

Verifying an Effect-Based Cooperative Concurrency Scheduler in Iris

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Abstract

In this thesis we work on the formal verification of the OCaml library “Eio” which provides user-level concurrency using the new effect handlers feature of OCaml 5. As part of formal verification, the goal of program verification is to show that a program obeys a specification and is safe to execute, meaning that its execution will not run into any undefined behavior or crash. Program verification for languages with mutable state is commonly done using separation logics, and for languages with effect handlers there exists the program logic Hazel which is built on top of the Iris separation logic framework.

We use Hazel to tackle the question of safety for the central elements of the Eio library, which includes *spawning fibers* that are *run by a scheduler* and can wait for the completion of other fibers by *awaiting promises*. Therefore, our work serves as an extended case study on the usefulness of modelling and verifying programs with effect handlers in Hazel. The formal verification is carried out in the Iris framework and our results are mechanized in the Coq proof assistant.

We were able to verify the safety of the central elements of the Eio library, and prove specifications for its public API and for the declared effects. We also extended the Hazel language to include multithreading in order to adapt previous verification work on a data structure that Eio uses.

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1 Introduction

With the spread of the Internet and computers transmitting ever more data there has been a trend in programming languages to support *user-level concurrency* constructs where an application is responsible to schedule the execution of multiple *tasks* (i.e. some unit of work), analogous to how an operating system traditionally schedules multiple processes. User-level concurrency is especially beneficial when there are many small tasks that are often blocked until an I/O resource like a network socket becomes available (i.e. they are *I/O bound*). In this case the application can quickly switch to another task that is able to do work, avoiding costly jumps to kernel code and doing a context switch. Another advantage is that user-level concurrency has a lighter memory footprint. This way an application can organize many more tasks (possibly on the order of millions) than if it uses a traditional thread-per-task approach.

There is not one standardized implementation for user-level concurrency. It is generally said to use *lightweight threads* as opposed to operating system threads, but in different languages or language libraries the concept is known under terms like *async/await* (Rust, Python, Javascript), *goroutines* (Go), and *fibers* (Java's Project Loom, OCaml 5's Eio).

In this thesis we look at the Eio library of OCaml 5 and formally verify the safety of its core elements for user-level concurrency. The library uses the new effect handler feature [?] from OCaml 5 to implement fibers in an efficient way without stack copying [?]. In order to formally verify the code that uses effect handlers we use the Hazel program logic by de Vilhena [10, 2].

Formal Verification There is a growing need for the formal verification of programs or computer systems to provide a high assurance that they are "safe to use". Formal verification means mathematically modelling programs to enable rigorous proofs about their properties. As such, it also entails mathematically defining when a program is "safe to use". Two important concepts behind this intuition are **safety** and **functional correctness**. By safety, we mean that when evaluating a given program according to the rules of the language it will never get into a state where there are no rules of how to evaluate it further. In some languages this is called *undefined behavior*, but we often model it as crashing the program. Safety is the baseline for the type of program verification that we do and as a next step we can show that programs are functionally correct by proving that they obey a **specification**. Specifications further restrict the possible program executions to a defined set of "good behaviors", such as "for a given input n , this program computes the n th Fibonacci number".

Separation Logic We express specifications as logical propositions and do all reasoning in a separation logic called *Iris* [5]. Separation logics [?] are based on Hoare logic, which has the *Hoare triple* construct $\{P\}s\{Q\}$ to encode the specification of a program. It means that given preconditions P , execution of the program s either diverges or terminates so that the postcondition Q holds¹. Further, separation logics are a type of affine logic that have a *separating conjunction* connective $P * Q$ in addition to the standard logical connectives.

The separating conjunction allows an interpretation of propositions as *resources* that can be split up into disjoint parts P and Q . The most prominent example of a resource is the proposition $l \mapsto v$, representing a heap fragment where the location l holds the value v . This also implies *ownership* over the location l , i.e. no one else can access the location as long as we have that resource. A separating conjunction of heap fragments $l \mapsto v * l' \mapsto v'$ additionally implies that $l \neq l'$, because the heap fragments are necessarily disjoint. The dual connective of a separating conjunction is the *magic wand* $P \multimap Q$, which follows the elimination rule $P * (P \multimap Q) \vdash Q$.

Another type of proposition is duplicable *knowledge*, which is also called *persistent*. For example, Hoare triples $\{P\}s\{Q\}$ are defined as persistent because under the given assumptions P the evaluation of s should always be valid. Separation logics have been successfully applied in many program verification developments [?, ?, ?] as they are useful for modular reasoning about stateful and multithreaded programs.

Iris Iris is not only a separation logic, but a whole separation logic framework implemented in Coq that can be instantiated with different programming languages. This allows us to layer different *program logics* on top of the base separation logic, which contain additional reasoning rules about the evaluation

¹We only look at expression-based languages where Q is allowed to mention the final value of s .

of programs in a concrete language. Verifying a program in Iris follows the schema of first deciding which specifications are necessary for each of the program’s components. These are expressed using predicates in the logic, which we will call the *logical state definitions*. If necessary, one can also use so-called *ghost state*, which is a versatile feature of Iris that allows keeping track of program state and mutating it during a proof. For complicated programs we often define ghost state and derive additional rules that modify it, in order to model the complex state space and state transitions of the program execution. Ghost state updates in Iris are restricted to happen under an *update modality* $\dot{\vdash} P$.

The last step in proving the program specification consists of deriving a (partial) *weakest precondition* $\text{wp } e \{v. Q\}$ for the program expression e . The weakest precondition is defined such that, if evaluation of e eventually terminates (i.e. divergence is permitted) in a final value v , it must satisfy $Q\ v$. The name is derived from the fact that it is by definition the weakest precondition P that makes the Hoare triple $\{P\}e\{v. Q\}$ true. Hoare triples are even defined this way in Iris:

$$\{P\}e\{v. Q\} := \Box(P \multimap \text{wp } e \{v. Q\})$$

Since propositions are affine by default, the *persistence modality* $\Box P$ is used to define Hoare triples as persistent. Therefore, deriving a weakest precondition for an expression e proves a specification for it in terms of the assumptions P and conclusion Q . This also establishes the safety of the expression due to a soundness lemma of the logic.

One other powerful feature of Iris are *shared invariants* $\boxed{I}^{\mathcal{N}}$, which represent knowledge that a resource does not change over time, so they are also persistent. They are used to encapsulate a resource I in order to share it under the restriction that the invariant can only be opened for one atomic step of execution at a time. If the invariant is opened, the contained resource I can be accessed but must be restored at the end of the execution step. This ensures that even in the presence of multiple threads executing in parallel, the invariant is never observably violated.

The standard language for Iris is called *heaplang* and is an ML-type language with mutable state and multithreading. However, it does not support effect handlers as present in OCaml 5. So for reasoning about programs with effect handlers we use the *Hazel* language for Iris.

Effect Handlers Effect handlers are a versatile concept explored in some research languages [koka, eff] and now also implemented in OCaml 5. The OCaml 5 implementation brings with it an extensible variant type `Effect.t`, meaning one can add new constructors to the type, and a keyword `perform` to perform an effect, which transfers control to an appropriate effect handler. They are often called “resumable exceptions” because analogous to exception handlers, one installs an effect handler around an expression e to handle its effects, but the effect handler also receives a delimited continuation k , representing the rest of the computation of e from the point where the effect was performed.

We present code examples in a simplified OCaml 5 syntax² as shown in figure 1, because the concrete syntax of effect handlers is verbose. We use an overloading of the `match` expression, which includes cases for handled effects, that is common in the literature.

The biggest advantage of effect handlers for treating effects in a language over using monads is that they are more composable. For one, using non-monadic functions together with monadic functions often requires rewriting parts of the code into monadic style. Also, composing multiple monads results in monad transformer stacks which are notoriously confusing. Instead, effect handlers can be layered just like normal exception handlers and code written without the use of effect handlers can be used as-is.

Languages like Koka additionally track the possible effects of an expression in their type. This might be implemented for OCaml 5 in the future, but for now effects are not tracked by the type system. It is the responsibility of the programmer to install effect handlers that handle all possible effects of their program. This raises the question of **effect safety** for OCaml programs using effect handlers, which means that a program does not perform any unhandled effects. The OCaml 5 runtime treats unhandled effects as an error and crash the program. So to prove the safety of OCaml 5 programs we must additionally establish their effect safety.

Hazel & Protocols In our development we use the Iris language *Hazel* by de Vilhena [10, 2] which formalizes an ML-like language with effect handlers. We restate the most important concepts but for a deeper understanding we recommend reading [10].

²This syntax is planned to be implemented in OCaml 5 in the future: <https://github.com/ocaml/ocaml/pull/12309>

```

1  (* Declares a new constructor for the effect type
2   * E : int -> bool Effect.t *)
3  effect E : int -> bool
4
5  (* Evaluating a perform expression with a value of type 'a Effect.t
6   * transfers control to the enclosing handler and (possibly)
7   * terminates in a value of type 'a. *)
8  let e () =
9    let (b : bool) = perform (E 1) in
10    b
11
12  (* Evaluates the expression e () and if the effect E is performed,
13   * control is transferred to the second branch.
14   * The match acts as a deep handler, i.e. even if during the
15   * evaluation of e the effect E is performed multiple times, the
16   * second branch is evaluated every time.
17   * When e is reduced to a value, the non-effect branches are
18   * used for pattern matching as usual. *)
19  match e () with
20  | v -> v
21  (* This handler just checks if the passed value is 1.
22   * Applying k to a value adds the continuation to the stack,
23   * so control is transferred back to where the perform expression
24   * was evaluated. *)
25  | effect (E v) k -> k (v = 1)

```

Figure 1: Example for the effect handler syntax.

Hazel defines an *extended weakest precondition* $\text{ewp } (e) \langle \Psi \rangle \{v, Q\}$ which – in addition to what is implied by a normal weakest precondition – shows we can observe that the expression e performs effects according to the protocol Ψ . A protocol Ψ acts as a specification for effects in terms of their “input” and “output”, casting them in a similar light to function calls. The main way to specify a protocol is by the following constructor.

$$! \vec{x}(v) \{P\}. ? \vec{y}(w) \{Q\}$$

The input (!) and output (?) syntax is inspired by session types [4] which are used to describe the behavior of communicating parties. Intuitively, the part after the exclamation mark gets “sent” to the effect handler and the part after the question mark is “received” as an answer. \vec{x} and \vec{y} are binders whose scope extends from their position all the way to the right. The client who performs the effect transmits the value v to the effect handler and must prove the proposition P . In return, the client receives from the effect handler a value w and gets to assume Q . In total, this can be thought of as an analogue to a Hoare triple like $\{P\} \text{handler } v \{w, Q\}$, where we explicitly name the handler that handles the effect. But the client only indirectly invokes the effect handler by evaluating a *perform* expression, so in practice we prove the following Hoare triple.

$$\{P\} \text{perform } v \{w, Q\}$$

Apart from the above there are three additional ways to define protocols. There is the sum constructor $\Psi_1 + \Psi_2$ to combine two protocols, allowing e to perform effects according to both, and its neutral element, the empty protocol \perp , which allows no effects. Finally, there is a tag constructor $\ell \# \Psi$ to give a name to protocols. Our example effect E from figure 1 could therefore be formalized using the following protocol Ψ_E .

$$\Psi_E := E \# !i(i) \{i \in \text{int}\}. ?b(b) \{b \in \text{bool}\}$$

maybe more
expressive
example

Using the extended weakest precondition with the \perp protocol then enables us to prove that a program is **effect safe**, as it shows that we cannot observe any effects from the top level. Note that internally the program can of course perform effects, but an effect handler hides the effects of its discriminant expression which leads to an empty protocol at the top.

1.1 The Eio Library

We first give a general overview of the functionality provided by the Eio library before discussing what we focus on in our verification work in the next section. Eio is a library for cooperative user-level concurrency

where individual tasks are represented by *fibers*³. Fibers are just OCaml functions that are allowed to perform a defined set of effects to interact with the cooperative scheduler. A scheduler is responsible for running an arbitrary amount of fibers in a single thread. However, if multithreading is required it is possible to spawn additional schedulers in new threads, providing some initial fiber.

In a cooperative user-level concurrency setting, many existing APIs for operating system resources in OCaml are not suitable anymore because they are blocking. Therefore, Eio also provides concurrency-aware abstractions to these resources, such as network sockets, the file system, and timers, i.e. they suspend the running fiber instead of blocking the system-level thread. Since these schedulers must interact with operating system, there are specialized schedulers for multiple platforms such as Windows, Linux, and a generic POSIX scheduler. Eio also offers synchronization and message passing constructs like mutexes and channels which are also concurrency-aware.

1.2 Focus and Structure of the Thesis

Eio aims to be the standard cooperative concurrency library for OCaml 5, so it includes many functions implementing structured concurrency of fibers (e.g. `Fiber.{first, any, both, all}`, which run two or more fibers and combine their results), support for cancelling fibers, abstractions for operating system resources, a different scheduler implementation per platform, and synchronization constructs like promises and mutexes. But for this work we restrict ourselves to verifying the safety and effect safety of Eio's core functionalities:

1. Running fibers in a "common denominator" scheduler that does not interact with any operating system resources but just schedules fibers.
2. Awaiting the result of other fibers using the *promise* synchronization construct.
3. And spawning new schedulers to run fibers in another thread.

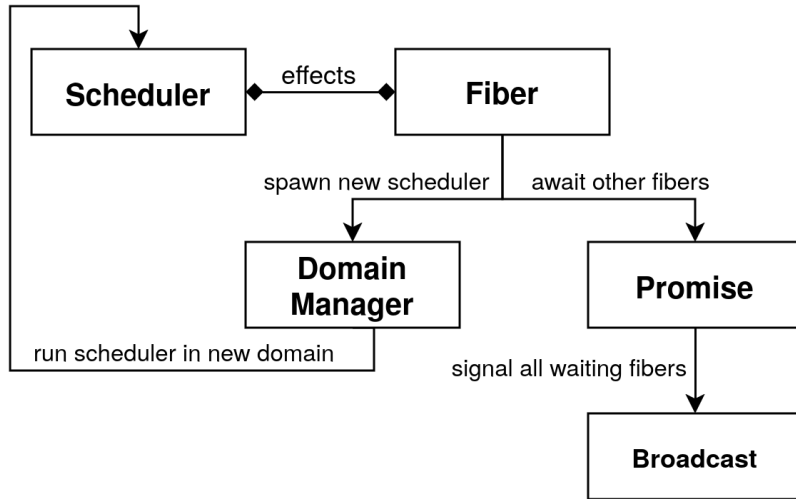


Figure 2: Eio module hierarchy.

Figure 2 shows the simplified module hierarchy of the concepts we focus on. A standard arrow stands for a direct source code dependency from one module to another. The diamond arrow between `Scheduler` and `Fiber` stands for the implicit dependency that fibers perform effects which are handled by code in the scheduler module.

Fibers can fork off new fibers using the *Fork* effect, suspend execution using the *Suspend* effect, and get access to some context data using the *GetContext* effect, all of which are handled by the scheduler

³Note that these are technically different from the existing fiber concept in OCaml 5, where a fiber denotes a stack frame under an effect handler, and the runtime stack is a linked list of those fibers. But since Eio fibers are evaluated under an effect handler, they all have an associated OCaml fiber. See also: <https://v2.ocaml.org/manual/effects.html#s:effects-fibers>

they are running in. The implementation of the fiber and scheduler functions are discussed in section 2.1. *Promises* are built on top of the *broadcast* data structure, which is a lock-free signalling construct that is used by fibers to signal other fibers when they are done. The specification of promises is discussed in section 2.2. Broadcast is based on the *CQS* data structure, whose specification is already verified using Iris [6], but Eio customizes the implementation so we had to adapt the proof. We discuss this process in section 3. Fibers in Eio also have access to *thread-local variables* by performing a *GetContext* effect, which is discussed in section 5. They are thread-local in the sense that they are shared between all fibers of one scheduler. Finally, we discuss our addition of multithreading to the Hazel operational semantics in order to model running schedulers in different threads. This turned out to be technically trivial, so we only discuss it in appendix B and take a multithreaded semantics and support for Iris *shared invariants* as a given in the remainder of the main text.

1.3 Contributions

To summarize our contributions, in this thesis we verify the **safety** and **effect safety** of a simplified model of Eio which serves as an extended case study on the viability of Hazel for verifying programs with effect handlers. This includes:

- The verification of the basic Eio **fiber abstraction** running on a common denominator scheduler.
- Proving reusable specifications for the main three effects of Eio: *Fork*, *Suspend*, and *GetContext*.
- An adaptation of the existing verification of CQS to the customized version used by Eio.
- Adding multithreading to Hazel’s operational semantics, which shows we can reason about programs that use both **multithreading** and **effect handlers**.

2 Verifying a Simplified Eio Scheduler with Promises

Cooperative concurrency schedulers for user-level threads (i.e. *fibers*) are commonly treated in the literature on effect handlers [3, 7, 10] to because they are a good example for the usefulness of manipulating delimited continuations with effect handlers. Generally, the architecture contains an effect handler as the scheduler and fibers are normal functions which perform effects to yield execution. This is because performing an effect causes execution to jump to the enclosing effect handler (i.e. the scheduler), providing it with the rest of the fiber’s computation in the form of a delimited continuation. The scheduler keeps track of a collection of these continuations and by invoking one of them the next fiber is scheduled. This approach is also used in Eio.

We can therefore use the simple cooperative concurrency scheduler case study from the dissertation of de Vilhena [2] as a starting point for our verification work. In the following section we first discuss our simplified implementation of Eio and give an intuition about the specification of each component. Based on this intuition we then build a formalization in section 2.2.

Mention that all code examples are an OCaml rendering of the verified Hazel code, based on but not equal to the Eio code

2.1 Implementation

Let us first get an idea of how different components of the core Eio fiber abstraction interact by looking at their types. `Scheduler.run`⁴ is the main entry point to Eio. It runs a scheduler and is provided a function which represents the first fiber to be executed. A scheduler runs the main fiber and all forked off fibers in a single thread. However, a fiber can also spawn new schedulers in separate threads to run other fibers in parallel as detailed in appendix B. The `Fiber.fork_promise` function is used to spawn fibers in the current scheduler. The function returns a promise holding the eventual return value of the new fiber. The promise is thread-safe so that it can be shared with fibers running in different threads. The `Promise.await` function can be used by any fiber to wait until the value of a promise is available. Common problems like deadlocks are not prevented in any way and are the responsibility of the programmer.

```
1 (* Basic interface of the Eio library. *)
2 Scheduler.run : (unit -> 'a) -> 'a option
3 Fiber.fork_promise : (unit -> 'a) -> 'a Promise.t
4 Promise.await : 'a Promise.t -> 'a
```

2.1.1 Scheduler.run

As mentioned above this is the main entry point to the Eio library and its code is shown in figure 3. It sets up the scheduler environment and runs the main fiber that is passed as an argument.

The `run_queue` (line 6) contains closures that invoke the continuation of an effect. This represents ready fibers which can continue execution from the point where they performed an effect. The `next` function (line 7) pops one fiber (i.e. function) from the `run_queue` and executes it. If no more ready fibers remain – either because all fibers terminated or there is a deadlock – the `next` function returns and the scheduler exits.

The inner `execute` function (line 12) is called once on each fiber to evaluate it and handle any performed effects.

Value Case

The non-effect case of the `match` (line 14) only runs the next fiber because Eio adopts the convention that all fibers return a unit value and their real return value is handled out of band.

- The main fiber is wrapped in a closure that saves its return value in a reference (line 24) that is read when the scheduler exits (line 25).
- All other fibers are forked using `Fiber.fork_promise`, which wraps them in a closure that saves their return value in a promise.

This emphasizes the fact that an Eio scheduler is only used for running fibers. The interaction between fibers waiting for values of other fibers is handled separately by promises.

⁴The scheduler’s result is optional because the main fiber might deadlock.

```

1  effect Fork : (unit -> 'a) -> unit
2  type 'a waker : 'a -> unit
3  effect Suspend : ('a waker -> unit) -> 'a
4
5  let run (main : unit -> 'a) : 'a option =
6    let run_queue = Lf_queue.create () in
7    let next () =
8      match Lf_queue.pop run_queue with
9      | None -> ()
10     | Some cont -> cont ()
11   in
12   let rec execute fiber =
13     match fiber () with
14     | () -> next ()
15     | effect (Fork fiber) k ->
16       Lf_queue.push run_queue (fun () -> invoke k ());
17       execute fiber
18     | effect (Suspend register) k =>
19       let waker = fun v -> Lf_queue.push run_queue (fun () -> invoke k v) in
20       register waker;
21       next ()
22   in
23   let result = ref None in
24   execute (fun () -> result := main ());
25   !result

```

Figure 3: Implementation of Scheduler.run.

Fork Case

Handling a *Fork* effect (line 15) is simple because it only carries a new *fiber* to be executed, so the handler recursively calls the *execute* function (line 17) to execute it immediately. The execution of the original fiber is paused due to performing an effect and its continuation *k* is placed in the run queue so that it can be scheduled again (line 16). This prioritizes the execution of a new fiber and is a design decision by Eio. It would be equally valid to place the *fiber* argument in the run queue instead.

Suspend Case

Handling a *Suspend* effect (line 18) may look complicated at first due to the higher-order register function. This effect is used by fibers to suspend execution until a condition is met. The fiber defines this condition by constructing a *register* function which in turn receives a wake-up capability by the scheduler in the form of a *waker* function. The key point is that as long as the continuation *k* is not invoked, the fiber does not continue execution. So the *waker* function “wakes up” a fiber by placing its continuation *k* into the run queue (line 19). The *register* function is called by the scheduler right after the fiber suspends execution (line 20) and is responsible for installing *waker* as a callback at a suitable place (or even call it directly). For example, to implement promises, the *waker* function is saved in a data structure that calls the function after the promise is fulfilled.

Note that the *waker* function’s argument *v* has a *locally abstract type*, which is a typical pattern in effect handlers. From the point of view of the fiber, the polymorphic type *'a* of the *Suspend* effect is instantiated depending on how the effect’s return value is used. But the scheduler does not get any information about this so the argument type of the continuation *k* and the *waker* function is abstract.

Waking up must be possible across thread boundaries, which is why the *run_queue* in the scheduler is a thread-safe queue. For the verification we assume the specification of a suitable *Lf_queue* module that supports thread-safe push and pop operations, which exists in Eio under the same name.

2.1.2 Fiber.fork_promise

This function is the basic way to fork a new fiber in Eio and the only one we model in our development. The code is presented in figure 4. It creates a promise (line 17) and spawns the provided function as a new fiber using the *Fork* effect (line 22). Promises are always created in a *Waiting* (we also say *unfulfilled*)

```

1  (* promise.ml *)
2  type 'a t = Done of 'a | Waiting of Broadcast.t
3
4  let create () : 'a t =
5    let bcst = Broadcast.create () in
6    Atomic.create (Waiting bcst)
7
8  let fulfill p result =
9    match Atomic.get p with
10   | Done _ -> error "impossible"
11   | Waiting bcst ->
12     Atomic.set p (Done result);
13     Broadcast.signal_all bcst
14
15  (* fiber.ml *)
16  let fork_promise (f : unit -> 'a) : 'a Promise.t =
17    let p = Promise.create () in
18    let fiber = fun () ->
19      let result = f () in
20      Promise.fulfill p result
21    in
22    perform (Fork fiber)
23    p

```

Figure 4: Excerpt of the Promise module & implementation of `Fiber.fork_promise`.

state and calling `Promise.fulfill` sets it to the `Done` state, at which point the final value can be retrieved. The meaning of the `Broadcast.t` is explained in the next section.

When `f` is reduced to a value `result`, `Fiber.fork_promise` then fulfills the promise with that value (line 20), which signals all fibers waiting for that result to wake up (line 13). The major difference with respect to the implementation of de Vilhena is that promises in Eio are entirely handled by the fiber, and not in the effect handler code of the scheduler. This achieves a better separation of concerns and simplifies the logical state needed for the proof.

2.1.3 `Promise.await`

```

1  let make_register (p: 'a t) (bcst: Broadcast.t) : (unit waker -> unit) =
2    fun waker ->
3      let register_result = Broadcast.register bcst waker in
4      match register_result with
5      | None -> ()
6      | Some register_handle ->
7        match Atomic.get p with
8        | Done result ->
9          if Broadcast.try_unregister register_handle
10           then waker ()
11           else ()
12        | Waiting _ -> ()
13
14  let await (p: 'a t) : 'a =
15    match Atomic.get p with
16    | Done result -> result
17    | Waiting bcst ->
18      let register = make_register p bcst
19      perform (Suspend register);
20      match Atomic.get p with
21      | Done result -> result
22      | Waiting _ -> error "impossible"

```

Figure 5: Implementation of `Promise.await`.

This is the most complex looking function in our development which is partly due to the *Suspend* effect and also due to the use of *broadcast* functions. Its code is presented in figure 5. The purpose of

`Promise.await p` is to suspend execution of the calling fiber until `p` is fulfilled with a value and then return this value. The “suspend execution” part is handled by performing a *Suspend* effect. Then, the “until `p` is fulfilled” part is implemented by using a *broadcast* data structure.

In Eio, a *broadcast* is an implementation of a signalling mechanism used for similar purposes as condition variables in various languages. The major difference is that callers do not directly suspend execution if the condition is not met, but supply a callback that will be called when the condition is signalled.

In figure 6 we show the public API of the Broadcast module. The `Broadcast.register` function attempts to register a given callback with the data structure while `Broadcast.signal_all` calls all registered callbacks. For `Broadcast.register`, a return value of `Invoked` means that it already called the supplied callback because the function detected the signal while it was running. Otherwise, a return value of `Registered register_handle` means that the callback was registered but the signal might have been already sent but missed. It is the responsibility of the caller to check if the signal was already sent and if it was, to then cancel the registration again. This is done by calling the `Broadcast.try_unregister` function on the `register_handle`, which returns a boolean indicating the cancellation status. If the cancellation was successful, the previously registered callback is not called when `Broadcast.signal_all` is executed. The specifications of the functions is explained in more detail in section 3.3, for now we just explain their usage in the context of `Promise.await`.

```

1  type t
2  type signal = unit -> unit
3  type register_result = Invoked | Registered of register_handle
4  type register_handle
5
6  val create : unit -> t
7  val register : t -> signal -> register_result
8  val try_unregister : register_handle -> bool
9  val signal_all : t -> unit

```

Figure 6: Interface of the Broadcast module.

In the `Promise.await` function if the promise is not fulfilled initially (figure 5 line 17) then the fiber should wait until that is the case, so it performs a *Suspend* effect (line 19). The `register` function passed to the effect registers the waker function using `Broadcast.register` (line 3). When at some point the `Broadcast.signal_all` function is called – this happens in `Fiber.fork_promise` – all registered wakers are called in turn. Recall that calling a waker function enqueues the fiber that performed the *Suspend* effect in the scheduler’s run queue so that it can continue execution.

In the default case the following simplified chain of events happens:

1. The fiber suspends execution at the point of evaluating `perform (Suspend register)`.
2. The waker function is registered with a broadcast.
3. The promise is fulfilled.
4. The waker function is called.
5. The fiber resumes execution at the point of evaluating `perform (Suspend register)`.

Therefore, when matching on the promise state again after the *Suspend* effect returns (line 20) we know the state of the promise is `Done` and the final value can be returned.

But because broadcast is a lock-free data structure and promises can be shared between different threads there are a number of possible interleavings that the `register` function must take care of as well. The definition of the `register` function is interesting enough that we split it out into `make_register` and give a separate specification, which is not part of the public API of the module. First, there could be a race on the state of the promise itself. Right after the state is read (figure 5 line 15) another thread might change the state to `Done` and go on to call `Broadcast.signal_all`. If that happens there is another possible race between the call to `Broadcast.register` (line 3) and the call to `Broadcast.signal_all` in the other thread⁵. If `Broadcast.register` detects that it lost the race, it directly calls the waker function

⁵There is a possible race to set an atomic location that holds the state of the registration. Interested readers are directed to the implementation linked in [6].

and returns `Invoked`. Otherwise, the waker function is registered but in fact the `Broadcast.signal_all` might have already finished before `Broadcast.register` even started, so it failed to detect the race. In this case the waker would be “lost” in the broadcast, never to be called. To avoid this, `register` must check the state of the promise again (line 7), and – if it is fulfilled – try to cancel the waker registration. The cancellation fails if the waker function was already called. Otherwise, the cancellation succeeds and the `register` function has the responsibility of calling waker itself (line 10).

The only **safety** concerns in the above implementation are `Fiber.fork_promise` expecting the promise to be unfulfilled after the fiber has finished execution (figure 4 line 10), and `Promise.await` expecting the promise to be fulfilled in the last match (figure 5 line 22). In both cases, the program would crash (signified by the error expression) if the expectation is violated. So to establish the safety of Eio we wish to prove that the expectations always hold, and the two error expressions are never reached. In the next section we show how the former situation is addressed by defining an affine permission to fulfill a promise, and the latter is a consequence of the protocol of the *Suspend* effect.

2.2 Specification

To prove specifications for an effectful program in Hazel we have to define not only ghost state constructs to track program state but also protocols which describe the behavior of the program’s effects. For our Eio development we adapt both the ghost state and the effect protocols from the cooperative concurrency scheduler development from chapter 4 of de Vilhena’s dissertation [2].

2.2.1 Protocols

The protocols for the *Fork* and *Suspend* effect are shown in figure 7. The subscripts on definitions indicate that we will change them later when extending the model.

$$\begin{aligned}
isWaker_1 \text{ wkr } W &\triangleq \forall v. W \text{ } v \multimap ewp \text{ (wkr } v) \langle \perp \rangle \{ \top \} \\
isRegister_1 \text{ reg } W &\triangleq \forall wkr. isWaker_1 \text{ wkr } W \multimap ewp \text{ (reg wkr)} \langle \perp \rangle \{ \top \} \\
Coop_1 &\triangleq \text{ Fork } \# ! e \text{ (} e \text{)} \{ \triangleright ewp \text{ (} e () \text{)} \langle Coop_1 \rangle \{ \top \} \} .? () \{ \top \} \\
&\quad \text{ Suspend } \# ! \text{ reg } W \text{ (reg)} \{ isRegister_1 \text{ reg } W \} .? y \text{ (} y \text{)} \{ W \ y \}
\end{aligned}$$

Figure 7: Definition of $Coop_1$ protocol with *Fork* & *Suspend* effects.

Fork The *Fork* effect accepts a value e which represents the computation that a new fiber executes. To perform the effect one must prove that e acts as a function that can be called on unit and obeys the $Coop_1$ protocol itself. This means all forked off fibers can again perform *Fork* and *Suspend* effects. The weakest precondition argument is guarded behind a later modality because of the recursive occurrence of $Coop_1$.

Suspend From the type of the *Suspend* effect in figure 3 we know that a value can be transmitted from the party that calls the waker function to the fiber that performed the effect. The *Suspend* protocol now expresses the same idea on the level of resources. To suspend, a fiber must supply a function `register` that satisfies the *isRegister* predicate. This predicate says that `register` must be callable on a waker function for which we get to assume that it is callable on any value v that satisfies $W \ v$.

Both `register` and `waker` must not perform effects and are callable only once (since the *ewp* is an affine resource itself). The predicate W appears twice in the definition of the protocol. Once in the precondition of `waker` and then in the postcondition of the whole protocol. It signifies the resources that are transmitted from the party that calls the waker function to the fiber that performed the effect. By appropriately instantiating W , we can enforce that some condition holds before the fiber can be signalled to continue execution, and we get to assume the resources $W \ v$ for the rest of the execution.

2.2.2 Logical State

The most basic logical state definition we use is whether a promise is fulfilled or not. If a promise p is unfulfilled, two copies of *osWaiting* exist, one owned by the fiber and one by the invariant that tracks

Maybe use
meta_tokens
to hide
gamma

$$\begin{array}{c}
\text{Persistent}(osAssigned\ \gamma) \quad \text{OS-CREATE} \quad \frac{}{\vdash \exists \gamma. osWaiting\ \gamma * osAssigned\ \gamma} \quad \text{OS-COMBINE} \quad \frac{osWaiting\ \gamma * osWaiting\ \gamma}{\Box osAssigned\ \gamma} \\
\text{OS-CONTRA} \quad \frac{osWaiting\ \gamma * osAssigned\ \gamma}{\perp}
\end{array}$$

Figure 8: Rules for the *osWaiting* and *osAssigned*.

the state of all promises. When fulfilling the promise, both copies can be combined and converted to a persistent *osAssigned* resource. The *osWaiting* and *osAssigned* resources cannot exist at the same time. This design allows us to deduce the current state of the promise depending on if we own a *osWaiting* or a *osAssigned*. This is formalized in the rules in figure 8.

Other pieces of ghost state are *PlnInner*, *isPromise*, and *Ready* described in figure 9. *PlnInner* tracks additional resources for all existing promises by using an authoritative map which contains for each promise: a location *p* holding its current program value, a ghost name *γ* that is used for the *osWaiting* and *osAssigned* resources, and a predicate *Φ* that describes the value the promise will eventually hold.

Additionally, for each promise in the map we own some resources as part of *PlnInner* that depend on the current state of the promise. As long as the promise is not fulfilled we own a broadcast, one copy of *osWaiting*, and a *signalAllPermit*. The *signalAllPermit* is used to call the `Broadcast.signal_all` function which must only be called once. When the promise has been fulfilled, we instead own a *osAssigned* and the knowledge that the final value satisfies the given postcondition *Φ*.

isPromise is a persistent resource that denotes that *p* exists as a promise in *PlnInner*. The *pn* ghost name is globally unique and included in the resource algebra we use for the proofs.

The *Ready* predicate describes fibers in a scheduler's `run_queue`. It expresses that *f* is safe to be executed and is used as the invariant for a scheduler's run queue, i.e. it should hold for all fibers in the run queue that they can be executed.

PromiseInv is an invariant that wraps *PlnInner* so that we can share it.

$$\begin{aligned}
\text{PromiseState } p\ \gamma\ \Phi &\triangleq (\exists v. p \mapsto \text{Done } v * osAssigned * \Box \Phi\ v) \\
&\vee (\exists bcst. p \mapsto \text{Waiting } bcst * isBroadcast\ bcst * osWaiting * signalAllPermit) \\
\text{PlnInner} &\triangleq \exists M. [\bullet M]^{pn} * \forall (p, \gamma) \mapsto \Phi \in M. \text{PromiseState } p\ \gamma\ \Phi \\
\text{PromiseInv} &\triangleq [\text{PlnInner}]^{\mathcal{N}} \\
isPromise\ p\ \Phi &\triangleq \exists \gamma. [\circ \{[(p, \gamma) \mapsto \Phi]\}]^{pn} \\
\text{Ready}_1\ f &\triangleq ewp\ (f\ ())\ \langle \perp \rangle\ \{\top\}
\end{aligned}$$

Figure 9: Logical state definitions for the verification of our Eio model.

In the next sections we discuss the specifications we proved for the three functions. We show a detailed proof of the specification only for `Promise.await` because it is the most involved.

2.2.3 Scheduler.run

The interesting part about the scheduler specification `SPEC-RUN` is that it proves **effect safety** of the fiber runtime, i.e. no matter what a fiber does it will not crash the scheduler due to an unhandled effect. This is expressed by allowing the fiber *main* to perform effects according to the *Coop* protocol, but running the scheduler on the main fiber (*run main*) obeys the empty protocol, so no effects escape. Of course, the *ewp* itself also implies **safety** of running both the main fiber and the scheduler.

$$\text{SPEC-RUN} \quad \frac{ewp\ (\text{main } ())\ \langle \text{Coop} \rangle\ \{v, \Box \Phi\ v\}}{ewp\ (\text{run main})\ \langle \perp \rangle\ \{v, \Box \Phi\ v\}}$$

However, the specification only talks about effect safety and not about handling fibers correctly in any other way, e.g. regarding fairness of scheduling or just not dropping fibers. For example, a trivial *run* function which ignores the *main* argument and immediately returns satisfies the same specification. For a scheduler it would be desirable to prove these properties, too, but since they are liveness properties it is hard to do in Iris and not a focus of this thesis.

Explain why
it's hard

2.2.4 **Fiber.fork_promise**

The specification SPEC-FORKPROMISE expresses that we receive from *fork_promise* a value *p* that will eventually hold a value satisfying Φ . It has two preconditions, for one we must give it an arbitrary expression *f* representing the new fiber. When called, *f* obeys the *Coop* protocol and returns some value *v* satisfying Φ . Also, *fork_promise* needs the *PromiseInv* invariant to interact with the global collection of promises, because it creates a new promise and fulfills it after *f* has finished executing.

$$\frac{\text{SPEC-FORKPROMISE} \quad \text{PromiseInv} * \text{ewp} (f ()) \langle \text{Coop} \rangle \{v, \Box \Phi v\}}{\text{ewp} (\text{fork_promise } f) \langle \text{Coop} \rangle \{p, \text{isPromise } p \Phi\}}$$

2.2.5 **Promise.await**

The specification SPEC-AWAIT is the direct counterpart to SPEC-FORKPROMISE. It shows that *await* consumes a promise *p* and eventually returns its value *v* satisfying the predicate Φ . The precondition *PromiseInv* is again necessary to interact with the global collection of promises and *isPromise* is used to identify the promise *p* in that collection.

If *p* is still unfulfilled the first time *await* checks the promise state, it calls *make_register* to create a register function which it passes to the *Suspend* effect. As the SPEC-MAKEREISTER specification shows, *make_register* returns a suitable function that satisfies the *isRegister* predicate, instantiating *W* with $(\lambda v, \ulcorner v = () \urcorner * \text{osAssigned})$ so that we obtain a *osAssigned* resource when the effect returns.

$$\frac{\text{SPEC-MAKEREISTER} \quad \text{PromiseInv} * \text{isPromise } p \Phi * \text{isBroadcast } \text{bcst}}{\text{ewp} (\text{make_register } p \text{ bcst}) \langle \perp \rangle \{\text{reg}, \text{isRegister } \text{reg} (\lambda v, \ulcorner v = () \urcorner * \text{osAssigned})\}}$$

$$\frac{\text{SPEC-AWAIT} \quad \text{PromiseInv} * \text{isPromise } p \Phi}{\text{ewp} (\text{await } p) \langle \text{Coop} \rangle \{v, \Box \Phi v\}}$$

In figures 10 and 11 we give Hoare-style proof annotations for the two functions *make_register* and *Promise.await* from figure 5. The proof of SPEC-MAKEREISTER uses the specifications of some broadcast functions. We briefly explain these specifications and their logical state definitions now and expand upon them in section 3.3.

$$\begin{aligned} \text{isCallback } cb \ R &\triangleq R \multimap \text{ewp} (cb ()) \langle \perp \rangle \{\top\} \\ \text{isBroadcastRegisterResult } r \ cb \ R &\triangleq (\ulcorner r = \text{Invoked} \urcorner) \\ &\quad \vee (\ulcorner r = \text{Registered } h \urcorner * \text{isBroadcastRegisterHandle } h \ cb \ R) \\ \text{isBroadcastRegisterHandle} &: \text{Val} \rightarrow \text{Val} \rightarrow \text{iProp} \rightarrow \text{iProp} \end{aligned}$$

$$\frac{\text{SPEC-BROADCASTREGISTER} \quad \text{isBroadcast } \text{bcst} * \text{isCallback } \text{callback } R}{\text{ewp} (\text{register } \text{bcst } \text{callback}) \langle \perp \rangle \{r, \text{isBroadcastRegisterResult } r \ \text{callback } R\}}$$

$$\frac{\text{SPEC-BROADCASTTRYCANCEL} \quad \text{isBroadcastRegisterHandle } h \ cb \ R}{\text{ewp} (\text{try_unregister } h) \langle \perp \rangle \{b, \text{if } b \text{ then } \text{isCallback } cb \ R \text{ else } \top\}}$$

The function `Broadcast.register` takes a callback *cb* that satisfies the *isCallback* predicate to register it in the broadcast data structure. This predicate is structurally similar to *isWaker* and, in fact, in the proof of `SPEC-MAKEREREGISTER` we instantiate the precondition *R* with *osAssigned* and pass as the callback a waker function, which has the precondition $(\lambda v, \ulcorner v = () \urcorner * \text{osAssigned})$ as described above. The result of `Broadcast.register` is either a value *Invoked*, which expresses that it called the callback directly, or a register handle, which can be used to call `Broadcast.try_unregister`.

`Broadcast.try_unregister` attempts to cancel a previous registration identified by the given *handle*. If the cancellation is successful, we receive a *isCallback* resource which shows that we can safely call the callback.

Hoare-Style Proofs for `SPEC-MAKEREREGISTER` and `SPEC-AWAIT` In the proof below an opened invariant *Inv* is represented as Inv and resources that are not needed for the rest of the proof are dropped implicitly.

The proof of `SPEC-MAKEREREGISTER` is straightforward and follows from the specifications of `Broadcast.register` and `Broadcast.try_unregister`. For `SPEC-AWAIT`, the crux is that we define `SPEC-MAKEREREGISTER` so that it returns a *register* function which satisfies *isRegister register* $(\lambda v, \ulcorner v = () \urcorner * \text{osAssigned})$. Then, we get access to the *osAssigned* resource when the *Suspend* effect returns, and we can refute the case of the promise still being unfulfilled when checking the state of promise again for the last time.

$$\frac{}{ewp (make_register p bcst) \langle \perp \rangle \{reg, isRegister reg (\lambda v, \lceil v = () \rceil * osAssigned)\}}$$

<pre> let make_register (p: 'a t) (bcst: Broadcast.t) : (unit waker -> unit) = {PromiseInv * isPromise p * isBroadcast bcst} fun (waker: unit waker) -> {PromiseInv * isPromise p * isBroadcast bcst * (osAssigned -> ewp (waker ()) <⊥> {T})} let regres = Broadcast.register bcst waker in {PromiseInv * isPromise p * isBroadcast bcst * isBroadcastRegisterResult regres} match regres with </pre>		
<pre> 1. {regres = None} None -> () {T} </pre>		[intro waker that satisfies <i>isWaker</i>]
<pre> 2. { PromiseInv * isPromise p * isBroadcast bcst * regres = Some handle * isBroadcastRegisterHandle handle Some handle -> { PromiseInv * isBroadcast bcst * isBroadcastRegisterHandle handle * PromiseState p γ Φ } match Atomic.get p with </pre>		[apply SPEC-BROADCASTREGISTER with $R := osAssigned$]
<pre> 2.1. { PromiseInv * isBroadcast bcst * isBroadcastRegisterHandle handle * p ↦ Done result * osAssigned Done result -> { isBroadcast bcst * isBroadcastRegisterHandle handle * osAssigned } if Broadcast.try_unregister handle </pre>		[CA on <i>regres</i>]
<pre> 2.1.1. {osAssigned * (osAssigned -> ewp (waker ()) <⊥> {T})} {ewp (waker ()) <⊥> {T}} then waker () {T} </pre>		[open <i>PromiseInv</i> , lookup <i>p</i> using <i>isPromise p</i>]
<pre> 2.1.2. {T} else () {T} </pre>		[CA on <i>PromiseState</i>]
<pre> 2.2. {PromiseInv * p ↦ Waiting _} Waiting _ -> () {T} </pre>		[close <i>PromiseInv</i> , goal is <i>trivial</i>]

Figure 10: Annotated proof of SPEC-MAKERREGISTER.

$$\frac{\text{PromiseInv} * \text{isPromise } p \ \Phi}{\text{ewp } (\text{await } p) \langle \text{Coop} \rangle \{v, \Box \Phi \ v\}}$$

<code>let await (p: 'a t) : 'a =</code> <code>{PromiseInv * isPromise p}</code> [open <i>PromiseInv</i> , lookup <i>p</i> using <i>isPromise p</i>] <code>{PromiseInv * isPromise p * PromiseState p γ Φ}</code> <code>match Atomic.get p with</code> [CA on <i>PromiseState</i>]	
1. $\left\{ \begin{array}{l} \text{PromiseInv} * \\ p \mapsto \text{Done result} * \Box(\Phi \text{ result}) \end{array} \right\}$	
<code>Done result -></code>	[close <i>PromiseInv</i>]
$\{ \text{PromiseInv} * \Box(\Phi \text{ result}) \}$	
result	[by assumption]
$\{ \Box(\Phi \text{ result}) \}$	
2. $\left\{ \begin{array}{l} \text{PromiseInv} * \text{isPromise } p * \\ p \mapsto \text{Waiting bcst} * \text{isBroadcast bcst} \end{array} \right\}$	
<code>Waiting bcst -></code>	[close <i>PromiseInv</i>]
$\left\{ \begin{array}{l} \text{PromiseInv} * \text{isPromise } p * \\ \text{isBroadcast bcst} \end{array} \right\}$	
<code>let register = make_register p bcst</code>	[apply SPEC-MAKEREGISTER]
$\left\{ \begin{array}{l} \text{PromiseInv} * \text{isPromise } p * \\ \text{isRegister register} \end{array} \right\}$	
<code>perform (Suspend register);</code>	[protocol of <i>Suspend</i> with ($W := \lambda v, \lceil v = () \rceil * \text{osAssigned}$)]
$\left\{ \begin{array}{l} \text{PromiseInv} * \text{isPromise } p * \\ \text{osAssigned} \end{array} \right\}$	[open <i>PromiseInv</i> , lookup <i>p</i> using <i>isPromise p</i>]
$\left\{ \begin{array}{l} \text{PromiseInv} * \text{osAssigned} \\ * \text{PromiseState } p \gamma \Phi \end{array} \right\}$	
<code>match Atomic.get p with</code>	[CA on <i>PromiseState</i>]
2.1. $\left\{ \begin{array}{l} \text{PromiseInv} * \\ p \mapsto \text{Done result} * \Box(\Phi \text{ result}) \end{array} \right\}$	
<code>Done result -></code>	[close <i>PromiseInv</i>]
$\{ \text{PromiseInv} * \Box(\Phi \text{ result}) \}$	
result	[by assumption]
$\{ \Box(\Phi \text{ result}) \}$	
2.2. $\left\{ \begin{array}{l} \text{PromiseInv} * \text{osAssigned} * \\ p \mapsto \text{Waiting bcst} * \text{osWaiting} \end{array} \right\}$	
<code>Waiting _ -></code>	[specialize PS-CONTRA]
$\{ \text{PromiseInv} * \perp \}$	
error "impossible"	[by contradiction]
$\{ \perp \}$	

Figure 11: Annotated proof of SPEC-AWAIT.

3 Verifying Eio's Broadcast

In this section we describe the *broadcast* data structure that Eio uses to implement of *promises*. Broadcasts are a customization of the recently developed CQS data structure [6]. CQS (for CancellableQueueSynchronizer) is a lock-free synchronization primitive that allows execution contexts to wait until signalled. Its specification is already formally verified in Iris, so we were able to adapt the proofs to use them in our development. CQS keeps the nature of an execution context abstract, but it is assumed that they support stopping execution and resuming with some value. This is because CQS is designed to be used in the implementation of other synchronization constructs (e.g. mutex, barrier, promise, etc.) which take care of actually suspending and resuming execution contexts as required by their semantics.

In the case of Eio an "execution context" is an Eio fiber. CQS is multithreaded by design, so fibers can use the adapted broadcast functions to synchronize with fibers running in another thread. In the following we describe the behavior of Eio's *broadcast*, highlight differences to the *original CQS*, and explain how we adapted the verification of the original CQS for our development.

3.1 Operations of Broadcast

The original CQS supports three operations that are interesting to us: *suspend*, *resume*, and *tryCancel*. The equivalent operations in a broadcast are *register*, *signalAll*, and *tryUnregister*, respectively. While we established Eio's broadcast as an implementation of a signalling mechanism where fibers can register callbacks to be notified about events, the original formulation of CQS uses a more abstract future-based interface for the same purpose.

suspend/register In the original CQS, an execution context that wants to wait for an event performs a suspend operation. This operation creates and returns a new future that is used to stop execution because it is assumed that the language runtime supports suspending an execution context until a future is completed. But Eio uses the broadcast data structure to **build** the runtime that allows its execution contexts (fibers) to suspend until an event happens (a promise is fulfilled). So in the broadcast data structure, instead of returning a future, the register operation takes a callback as an additional argument and registers it to be called when the event happens.

resume/signalAll As a dual to suspend, a resume operation in the original CQS completes a single registered future so that the language runtime resumes the associated execution context. For broadcast, this is replaced by the signalAll operation, which invokes all callbacks that are registered with the data structure. Eio uses signalAll instead of a signal operation that only invokes one callback in order to make the implementation of promises more straightforward. When a promise is fulfilled, all fibers waiting on its value can continue execution, so the fine-grained control of a single signal operation is not needed.

tryCancel/tryUnregister The semantics of the tryUnregister operation do not markedly change from the original. A tryCancel operation can be used by an execution context to cancel the future returned by a suspend operation, so that the future is not completed by a call to resume. Analogously, tryUnregister tries to undo the registration of a callback, so that it is not invoked in a call to signalAll. The operation fails if a corresponding resume or signalAll happens first.

To understand the broadcast operations better it is helpful to view them in the context in which they are used. Like in the original CQS, an interaction with a broadcast is always guarded by first accessing an atomic variable that holds the state of the outer synchronization construct, in this case the state of the promise. Since the whole data structure is lock-free, the atomic variable ensures that the operations have a synchronized view of the state. For example, a register operation is only attempted if the promise is not fulfilled yet. Figure 12 shows the possible interactions between fibers and a promise. The calls to `Atomic.get` and `Atomic.set` happen in the functions `Promise.await` and `Promise.fulfill`, as shown in section 2.1. If the promise is not fulfilled yet, `Promise.await` then performs a *Suspend* effect and calls `Broadcast.register` and `Broadcast.try_unregister` if necessary.

Note that because it is lock-free and fibers can run on different threads, there can be a race between concurrent register, tryUnregister, and signalAll operations. Possible interleavings and the necessity of the tryUnregister were explained in section 2.1.3.

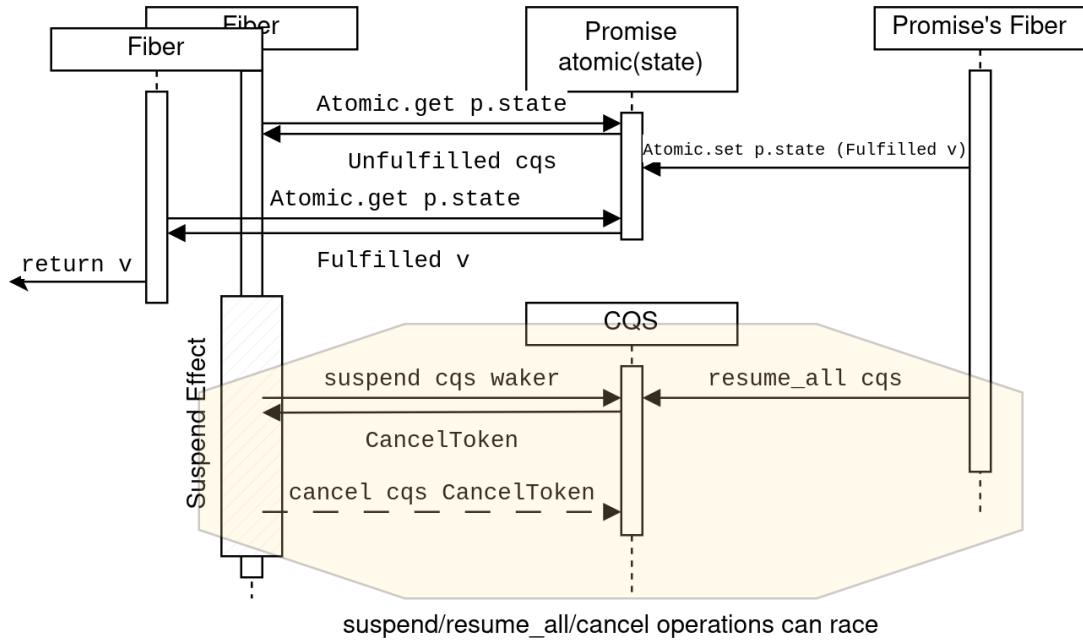


Figure 12: Usage of broadcast in the context of a promise.

3.2 Implementation and Logical Interface of Broadcast

Like the original CQS, broadcast is implemented as a linked list of arrays (called segments) that contain *cells*⁶. There are two pointers pointing to the beginning and end of the active cell range, the signal pointer and the register pointer, and cells not reachable from either pointer are garbage collected. There is a set of operations for manipulating the linked list and pointers to implement the higher-level functionality, but they are not part of the public API, so we do not focus on them. Each cell is a container for one callback and the logical state of the broadcast tracks the current state of all existing cells. The possible states for a single cell are shown in figure 13, where the arrows are annotated with the operation that causes a state transition.

The state of a cell is initialized to **EMPTY** when it is reached by the register pointer⁷. When a register and signalAll operation happen concurrently, they race to set the value of the empty cell. If the signalAll operation wins, it writes a token value into the cell and the state becomes **SIGNALLED**. The register operation can then read the token and invoke its callback directly. The state is thus **INVOKED**. If instead the register operation wins the race, it writes the callback into the cell, so the state takes the right path to **CALLBACK_{waiting}**. Then there can be another race between concurrent tryUnregister and signalAll operations. Both try to overwrite the callback with a token value, which changes the state to **CALLBACK_{invoked}** or **CALLBACK_{unregistered}**, respectively, depending on the winner.

3.3 Verification of Broadcast

In the following we describe the specifications we proved for the functions implemented in Eio's Broadcast module. Note that all specifications obey the empty protocol because the code does not perform any effects. For all three operations, the Eio implementation and specification differs from what is already verified in the original CQS (e.g. due to some reordered instructions or a different control flow). However, the specifications of the underlying operations for manipulating cell pointers are modular enough to allow us to prove the new specifications for Broadcast.create, Broadcast.register, and Broadcast.try_unregister.

As for Broadcast.signal_all, Eio implements this function by atomically increasing the signal pointer by the number n of registered callbacks and then processing all n cells between the old and new pointer position. Because of technical differences in handling these pointers between the original CQS implemen-

⁶Using segments instead of single cells in the linked list is an optimization to amortize the linear runtime of linked list operations

⁷As opposed to the original CQS, in broadcast the signal pointer never overtakes the register pointer.

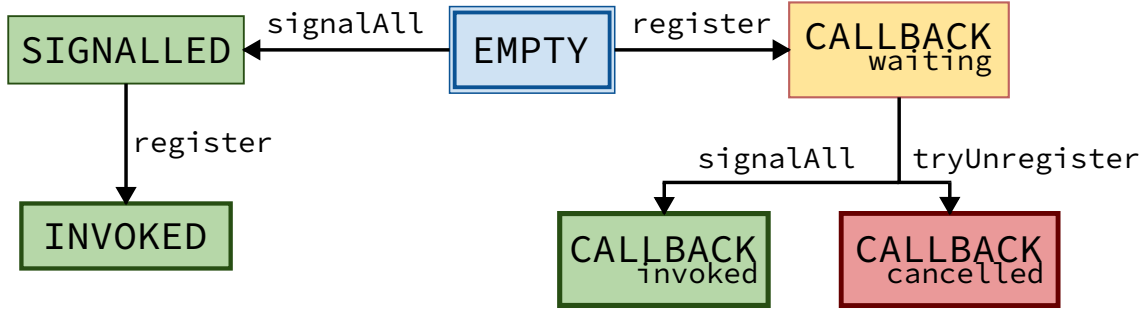


Figure 13: State transition diagram for a single cell.

tation of the paper [6] and the broadcast implementation of Eio we opted to verify a different implementation of `Broadcast.signal_all`, that increments the signal pointer n times in a loop. We argue this does not change the observable behaviors of the function since we ensure that it can only be called once.

3.3.1 Broadcast.create

The only precondition to create a new broadcast is the proposition inv_heap_inv . This is a piece of ghost state defined by the Iris standard library that models invariant locations, which are locations that can always be read. That means they cannot be explicitly deallocated and can only exist in a garbage-collected setting, like OCaml 5. The implementation of the linked list uses this internally.

The function returns a broadcast instance $bcst$, along with the persistent $isBroadcast\ bcst$ proposition that shows the value actually is a broadcast. We also obtain the unique resource $signalAllPermit$, which is held by the enclosing promise and allows calling the `Broadcast.signal_all` function once.

$$\frac{\text{SPEC-BROADCASTCREATE} \quad inv_heap_inv}{ewp\ (create\ ())\ \langle \perp \rangle\ \{bcst,\ isBroadcast\ bcst * signalAllPermit\}}$$

3.3.2 Broadcast.register

A register operation takes a callback cb and the associated resource $isCallback\ cb\ R$ which represents the permission to invoke the callback. We instantiate R with $osAssigned$ so that the callback transports the knowledge that the promise has been fulfilled. $isCallback$ is not persistent because the callback must be invoked only once.

$$\begin{aligned} isCallback\ cb\ R &\triangleq R * ewp\ (cb\ ())\ \langle \perp \rangle\ \{\top\} \\ isBroadcastRegisterResult\ r\ cb\ R &\triangleq (\ulcorner r = Invoked \urcorner) \\ &\quad \vee (\ulcorner r = Registered\ h^\top * isBroadcastRegisterHandle\ h\ cb\ R \urcorner) \\ isBroadcastRegisterHandle &: Val \rightarrow Val \rightarrow iProp \rightarrow iProp \end{aligned}$$

The `Broadcast.register` function tries to insert a callback into the next cell designated by the register pointer. If it succeeds the function returns a `Registered handle` value that can be used by `Broadcast.try_unregister`. But if the cell is already in the **SIGNALLED** state, the function immediately invokes the callback and returns a `Invoked` value.

$$\frac{\text{SPEC-BROADCASTREGISTER} \quad isBroadcast\ bcst * isCallback\ callback\ R}{ewp\ (register\ bcst\ callback)\ \langle \perp \rangle\ \{r,\ isBroadcastRegisterResult\ r\ callback\ R\}}$$

3.3.3 Broadcast.try_unregister

Given a handle and its $isBroadcastRegisterHandle\ h\ cb\ R$ resource, `Broadcast.try_unregister` tries to cancel the registration of the callback.

If the callback had already been invoked by `Broadcast.signal_all` (i.e. the state is `CALLBACKinvoked`) the function returns `false` and no resources are returned to the caller. Otherwise, the permission to invoke the callback `isCallback cb` is returned.

$$\frac{\text{SPEC-BROADCASTTRYCANCEL} \quad \text{isBroadcastRegisterHandle } h \text{ } cb \text{ } R}{\text{ewp } (\text{try_unregister } h) \langle \perp \rangle \{b, \text{ if } b \text{ then } \text{isCallback } cb \text{ } R \text{ else } \top\}}$$

3.3.4 Broadcast.signal_all

To call `Broadcast.signal_all` the unique `signalAllPermit` resource is needed, along with a duplicable R , so that it can be used to invoke multiple callbacks. The function does not return any resources because its only effect is making an unknown number of fibers resume execution, which we cannot easily formalize in Iris.

$$\frac{\text{SPEC-BROADCASTSIGNALALL} \quad \text{isBroadcast } bcst * \Box R * \text{signalAllPermit}}{\text{ewp } (\text{signalAll } bcst) \langle \perp \rangle \{\top\}}$$

3.4 Changes from the Original CQS

The original CQS supports multiple additional features like a synchronous mode for suspend and resume, and also a smart cancellation mode. These features enlarge the state space of CQS and complicate the verification but are not used in Eio so when we ported the verification of CQS to our Eio development we removed support for these features. This reduced the state space of a cell shown in figure 14 to a more manageable size when adapting the proofs.

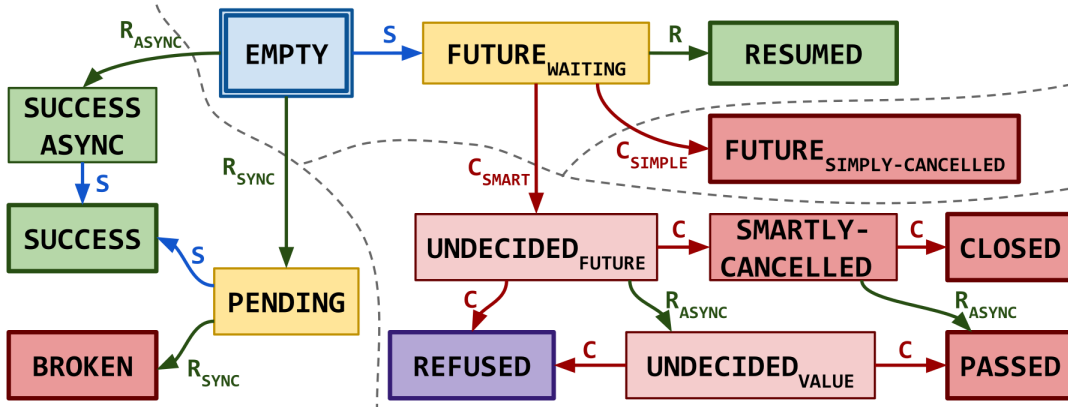


Figure 14: Cell states in the original CQS from [6] (page 42).

The part of the verification of the original CQS that we had to customize for Eio was originally 3600 lines of Coq code but – due to these simplifications – we could reduce it by approximately 1300 lines of Coq code. Additionally, there are 4000 lines of Coq code about lower-level functionality that we did not need to adapt when porting them to our development.

4 Adding Support for Multiple Schedulers

So far we have always considered the possibility of schedulers running in multiple threads when explaining design choices of Eio. These additional schedulers are created using Eio's *domain manager* and in this section we discuss how we integrate the domain manager into our model. It exposes a function `Domain_manager.new_scheduler` (shown in figure 15) which, given some function `f`, forks a new thread, runs a scheduler with `f` as its main fiber and returns the final result of `f`.

4.1 Implementation

To interact with threads⁸, the function uses the standard `thread_fork` and `thread_join` functions exposed by many thread implementations, which fulfill the specifications below.

$$\begin{array}{c}
 \text{THREAD-FORK} \\
 \frac{ewp (f ()) \langle \perp \rangle \{v, Q v\}}{ewp (\text{thread_fork } f) \langle \perp \rangle \{j, \text{joinHandle } j\} Q}
 \end{array}
 \qquad
 \begin{array}{c}
 \text{THREAD-JOIN} \\
 \frac{\text{joinHandle } j\ Q}{ewp (\text{thread_join } j) \langle \perp \rangle \{v, Q v\}}
 \end{array}$$

We implemented threads for the operational semantics of Hazel and proved the specifications for these functions as described in appendix B. This pair of functions is analogous to `Fiber.fork_promise` and `Promise.await` but on the level of threads. The difference is that `thread_join` is considered *blocking* in the sense that the calling thread will not continue execution until the thread associated with the `joinHandle` has terminated.

```

1  let new_scheduler f =
2    let handle = ref None in
3    let register = (fun waker ->
4      let thread_fun = (fun () ->
5        let result = run f in
6        waker ();
7        result
8      ) in
9      let join_handle = thread_fork thread_fun in
10     handle := Some join_handle
11   ) in
12   suspend register;
13   match !handle with
14   | None -> error "impossible"
15   | Some join_handle -> thread_join join_handle

```

Figure 15: Implementation of `Domain_manager.new_scheduler`.

The main complexity of the implementation of `Domain_manager.new_scheduler` comes from avoiding this blocking behavior. As this function is called by fibers, blocking the current thread would prevent the scheduler of the current thread from switching to another fiber. This situation must be avoided and is a great source of complexity when calling blocking operations in a user-level concurrency context.

`Domain_manager.new_scheduler` solves this by suspending the calling fiber (line 12) until the new thread is terminating. This is done by calling the `waker` function at the end of `thread_fun` (line 6) which is forked inside the `register` function (line 9) of the *Suspend* effect. The resulting join handle is saved in a reference (line 10) to be accessed later. By the time the original fiber continues execution, the new thread will have terminated, so it extracts the join handle from the reference and retrieves the thread's final value (line 15) without blocking.

⁸OCaml 5 uses the term *domain* but we use the standard thread terminology for shared-memory execution contexts running in parallel.

4.2 Specification and Changes to Logical State

Because the function essentially delegates to `Scheduler.run`, it has the same type⁹ and we were able to prove an analogous spec as shown below.

$$\frac{\text{SPEC-NEWSCHEDULER} \quad \text{isPromise} * \text{ewp} (f \ ()) \langle \text{Coop}_2 \rangle \{v. \Box \Phi v\}}{\text{ewp} (\text{new_scheduler } f) \langle \text{Coop}_2 \rangle \{v. \Box \Phi v\}}$$

However, we need to update several definitions to make this proof possible. One of them is the specification of the *Suspend* effect, which is why we now say Coop_2 . The match in line 13 is only safe because the reference is assigned a join handle in the register function which runs to completion before the effect returns. We track the status of the reference by reusing the *OneShotAssign* ghost-state from figure 8. By performing the *Suspend* effect we want to receive $\text{osAssigned } \gamma_{\text{handle}}$, where γ_{handle} is specific to the reference. Consequently, we update the protocol and its related definitions (shown in figure 16) so that *Suspend* additionally returns a persistent resource¹⁰ S that results from calling the `register` function.

$$\begin{aligned} \text{isWaker } wkr \ W &\triangleq \forall v. W \ v \multimap \text{ewp} (wkr \ v) \langle \perp \rangle \{ \top \} \\ \text{isRegister}_2 \ \text{reg} \ W \ S &\triangleq \forall wkr. \text{isWaker } wkr \ W \multimap \text{ewp} (\text{reg } wkr) \langle \perp \rangle \{ \Box S \} \\ \text{Coop}_2 &\triangleq \text{Fork } \# ! e \ (e) \{ \triangleright \text{ewp} (e \ ()) \langle \text{Coop}_1 \rangle \{ \top \} \} .? \ () \{ \top \} \\ \text{Suspend } \# ! \text{reg } W \ S \ (\text{reg}) \ \{ \text{isRegister}_2 \ \text{reg } W \ S \} .? \ y \ (y) \ \{ W \ y * S \} \end{aligned}$$

Figure 16: Definition of Coop_2 protocol with *Fork* & *Suspend* effects.

As a result of changing the effect postcondition, the continuation k of *Suspend* that the effect handler receives now also has S as a precondition.

$$\forall v. W \ v \multimap S \multimap \text{ewp} (k \ ()) \langle \perp \rangle \{ \top \}$$

Recall that the waker function receives $W \ v$ and pushes k into the scheduler's run queue, where the queue invariant says that k must be callable as-is. Since *waker* is called from a different thread – and might even be called before the `register` function finishes – it cannot supply the S . Therefore, when k is pushed into the queue it is still missing the S to satisfy the queue invariant, so we must change the specification of the run queue to allow pushing elements that temporarily do not satisfy the queue invariant.

4.3 Specification for a Deferred Queue

We call such a queue a *deferred queue*, because the queue invariant can temporarily be violated but must be repaired eventually. We proved a suitable specification for a standard implementation of a multi-producer, single-consumer (or *mpsc*) queue. An *mpsc* queue has different resources for pushing and popping, the push resource is persistent and can be shared with multiple threads, while the pop resource is unique. The specification of our deferred queue is shown in figure 17.

isQueue is the invariant containing the state of the queue and is therefore persistent. *isQueueReader* is the same as *isQueue* with an additional token to make it unique and represents the pop permission. Using `SPEC-DQUEUEREGISTER` for some S , the *isQueueReader* can be exchanged for an affine *fulfillPermission* S and a persistent *pushPermission* $\gamma \ S$. The latter allows pushing elements that are missing an S to fulfill the queue invariant $I \ v$ according to `SPEC-DQUEUEPUSH`. We do this by internally converting the whole queue invariant to the predicate $I'v \triangleq S \multimap I \ v$. Elements already in the queue, satisfying $I \ v$, can be trivially converted to this form by ignoring the S and new elements inserted by `SPEC-DQUEUEPUSH` satisfy I' by definition. Since every element is now missing an S we can use `SPEC-DQUEUEFULFILL` with $\Box S$ to restore the original invariant and get back the *isQueueReader* by supplying each element with one copy of S . As a result, the pop operation has a standard specification `SPEC-DQUEUEPOP`, if it returns an element v it will always satisfy $I \ v$.

⁹(unit -> 'a) -> 'a option

¹⁰We think it is possible to formulate the protocol with an arbitrary resource, but it would complicate the construction of the deferred queue that follows. For our purpose of proving `SPEC-NEWSCHEDULER` the persistent S is enough.

SPEC-DQUEUECREATE	SPEC-DQUEUEREGISTER
$\frac{}{ewp \text{ (queue_create ()) } \langle \perp \rangle \{q. \forall I. \models isQueueReader \ q \ I\} \models isQueue \ q \ I * fulfillPermission \ S * \exists \gamma. pushPermission \ \gamma \ S}$	$\frac{isQueueReader \ q \ I}{\models isQueue \ q \ I * fulfillPermission \ S * \exists \gamma. pushPermission \ \gamma \ S}$
SPEC-DQUEUEFULFILL	SPEC-DQUEUEPUSH
$\frac{isQueue \ q \ I * fulfillPermission \ S * \Box S}{\models isQueueReader \ q \ I}$	$\frac{isQueue \ q \ I * pushPermission \ \gamma \ S * \triangleright (S \multimap I \ v)}{ewp \text{ (queue_push \ q \ v) } \langle \perp \rangle \{T\}}$
SPEC-DQUEUEPOP	
$\frac{isQueueReader \ q \ I}{ewp \text{ (queue_pop \ q) } \langle \perp \rangle \{v'. isQueueReader \ q \ I * (\ulcorner v' = None \urcorner \vee \exists v. \ulcorner v' = Some \ v \urcorner * I \ v)\}}$	

Figure 17: Specification of a deferred queue.

4.4 Integrating the Deferred Queue into the Scheduler

Since our deferred queue reuses the code from the Queue module, we do not need to update the source code of `Scheduler.run`. But we must amend the proof of SPEC-RUN, namely the case for handling the *Suspend* effect, shown below because the queue specifications changed.

```

1  match fiber () with
2  ...
3  | effect (Suspend register) k =>
4    let waker = fun v -> Queue.push run_queue (fun () -> invoke k v) in
5    register waker;
6    next ()

```

First, do to a pop operation, the execute function now needs the unique *isQueueReader* resource. Since we call execute recursively for each fiber, we must pass this resource to each fiber continuation when running it. The queue invariant therefore becomes recursive, where *isQueueReader* is passed into and out of every continuation in the queue.

$$Ready_2 \ q \ f \triangleq \triangleright isQueueReader \ q \ (Ready_2 \ q) \multimap ewp \ (f \ ()) \langle \perp \rangle \{\triangleright isQueueReader \ q \ (Ready_2 \ q)\}$$

Before constructing the waker function we must now use SPEC-DQUEUEREGISTER to temporarily change the queue invariant to $\lambda k. S \multimap Ready_2 \ q \ k$ and obtain a *pushPermission* $\gamma \ S$. Using this resource we can then prove that waker still satisfies *isWaker*. After calling the `register` function we obtain the resource *S* and can use SPEC-DQUEUEFULFILL to restore the queue invariant and receive the *isQueueReader* resource. This resource is then passed to `next` to pop a *Ready₂* continuation from the queue and is then passed to the continuation itself.

To summarize, using a non-standard *deferred* queue specification we were able to strengthen the specification of the *Suspend* protocol. This was needed to prove the specification of Eio's domain manager because it relies on pushing unsafe functions to the scheduler's run queue that become safe to execute by the time the scheduler attempts to pop the next element from the queue. Our deferred queue specification works generically for an mpsc queue without changing its code, and we conjecture that a stronger specification with a non-persistent *S* is provable, but unnecessary in our case.

5 Adding Support for Thread-Local Variables

So far we have looked at a protocol $Coop_2$ that has two effects which suffice to model fibers that can suspend and fork off new fibers. But fibers in Eio can use an additional effect called *GetContext* that we discuss in this section. For each fiber the scheduler keeps track of context metadata, one part of which are *thread-local variables*. Thread-local variables are state that is shared between all fibers of one scheduler (hence thread-local) and a fiber gets access to them via the *GetContext* effect.

Since all fibers of one scheduler execute concurrently on one system-level thread, they have exclusive access to the thread-local variables while they are running. This allows a practical form of shared state without the overhead of synchronization primitives of multithreaded data structures. Two example use-cases are per-scheduler tracing of events, where all fibers of one scheduler write to a common log, and inter-fiber message passing, where fibers use a simple queue to exchange messages. Of course, this comes with the restriction that it is only usable for fibers running in the same thread.

In Eio thread-local variables are represented by a dictionary from variable names to arbitrary values and expose an intended API that only allows adding new entries. However, it is still possible for fibers to arbitrarily modify the whole dictionary, so for demonstration purposes we model thread-local variables as a single mutable reference that is part of the context record: `ctx.tlv`. Properties we want to prove about thread-local variables are:

1. Each time a fiber performs a *GetContext* effect it receives the same reference.
2. As long as a fiber does not perform other effects like *Fork* or *Suspend*, it holds exclusive ownership of the reference.

Code examples illustrating the properties are shown in figure 18. Note that these are only the most basic properties showing that `ctx.tlv` acts like a normal reference, but one that can be accessed via an effect. To enable modular proofs of concrete fibers using thread-local variables, we include in our logical definition a predicate T on the stored value that can be instantiated by fibers as needed.

```

1  let fiber1 () =
2    let ctx = perform (GetContext ()) in
3    let ctx2 = perform (GetContext ()) in
4    assert (ctx.tlv == ctx2.tlv)
5
6  let fiber2 () =
7    let ctx = perform (GetContext ()) in
8    let v = !ctx.tlv in
9    (* some computation that does not perform Fork/Suspend *)
10   ...
11  assert (!ctx.tlv == v)

```

Figure 18: Constructed example of safety for thread-local variables.

5.1 Changes to Logical State

To handle thread-local variables in our development we must change both the implementation and logical definitions. The necessary changes to the implementation are trivial, so we just refer to the mechanization¹¹. The new definitions are described in figure 19. $tlvAg \ \delta \ tlv$ is used to show the uniqueness of the location tlv . $isFiberContext \ \delta \ tlv$ represents the context that is tracked for each fiber, where δ is a shorthand for multiple ghost names. It expresses that the location tlv is a thread-local variable which maps to some value v satisfying T . The predicate T is hidden behind a *savedPred* indirection to make the mechanization easier. $fiberResources \ \delta$ is then used to abstract away the concrete location tlv . This predicate represents all resources that a fiber owns while it is running, so each fiber specification now has this as a precondition. Finally, we must change the definition of *Ready* to require $fiberResources$ as a precondition because it is needed to invoke the continuations saved in the scheduler's run-queue.

The effect protocols of *Fork* and *Suspend* are amended so that they pass $fiberResources$ from a fiber to the scheduler and from there to the next running fiber via the protocol pre- and postconditions as shown

¹¹TODO insert link

$$\begin{aligned}
tlvAg \ \delta \ tlv &\triangleq [\overline{agree}(tlv)]^\delta \quad \text{Persistent}(tlvAg \ \delta \ tlv) \\
isFiberContext \ \delta \ tlv &\triangleq tlvAg \ \delta \ tlv * \exists T \ v. \ tlv \mapsto v * savedPred \ \delta \ T * T \ v \\
fiberResources \ \delta &\triangleq \exists tlv. isFiberContext \ \delta \ tlv \\
Ready \ \delta \ f &\triangleq fiberResources \ \delta \ \multimap ewp \ (f \ ()) \ \langle \perp \rangle \ \{\top\}
\end{aligned}$$

Figure 19: Logical state definitions for the verification of our Eio model.

in figure 20. The *Fork* effect now also passes the concrete reference that should be used as the thread-local variable of the new fiber. A fiber uses the *GetContext* effect to receive the fiber context value and a copy of $tlvAg$. This is used to show that the reference $ctx.tlv$ is equal to the one from $fiberResources$ that the fiber already owns so that the contained points-to predicate can be used.

The crux is that now the protocol *Coop* is parameterized by the ghost name δ that identifies the thread-local variable. This so that both the fiber and the scheduler agree on this ghost name.

$$\begin{aligned}
Coop \ \delta &\triangleq \quad Fork \ \# \ ! \ tlv \ e \ ((tlv, e)) \ \{ fiberResources \ \delta \ T * tlvAg \ \delta \ tlv * \\
&\quad \triangleright (fiberResources \ \delta \ T * ewp \ (e) \ \langle Coop \rangle \ \{ fiberResources \ \delta \ T \}) \} \\
&\quad ? \ () \ \{ fiberResources \ \delta \ T \} \\
&\quad Suspend \ \# \ ! \ reg \ W \ (reg) \ \{ fiberResources \ \delta \ T * isRegister \ reg \ W \}. \\
&\quad ? \ y \ (y) \ \{ fiberResources \ \delta \ T * W \ y \} \\
&\quad GetContext \ \# \ ! \ () \ \{ \top \}. \ ? \ ctx \ (ctx) \ \{ tlvAg \ \delta \ ctx.tlv \}
\end{aligned}$$

Figure 20: Definition of extended *Coop* protocol with *Fork*, *Suspend*, and *GetContext* effects.

These changes suffice to prove the safety of the two examples in figure 18.

6 Evaluation

We evaluate our model of Eio on a simple example program that uses all features supported by our implementation. The example program (shown in figure 21) may look contrived since it does not do any “useful” computation, but the value of Eio as a library comes from composing computations – not in what is computed concretely.

The program’s `main_fiber` function forks off a new fiber dispatch (line 23) and communicates with it over a one-element channel represented by the thread-local variable. The channel is initially empty (first argument to `Scheduler.run` in line 29) and dispatch polls for data (line 15). `main_fiber` sends one integer data (lines 11,25) to dispatch which will then run two copies of (`work data`) (line 16) in separate threads, and sum their results. The `work` function simulates time passing using the `yield` function (line 5) and returns its first argument. `Yield` performs a *Suspend* effect but calls the `waker` function immediately, which has the effect of placing the current fiber at the back of the scheduler’s run queue to give other fibers a chance to run.

The example program therefore uses the basic functions for forking and awaiting the completion of fibers, multiple schedulers running in different threads, as well as thread-local variables to communicate between fibers within one thread.

```

1  let yield () =
2    perform (Suspend (fun waker -> waker ()))
3
4  let work x () =
5    yield ();
6    x
7
8  let rec wait_for_read tlv =
9    match !tlv with
10   | None -> yield (); wait_for_read tlv
11   | Some data -> tlv <- None; data
12
13  let dispatch () =
14    let tlv = get_context ().tlv in
15    let data = wait_for_data tlv in
16    let p1 = Fiber.fork_promise (Domain_manager.run (work data)) in
17    let p2 = Fiber.fork_promise (Domain_manager.run (work data)) in
18    let r1 = Promise.await p1 in
19    let r2 = Promise.await p2 in
20    r1 + r2
21
22  let main_fiber data () =
23    let p = Fiber.fork_promise dispatch in
24    let tlv = get_context ().tlv in
25    tlv <- Some data
26    Promise.await p
27
28  let main () =
29    Scheduler.run None (main_fiber 21)

```

Figure 21: Example program to use all implemented features.

We first give the final specifications of the most important components of our model library in figure 22. The specifications contain both extensions we discussed in sections 4 and 5.

Using these specifications we proved the safety of the example program and its functional correctness by establishing specifications for each function as shown in figure 23. We can see that there is some amount of boilerplate (colored in blue). Each function that yields execution to another fiber by performing an effect – either directly or indirectly through another function call – needs *fiberResources* $l_{tlv} \Omega$, which signifies the ownership over the thread-local variable. Additionally, any fiber that wants to fork off another fiber using `Fiber.fork_promise` needs the persistent *PromiseInv* resource to interact with the global collection of promises. The predicate $\Omega_{chan} \gamma$ as part of *fiberResources* $l_{tlv} (\Omega_{chan} \gamma)$ restricts the thread-local variable l_{tlv} to be a channel for a single message n .

While we proved the safety of this program (and of the core abstractions of the Eio library), the complete Eio library has more features that are still unexplored. This includes cancellation of fibers, resource

$$\begin{aligned}
& \text{Ready } l \ \Omega \ \gamma \ q \triangleq \text{fiberResources } l \ \Omega \multimap \\
& \quad \triangleright \text{isQueueReader } q \ (\text{Ready } l \ \Omega \ \gamma \ q) \multimap \\
& \quad \text{ewp } (k \ ()) \langle \perp \rangle \{ _ . \text{fiberResources } l \ \Omega \multimap \triangleright \text{isQueueReader } q \ (\text{Ready } l \ \Omega \ \gamma \ q) \ast \text{osAssigned } \gamma \} \\
& \text{isWaker } wkr \ W \triangleq \forall v. W \ v \multimap \text{ewp } (wkr \ v) \langle \perp \rangle \{ \top \} \\
& \text{isRegister } reg \ W \ S \triangleq \forall wkr. \text{isWaker } wkr \ W \multimap \text{ewp } (reg \ wkr) \langle \perp \rangle \{ \square S \} \\
& \text{Coop } l \ \Omega \triangleq \text{Fork } \# ! \ e \ ((l, e)) \{ \text{fiberResources } l \ \Omega \ast \\
& \quad \triangleright (\text{fiberResources } l \ \Omega \multimap \text{ewp } (e \ ()) \langle \text{Coop } l \ \Omega \rangle \{ \text{fiberResources } l \ \Omega \}) \} \\
& \quad ? \ () \{ \text{fiberResources } l \ \Omega \} \\
& \text{Suspend } \# ! \ reg \ W \ S \ (reg) \{ \text{fiberResources } l \ \Omega \ast \text{isRegister } reg \ W \ S \}. \\
& \quad ? \ v \ (v) \{ \text{fiberResources } l \ \Omega \ast W \ v \ast S \} \\
& \text{GetContext } \# ! \ () \{ \top \}. ? \ (l) \{ \top \} \\
\\
& \text{SPEC-RUN} \\
& \quad \frac{\Omega \text{ init } \ast \quad \forall l_{lv}. \text{fiberResources } l_{lv} \ \Omega \multimap \text{ewp } (\text{main } ()) \langle \text{Coop } l_{lv} \ \Omega \rangle \{ v. \square \Phi \ v \ast \text{fiberResources } l_{lv} \ \Omega \}}{\text{ewp } (\text{run init main}) \langle \perp \rangle \{ v. \square \Phi \ v \ast \text{fiberResources } l_{lv} \ \Omega \}} \\
\\
& \text{SPEC-FORKPROMISE} \\
& \quad \frac{\text{PromiseInv } \ast \text{fiberResources } l_{lv} \ \Omega \ast \quad \text{fiberResources } l_{lv} \ \Omega \multimap \text{ewp } (f \ ()) \langle \text{Coop } l_{lv} \ \Omega \rangle \{ v. \square \Phi \ v \ast \text{fiberResources } l_{lv} \ \Omega \}}{\text{ewp } (\text{fork_promise } f) \langle \text{Coop } l_{lv} \ \Omega \rangle \{ p. \text{isPromise } p \ \Phi \ast \text{fiberResources } l_{lv} \ \Omega \}} \\
\\
& \text{SPEC-AWAIT} \\
& \quad \frac{\text{PromiseInv } \ast \text{fiberResources } l_{lv} \ \Omega \ast \text{isPromise } p \ \Phi}{\text{ewp } (\text{await } p) \langle \text{Coop } l_{lv} \ \Omega \rangle \{ p. \text{isPromise } p \ \Phi \ast \text{fiberResources } l_{lv} \ \Omega \}} \\
\\
& \text{SPEC-NEWSCHEDULER} \\
& \quad \frac{\Omega' \text{ init } \ast \quad \forall l'_{lv}. \text{fiberResources } l'_{lv} \ \Omega' \multimap \text{ewp } (\text{main } ()) \langle \text{Coop } l'_{lv} \ \Omega' \rangle \{ v. \square \Phi \ v \ast \text{fiberResources } l'_{lv} \ \Omega' \}}{\text{ewp } (\text{new_scheduler init main}) \langle \text{Coop } l \ \Omega \rangle \{ v. \square \Phi \ v \ast \text{fiberResources } l \ \Omega \}}
\end{aligned}$$

Figure 22: Specification of the public interface of the Eio library model.

management using switches and several operating system primitives like timers, so we cannot make any statements about programs using these features. Nevertheless, our model is an important step in the direction of proving the safety of Eio and programs that use it. Iris along with its features like ghost state and shareable invariants to reason about multithreaded and stateful code were key in this development.

$$\Omega_{chan} \gamma v \triangleq \begin{array}{l} \lceil v = None \rceil \\ \vee \exists n. \lceil v = Some\ n \rceil * [\overline{\overline{\overline{ag}(n)}}]^Y \end{array}$$

SPEC-WORK

$$\frac{\textcolor{blue}{fiberResources}\ l_{lv}\ \Omega}{ewp\ (\text{work}\ n\ ())\ \langle Coop \rangle\ \{v. \lceil v = n \rceil * \textcolor{blue}{fiberResources}\ l_{lv}\ \Omega\}}$$

SPEC-WAITFORDATA

$$\frac{\textcolor{blue}{fiberResources}\ l_{lv}\ (\Omega_{chan}\ \gamma)}{ewp\ (\text{wait_for_data}\ \perp)\ \langle Coop \rangle\ \{v. \exists n. \lceil v = n \rceil * [\overline{\overline{\overline{ag}(n)}}]^Y * \textcolor{blue}{fiberResources}\ l_{lv}\ (\Omega_{chan}\ \gamma)\}}$$

SPEC-DISPATCH

$$\frac{\textcolor{blue}{PromiseInv} * \textcolor{blue}{fiberResources}\ l_{lv}\ (\Omega_{chan}\ \gamma)}{ewp\ (\text{dispatch}\ ())\ \langle Coop \rangle\ \{v. \exists n. \lceil v' = n + n \rceil * [\overline{\overline{\overline{ag}(n)}}]^Y * \textcolor{blue}{fiberResources}\ l_{lv}\ (\Omega_{chan}\ \gamma)\}}$$

SPEC-MAINFIBER

$$\frac{\textcolor{blue}{PromiseInv} * \textcolor{blue}{fiberResources}\ l_{lv}\ (\Omega_{chan}\ \gamma) * [\overline{\overline{\overline{ag}(n)}}]^Y}{ewp\ (\text{main_fiber}\ n\ ())\ \langle Coop \rangle\ \{v. \lceil v = n + n \rceil * \textcolor{blue}{fiberResources}\ l_{lv}\ (\Omega_{chan}\ \gamma)\}}$$

SPEC-MAIN

$$\frac{}{ewp\ (\text{main}\ ())\ \langle \perp \rangle\ \{v. \lceil v = 42 \rceil\}}$$

Figure 23: Specification of the example program.

7 Conclusion

7.1 Related Work

Concurrency With Effects There are other approaches to implementing cooperative concurrency with effects even within OCaml 5. One example is the Picos framework [8], an interoperability framework that defines a small set of data types and effects that can be reused by other cooperative concurrency libraries (such as Eio) in order to speak a common protocol and be mutually interoperable. Picos defines *computations* and *fibers*, which are mostly equivalent, respectively, to Eio’s promises and fibers. The main difference is the *trigger* concept, which in Eio’s terms can be thought of as a mutable reference to an optional waker function. The workflow to await a future result (i.e. a Picos computation) is to first attach an empty trigger to the computation and then perform an *Await* effect. The effect handler (implemented by a library such as Eio) must then create a waker function and assign it to the trigger. When the computation finishes it will signal the trigger, which calls the waker function and consequently places the original fiber in the scheduler’s run queue.

While the *Await* effect carrying a trigger is technically first-order – as opposed to Eio’s higher-order *Suspend* effect carrying a *register* function – a trigger still contains higher-order state. So it is unclear to us whether a specification for the Picos primitives would be any simpler to prove or easier to use than the specification for Eio primitives we have presented so far.

mention re-
semblance
to Landin’s
Knot?

Session Types as Effect Specifications Protocols in Hazel take some inspiration from session types but with the restriction that a protocol is always an infinite repetition of a single step, whereas session types usually allow defining a sequence of different steps. Current work by Tang [9] explores the connection between session types and effect protocols further and defines a lambda calculus $\lambda_{\text{eff}}^{\boxtimes}$ that uses a standard session type formalization for its effect system. This allows a programmer to define multistep protocols and even bidirectional effects where the handler and client swap roles. However, for our purposes Hazel is completely sufficient since multistep protocols can be simulated by Hazel’s protocols and bidirectional effects are not possible in OCaml 5 to begin with.

7.2 Future Work

The work we presented so far suffices to prove the safety of programs that use a small subset of the full functionality provided by Eio. To improve the usefulness of our model and be applicable to more programs it would be desirable to incorporate more features into our model of Eio in future work, such as switches and support for cancelling fibers. While switches are mainly used for a hierarchical organization of fibers and to efficiently clean up fiber resources, cancellation poses some interesting safety questions because there are situations that must be avoided, such as being able to cancel a fiber twice.

Instead of growing the model of Eio it would also be interesting to extend the existing specifications. Mainly, we would be interested in proving that a scheduler will never “forget fibers”. Since weakest preconditions in Iris do not prove termination our specifications have the unfortunate drawback of being fulfilled by functions that diverge. Because a scheduler explicitly handles fiber continuations it would be possible to accidentally drop a continuation which has the effect of making the fiber diverge, as well as any other fiber that awaits its result.

While we cannot solve the whole termination problem (since deadlocks are possible), intuitively we should be able to track the state of each fiber to ensure that when a fiber is captured in a continuation, the continuation is used linearly, which means that it is explicitly invoked or discarded at some point. This also extends to data structures that contain continuations like the scheduler’s run queue and a broadcast, as they must never drop the contained continuations. To track the linear usage of continuations it could be helpful to draw inspiration from Iron [1], a separation logic built on Iris to enable reasoning about linear resources.

7.3 Results

In this thesis we have proven specifications for a subset of the Eio library, including a common denominator scheduler that controls fibers which can await the completion of promises in a multithreaded setting. We have also defined and verified general and reusable protocols for the main three effects of Eio: *Fork*, *Suspend*, and *GetContext*. We showed that the function specifications and the effect protocols are enough

to verify the safety (including effect safety) of an example program that uses all of our modelled features. Additionally, we have verified specifications for two nontrivial data structures used by Eio. For the broadcast data structure we adapted the existing proof of CQS by Koval et al. [6] and for the scheduler's run queue we proved a – to our knowledge novel – specification for a multi-producer single-consumer queue with a temporarily suspendable invariant. Finally, we have extended the original Hazel language with multithreading primitives and amended the adequacy result which shows that we can use this language to reason about programs that use both multithreading and effect handlers.

Appendix

A Translation Table

Eio	Thesis	Mechanization
enqueue	waker function	waker
f	register function	register
Fiber.fork_promise	Fiber.fork_promise	fork_promise
Promise.await	Promise.await	await
Sched.run	Scheduler.run	run

B Towards A multithreaded Scheduler

OCaml 5 added not only effect handlers but also the ability to use multiple threads of execution, which are called *domains* (in the following we use the terms interchangeably). Each domain in OCaml 5 corresponds to one system-level thread and the usual rules of multithreaded execution apply, i.e. domains are preemptively scheduled and can share memory. Eio defines an operation to make use of multi-threading by forking off a new thread and running a separate scheduler in it. So while each Eio scheduler is only responsible for fibers in a single thread, fibers can await and communicate with fibers running in other threads.

In order for a fiber to be able to await fibers in another thread, the `wakers_queue` [note it will be in the Simple Scheduler section] from above is actually a thread-safe queue based on something called CQS, which we will discuss in detail in a later section.

Heaplang supports reasoning about multithreaded programs by implementing fork and join operations for threads and defining atomic steps in the operational semantics, which enables the use of Iris *invariants*. In contrast, Hazel did not define any multithreaded operational semantics but it contained most of the building blocks for using invariants. In the following we explain how we added a multithreaded operational semantics and enabled the use of invariants.

Adding Invariants to Hazel

Invariants in Iris are used to share resources between threads. They encapsulate a resource to be shared and can be opened for a single atomic step of execution. During this step the resource can be taken out of the invariant and used in the proof but at the end of the step the invariant must be restored.

Hazel did already have the basic elements necessary to support using invariants. It defined a ghost cell to hold invariants and proved an invariant access lemma which allows opening an invariant if the current expression is atomic. In order to use invariant we only had to provide proofs for which evaluation steps are atomic. We provided proofs for all primitive evaluation steps. The proofs are the same for all steps so we just explain the one for `Load`.

```
1 Lemma ectx_language_atomic a e :  
2   head_atomic a e → sub_exprs_are_values e → Atomic a e.  
3  
4 Instance load_atomic v : Atomic StronglyAtomic (Load (Val v)).  
5 Instance store_atomic v1 v2 : Atomic StronglyAtomic (Store (Val v1) (Val v2)).  
6 ...
```

An expression is atomic if it takes one step to a value, and if all subexpressions are already values. The first condition follows by definition of the step relation and the second follows by case analysis of the expression.

Since performing an effect starts a chain of evaluation steps to capture the current continuation, it is not atomic. For the same reason an effect handler and invoking a continuation are not atomic except in degenerate cases. Therefore, invariants and effects do not interact in any interesting way.

Adding Multi-Threading to Hazel

To allow reasoning in Hazel about multithreaded programs we need a multithreaded operational semantics as well as specifications for the new primitive operations *Fork*, *Cmpxcgh* and *FAA*.

How we add support for the `iInv` tactic to use invariants more easily.

The language interface of Iris provides a multithreaded operational semantics that is based on a thread-pool. The thread-pool is a list of expressions that represents threads running in parallel. At each step, one expression is picked out of the pool at random and executed for one thread-local step. Each thread-local step additionally returns a list of forked off threads, which are then added to the pool. This is only relevant for the *Fork* operation as all other operations naturally don't fork off threads.

Heaplang implements multi-threading like this and for Hazel we do the same thing. We adapt Hazel's thread-local operational semantics to include *Fork*, *Cmpxchg* and *FAA* operations and to track forked off threads and get a multithreaded operational semantics "for free" from Iris' language interface.

Additionally, we need to prove specifications for these three operations. *Cmpxchg* and *FAA* are standard so we will not discuss them here. The only interesting design decision in the case of Hazel is how effects and *Fork* interact. This decision is guided by the fact that in OCaml 5 effects never cross thread-boundaries. An unhandled effect just terminates the current thread. As such we must impose the empty protocol on the argument of *Fork*.

Using these primitive operations we can then build the standard *CAS*, *Spawn*, and *Join* operations on top and prove their specifications. For *Spawn* & *Join* we already need invariants as the point-to assertion for the done flag must be shared between the two threads.

Note that for *Spawn* we must also impose the empty protocol on *f* as this expression will be forked off.

This allows us to implement standard multithreaded programs which also use effect handlers. For example, we can prove the specification of the function below that is based on an analogous function in *Eio* which forks a thread and runs a new scheduler inside it. Note that same as in *Eio* the function blocks until the thread has finished executing, so it should be called in separate fiber.

The scheduler *run* and therefore also the *spawn_scheduler* function don't have interesting return values, so this part of the specification is uninteresting. What is more interesting is that they encapsulate the possible effects the given function *f* performs.

C A Note on Cancellation

- That we tried to model cancellation but the feature is too permissive to give it a specification.
- There is still an interesting question of safety (fibers cannot be added to a cancelled *Switch*).
- But including switches & cancellation in our model would entail too much work so we leave it for future work.

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