) without multipliers. A number of similar examples is discussed in [86]. Overall, many of the particle symmetries can be employed, but that is user’s responsibility to carefully account for them.

The example of the parameter file is included in the distribution (input/scat\_params.dat), it is commented to facilitate its editing. The order of all the parameters is important, however comments can be inserted anywhere, except in lists of angle values or pairs. A file with a different name can be used if specified in the command line (see §11.2).

* 1. Geometry files

This file specifies the shape of the scatterer (§6.3). Two default formats are supported: for single- and multi-domain particles. A single-domain particle is described as the following:

#comments  
0 0 1  
2 1 0  
…

First several lines are comments, after that each line contains three integers separated by space. That is *x*, *y*, and *z* coordinates of a dipole (in units of the dipole size). These coordinates can be considered relative to any (integer) reference point; ADDA automatically places the minimum computational box (§6.2) around all dipoles and centers it as described in §6.1. The format for multi-domain particles is similar:

#comments  
Nmat=2  
4 4 0 1  
5 4 0 1  
…

The first uncommented line specifies number of domains (different materials) and the last integer in every line specifies the domain number (1,…,Nmat). However, given Nmat is largely ignored, since its more robust estimate is the maximum of the domain numbers among all dipoles. If these two are not equal, ADDA produces a warning and continues with the latter, ignoring the former.

ADDA also supports DDSCAT formats corresponding to its shape option FRMFIL (in version 6) and FROM\_FILE (in version 7) and output of calltarget utility [87,88], which looks like (the 6th line is present only in DDSCAT 7):

*comment line*  
2176 = NAT  
1 0 0 = A\_1 vector  
0 1 0 = A\_2 vector  
1 1 1 = lattice spacings (d\_x,d\_y,d\_z)/d

0 0 0 = coordinates (x0,y0,z0)/d of the zero dipole (IX=IY=IZ=0)  
*comment line, e.g.* JA IX IY IZ ICOMP(x,y,z)  
*dummy* 4 4 0 1 1 1  
*dummy* 5 4 0 1 1 1  
…

However, ADDA’s philosophy is slightly different from that of DDSCAT; in particular, shape file should describe only the dipole configuration, possibly multi-domain, but *neither* orientation nor size of the particle, which should be specified independently in the command line. Moreover, in case of anisotropic refractive index ADDA uses one domain number to distinguish all different refractive index tensors, even those which differ only by rotation of the tensor. Therefore, support of DDSCAT formats is limited in the following respects: (a) ADDA completely discards first 6 or 7 lines of the shape file, i.e. it always assumes default orientation and size of the particle, unless these are specified in the command line. (b) For each “dipole” row ADDA uses only dipole positions (2nd–4th numbers) and identifier of *x*-component of refractive index tensor (5th number) as domain number, discarding the other two components.[[91]](#footnote-91)

ADDA automatically determines the format of input dipole file, analyzing its several first lines. However, with increasing number of supported formats, probability of autodetection failure increases. If this happens, ADDA produces an error because of different format of further lines. The error message contains the detected format, which can be used to diagnose the problem. Also, for all shape formats the positions of any two dipoles must not coincide. Usually ADDA will detect such an error, but not in sparse mode.

* 1. Contour file

This file specifies contour in the *ρz*‑plane defining the axisymmetric shape §6.4. It looks like:

#comments  
0 0.5  
0.2 -0.8  
…

First several lines are comments, after that each line contains two floats defining *ρ* and *z* coordinates (in µm) of a contour point. At least three points should be specified. The contour is automatically closed by connecting the last and the first points. Linear interpolation is used between the specified points. The only requirement for the contour is that (by definition) *ρ* coordinates should be non-negative – ADDA will produce an error otherwise. For example, if a particle contains the interval of the *z*‑axis, it is natural (although not necessary) to choose the first and the last points of the contour on the *z*‑axis. Apart from this requirement, any set of points can be used; in particular, the contour may intersect itself or contain identical points.

* 1. Field files

This file determines the incident wave (§9.2) or initial field for the iterative solver (§12.1) on dipole-per-dipole basis. The format is the same as output format for file IncBeam or IntField (§C.9). In particular, the file should look like:

x y z |E|^2 Ex.r Ex.i … Ez.i

#comments

-0.2094395102 … -0.1844808236

…

0.2094395102 … -0.32940396

The first (header) line is ignored, as well as any number of following comment lines (starting with #). For each following data line first four numbers are ignored and next six numbers define the complex vector field in the following order: real and imaginary parts of *x*‑component, the same for *y*‑component, and then for *z*‑component (all in particle reference frame). It should be stressed that dipole coordinates (first three numbers) are ignored, and correspondence between a field value and a dipole is based solely on the order of lines in the file. In other words, index of non-trivial data line exactly equals index of dipole. Thus, the safest way to produce correct input files is to use file IncBeam or IntField, produced by ‑store\_beam (§9) or ‑store\_int\_field (§11.7) command line option respectively, as a template, changing only the values of the fields according to dipole coordinates. Finally, keep in mind that ADDA assumes the same normalization conditions for the input beam, as used for built-in beam types (§9.2).

1. Output Files

ADDA outputs some information about its execution to stdout (§C.2), but most of information is saved in special files, which are created in a separate output directory (§C.3). All spreadsheet files use space as separator (both between column names and values). All files in this section are in ASCII format to ensure portability.

* 1. stderr, logerr

If any inconsistency is detected by ADDA during execution, it produces error and warnings. They are shown in stderr and duplicated in log files, as lines starting with

ERROR:

or

WARNING:

respectively. Most error messages are saved in the main log (§C.4), however in parallel mode each processor may produce specific error messages. The latter are saved in special files, named logerr.n, where n is a number of processor. In case of an error ADDA terminates execution, hence the errors that were detected before the output directory was created (§C.3) are not saved to file and appear only in stderr. Warnings indicate that probably the simulation goes not exactly the way intended by user, but ADDA continues execution.

* 1. stdout

ADDA’s output to stdout is mainly designed to show the progress of the execution, when ADDA is run in the terminal session. More detailed information is saved to log (§C.4) and other output files, except for few information messages that appear only in stdout. The stdout from the sample calculation (§3.1) looks like

all data is saved in 'run000\_sphere\_g16\_m1.5'  
box dimensions: 16x16x16  
lambda: 6.283185307 Dipoles/lambda: 15  
Required relative residual norm: 1e-005  
Total number of occupied dipoles: 2176  
Memory usage for MatVec matrices: 1.3 MB  
Calculating Green's function (Dmatrix)  
Fourier transform of Dmatrix......  
Initializing FFTW3  
Total memory usage: 2.2 MB  
  
here we go, calc Y  
  
CoupleConstant:0.005259037197+1.843854148e-005i  
x\_0 = 0  
RE\_000 = 1.0000000000E+000  
RE\_001 = 8.4752662637E-001 +  
…  
RE\_022 = 3.1673391134E-006 +  
Cext = 135.0449041

Qext = 3.791149597

Cabs = -0

Qabs = -0

It provides name of the output directory for this calculation, basic information about the scattering problem, memory requirements, progress of the iterative solver, and results for extinction and absorption cross section. It may provide more information depending on the particular simulation parameters. When precise timing (§13.2) is enabled, all results go to stdout.

In some cases reading long lines in stdout (as well as in stderr) can be “inconvenient”, since such lines can be broken in the middle of the word to fit the terminal width. To improve this situation ADDA automatic wraps lines moving whole words to the new line. It tries to determine terminal width from the environmental variable COLUMNS,[[92]](#footnote-92) otherwise uses the value, which is defined at compilation time by the parameter DEF\_TERM\_WIDTH in the file const.h (80 by default).

* 1. Output directory

Output directory is generated by ADDA automatically to store all output files. The name of the directory has the following format

<type><N>\_<shtype>\_g<nx>\_m<m1Re>[\_id<jobid>]

where <type> is either run or test. The latter is only used if ‑prognosis (§5) is enabled or

-test

command line option is specified. <N> is a run number that is read from ExpCount file (§B.1) and written in a format including at least three digits. <shtype> is shape name (§6.3). <nx> is dimension of the computational grid along the *x*‑axis (§6.2), <m1Re> is real part of the first given refractive index (§6.3) written with up to 4 significant digits and decimal point replaced by “\_”. The last part of the name is added only if any of environmental variables PBS\_JOBID, JOB\_ID, or SLURM\_JOBID is defined (they are defined by PBS, SGE, and SLURM[[93]](#footnote-93) respectively, §3.2), then <jobid> is its value. For example, directory name may look like:

run000\_sphere\_g16\_m1.5  
test123\_box\_g40\_m1.33\_id123456

The first one corresponds to the sample simulation (§3.1), it is included in the distribution with 3 output files in it (sample/run000\_sphere\_g16\_m1.5). To disable automatic naming of the output directory specify its name as an argument to the command line option

-dir <dirname>

* 1. log

This file contains most of the information that characterize the ADDA simulation. The log for the sample calculation (§3.1) is the following

Generated by ADDA v.1.4.0-alpha  
The program was run on: …  
command: '…\adda.exe '  
lambda: 6.283185307  
shape: sphere; diameter:6.734551818  
box dimensions: 16x16x16  
refractive index: 1.5+0i  
Dipoles/lambda: 15  
 (Volume correction used)  
Required relative residual norm: 1e-005  
Total number of occupied dipoles: 2176  
Volume-equivalent size parameter: 3.367275909  
  
---In laboratory reference frame:---  
Incident beam: plane wave  
Incident propagation vector: (0,0,1)  
Incident polarization Y(par): (0,1,0)  
Incident polarization X(per): (1,0,0)  
  
Particle orientation: default  
  
Calculating only Mueller scattering matrix

Polarizability relation: 'Lattice Dispersion Relation'  
Scattering quantities formulae: 'by Draine'  
Interaction term prescription: 'as Point dipoles'  
FFT algorithm: FFTW3  
Iterative Method: QMR (complex symmetric)

Symmetries: XYR  
Optimization is done for maximum speed  
The FFT grid is: 32x32x32  
Memory usage for MatVec matrices: 1.3 MB  
Total memory usage: 2.2 MB  
  
here we go, calc Y  
  
CoupleConstant:0.005259037197+1.843854148e-005i  
x\_0 = 0  
RE\_000 = 1.0000000000E+000  
RE\_001 = 8.4752662637E-001 + progress = 0.152473  
…  
RE\_022 = 3.1673391134E-006 + progress = 0.791210  
  
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~  
 Timing Results   
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~  
Total number of iterations: 22

Total number of matrix-vector products: 22  
Total planes of E field calculation (each 181 points): 2  
  
Total wall time: 1  
…

Most of the information is self-descriptive. The hostname (on the second line) is read from the environmental variable HOST (in Unix) or by function GetComputerName (in Windows). Command line that was used to call ADDA is duplicated. The scatterer (§6) is completely described, then the incident beam (§9), scatterer orientation (§8), and which scattering matrices are calculated (§11.2, §11.3). The DDA formulation (§10) is described, then FFT algorithm (§12.2), iterative method (§12.1), symmetries of the problem (§6.7), and type of optimization (§5) are specified. Memory usage is given (both total and for FFT part, §5). “calc Y” denotes beginning of calculation for *y* incident polarization. “CoupleConstant” is dipole polarizability, “x\_0” denotes which initial vector is used for iterative solver (§12.1). After each iteration the relative norm of the residual is shown together with its relative decrease compared to the previous iteration (progress). A sign in between is one of +, - or -+ indicating respectively that the residual is the smallest of all the previous iterations, larger than the previous one, and smaller than the previous one but not the smallest of all the previous. log finishes with timing information (§13.1). This file may contain more information depending on the particular simulation parameters, the one that is described above is included in the distribution (sample/run000\_sphere\_g16\_m1.5/log).

Package misc/parse\_log contains Mathematica program to parse multiple log files, which may be useful for analyzing results of massive ADDA simulations.

* 1. mueller

This file contains results of the Mueller matrix at different scattering angles (§11.2). There are a number of output files, which name starts with mueller, but they all look very similar. When scattering is computed in one scattering plane or orientation averaging (§8.2) is performed the simplest file mueller is produced:

theta s11 s12 s13 s14 s21 … s44

0.00 1.4154797793E+002 0.0000000000E+000 0.0000000000E+000 \  
-5.0959034824E-012 0.0000000000E+000 … 1.4154797793E+002

1.00 1.4140075337E+002 -5.8903788393E-003 7.3212262090E-013 \  
-2.0347873246E-012 -5.8903788393E-003 … 1.4140075290E+002

…

180.00 2.9143742276E+000 1.0348709736E-015 -1.0104462691E-017 \  
3.8122857626E-012 1.0348709736E-015 … -2.9143742276E+000

where “\” denotes continuation of the line. All 16 Mueller matrix elements for each scattering angle are saved. Shown is the output of the sample calculation (§3.1) – sample/run000\_sphere\_g16\_m1.5/mueller. If grid of scattering angles (any type) is calculated mueller\_scatgrid is produced, which differs only by the additional column of azimuthal angle *φ* (and usually larger number of lines):

theta phi s11 … s44  
0.00 0.00 1.4154797792E+002 … 1.4154797792E+002  
…  
180.00 360.00 2.9143742274E+000 … -2.9143742274E+000

This file can be produced by the command

adda -store\_scat\_grid

with default scat\_params.dat (§B.4). If integration over *φ* is enabled, up to 5 different files are produced depending on the parameters (different multipliers for integration, §11.2). They are called mueller\_integr, mueller\_integr\_c2, mueller\_integr\_s2, mueller\_integr\_c4, and mueller\_integr\_s4. The format is the same as that of mueller but with addition of the column with error

theta s11 … s44 RMSE(integr)  
0.00 1.4154797792E+002 … 1.4154797792E+002 2.150E-017  
…  
50.00 8.7607151503E+000 … 8.4048020875E+000 3.663E-010  
…  
180.00 2.9143742274E+000 … -2.9143742274E+000 3.601E-017

The shown error is relative root-mean-square error over all 16 elements of Mueller matrix,[[94]](#footnote-94) integration error of each element is an estimation from the Romberg routine (§12.6). In this example the error is extremely low because of the spherical symmetry of the target and large number of integration points used (32). It is important to note that, strictly speaking, averaging but not integration is performed over *φ*. The above file can be produced by the command

adda -phi\_integr 1

with default scat\_params.dat (§B.4). Scattering angles are defined in §11.1

* 1. ampl

This file contains results of the amplitude matrix at different scattering angles (§11.3). There are two output files, which name starts with ampl, but they all look very similar. When scattering is computed in one scattering plane, file ampl is produced:

theta s1.r s1.i … s4.i

0.00 1.0746532054E+001 -5.1049022279E+000 … 2.4881279126E-013

1.00 1.0741905097E+001 -5.1007958857E+000 … 3.8850759557E-013

…

180.00 3.5097745561E-001 1.6706852073E+000 … -2.6713706097E-013

Four complex amplitude matrix elements for each scattering angle are saved (separately real and imaginary parts). Traditional way to number the amplitude matrix elements is by a single index, i.e. *S*1–*S*4 [53]. The above file can be produced by the command

adda –scat\_matr ampl

If a grid of scattering angles (any type) is calculated, ampl\_scatgrid is produced, which differs only by the additional column of azimuthal angle *φ* (and usually larger number of lines):

theta phi s1.r … s4.i  
0.00 0.00 1.0746532054E+001 … 1.1550780581E-013  
…  
180.00 360.00 3.5097745561E-001 … -1.0410157053E-013

This file can be produced by the command

adda –scat\_matr ampl -store\_scat\_grid

with default scat\_params.dat (§B.4).

* 1. CrossSec

This file contains the results for integral scattering quantities (§11.4). If orientation averaging (§8.2) is performed the result is saved to CrossSec file, otherwise a separate file is used for each incident polarization: CrossSec‑X and CrossSec‑Y. Only one file (CrossSec‑Y) is produced if symmetry of the particle is used to simulate only one incident polarization independently (§6.7). The format is self-explanative, for example the output of the sample simulation (§3.1) looks like (sample/run000\_sphere\_g16\_m1.5/Crosssec‑Y):

Cext = 135.0449046  
Qext = 3.79114961  
Cabs = 0  
Qabs = 0

More results are shown in this file if additional (to default) scattering quantities are calculated.

* 1. RadForce

This file stores the results for radiation force on each dipole (§11.6). A separate file is used for each simulated incident polarization: RadForce‑X and RadForce‑Y. It looks like

x y z |F|^2 Fx Fy Fz

-0.2094395102 -1.047197551 -3.141592654 2.348525769e-005 \  
-0.001450116615 0.004378387866 -0.001487326185

…

0.2094395102 1.047197551 3.141592654 0.001840340346 \  
0.01038653728 -0.04118221174 -0.006040333213

where “\” denotes continuation of the line. This file describes the dependence of the force vector on the coordinates inside the particle (in µm). All values are specified in the particle reference frame (§6.1). The squared norm of the force vector is presented for convenience. The unit of force is 10−8 dyne when all lengths are measured in µm and unity amplitude (1 statV/cm) of incident field is assumed (see §11.6 for details). The above file can be produced by the command

adda -store\_force

* 1. IntField, DipPol, and IncBeam

Internal fields, dipole polarizations (§11.7), and incident fields (§9) are saved to files IntField‑X, DipPol‑X, and IncBeam‑X respectively. A separate file is used for each simulated incident polarization, their names end with different suffixes (X or Y). For instance, IntField‑Y looks like:

x y z |E|^2 Ex.r Ex.i … Ez.i

-0.2094395102 -1.047197551 -3.141592654 0.6988347019 \  
-0.01668015393 0.006582289815 … -0.1844808236

…

0.2094395102 1.047197551 3.141592654 5.876037053 \  
0.01112798497 -0.06772761653 … -0.32940396

where “\” denotes continuation of the line. This file describes the dependence of the electric field vector (normalized to the incident field) on the coordinates inside the particle (in µm), suffixes r and i denote real and imaginary parts respectively. All values are specified in the particle reference frame (§6.1). The squared norm of the electric field is presented for convenience, it is proportional to the energy density of the electric field and absorption power per unit volume for isotropic materials. The above file can be produced by the command

adda -store\_int\_field

Symbol used in the first row for column labels is different for different fields. It is “E” for the internal field, “P” for the dipole polarization, and “Einc” for the incident field. Electric fields are considered relative to the amplitude of the incident field, i.e. the values in the files are effectively dimensionless. The unit of the dipole polarizations is then the same as of volume (µm3).

* 1. log\_orient\_avg and log\_int

These files contain information about the 2D Romberg integration (§12.6), they are produced directly by the routine and hence have the same format. Their names are log\_orient\_avg, log\_int\_Csca‑X, and log\_int\_asym\_x‑X, log\_int\_asym\_y‑X, log\_int\_asym\_z‑X for orientation averaging (§8.2) and calculation of scattering cross section and asymmetry vector (§11.4) respectively. The latter 4 files have different suffixes (X or Y) for different incident polarizations. For example, log\_int\_Csca‑Y looks like:

PHI(rad) cos(THETA)  
EPS 0 0  
Refinement stages:  
Minimum 2 2  
Maximum 5 6  
lower boundary 0 -1  
upper boundary 6.28319 1  
equivalent min&max true false  
periodic true false  
  
  
Outer-Loop Inner Loop  
Inner\_qromb converged only to d=7.61895e-017 for cosine value #0  
Inner\_qromb converged only to d=0 for cosine value #64  
init 64 integrand-values were used.  
Inner\_qromb converged only to d=5.88e-010 for cosine value #32  
1 32 integrand-values were used.

Inner\_qromb converged only to d=4.77002e-010 for cosine value #16

Inner\_qromb converged only to d=1.74306e-010 for cosine value #48

2 64 integrand-values were used.  
…  
6 1024 integrand-values were used.  
65 inner integrations did not converge.  
The outer integration did not converge  
The outer integration reached d=3.70825e-009  
In total 2080 evaluations were used

The first part with parameters is self-descriptive. Then for every step of outer integration (over *θ*), convergence of all the inner integrations and total number of integrand evaluation are shown. At the end final statistics over the whole integration is shown. An integration (outer or one of the inner) is considered converged if its estimated relative error falls below eps (shown in the second line), which is given in a corresponding parameter file. For orientation averaging relative error of *C*ext is shown. For this example no adaptation is used (eps = 0), hence none of the integrals converge, but the reached relative errors are informative. The range for angles (in the first column, *φ* or *γ*) is specified in *radians*. The above file can be produced by the command

adda -Csca

* 1. Geometry files

These files hold the information about the scatterer shape. They have exactly the same format as *input* geometry files (§B.5), the only difference is that ADDA automatically puts basic information in comments. By default, either single- or multi-domain format is used depending on the number of domains in the specified shape. For example, the command

adda -save\_geom

produces the file sphere.geom that looks like:

#generated by ADDA v.1.4.0-alpha  
#shape: 'sphere'  
#box size: 16x16x16  
7 5 0  
…  
8 10 15

It is important to note, that specified “box size” is the size of the computational domain. It always includes all the listed dipole positions, but in certain rare cases it may be larger than the minimal possible circumscribing box. In other words, for box size *nx*×*ny*×*nz* the first number is always between 0 and *nx* − 1 and so on, but the limiting bounds are not necessarily reached. Moreover, the center of the computational domain can (rarely) be different from the center of the minimal circumscribing box around the particle. These issues should be carefully considered when processing the shape files.

ADDA can also save geometry in DDSCAT formats, if specified by the command line option ‑sg\_format (§6.3), with the following limitations: (a) particle orientation and size is always saved as default, ignoring the actual values used in a specific simulation; (b) all three identifiers of components of the refractive index tensor are saved equal to the domain number, thus effectively transforming anisotropic particles to isotropic with (possibly) larger number of domains[[95]](#footnote-95) (see §B.5 for philosophical reasons of these limitations). First number saved in each row is a dipole number, starting from 1.

* 1. granules

This file stores the coordinates of the granules produced by granule generator (§6.5). Currently the result looks like:

#generated by ADDA v.1.4.0-alpha  
#granule diameter = 0.9980867612  
-0.6693706848 1.833970089 -0.9894352851  
…  
-2.217014497 0.5198635377 -2.576990365

where each line specifies *x*, *y*, and *z* coordinates of a granule center in particle reference frame (§6.1). However the format should be considered in development and it may change in the future, e.g., to correspond the input shape format for cluster of spheres (when the latter will be developed). The above file, with different numbers due to random placement, can be produced by the command

adda -granul 0.1 1 -store\_grans -prognosis

1. Auxiliary Files

These files can be used by ADDA under certain circumstance, however they are not intended to be inspected or modified by user (except chp.log, §D.2). This is just general information to facilitate the understanding of how the ADDA actually works.

* 1. tables/

This is the directory that contains precalculated tables of some integrals, that are used by ADDA for IGTSO and SO prescriptions for the interaction term (§10.2). The tables and their format may change in future. Currently it contains 10 files: t1f.dat, … , t10f.dat. These files are in text format to be completely portable, and occupy totally about 150 kB of disk space. They are included in the distribution (input/tables/).

* 1. Checkpoint files

These files are produced when ADDA saves a checkpoint (§12.5), and are used when ADDA loads one. By default the directory chpoint is used to store all files, however different directory name can be specified in a command line (§12.5). This directory contains one text file chp.log, which contains some information for the user. Currently it is only the name of the directory, where the output of the ADDA instance, which produced the checkpoint, was saved. Each processor (number *k*) produces a file named chp.*k* that contains the information, completely describing the state of the iterative solver on this processor, in binary format.[[96]](#footnote-96)

1. <https://github.com/adda-team/adda/wiki/EarlyHistory> [↑](#footnote-ref-1)
2. <https://github.com/adda-team/adda/graphs/contributors> [↑](#footnote-ref-2)
3. However, in some parts modularity was sacrificed for the sake of performance. E.g. iterative solvers (§12.1) are implemented not to perform any unnecessary operations (which usually happens when using standard libraries). [↑](#footnote-ref-3)
4. See <https://github.com/adda-team/adda/wiki/References> for more specific references. [↑](#footnote-ref-4)
5. https://github.com/adda-team/adda/issues [↑](#footnote-ref-5)
6. <http://www.gnu.org/copyleft/gpl.html> [↑](#footnote-ref-6)
7. To do this send an e-mail to [adda-announce+subscribe@googlegroups.com](mailto:adda-announce+subscribe@googlegroups.com) [↑](#footnote-ref-7)
8. <https://github.com/adda-team/adda/wiki/FAQ> [↑](#footnote-ref-8)
9. Just send an e-mail to [adda-discuss@googlegroups.com](mailto:adda-discuss@googlegroups.com) [↑](#footnote-ref-9)
10. <http://groups.google.com/group/adda-discuss/topics> [↑](#footnote-ref-10)
11. To do this send an e-mail to [adda-discuss+subscribe@googlegroups.com](mailto:adda-discuss+subscribe@googlegroups.com) [↑](#footnote-ref-11)
12. See <https://github.com/adda-team/adda/wiki/CompilingADDA> for compiling instructions. [↑](#footnote-ref-12)
13. See <https://github.com/adda-team/adda/wiki/PackageDescription> for available packages. [↑](#footnote-ref-13)
14. <https://github.com/adda-team/adda/archive/master.zip> [↑](#footnote-ref-14)
15. git clone https://github.com/adda-team/adda.git [↑](#footnote-ref-15)
16. If current directory is not in the PATH system variable you should type “./adda”. It may also differ on non-Unix systems, e.g. under Windows you should type “adda.exe”. Moreover, the name of executable is different for MPI (§3.2) and OpenCL versions (§3.3). This applies to all examples of command lines in this manual. [↑](#footnote-ref-16)
17. <https://github.com/adda-team/adda/wiki/Tutorial> [↑](#footnote-ref-17)
18. Only a limited set of compilers is recognized (currently: Borland, Compaq, GNU, Intel, Microsoft). [↑](#footnote-ref-18)
19. <http://www.openpbs.org/> [↑](#footnote-ref-19)
20. <http://gridengine.sunsource.net/> [↑](#footnote-ref-20)
21. <https://github.com/adda-team/adda/wiki/OpenCL> [↑](#footnote-ref-21)
22. This limit can be circumvented on a supercomputer consisting of nodes with several processors (cores) sharing the same memory. Using only part (down to 1) of the processors per node increases available memory per processor at the expense of wasted system resources, which are usually measured in node-hours. [↑](#footnote-ref-22)
23. Currently this option does need a certain amount of RAM, about 11(*N*+ *N*real) bytes. It enables saving of the particle geometry in combination with –prognosis. [↑](#footnote-ref-23)
24. Only one incident polarization was calculated, execution time for non-symmetric shapes (§6.7) will be at least twice larger. [↑](#footnote-ref-24)
25. <https://github.com/adda-team/adda/wiki/LargestSimulations> [↑](#footnote-ref-25)
26. Specifying all three dimensions (or even one when particle geometry is read from file) make sense only to fix these dimensions (larger than optimal) e.g. for performance studies. [↑](#footnote-ref-26)
27. If dpl is not defined, it is set to the default value. Then, if still less than two parameters are initialized, grid dimension is also set to the default value. [↑](#footnote-ref-27)
28. See <https://github.com/adda-team/adda/wiki/AddingShapeFileFormat> for detailed instructions. [↑](#footnote-ref-28)
29. This option may be used e.g. to directly study the shape errors in DDA (i.e. caused by imperfect description of the particle shape) [21]. [↑](#footnote-ref-29)
30. ADDA uses exp(−i*ωt*) convention for time dependence of harmonic electric field, therefore absorbing materials have *positive* imaginary part. [↑](#footnote-ref-30)
31. See <https://github.com/adda-team/adda/wiki/AddingShape> for detailed instructions. [↑](#footnote-ref-31)
32. <http://www.math.sci.hiroshima-u.ac.jp/~m-mat/MT/emt.html> [↑](#footnote-ref-32)
33. <https://github.com/adda-team/adda/issues/21> [↑](#footnote-ref-33)
34. Exceptions are cubes and any other particles, for which area of any cross section perpendicular to the z‑axis is constant. [↑](#footnote-ref-34)
35. That is additionally to the communication overhead that always exists (§12.4). [↑](#footnote-ref-35)
36. Rotation of the particle with respect to the *laboratory* reference frame (§6.1) does not help because it does not affect the particle in the *particle* reference frame. [↑](#footnote-ref-36)
37. That is probably not worth the efforts for most of the problems. [↑](#footnote-ref-37)
38. For example, a sphere is symmetric for any incident direction, but the corresponding dipole set (Fig. 2) is only symmetric for incidence along a coordinate axis. [↑](#footnote-ref-38)
39. <https://github.com/adda-team/adda/issues/171> [↑](#footnote-ref-39)
40. <https://github.com/adda-team/adda/issues/89> [↑](#footnote-ref-40)
41. More specifically, the wave is inhomogeneous when **k** is not proportional to a real vector. This is the case either for non-real *m*s, or for total internal reflection. [↑](#footnote-ref-41)
42. For instance, for slightly absorbing *m*s ℑ(*kt*,*z*) ~ −*k*, ℜ(**k**) is directed almost along the surface, while ℑ(**k**) is almost along −**e***z*. The amplitude of the transmitted electric field indeed increases with *z*, but this field comes from distant points on the surface, which has much larger amplitude of the incident wave from below (compared to that under the observation point) due to (significantly) different paths in absorbing substrate. [↑](#footnote-ref-42)
43. See <https://github.com/adda-team/adda/wiki/AddingBeam> for detailed instructions. [↑](#footnote-ref-43)
44. <https://github.com/adda-team/adda/issues/30> [↑](#footnote-ref-44)
45. See development branch <https://github.com/adda-team/adda/tree/wd>. [↑](#footnote-ref-45)
46. See <https://github.com/adda-team/adda/wiki/AddingPolarizability> for detailed instructions. [↑](#footnote-ref-46)
47. See <https://github.com/adda-team/adda/wiki/AddingInteraction> for detailed instructions. [↑](#footnote-ref-47)
48. See <https://github.com/adda-team/adda/wiki/AddingReflection> for detailed instructions. [↑](#footnote-ref-48)
49. They are exact in all cases, except for absorbing substrate. Otherwise, the definition of *C*sca and **g** is ambiguous anyway. If ℑ(*k*sca)*r* >> 1, then one should consider the integral only over the upper hemisphere. Otherwise, the integral over the lower hemisphere is also relevant albeit with a correction factor exp(−2ℑ(*k*sca)*r*). [↑](#footnote-ref-49)
50. Except for IGT interaction term (§10.2), then the optical theorem is expected to be correct only within 𝒪((*kd*)2). [↑](#footnote-ref-50)
51. For example, the default scattering plane, *yz*‑plane, will be the one based on the new propagation vector and new incident polarization, which corresponds to the *y*‑polarization for the default incidence. [↑](#footnote-ref-51)
52. This may also become the default behavior for the free-space mode in the future, <https://github.com/adda-team/adda/issues/170>. [↑](#footnote-ref-52)
53. For instance, multiplication by *k*−2 transforms it into the Stokes phase matrix (**Z**, [58]), and further multiplication by 4*π*/*C*sca (total multiplier λ2/*πC*sca) – into (normalized) Stokes scattering matrix (**F**, [58]), which is often used for particles in random orientation. The 1,1‑element of the latter gives unity, when averaged over the whole solid angle. [↑](#footnote-ref-53)
54. For example, 1 corresponds to one integration with no multipliers, 6 – to two integrations with cos(2*φ*) and sin(2*φ*) multipliers. The rationale behind these multipliers is their appearance in formulae for the light-scattering patterns measured by the scanning flow cytometer [34,59], however they may also be useful in other applications. [↑](#footnote-ref-54)
55. Other definitions of amplitude matrix exist, e.g. without factor −i*k*sca in the denominator [58]. [↑](#footnote-ref-55)
56. To the best of our knowledge, all applications involving averaging over particle orientation or over azimuthal scattering angle deal with incoherent addition, i.e. the intensity, not the field amplitude, is averaged. [↑](#footnote-ref-56)
57. In particular, molar extinction coefficient of a suspension of particles can be easily obtained from *C*ext [53]. [↑](#footnote-ref-57)
58. Note the difference with commonly used geometric-shadow cross section. [↑](#footnote-ref-58)
59. i.e. –asym implies –Csca and –vec. [↑](#footnote-ref-59)
60. <https://github.com/adda-team/adda/issues/35> [↑](#footnote-ref-60)
61. <https://github.com/adda-team/adda/issues/149> [↑](#footnote-ref-61)
62. <https://github.com/adda-team/adda/issues/181> [↑](#footnote-ref-62)
63. <https://github.com/adda-team/adda/issues/135> [↑](#footnote-ref-63)
64. <https://github.com/adda-team/adda/issues/14> [↑](#footnote-ref-64)
65. <https://github.com/adda-team/adda/issues/178> [↑](#footnote-ref-65)
66. See <https://github.com/adda-team/adda/wiki/AddingIterativeSolver> for detailed instructions. [↑](#footnote-ref-66)
67. <https://github.com/adda-team/adda/issues/59> [↑](#footnote-ref-67)
68. It should be noted, however, that smaller residual of the initial vector does not necessarily leads to a faster convergence [72]. [↑](#footnote-ref-68)
69. Currently it is set to 3*N*, i.e. the number of equations in a linear system. [↑](#footnote-ref-69)
70. They are defined in structure array params in the beginning of the iterative.c. [↑](#footnote-ref-70)
71. Changing values in lines starting with “#define EPS” in the beginning of a function, implementing a certain iterative solver in iterative.c. [↑](#footnote-ref-71)
72. 2D FFT is described in [78], 3D-FFT algorithm – to be published. [↑](#footnote-ref-72)
73. It may be reduced further – <https://github.com/adda-team/adda/issues/177> [↑](#footnote-ref-73)
74. <https://github.com/adda-team/adda/wiki/InstallingFFTW3> [↑](#footnote-ref-74)
75. The maximum increase is 15% for Temperton FFT and 6% for FFTW3. [↑](#footnote-ref-75)
76. Otherwise Temperton FFT will fail and FFTW3 will perform less efficiently. [↑](#footnote-ref-76)
77. <https://github.com/adda-team/adda/wiki/InstallingclAmdFft> [↑](#footnote-ref-77)
78. <https://github.com/adda-team/adda/issues/157> [↑](#footnote-ref-78)
79. <https://github.com/adda-team/adda/wiki/SparseMode> [↑](#footnote-ref-79)
80. <https://github.com/adda-team/adda/issues/160> [↑](#footnote-ref-80)
81. <https://github.com/adda-team/adda/issues/175> [↑](#footnote-ref-81)
82. All fields are optional, “s” can be omitted, the format is not case sensitive. For example: “12h30M”, “1D10s”, “3600” (equals 1 hour). [↑](#footnote-ref-82)
83. This is done so to save the hard disk space. [↑](#footnote-ref-83)
84. <http://sharon.esrac.ele.tue.nl/users/pe1rxq/nec2c.rxq/nec2c.rxq-0.2.tar.gz> [↑](#footnote-ref-84)
85. <https://github.com/adda-team/adda/issues/176> [↑](#footnote-ref-85)
86. <https://github.com/adda-team/adda/issues/197> [↑](#footnote-ref-86)
87. It is hard to implement portable measurement of processor time with better precision than that of clock. [↑](#footnote-ref-87)
88. <https://github.com/baptiste/adda/wiki/wrapper_primer> [↑](#footnote-ref-88)
89. See <https://github.com/adda-team/adda/wiki> for an overview. [↑](#footnote-ref-89)
90. <https://github.com/adda-team/adda/wiki/Acknowledgements> [↑](#footnote-ref-90)
91. It is possible to analyze all three components and construct bijective mapping of all different combinations of them into domain numbers. However, in general case this mapping may be not intuitively clear, which may lead to confusion in assigning (anisotropic) refractive indices to different domains. Hence, it is currently not done. Instead ADDA produces a warning if it encounters anisotropic dipole in the dipole file. [↑](#footnote-ref-91)
92. This variable is defined on any POSIX system, but it is not necessarily exported, i.e. made available, to ADDA. On other systems it can be set manually if needed. It seems that using this variable is currently the most portable way. [↑](#footnote-ref-92)
93. <https://computing.llnl.gov/linux/slurm/> [↑](#footnote-ref-93)
94. In other words, RMS absolute error is divided by RMS value. [↑](#footnote-ref-94)
95. It is possible to remove this limitation, e.g. by mapping each domain number *n* into trio 3*n* – 2, 3*n* – 1, 3*n*. However, it will cause a lot of unnecessary complications for isotropic particles. [↑](#footnote-ref-95)
96. Hence it is not necessarily portable between different systems. [↑](#footnote-ref-96)