

## Exponential Rules

$$a^m \cdot a^n = a^{m+n}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$(a^m)^n = a^{mn}$$

$$a^0 = 1 \quad (a \neq 0)$$

$$a^{-n} = \frac{1}{a^n}$$

$$a^{1/n} = \sqrt[n]{a}$$

## Logarithmic Rules

$$\log_b(xy) = \log_b x + \log_b y$$

$$\log_b \left( \frac{x}{y} \right) = \log_b x - \log_b y$$

$$\log_b(x^r) = r \log_b x$$

$$\log_b b = 1$$

$$\log_b 1 = 0$$

$$\log_b x = \frac{\log_k x}{\log_k b}$$

$$b^{\log_b x} = x$$

$$\log_b(b^x) = x$$

## Practice Problems

1. Simplify:  $\log_2(8)$
2. Simplify:  $\log_5(25) + \log_5(4)$
3. Simplify:  $\log_{10}(1000) - \log_{10}(10)$
4. Simplify:  $\log_3\left(\frac{81}{3}\right)$
5. Simplify:  $2\log_2(5) - \log_2(\sqrt{25})$
6. Solve:  $2^x = 16$
7. Solve:  $3^{2x+1} = 81$
8. Solve:  $5^x = 1/25$
9. Solve:  $e^{2x} = 7$
10. Solve:  $10^x = 3$
11. Solve:  $\log_3(x) = 4$
12. Solve:  $\log(x+2) = 1$
13. Solve:  $\log_2(2x-1) = 3$
14. Solve:  $\log_5(x) + \log_5(x-4) = 1$
15. Solve:  $2\log_3(x) = \log_3(9)$
16. Solve for  $x$ :  $\log_2(3x) = \log_2(12)$
17. Solve for  $x$ :  $\log(x^2) = 2\log(x) - \log(5)$
18. Expand:  $\log(10x^2/\sqrt{y})$

19. Condense:  $\log(x) + 2\log(y) - \log(z)$
20. Solve for  $x$ :  $\ln(x^2) = \ln(5x)$
21. Simplify:  $\log_4(64)$
22. Simplify:  $\log_6(36) - \log_6(6)$
23. Simplify:  $\log_{10}(10000)$
24. Simplify:  $\log_9(81)$
25. Simplify:  $3\log_3(2) + \log_3(9)$
26. Solve:  $4^x = 1/16$
27. Solve:  $10^{2x-1} = 100$
28. Solve:  $7^x = 49$
29. Solve:  $e^x = 20$
30. Solve:  $2^x = 10$
31. Solve:  $\log_4(x) = 2$
32. Solve:  $\log(x - 3) = 2$
33. Solve:  $\log_2(x + 4) = 5$
34. Solve:  $\log_3(x) - \log_3(x - 1) = 1$
35. Solve:  $\log_6(x^2 - 9) = 2$
36. Solve for  $x$ :  $\log_5(4x) = \log_5(20)$
37. Solve for  $x$ :  $\log(x^3) = 3\log(x)$
38. Expand:  $\log\left(\frac{x^3y}{z^2}\right)$
39. Condense:  $2\log(a) - \frac{1}{2}\log(b) + \log(c)$
40. Solve for  $x$ :  $\ln(x^3) = \ln(27)$