

# Classify\_Traffic\_Sign\_Images\_Using\_LeNet

October 18, 2019

## 1 PROBLEM STATEMENT

In this case study, we have been provided with images of traffic signs and the goal is to train a Deep Network to classify them

Figure 1. Traffic Sign Classification-

- The dataset contains 43 different classes of images.
- Classes are as listed below:
  - ( 0, 'Speed limit (20km/h)')
  - ( 1, 'Speed limit (30km/h)')
  - ( 2, 'Speed limit (50km/h)')
  - ( 3, 'Speed limit (60km/h)')
  - ( 4, 'Speed limit (70km/h)')
  - ( 5, 'Speed limit (80km/h)')
  - ( 6, 'End of speed limit (80km/h)')
  - ( 7, 'Speed limit (100km/h)')
  - ( 8, 'Speed limit (120km/h)')
  - ( 9, 'No passing')
  - (10, 'No passing for vehicles over 3.5 metric tons')
  - (11, 'Right-of-way at the next intersection')
  - (12, 'Priority road')
  - (13, 'Yield') (14, 'Stop')
  - (15, 'No vehicles')
  - (16, 'Vehicles over 3.5 metric tons prohibited')
  - (17, 'No entry')
  - (18, 'General caution')
  - (19, 'Dangerous curve to the left')
  - (20, 'Dangerous curve to the right')
  - (21, 'Double curve')
  - (22, 'Bumpy road')
  - (23, 'Slippery road')
  - (24, 'Road narrows on the right')
  - (25, 'Road work')
  - (26, 'Traffic signals')
  - (27, 'Pedestrians')
  - (28, 'Children crossing')

- (29, 'Bicycles crossing')
  - (30, 'Beware of ice/snow')
  - (31, 'Wild animals crossing')
  - (32, 'End of all speed and passing limits')
  - (33, 'Turn right ahead')
  - (34, 'Turn left ahead')
  - (35, 'Ahead only')
  - (36, 'Go straight or right')
  - (37, 'Go straight or left')
  - (38, 'Keep right')
  - (39, 'Keep left')
  - (40, 'Roundabout mandatory')
  - (41, 'End of no passing')
  - (42, 'End of no passing by vehicles over 3.5 metric tons')
- The network used is called LeNet that was presented by Yann LeCun <http://yann.lecun.com/exdb/publis/pdf/lecun-01a.pdf>
  - Citation: J. Stallkamp, M. Schlipsing, J. Salmen, and C. Igel. *The German Traffic Sign Recognition Benchmark: A multi-class classification competition*. In *Proceedings of the IEEE International Joint Conference on Neural Networks*, pages 1453–1460. 2011. @inproceedings{Stallkamp-IJCNN-2011, author = {Johannes Stallkamp and Marc Schlipsing and Jan Salmen and Christian Igel}, booktitle = {IEEE International Joint Conference on Neural Networks}, title = {The {G}erman {T}raffic {S}ign {R}ecognition {B}enchmark: A multi-class classification competition}, year = {2011}, pages = {1453–1460} }

## 2 IMPORT LIBRARIES

```
[1]: import matplotlib.pyplot as plt
import numpy as np
import os
```

```
[2]: import pickle
import pandas as pd
import seaborn as sns
import PIL
```

```
[3]: from tensorflow.keras import layers
import tensorflow as tf
```

## 3 IMPORT DATASETS AND NORMALIZE IT

```
[4]: with open("traffic-signs-data/train.p", mode='rb') as training_data:
    train = pickle.load(training_data)
with open("traffic-signs-data/valid.p", mode='rb') as validation_data:
    valid = pickle.load(validation_data)
with open("traffic-signs-data/test.p", mode='rb') as testing_data:
    test = pickle.load(testing_data)
```

```
[5]: X_train, y_train = train['features'], train['labels']  
X_validation, y_validation = valid['features'], valid['labels']  
X_test, y_test = test['features'], test['labels']
```

```
[6]: X_train.shape
```

```
[6]: (34799, 32, 32, 3)
```

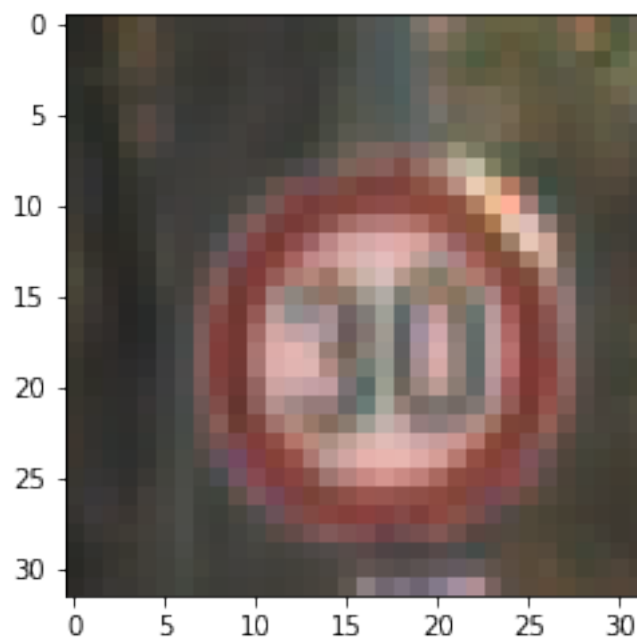
```
[7]: y_train.shape
```

```
[7]: (34799,)
```

## 4 VISUALIZE DATASET

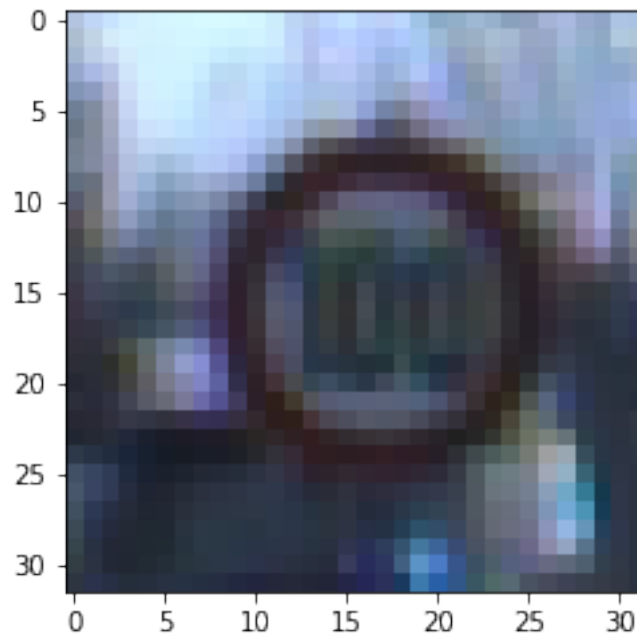
```
[8]: i = 3100  
plt.imshow(X_train[i])  
y_train[i]
```

```
[8]: 1
```



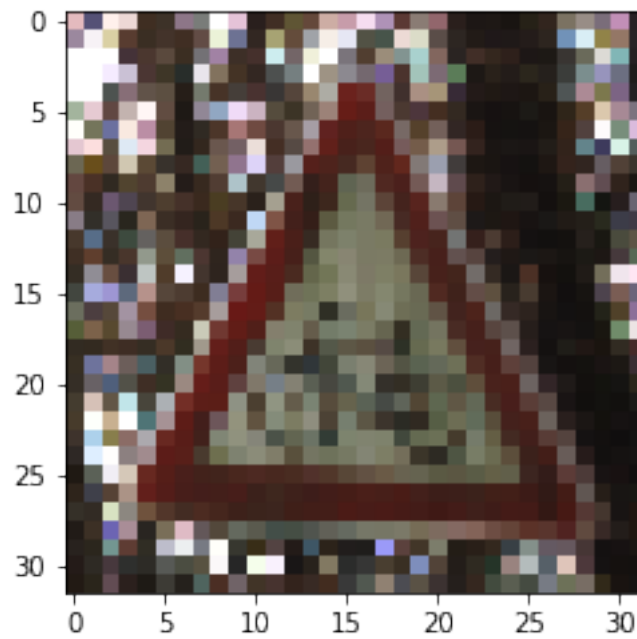
```
[9]: i = 3001  
plt.imshow(X_validation[i])  
y_validation[i]
```

```
[9]: 7
```



```
[10]: i = 2100  
plt.imshow(X_test[i])  
y_test[i]
```

[10]: 29



## 5 DATA PREPARATION

```
[11]: from sklearn.utils import shuffle
      X_train, y_train = shuffle(X_train, y_train)
```

```
[12]: X_train_gray = np.sum(X_train/3, axis = 3, keepdims = True)
      X_test_gray = np.sum(X_test/3, axis = 3, keepdims = True)
      X_validation_gray = np.sum(X_validation/3, axis = 3, keepdims = True)
```

```
[13]: X_train_gray.shape
```

[13]: (34799, 32, 32, 1)

```
[14]: X_test_gray.shape
```

[14]: (12630, 32, 32, 1)

```
[15]: X_validation_gray.shape
```

[15]: (4410, 32, 32, 1)

```
[16]: X_train_gray_norm = (X_train_gray - 128)/128
      X_test_gray_norm = (X_test_gray - 128)/128
      X_validation_gray_norm = (X_validation_gray - 128)/128
```

```
[17]: X_train_gray_norm
```

```
[17]: array([[[-0.7890625 ],
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               [-0.76822917],
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               [-0.78385417]],

               [[-0.78125    ],
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               [[-0.77864583],
               [-0.77604167],
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               ...,
               ...])
```

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...,

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  [-0.62239583],

```

```

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...,

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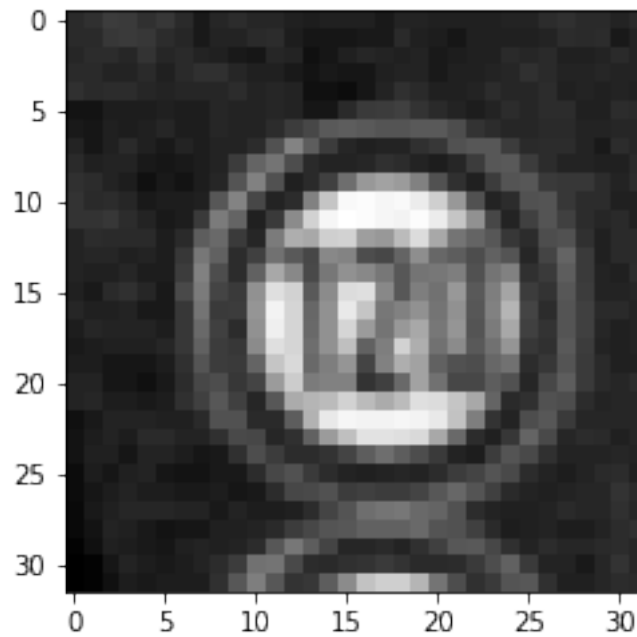
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 [-0.63020833]],

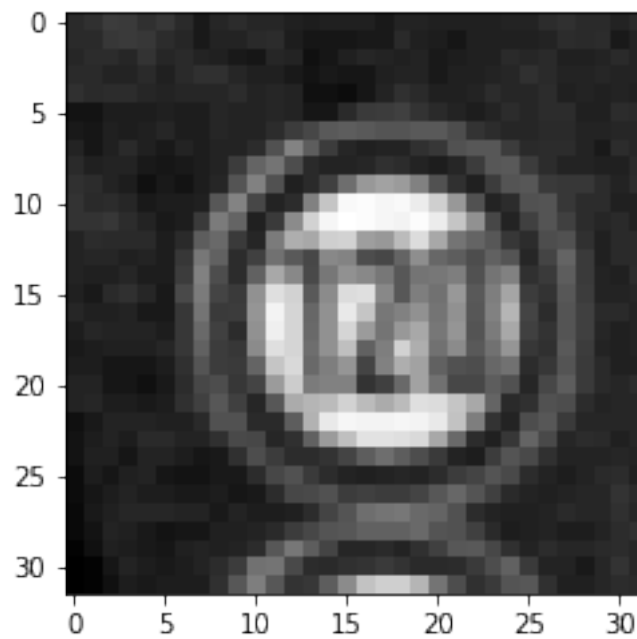
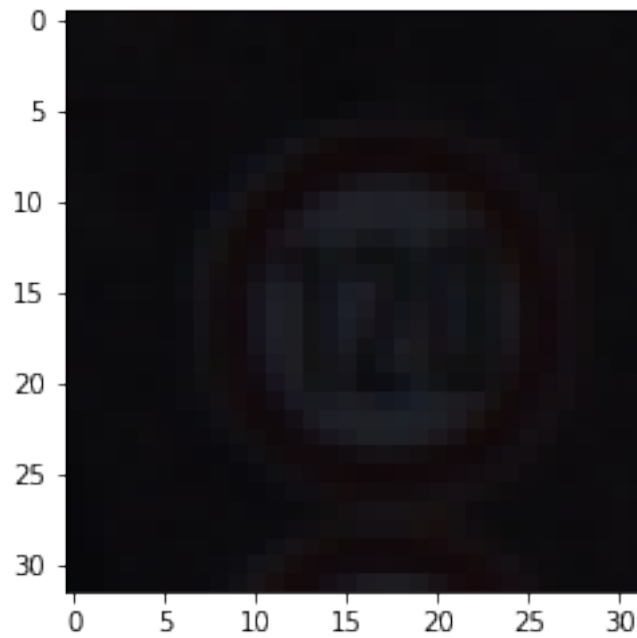
[[-0.56510417],
 [-0.57552083],
 [-0.58333333],
 ...,
 [-0.6484375  ],
 [-0.59895833],
 [-0.60416667]]])

```

```
[18]: i = 60
plt.imshow(X_train_gray[i].squeeze(), cmap = 'gray')
plt.figure()
plt.imshow(X_train[i])
plt.figure()
plt.imshow(X_train_gray_norm[i].squeeze(), cmap = 'gray')
```

```
[18]: <matplotlib.image.AxesImage at 0x1c70007fcf8>
```

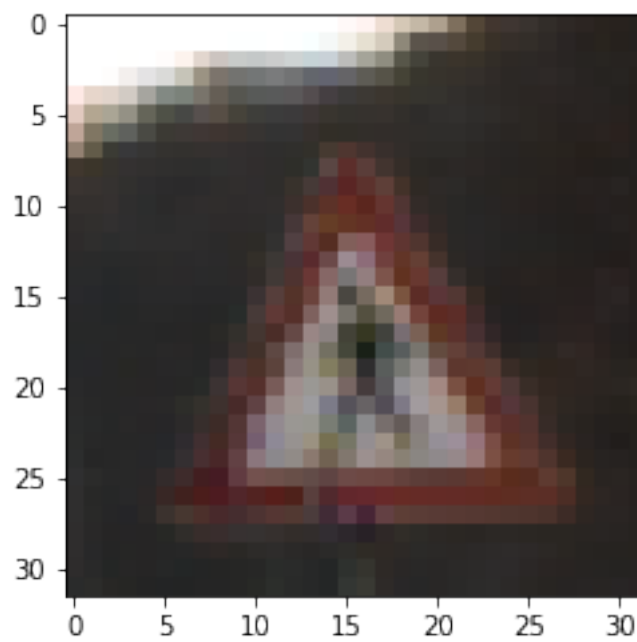
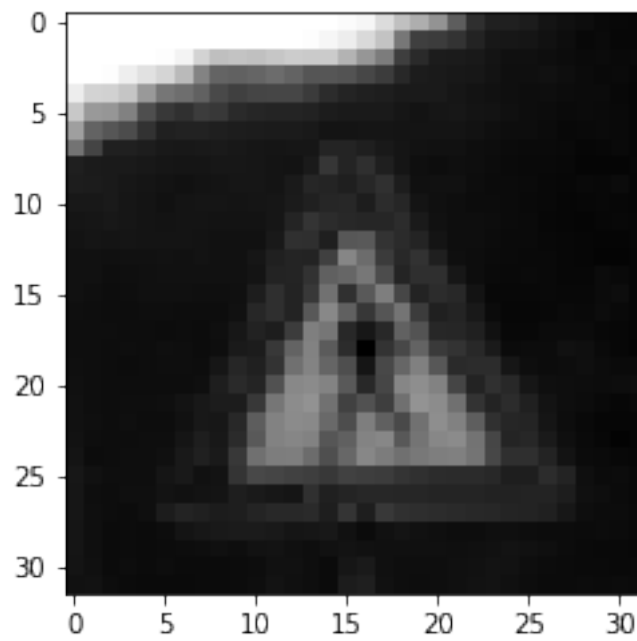


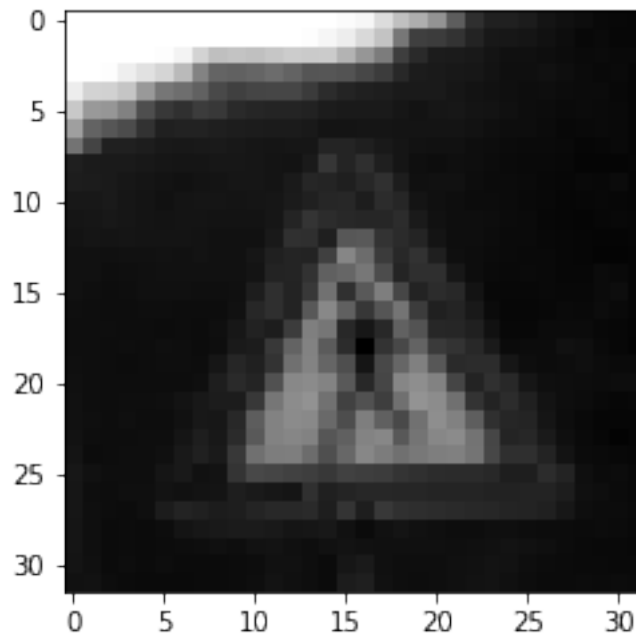


```
[19]: i = 610
plt.imshow(X_test_gray[i].squeeze(), cmap = 'gray')
plt.figure()
plt.imshow(X_test[i])
plt.figure()
```

```
plt.imshow(X_test_gray_norm[i].squeeze(), cmap = 'gray')
```

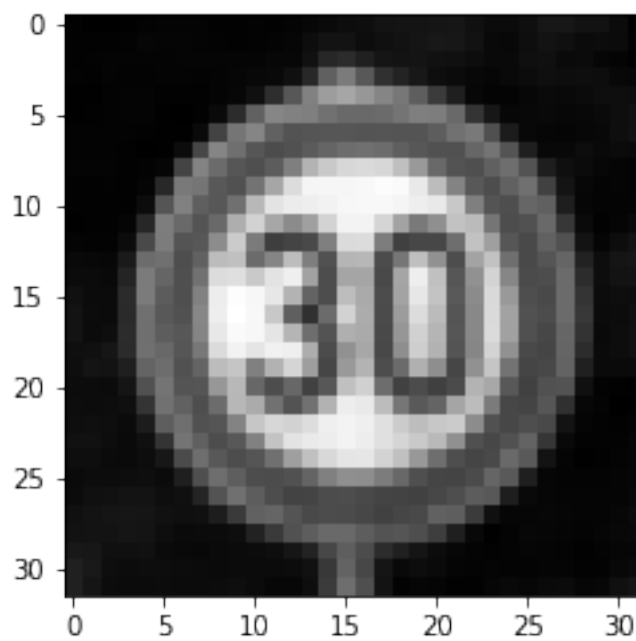
[19]: <matplotlib.image.AxesImage at 0x1c7001b34e0>

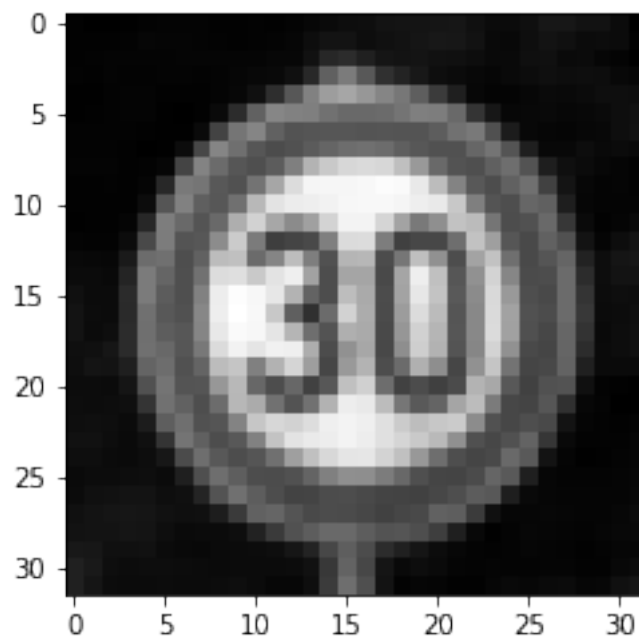
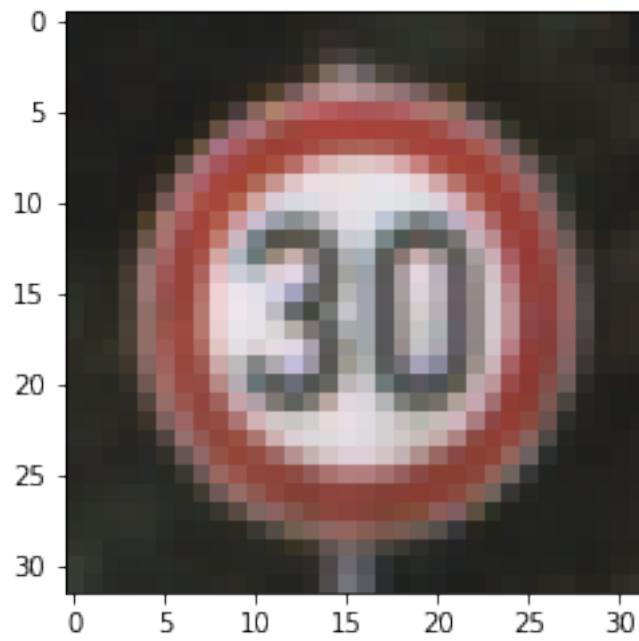




```
[20]: i = 500
plt.imshow(X_validation_gray[i].squeeze(), cmap = 'gray')
plt.figure()
plt.imshow(X_validation[i])
plt.figure()
plt.imshow(X_validation_gray_norm[i].squeeze(), cmap = 'gray')
```

[20]: <matplotlib.image.AxesImage at 0x1c75bb52f28>







## 6 MODEL TRAINING

The model consists of the following layers:

- **STEP 1: THE FIRST CONVOLUTIONAL LAYER #1**
  - Input = 32x32x1
  - Output = 28x28x6
  - Output = (Input-filter+1)/Stride\* => (32-5+1)/1=28
  - Used a 5x5 Filter with input depth of 3 and output depth of 6
  - Apply a RELU Activation function to the output
  - pooling for input, Input = 28x28x6 and Output = 14x14x6
  - Stride is the amount by which the kernel is shifted when the kernel is passed over the image.
- **STEP 2: THE SECOND CONVOLUTIONAL LAYER #2**
  - Input = 14x14x6
  - Output = 10x10x16
  - Layer 2: Convolutional layer with Output = 10x10x16
  - Output = (Input-filter+1)/strides => 10 = 14-5+1/1
  - Apply a RELU Activation function to the output
  - Pooling with Input = 10x10x16 and Output = 5x5x16
- **STEP 3: FLATTENING THE NETWORK**
  - Flatten the network with Input = 5x5x16 and Output = 400
- **STEP 4: FULLY CONNECTED LAYER**
  - Layer 3: Fully Connected layer with Input = 400 and Output = 120
  - Apply a RELU Activation function to the output
- **STEP 5: ANOTHER FULLY CONNECTED LAYER**
  - Layer 4: Fully Connected Layer with Input = 120 and Output = 84
  - Apply a RELU Activation function to the output
- **STEP 6: FULLY CONNECTED LAYER**
  - Layer 5: Fully Connected layer with Input = 84 and Output = 43

```
[21]: from tensorflow.keras import datasets, layers, models

LeNet = models.Sequential()

LeNet.add(layers.Conv2D(6, (5,5), activation = 'relu', input_shape = (32,32,1)))
LeNet.add(layers.AveragePooling2D())

LeNet.add(layers.Conv2D(16, (5,5), activation = 'relu'))
```

```

LeNet.add(layers.AveragePooling2D())

LeNet.add(layers.Flatten())

LeNet.add(layers.Dense(120, activation = 'relu'))

LeNet.add(layers.Dense(84, activation = 'relu'))

LeNet.add(layers.Dense(43, activation = 'softmax'))
LeNet.summary()

```

Model: "sequential"

Layer (type)	Output Shape	Param #
conv2d (Conv2D)	(None, 28, 28, 6)	156
average_pooling2d (AveragePo	(None, 14, 14, 6)	0
conv2d_1 (Conv2D)	(None, 10, 10, 16)	2416
average_pooling2d_1 (Average	(None, 5, 5, 16)	0
flatten (Flatten)	(None, 400)	0
dense (Dense)	(None, 120)	48120
dense_1 (Dense)	(None, 84)	10164
dense_2 (Dense)	(None, 43)	3655
Total params: 64,511		
Trainable params: 64,511		
Non-trainable params: 0		

[22]: `LeNet.compile(optimizer = 'Adam', loss = 'sparse_categorical_crossentropy',  
metrics = ['accuracy'])`

[23]: `history = LeNet.fit(X_train_gray_norm,  
y_train,  
batch_size = 500,  
nb_epoch = 50,  
verbose = 1,  
validation_data = (X_validation_gray_norm, y_validation))`

WARNING: Logging before flag parsing goes to stderr.

W1018 22:13:07.586207 16828 training.py:701] The `nb\_epoch` argument in `fit` has been renamed `epochs`.

Train on 34799 samples, validate on 4410 samples

Epoch 1/50

34799/34799 [=====] - 17s 478us/sample - loss: 3.1495 - accuracy: 0.1815 - val\_loss: 2.6016 - val\_accuracy: 0.3184

Epoch 2/50

34799/34799 [=====] - 15s 429us/sample - loss: 1.5505 - accuracy: 0.5693 - val\_loss: 1.2840 - val\_accuracy: 0.6236

Epoch 3/50

34799/34799 [=====] - 15s 438us/sample - loss: 0.8503 - accuracy: 0.7624 - val\_loss: 0.9664 - val\_accuracy: 0.7333

Epoch 4/50

34799/34799 [=====] - 15s 435us/sample - loss: 0.6108 - accuracy: 0.8341 - val\_loss: 0.8458 - val\_accuracy: 0.7651

Epoch 5/50

34799/34799 [=====] - 15s 437us/sample - loss: 0.4888 - accuracy: 0.8687 - val\_loss: 0.7665 - val\_accuracy: 0.7871

Epoch 6/50

34799/34799 [=====] - 15s 433us/sample - loss: 0.4101 - accuracy: 0.8903 - val\_loss: 0.7181 - val\_accuracy: 0.8111

Epoch 7/50

34799/34799 [=====] - 16s 454us/sample - loss: 0.3481 - accuracy: 0.9082 - val\_loss: 0.6641 - val\_accuracy: 0.8234

Epoch 8/50

34799/34799 [=====] - 16s 460us/sample - loss: 0.3001 - accuracy: 0.9228 - val\_loss: 0.6393 - val\_accuracy: 0.8297

Epoch 9/50

34799/34799 [=====] - 15s 444us/sample - loss: 0.2659 - accuracy: 0.9324 - val\_loss: 0.6417 - val\_accuracy: 0.8363

Epoch 10/50

34799/34799 [=====] - 17s 481us/sample - loss: 0.2316 - accuracy: 0.9404 - val\_loss: 0.6282 - val\_accuracy: 0.8433

Epoch 11/50

34799/34799 [=====] - 17s 476us/sample - loss: 0.2096 - accuracy: 0.9467 - val\_loss: 0.6213 - val\_accuracy: 0.8422

Epoch 12/50

34799/34799 [=====] - 15s 445us/sample - loss: 0.1943 - accuracy: 0.9499 - val\_loss: 0.6205 - val\_accuracy: 0.8531

Epoch 13/50

34799/34799 [=====] - 15s 434us/sample - loss: 0.1701 - accuracy: 0.9571 - val\_loss: 0.5958 - val\_accuracy: 0.8524

Epoch 14/50

34799/34799 [=====] - 16s 451us/sample - loss: 0.1537 - accuracy: 0.9620 - val\_loss: 0.5945 - val\_accuracy: 0.8522

Epoch 15/50

34799/34799 [=====] - 15s 433us/sample - loss: 0.1381 -

accuracy: 0.9648 - val\_loss: 0.5730 - val\_accuracy: 0.8574  
 Epoch 16/50  
 34799/34799 [=====] - 15s 444us/sample - loss: 0.1281 -  
 accuracy: 0.9685 - val\_loss: 0.6105 - val\_accuracy: 0.8587  
 Epoch 17/50  
 34799/34799 [=====] - 15s 438us/sample - loss: 0.1196 -  
 accuracy: 0.9700 - val\_loss: 0.5860 - val\_accuracy: 0.8583  
 Epoch 18/50  
 34799/34799 [=====] - 15s 436us/sample - loss: 0.1098 -  
 accuracy: 0.9734 - val\_loss: 0.6329 - val\_accuracy: 0.8533  
 Epoch 19/50  
 34799/34799 [=====] - 15s 423us/sample - loss: 0.1020 -  
 accuracy: 0.9741 - val\_loss: 0.6231 - val\_accuracy: 0.8617  
 Epoch 20/50  
 34799/34799 [=====] - 16s 467us/sample - loss: 0.0899 -  
 accuracy: 0.9774 - val\_loss: 0.5986 - val\_accuracy: 0.8719  
 Epoch 21/50  
 34799/34799 [=====] - 18s 508us/sample - loss: 0.0858 -  
 accuracy: 0.9791 - val\_loss: 0.6339 - val\_accuracy: 0.8637  
 Epoch 22/50  
 34799/34799 [=====] - 15s 427us/sample - loss: 0.0776 -  
 accuracy: 0.9814 - val\_loss: 0.6581 - val\_accuracy: 0.8649  
 Epoch 23/50  
 34799/34799 [=====] - 14s 416us/sample - loss: 0.0746 -  
 accuracy: 0.9818 - val\_loss: 0.6833 - val\_accuracy: 0.8553  
 Epoch 24/50  
 34799/34799 [=====] - 14s 401us/sample - loss: 0.0673 -  
 accuracy: 0.9833 - val\_loss: 0.6759 - val\_accuracy: 0.8667  
 Epoch 25/50  
 34799/34799 [=====] - 12s 340us/sample - loss: 0.0623 -  
 accuracy: 0.9856 - val\_loss: 0.6929 - val\_accuracy: 0.8628  
 Epoch 26/50  
 34799/34799 [=====] - 12s 340us/sample - loss: 0.0563 -  
 accuracy: 0.9866 - val\_loss: 0.7099 - val\_accuracy: 0.8594  
 Epoch 27/50  
 34799/34799 [=====] - 12s 339us/sample - loss: 0.0529 -  
 accuracy: 0.9874 - val\_loss: 0.6834 - val\_accuracy: 0.8692  
 Epoch 28/50  
 34799/34799 [=====] - 12s 334us/sample - loss: 0.0510 -  
 accuracy: 0.9879 - val\_loss: 0.7080 - val\_accuracy: 0.8696  
 Epoch 29/50  
 34799/34799 [=====] - 12s 338us/sample - loss: 0.0475 -  
 accuracy: 0.9887 - val\_loss: 0.7828 - val\_accuracy: 0.8660  
 Epoch 30/50  
 34799/34799 [=====] - 12s 348us/sample - loss: 0.0443 -  
 accuracy: 0.9895 - val\_loss: 0.7569 - val\_accuracy: 0.8612  
 Epoch 31/50  
 34799/34799 [=====] - 12s 337us/sample - loss: 0.0406 -

accuracy: 0.9905 - val\_loss: 0.7930 - val\_accuracy: 0.8669  
 Epoch 32/50  
 34799/34799 [=====] - 12s 334us/sample - loss: 0.0377 -  
 accuracy: 0.9915 - val\_loss: 0.7902 - val\_accuracy: 0.8669  
 Epoch 33/50  
 34799/34799 [=====] - 12s 351us/sample - loss: 0.0383 -  
 accuracy: 0.9905 - val\_loss: 0.7467 - val\_accuracy: 0.8669  
 Epoch 34/50  
 34799/34799 [=====] - 12s 342us/sample - loss: 0.0344 -  
 accuracy: 0.9917 - val\_loss: 0.7562 - val\_accuracy: 0.8660  
 Epoch 35/50  
 34799/34799 [=====] - 12s 334us/sample - loss: 0.0303 -  
 accuracy: 0.9933 - val\_loss: 0.7618 - val\_accuracy: 0.8728  
 Epoch 36/50  
 34799/34799 [=====] - 13s 366us/sample - loss: 0.0320 -  
 accuracy: 0.9919 - val\_loss: 0.7860 - val\_accuracy: 0.8735  
 Epoch 37/50  
 34799/34799 [=====] - 13s 386us/sample - loss: 0.0318 -  
 accuracy: 0.9919 - val\_loss: 0.8505 - val\_accuracy: 0.8680  
 Epoch 38/50  
 34799/34799 [=====] - 12s 357us/sample - loss: 0.0308 -  
 accuracy: 0.9916 - val\_loss: 0.6967 - val\_accuracy: 0.8739  
 Epoch 39/50  
 34799/34799 [=====] - 12s 347us/sample - loss: 0.0267 -  
 accuracy: 0.9937 - val\_loss: 0.6780 - val\_accuracy: 0.8900  
 Epoch 40/50  
 34799/34799 [=====] - 12s 338us/sample - loss: 0.0235 -  
 accuracy: 0.9942 - val\_loss: 0.8278 - val\_accuracy: 0.8671  
 Epoch 41/50  
 34799/34799 [=====] - 12s 341us/sample - loss: 0.0211 -  
 accuracy: 0.9948 - val\_loss: 0.7804 - val\_accuracy: 0.8741  
 Epoch 42/50  
 34799/34799 [=====] - 12s 354us/sample - loss: 0.0164 -  
 accuracy: 0.9966 - val\_loss: 0.7662 - val\_accuracy: 0.8748  
 Epoch 43/50  
 34799/34799 [=====] - 12s 351us/sample - loss: 0.0180 -  
 accuracy: 0.9957 - val\_loss: 0.7943 - val\_accuracy: 0.8680  
 Epoch 44/50  
 34799/34799 [=====] - 13s 367us/sample - loss: 0.0178 -  
 accuracy: 0.9957 - val\_loss: 0.7970 - val\_accuracy: 0.8710  
 Epoch 45/50  
 34799/34799 [=====] - 14s 396us/sample - loss: 0.0184 -  
 accuracy: 0.9951 - val\_loss: 0.9367 - val\_accuracy: 0.8499  
 Epoch 46/50  
 34799/34799 [=====] - 12s 356us/sample - loss: 0.0238 -  
 accuracy: 0.9932 - val\_loss: 0.9788 - val\_accuracy: 0.8578  
 Epoch 47/50  
 34799/34799 [=====] - 13s 386us/sample - loss: 0.0206 -

```
accuracy: 0.9937 - val_loss: 0.7591 - val_accuracy: 0.8778
Epoch 48/50
34799/34799 [=====] - 12s 349us/sample - loss: 0.0145 -
accuracy: 0.9966 - val_loss: 0.9223 - val_accuracy: 0.8624
Epoch 49/50
34799/34799 [=====] - 12s 344us/sample - loss: 0.0115 -
accuracy: 0.9976 - val_loss: 0.9173 - val_accuracy: 0.8660
Epoch 50/50
34799/34799 [=====] - 13s 369us/sample - loss: 0.0094 -
accuracy: 0.9980 - val_loss: 0.8907 - val_accuracy: 0.8692
```

## 7 MODEL EVALUATION

```
[24]: score = LeNet.evaluate(X_test_gray_norm, y_test)
      print('Test Accuracy: {}'.format(score[1]))
```

12630/1 [=

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```
=====
=====] - 2s 177us/sample - loss: 2.1799 - accuracy:
0.8745
Test Accuracy: 0.8745051622390747
```

```
[25]: history.history.keys()
```

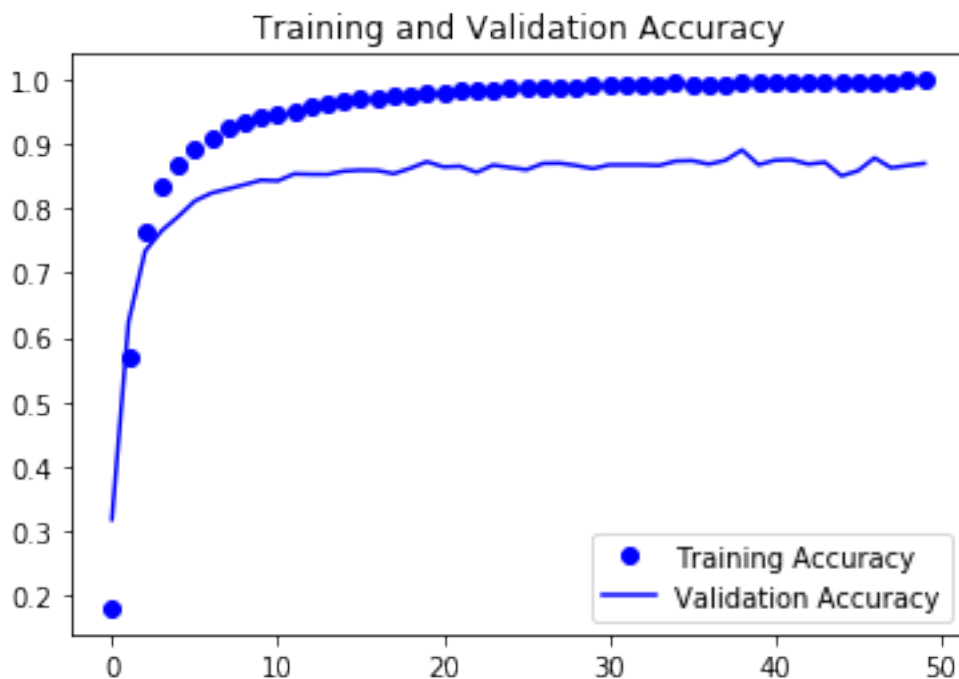
```
[25]: dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])
```

```
[26]: accuracy = history.history['accuracy']
      val_accuracy = history.history['val_accuracy']
      loss = history.history['loss']
      val_loss = history.history['val_loss']
```

```
[27]: epochs = range(len(accracy))

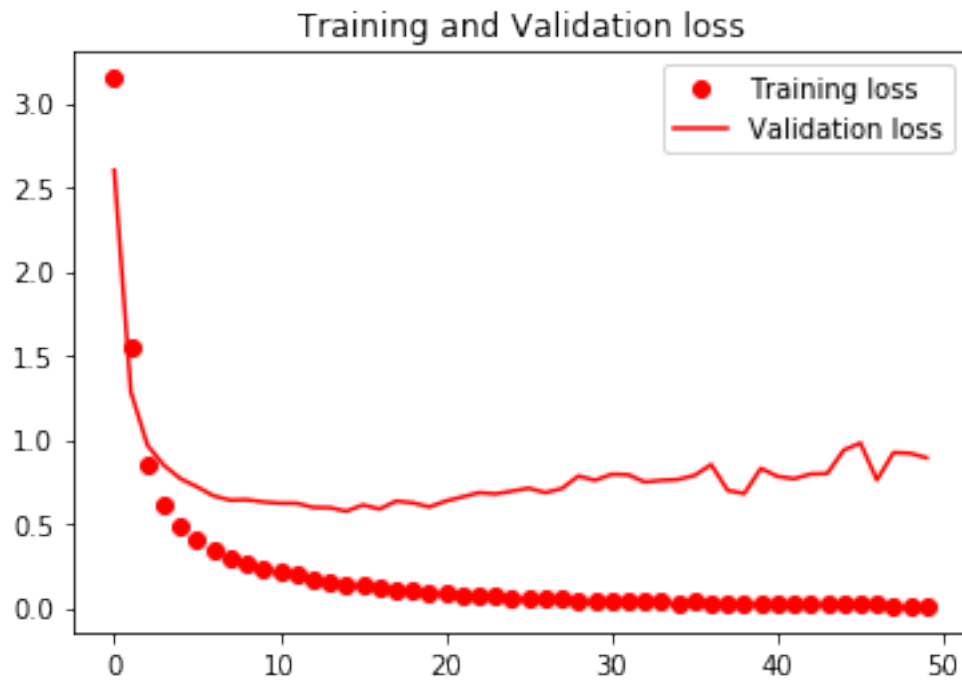
      plt.plot(epochs, accuracy, 'bo', label='Training Accuracy')
      plt.plot(epochs, val_accuracy, 'b', label='Validation Accuracy')
      plt.title('Training and Validation Accuracy')
      plt.legend()
```

```
[27]: <matplotlib.legend.Legend at 0x1c701a50be0>
```



```
[28]: plt.plot(epochs, loss, 'ro', label='Training loss')
      plt.plot(epochs, val_loss, 'r', label='Validation loss')
      plt.title('Training and Validation loss')
      plt.legend()
```

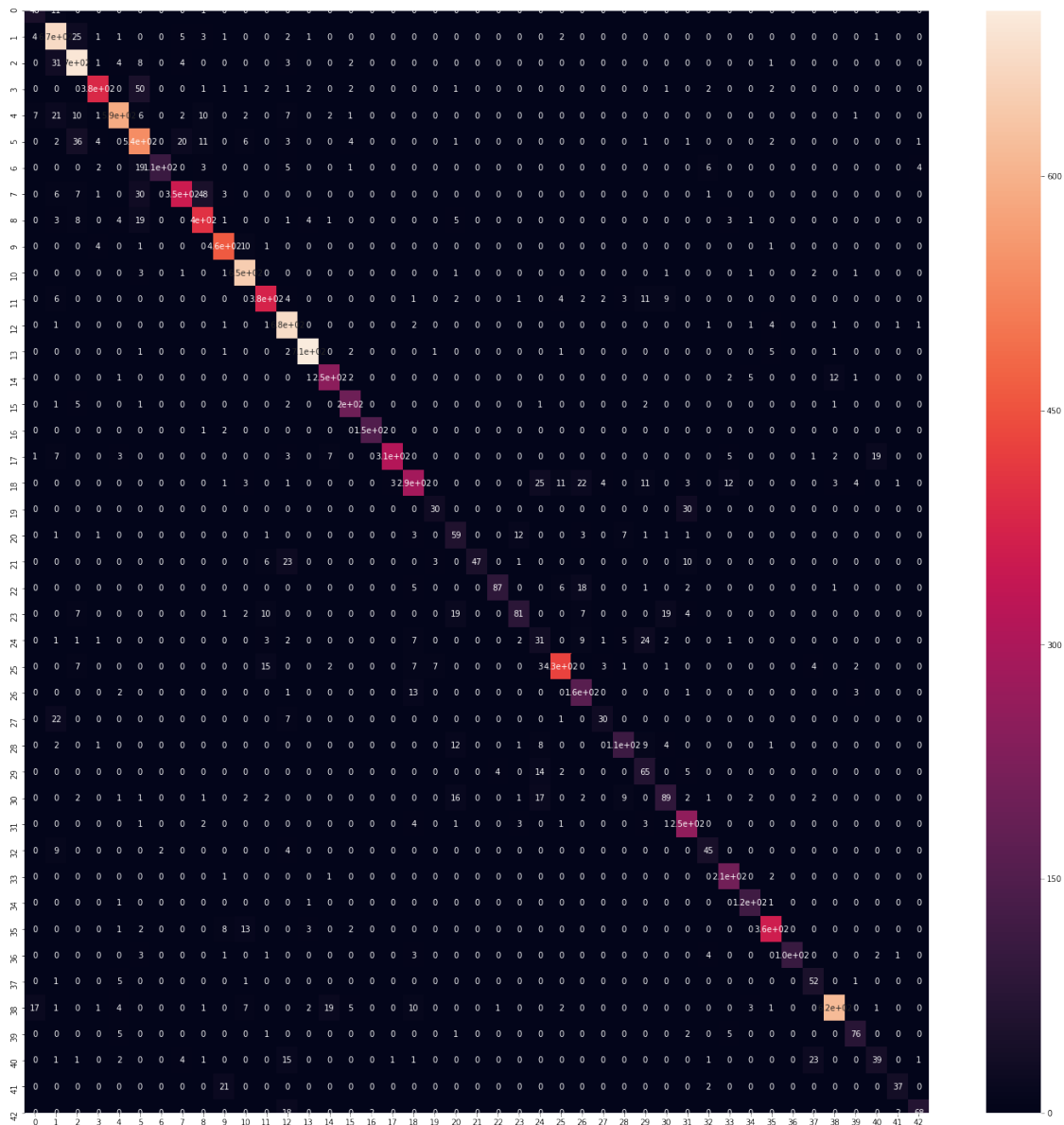
[28]: <matplotlib.legend.Legend at 0x1c70013bbe0>



```
[29]: predicted_classes = LeNet.predict_classes(X_test_gray_norm)
      y_true = y_test
```

```
[30]: from sklearn.metrics import confusion_matrix
      cm = confusion_matrix(y_true, predicted_classes)
      plt.figure(figsize = (25, 25))
      sns.heatmap(cm, annot = True)
```

[30]: <matplotlib.axes.\_subplots.AxesSubplot at 0x1c74d768780>

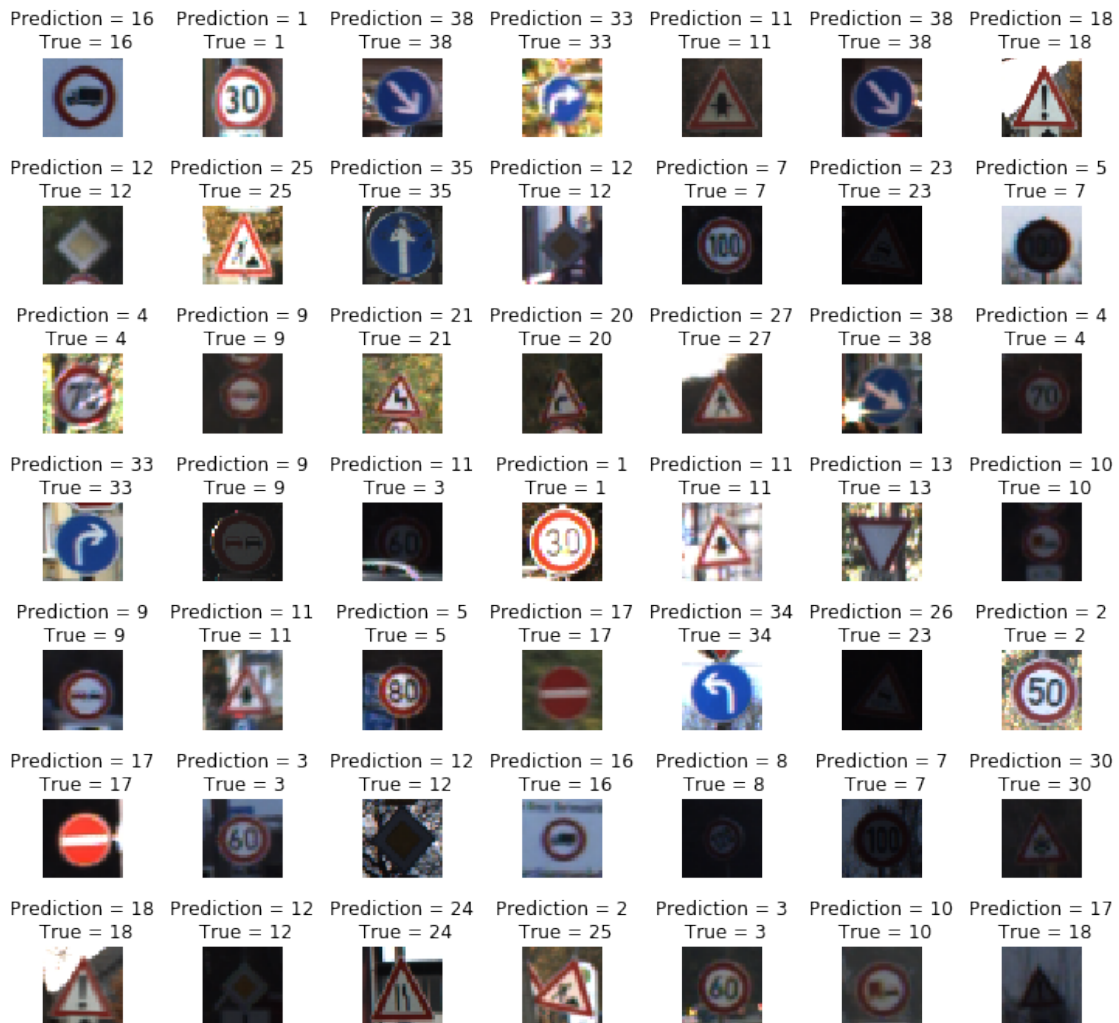


```
[31]: L = 7
      W = 7

fig, axes = plt.subplots(L, W, figsize = (12, 12))
axes = axes.ravel()

for i in np.arange(0, L*W):
    axes[i].imshow(X_test[i])
    axes[i].set_title('Prediction = {}\n True = {}'.format(predicted_classes[i],
→y_true[i]))
    axes[i].axis('off')
```

```
plt.subplots_adjust(wspace = 1)
```



## 8 Skills Utilized:

1. Convolutional NN
2. LeNet
3. RELU

## 9 Interesting Links:

- <http://setosa.io/ev/image-kernels/>
- <http://scs.ryerson.ca/~aharley/vis/conv/flat.html>

## 10 Notes:

- RELU layers are used to add non-linearity in the feature map.
- Pooling or down sampling layers are placed after convolutional layers to reduce feature map dimensionality.
- This improves the computational efficiency while preserving the features.
- Pooling helps the model to generalize by avoiding overfitting.
- Improve accuracy by adding more feature detectors/filters or adding a dropout.
- Dropout refers to dropping out units in a neural network
- Dropout is a regularization technique for reducing overfitting in neural networks.
- Dropout enables training to occur on several architectures of the neural network.
- Neurons develop co-dependency amongst each other during training