Analysis and Design of Deep Neural Networks

Ahmad Kalhor
Associate Professor
School of Electrical and Computer Engineering
University of Tehran
Spring 2022

Part1

Design of DNNs, by analyzing the well known layers, blocks, modules, and architectures

1. Structure analysis in DNNs

1.1 Layers, Blocks and Modules

- Fully Connected layers and blocks
- Convolution Layers-Blocks-Modules
- Recurrent Layers-Modules
- Attention Layers-Modules
- Pooling Layers
- Normalization Layers

1.2 Architectures

- CNNs
- R-CNNs
- RNNs and Transformers
- AEs and VAEs
- GANs

1.1 Layers, Blocks and Modules

1.1.1. Fully Connected layers and blocks

1.1.2 Convolution Layers-Blocks-Modules

1.1.3 Recurrent and Attention Layers –Modules

1.1.4 Attention Layers –Modules

1.1.5 Pooling and Down-sampling/Up-sampling Layers

1.1.6 Normalizing Layers

1.1.1 Fully Connected layers and their blocks

Ideal to make partitions, maps and encoded/decoded data from a set of distinct inputs.

- One FC layer
- A block of two FC layers
- A block of three FC layers
- A block of more than three FC layers

One FC layer

Definition

- $\boldsymbol{y} = \boldsymbol{f}(\mathrm{W}\boldsymbol{x} + \mathbf{b}),\ \mathrm{W} = [\boldsymbol{w}_{ji}]\ \mathrm{b} = [b_j]$
- $\boldsymbol{x} \epsilon R^n \quad \boldsymbol{y} \epsilon R^m \quad i \in \{1, \cdots, n\}\ j \in \{1, \cdots, n\}$
- Activation function:
- $f \in \{sign, \mathrm{step}, \tanh, sigmoid, Relu, identity \cdots\}$

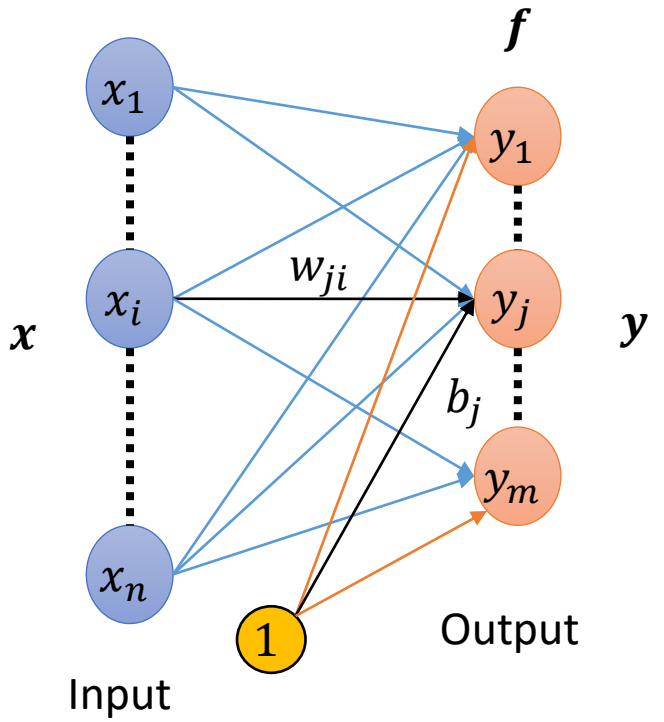
Functionality

(1) Forming an "n"dimensional hyper plane:

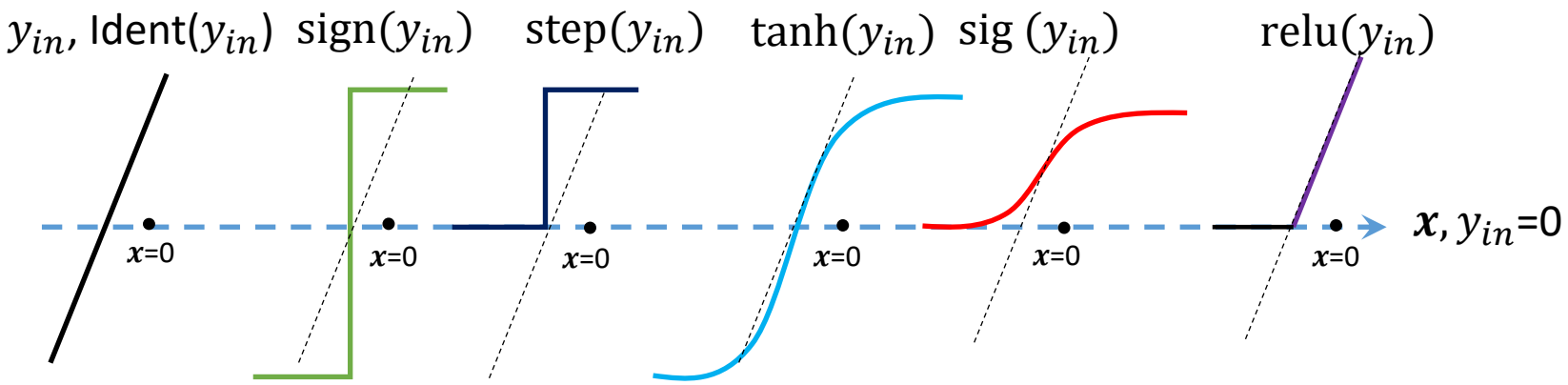
$$y_{in_j} = \mathrm{w_{j1}x_1} + \cdots + \mathrm{w_{jn}x_n} + \mathrm{b_j}$$

(2) Folding (hard/soft), Rectifying,.. on the hyper plane:

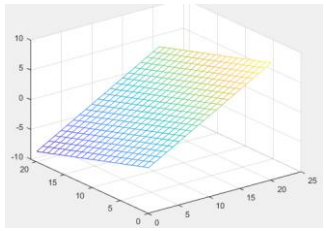
$$y_j = f(y_{in_j})$$



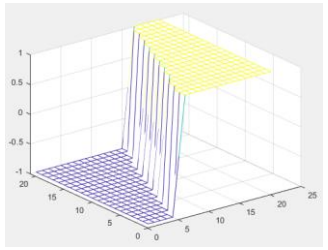
Example(1) for $n = 1$, $f(yin)$, $y_{in} = 2x + 1$ w:slope parameter , b: $(up \uparrow down \downarrow) shift\ parameter$



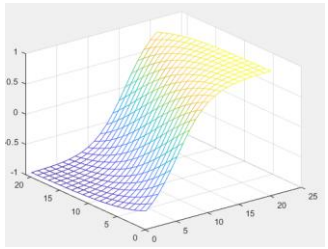
Example(2) for $n = 2$, $f(yin)$, $y_{in} = 2x_2 - x_1$+0



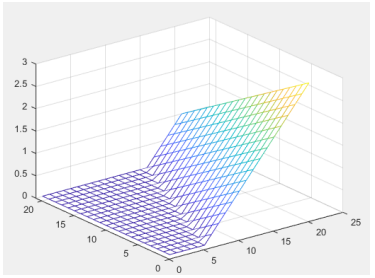
$y_{in}, ident(y_{in})$



sign(10y_{in})



tanh(y_{in})



Relu(y_{in})

❖ A “one FC layer” can transform the input space to a (hard or soft) folded or rectified hyper plane

Some Notes about one FC layer

1. One FC layer (with n inputs and m outputs) is formed from m neurons at output, where each neuron is connected to all n input units (fully connected).
2. Each input send a weighted signal to each neuron.
3. For each neuron, the summation of weighted inputs makes an independent hyper-plane just before activated by it.
4. The parameters of all hyper-planes are opted through a learning process.
5. For each neuron, the corresponding hyper-plane is hardly or softly folded or rectified just after activating by it.
6. Indeed, taking in inputs as a "n" dimensional vector, the FC layer provides "m" folded, or rectified hyper-planes at the output.
7. Assuming the inputs are binary or bipolar, and the activation functions make binary or bipolar values, a neuron in one FC layer can operate as a simple logic gate like “and”, “or, etc. (M&P neuron)
8. Assuming the activation functions of the neurons are identity, a FC layer operates as a linear transformer, which can approximate a linear regression model in a regression problem.
9. Assuming “r” independent linear or nonlinear correlations among inputs, the order of the formed hyper plan is “n-r”.

A block of two FC layers

Definition

- $\boldsymbol{y} = \boldsymbol{f}^2\left(\mathrm{W}^2 \underbrace{\boldsymbol{f}^{\mathbf{1}}\left(\mathrm{W}^1\boldsymbol{x} + \mathbf{b}^{\mathbf{1}}\right)}_{z} + \boldsymbol{b}^2\right)$
- $\boldsymbol{x} \epsilon R^n \boldsymbol{z} \epsilon R^{m_1} \boldsymbol{y} \epsilon R^m \quad i \in \{1, \cdots, n\}\ j \in \{1, \cdots, m_1\}\ k \in \{1, \cdots, m\}$
- Activation functions:
- $f^{1,2} \in \{sign, \text{step}, \tanh, sigmoid, Relu, identity \cdots\}$

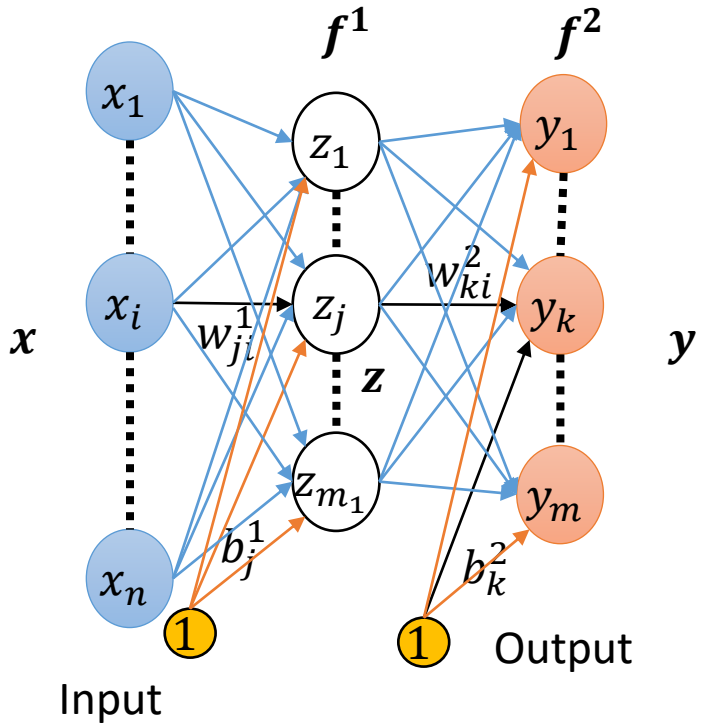
Overall Functionality

(1) A hyper plane: $z_{in_\mathrm{j}} = \mathrm{w}^1_{\mathrm{j1}}\mathrm{x}_1 + \cdots + \mathrm{w}^2_{\mathrm{jn}}\mathrm{x}_\mathrm{n} + \mathrm{b}^1_\mathrm{j}$

(2) Folding, Rectifying,.. on the hyper plane: $z_j = f^1(z_{in_\mathrm{j}})$

(3) A hyper plane: $y_{in_k} = \mathrm{w}^2_{\mathrm{k1}}\mathrm{z}_1 + \cdots + \mathrm{w}^2_{\mathrm{k}m_1}\mathrm{z}_{\mathrm{m}_1} + \mathrm{b}^2_\mathrm{k}$

(4) Folding, Rectifying,.. on the hyper plane: $y_k = f^2(y_{in_k})$



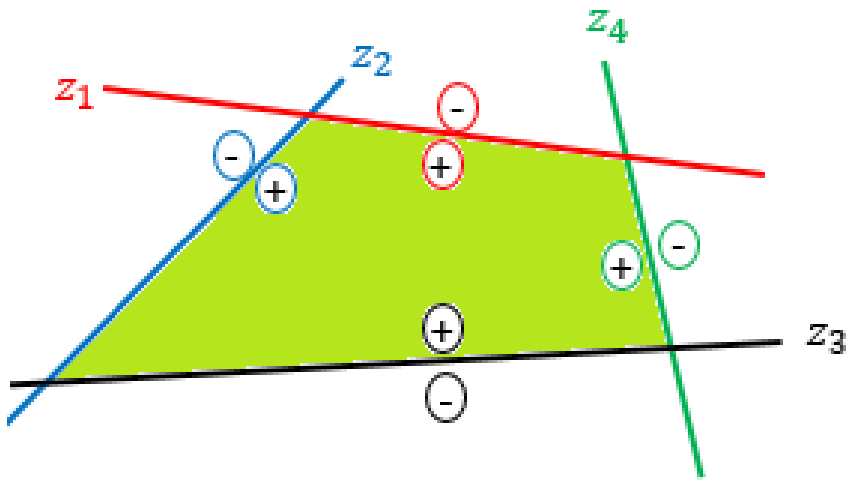
A Desired Functionality in classification /Regression problems

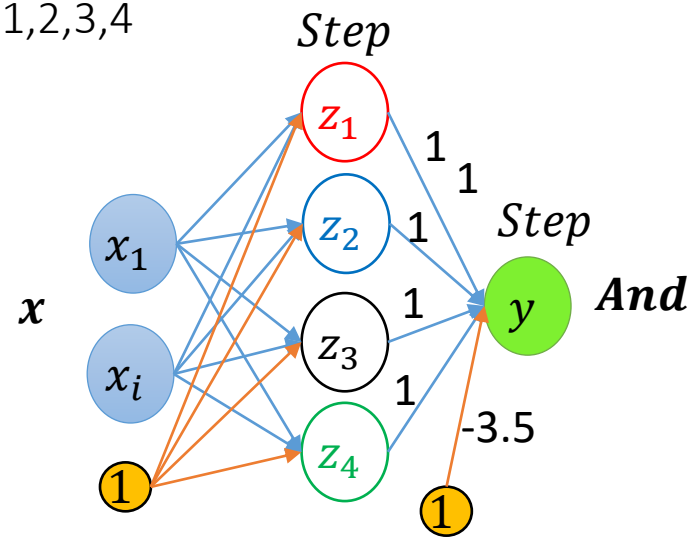
(1) A hyper plane: $z_{in_j} = w_{j1}^1 x_1 + \cdots + w_{jn}^2 x_n + b_j^1$

(2) Folding the hyper plane: $z_j = f^1(z_{in_j})$

(3) An "and" or "or logic gate for former folded hyper-planes is defined by "kth" neuron of last layer, by which "kth" convex hyper-polygon will be resulted.

Example for $n = 2, m_1 = 4, m=1$ $\quad z_j = w_{j1}^1 x_1 + w_{j2}^1 x_2 + b_j^1,$ $\quad$ j=1,2,3,4





- A block of two FC layers can transform the input space to multi convex hyper- polygon partitions
- Using soft activation functions, a block of two FC layers can transform the input space to multi soft convex hyper- polygon maps

A block of three FC layers

Definition

- $\boldsymbol{y} = f^3\left(\mathrm{W}^3\, \boldsymbol{f}^2\left(\mathrm{W}^2\, \underbrace{\boldsymbol{f}^{\mathbf{1}}\left(\mathrm{W}^1\boldsymbol{x} + \mathbf{b}^{\mathbf{1}}\right)}_{z} + \boldsymbol{b}^2\right)}_{u} + \boldsymbol{b}^3\right)$
- $\boldsymbol{x} \epsilon R^n \quad \boldsymbol{z} \epsilon R^{m_1} \quad \boldsymbol{u}\boldsymbol{z} \epsilon R^{m_2} \quad \boldsymbol{y} \epsilon R^m$
- $i \in \{1, \cdots, n\}\, j \in \{1, \cdots, m_1\}\, k \in \{1, \cdots, m_2\}\, l \in \{1, \cdots, m\}$
- Activation functions:
- $f^{1,2,3} \in \{sign, \text{step}, \tanh, sigmoid, Relu, idenity \cdots\}$

Overall Functionality

(1) A hyper plane: $z_{in_j} = \mathrm{w}^1_{j1}\mathrm{x}_1 + \cdots + \mathrm{w}^1_{jn}\mathrm{x}_n + \mathrm{b}^1_j$

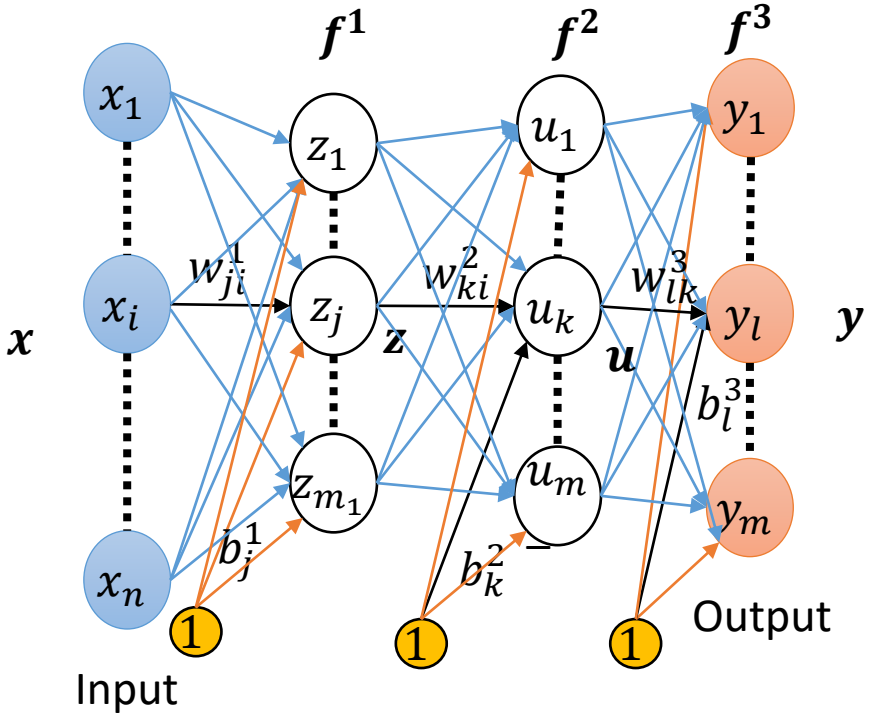
(2) Folding, Rectifying,.. on the hyper plane: $z_j = f^1(z_{in_j})$

(3) A hyper plane: $u_{in_k} = \mathrm{w}^2_{k1}\mathrm{z}_1 + \cdots + \mathrm{w}^2_{km_1}\mathrm{z}_{m_1} + \mathrm{b}^2_k$

(4) Folding, Rectifying,.. on the hyper plane: $u_k = f^2(y_{in_k})$

(5) A hyper plane: $y_{in_l} = \mathrm{w}^3_{l1}\mathrm{u}_1 + \cdots + \mathrm{w}^3_{lm_2}\mathrm{u}_2 + \mathrm{b}^3_l$

(6) Folding, Rectifying,.. on the hyper plane: $y_l = f^3(y_{in_l})$



A Desired Functionality in classification /Regression problems

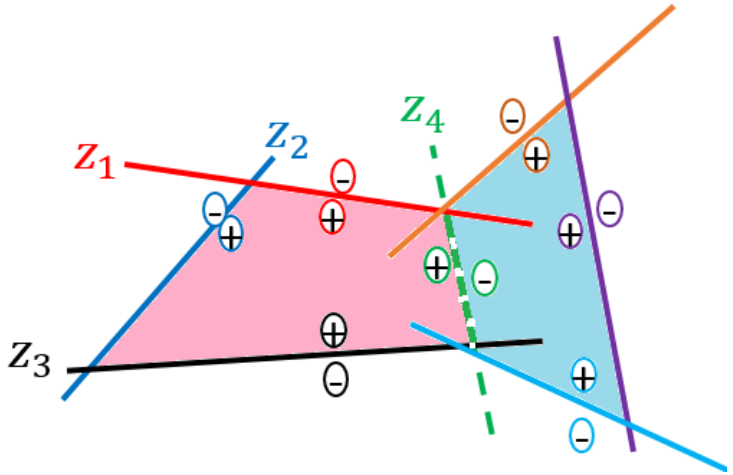
(1) A hyper plane: $z_{in_j} = w_{j1}^1 x_1 + \cdots + w_{jn}^1 x_n + b_j^1$

(2) Folding the hyper plane: $z_j = f^1(z_{in_j})$

(3) An "and" or "or logic gate for former folded hyper-planes is defined by "kth" neuron of second hidden layer 3, by which "kth" convex hyper-polygon will be resulted.

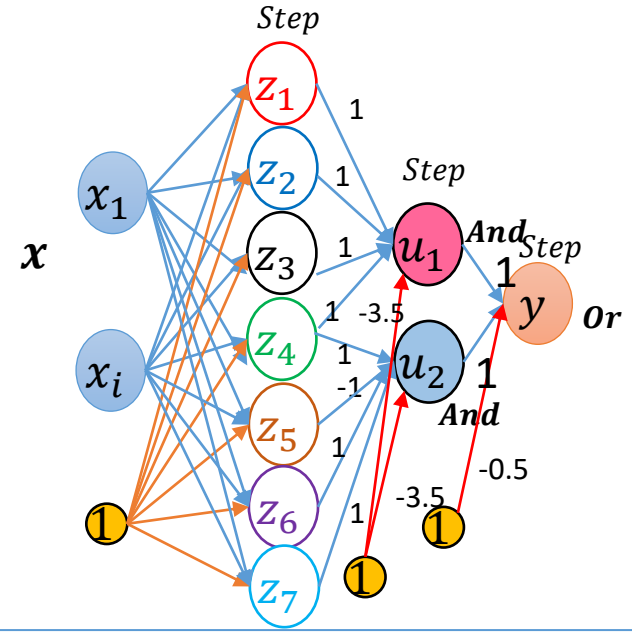
(4) An "and" or "or logic gate for former convex hyper-planes is defined by "lth" neuron of last layer, by which "lth" non-convex hyper-polygon will be resulted.

Example for $n = 2, m_1 = 7, m_2 = 2$ $m=1$



$$z_j = w_{j1}^1 x_1 + w_{j2}^1 x_2 + b_j^1, \quad \text{j=1,2,3,4,..,7}$$

$$u_k = w_{k1}^2 z_1 + w_{k2}^2 z_2 + b_k^2, \quad \text{k=1,2}$$

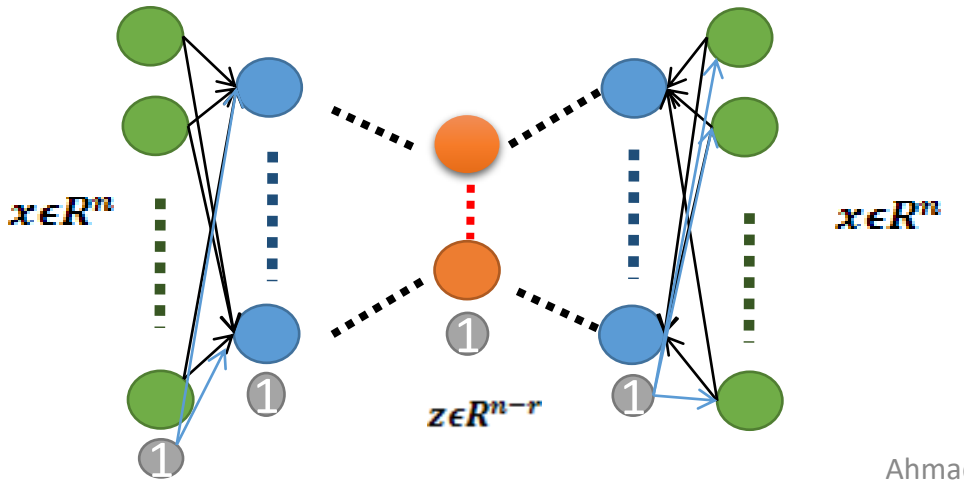


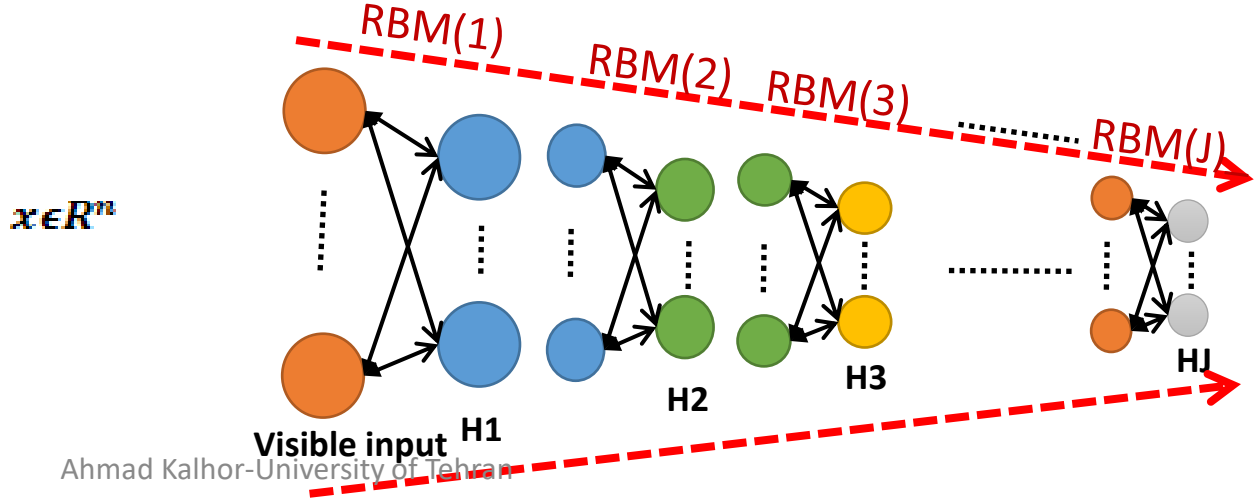
- A block of two FC layers can transform the input space to multi non-convex hyper- polygon partitions
- Using soft activation functions, a block of two FC layers can transform the input space to multi non-convex hyper- polygon volume maps

Some Notes about block of FC layers

1. A block of two or three FC layers are known as universal function approximator, through which any function by any desired accuracy can be approximated.
2. In comparison to a block of two FC layers, a block of three FC layers has better extrapolation (generalization) for unbounded regions and non-convex regions.

A block of FC layers with more than three layers are conventionally used in deep auto-encoders and cascaded restricted Boltzmann machines. In such blocks, each layer learns to encode or decode the taken data with a low change.





Some notes about FC layers

1. Fully connected layers are applied to a set of inputs reshaped as a vector; the spatial or temporal correlations among the inputs are not considered in its operation.
2. For high dimensional data, due to their massive wirings, they suffer from large memories, high computation load, and overfitting.
3. Although, they are appropriate for partitioning and mapping purposes, they are not ideal to remove disturbances, and filter and extract features from temporal, spatial , and multi modal signals.

1.1.2 Convolution Layers-Blocks-Modules*

Ideal to filter and encode/decode various, spatial, temporal and multi modal signals

- Simple Convolution
- Tiled Convolution
- Dilated Convolution
- Deconvolution (Transposed convolution)
- 1x1 Convolutions
- Flattened Convolutions
- Spatial and Cross-Channel convolutions
- Depth-wise Separable Convolutions
- Residual Blocks and types
- Grouped Convolutions
- Shuffled Grouped Convolutions

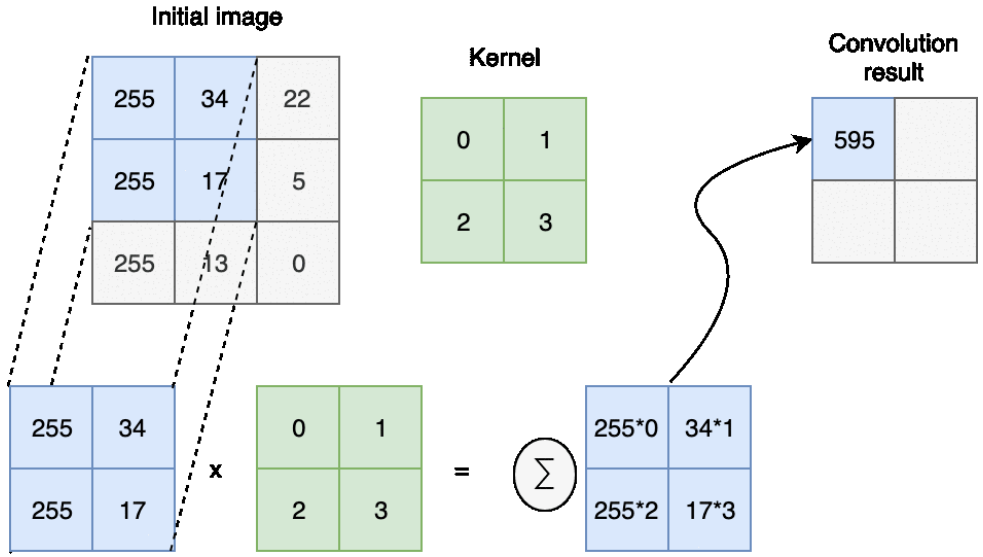
* Most of exampled are from https://ikhlestov.github.io/pages/machine-learning/convolutions-types/, Illarion Khlestov.

Simple Convolution

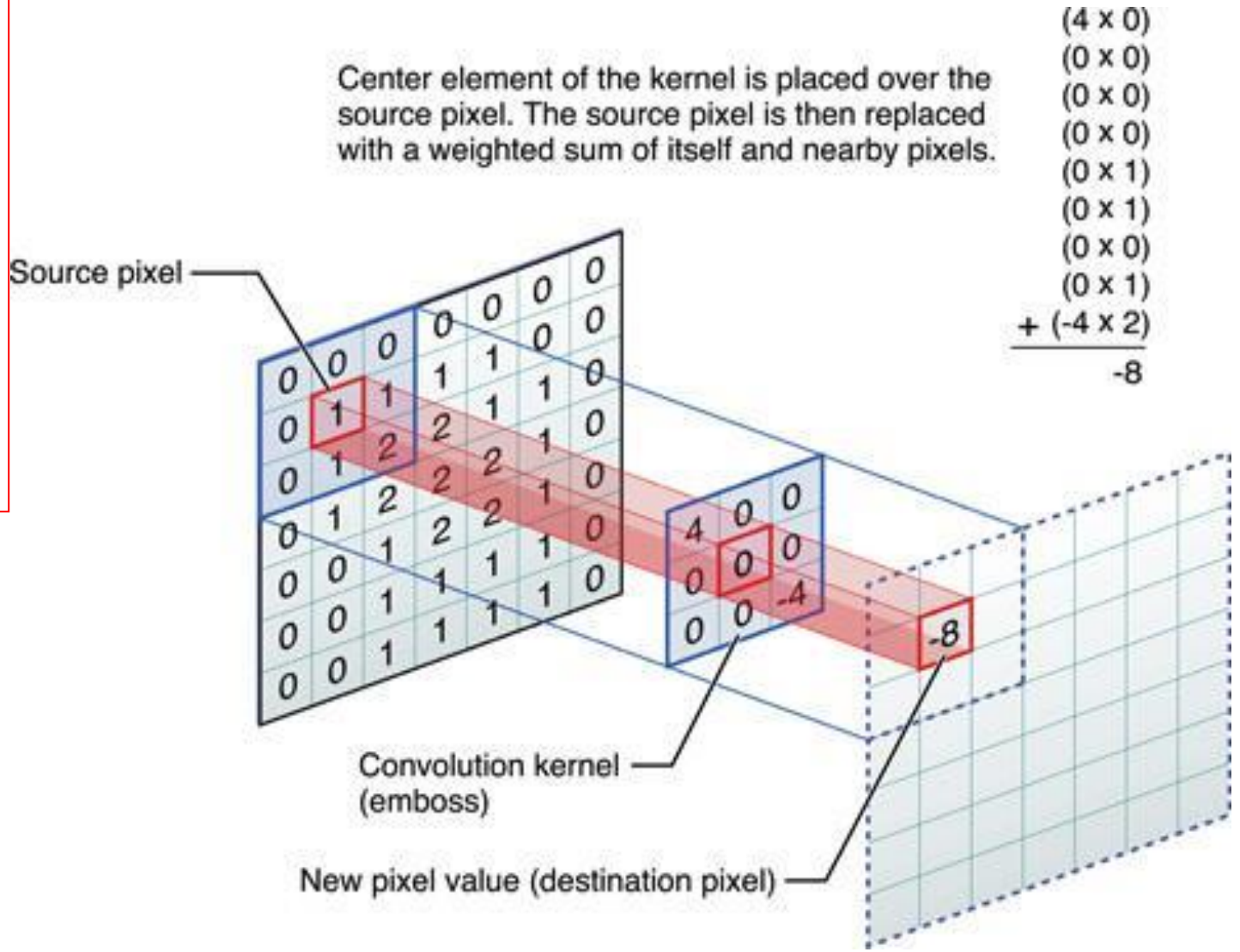
Take multiply dot products with same filter with some width/height shift.

Interesting because:

- Weights sharing and local connection
- it can capture and intensify all those patches which are adequately similar to the kernel and remove other ones by “relu”
- It can be interpreted as a filter that remove all patches which have weak linear correlation with the kernel



Example of convolution on two dimensional signal (image)

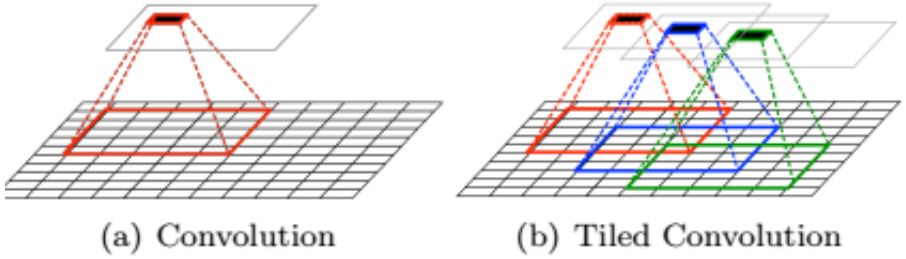


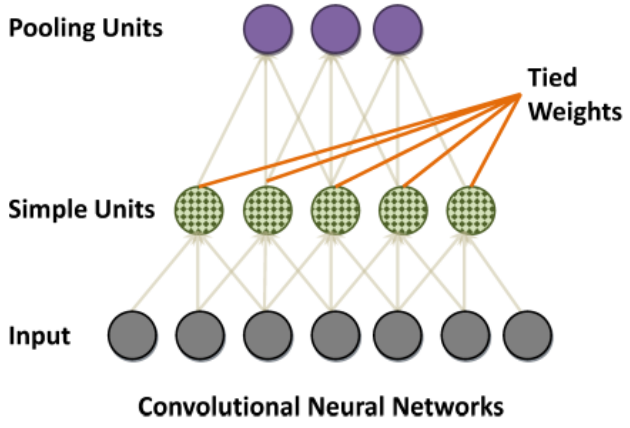
Tiled Convolution

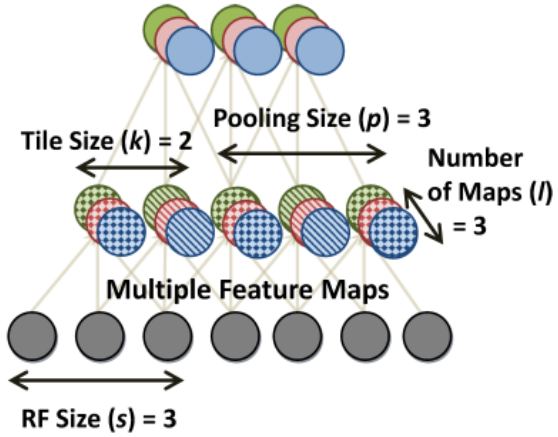
- It means that we can learn multiples feature maps rather than one feature map by considering several different filters
- In tiled convolution we can provide different kinds of invariance.
- Separate kernels are learned within the same layer

Example of Tiled convolution on one dimensional signal(time series)

Example of Tiled convolution on two dimensional signal







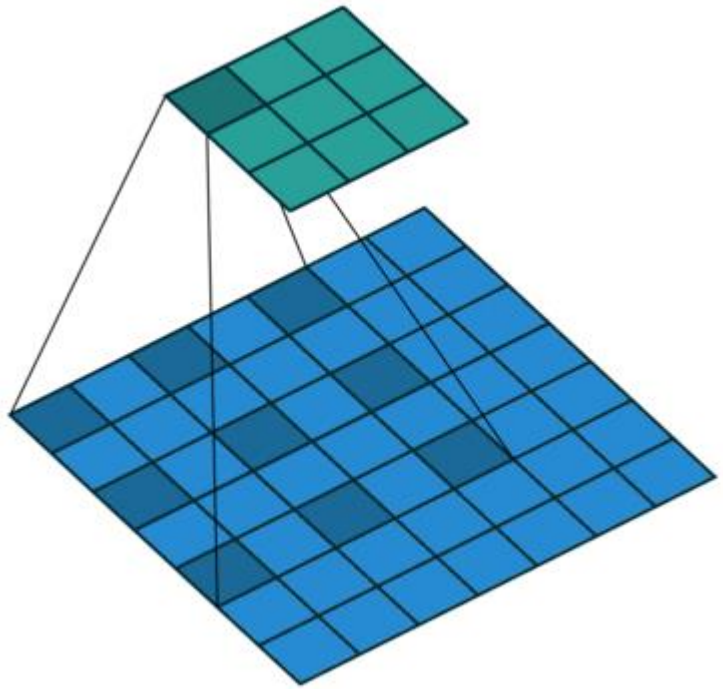
Some notes about the convolution layer

1. The convolution layer is a variant of the convolution operation used in LTI systems
2. A convolution layer actually transform an input (spatial, temporal, or multi modal) signal to several feature maps.
3. All units of feature maps just after convolution may be activated by applying an activation function like “relu”.
4. Using a filter, each feature map captures a certain feature from different local regions of the former signal.
5. Features, which are captured by filters, are actually frequently repeating sub-patterns within a signal.
6. The kernel size and the number of filters depend to the size and the number of the existing independent features, respectively.
7. Using stride=1 and padding, the size of a feature map is equal to the spatial size of the signal but using stride>1 (stride<1), the signal becomes down-sampled (up-sampled) by the convolution layer.
8. The resulting feature maps from a convolution layer, can be convolved again through a new convolution layer.
9. Through using a black of sequenced convolution layers (may come with activation functions, pooling and normalizing layers), actually redundancies and disturbances are removed and exclusive features for appropriate classification or regression problem will be appeared.

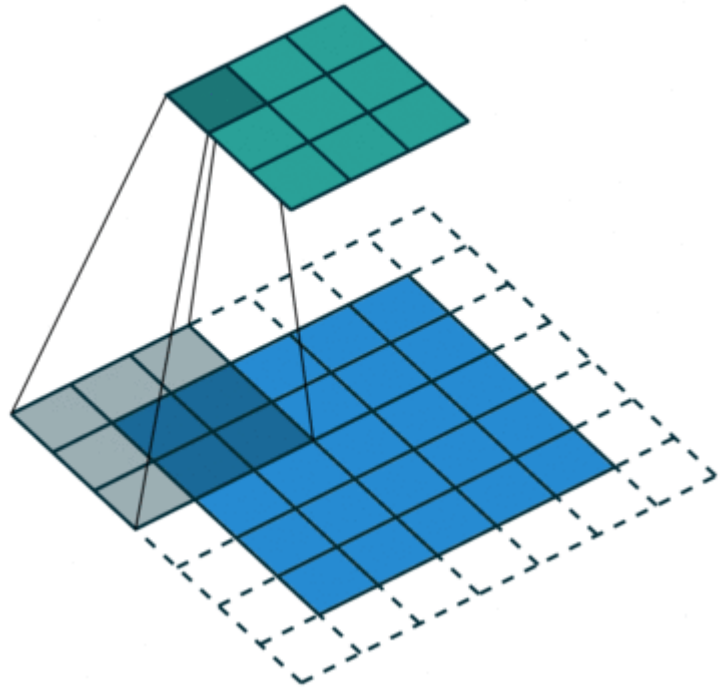
Dilated Convolution

To convolve and down-sample signals with very large spatial/temporal size

It is **a technique that expands the kernel (input) by inserting holes between the its consecutive elements**. In simpler terms, it is same as convolution but it involves pixel skipping, so as to cover a larger area of the input. ... In essence, normal convolution is just 1-dilated convolution



Dilated Convolution (l=2)

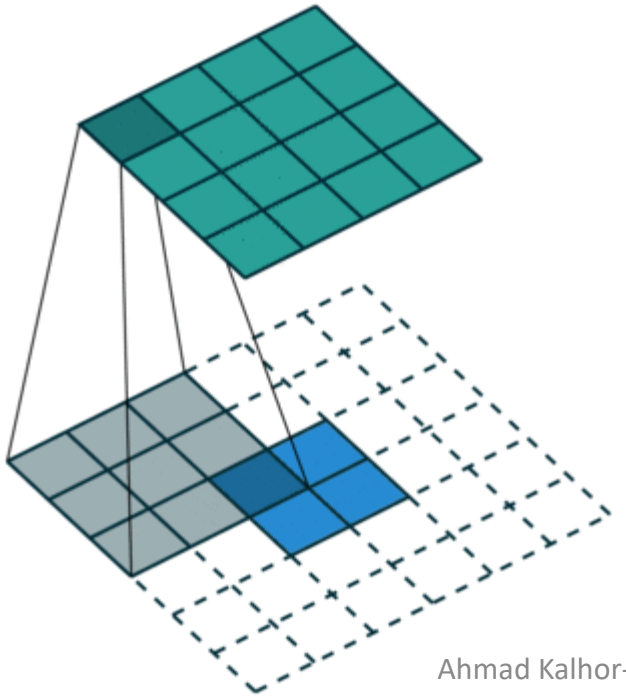


Standard Convolution (l=1)

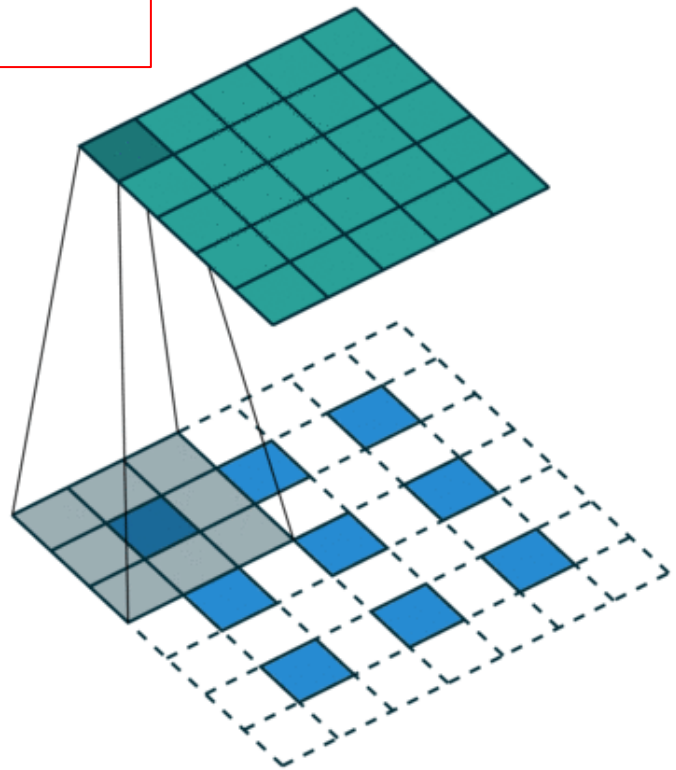
Deconvolution (Transposed Convolution)

Transposed convolution can be seen as the backward pass of a corresponding traditional convolution.
Transpose Convolution is a convolution layer which reverses the operation done by the corresponding convolution.
High pass Filter (corresponding Conv.)→ Low pass Filter (Tran. Conv.)
Smooth Filter (corresponding Conv.) → Difference Filter (Tran. Conv.)

Visually, for a transposed convolution with stride one and no padding, we just pad the original input (blue entries) with zeroes (white entries)).



In case of stride two and padding, the transposed convolution would look like this

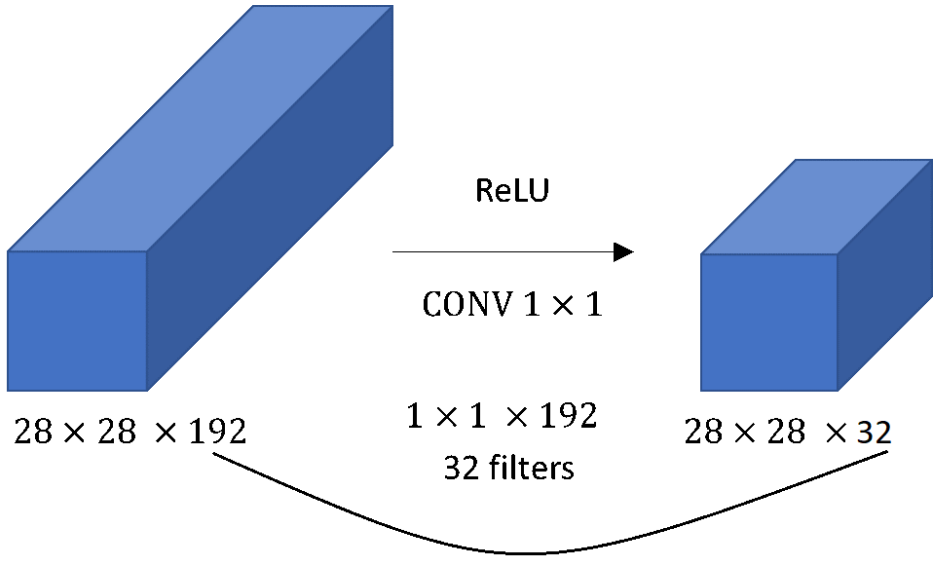


1x1 Convolutions

Initially 1x1 convolutions were proposed at Network-in-network(NiN). After they were highly used in GoogleNet architecture. Main features of such layers:

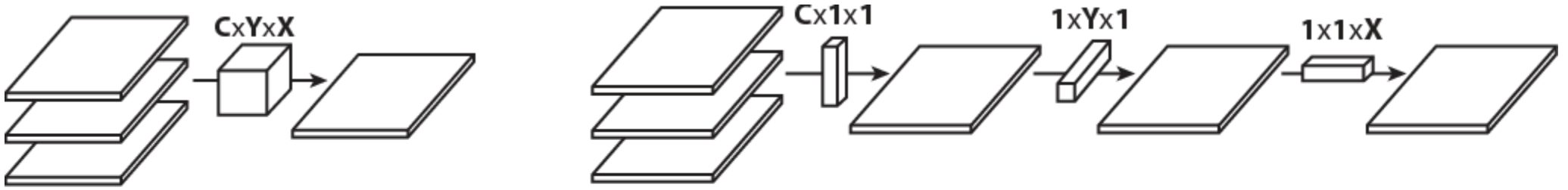
- Reduce or increase dimensionality
- Apply nonlinearity again after convolution
- Can be considered as “feature pooling”

They are used in such way: we have image with size 28x28x192, where 192 means features, and after applying 32 1x1 convolutions filters we will get images with 28x28x32 dimensions.



Flattened Convolutions

Were published in [Flattened Convolutional Neural Networks for Feedforward Acceleration](). Reason of usage same as 1x1 convs from NiN networks, but now not only features dimension set to 1, but also one of another dimensions: width or height.



(a) 3D convolution

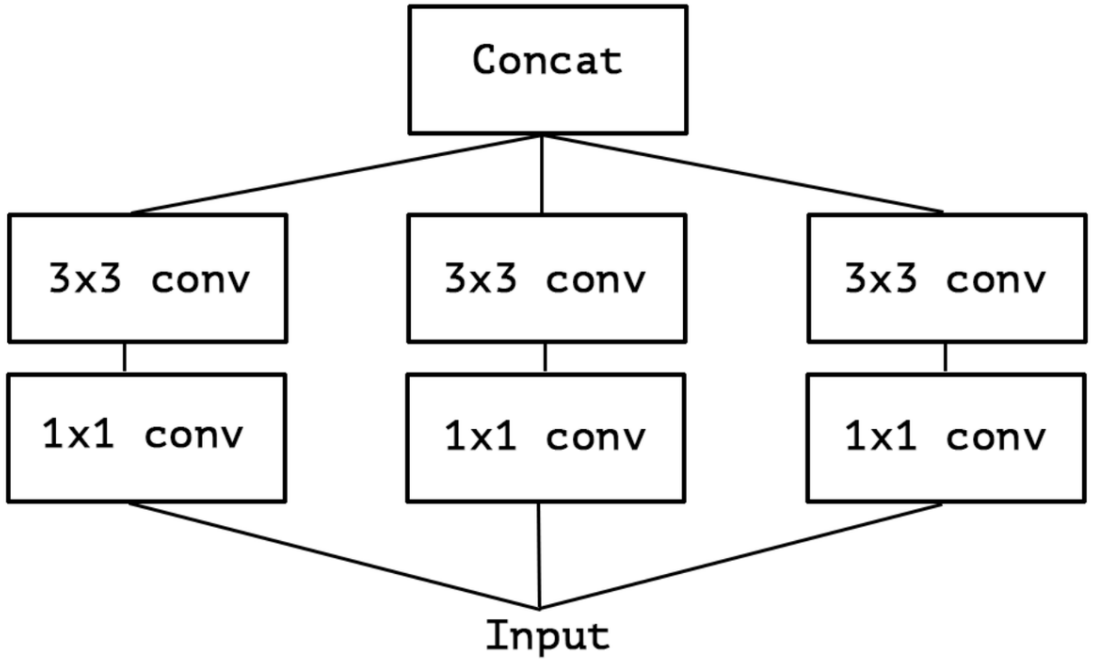
(b) 1D convolutions over different directions

The number of operations at each feature map is= a*a*(C*Y*X)

The number of operations at each feature map is= a*a*(C+Y+X)

Spatial and Cross-Channel convolutions

First this approach was widely used in **Inception network**. Main reason is to split operations for cross-channel correlations and at spatial correlations into a series of independently operations. Spatial convolutions means convolutions performed in **spatial dimensions** - **width** and **height**



- Grouping convolutions in independent parallel paths cause acceleration in computations and reduction in the required memory

Inception Module

Inception module is introduced by Szegedy *et al*. * which can be seen as a logical culmination of NIN. They use variable filter sizes to capture different visual patterns of different sizes, and approximate the optimal sparse structure by the inception modul

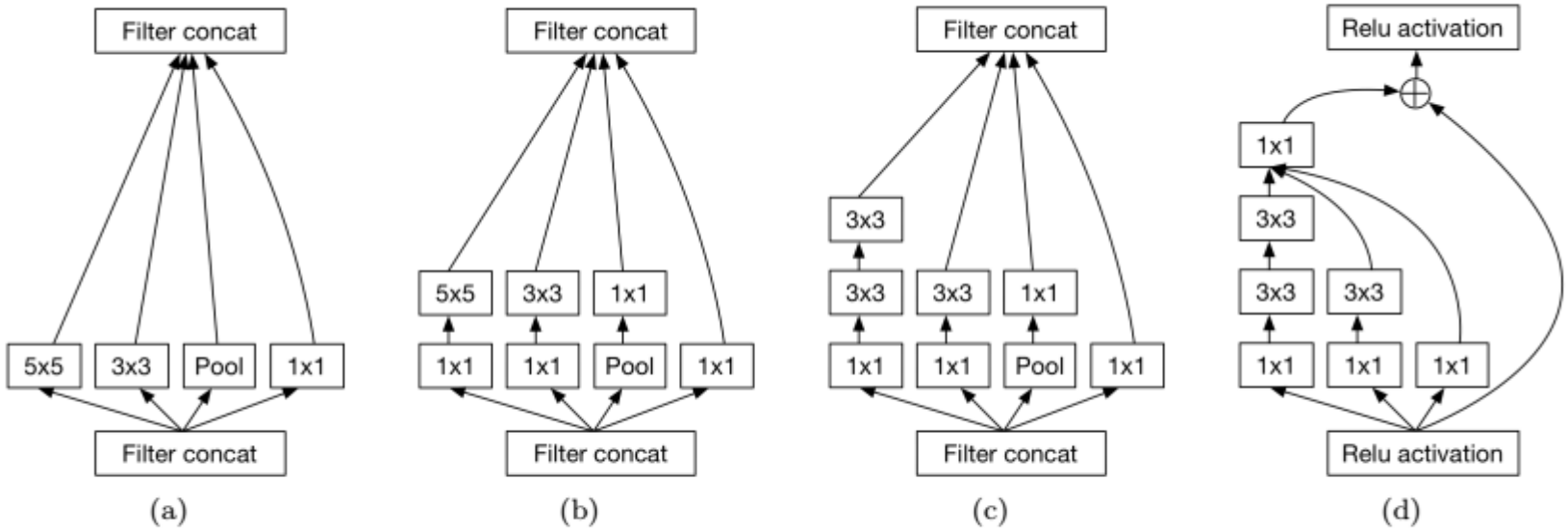


Figure 5: (a) Inception module, naive version. (b) The inception module used in [10]. (c) The improved inception module used in [41] where each 5×5 convolution is replaced by two 3×3 convolutions. (d) The Inception-ResNet-A module used in [42].

❖ Using parallel convolution paths with different kernel sizes increases the chance of better feature extraction

* C. Szegedy, W. Liu, Y. Jia, P. Sermanet, S. Reed, D. Anguelov, D. Erhan, V. Vanhoucke, A. Rabinovich, Going deeper with convolutions, in: Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR), 2015,
pp. 1–9.

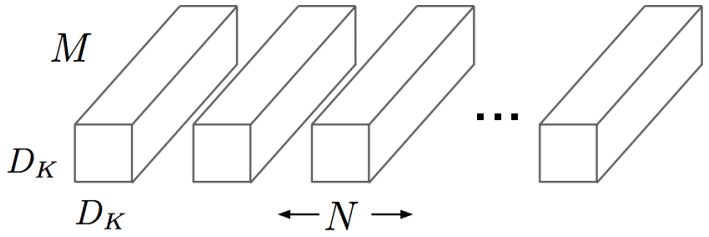
Depthwise Separable Convolutions

A lot about such convolutions published in the (Xception paper) or (MobileNet paper).
Consist of:

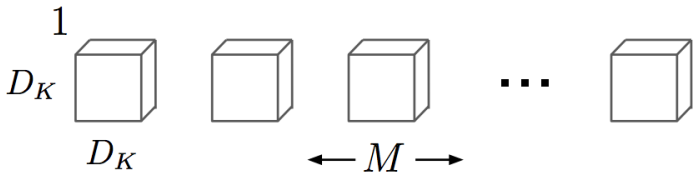
- **Depthwise convolution**, i.e. a spatial convolution performed independently over each channel of an input.
- **Pointwise convolution**, i.e. a 1x1 convolution, projecting the channels output by the depthwise convolution onto a new channel space.

Difference between Inception module and separable convolutions:

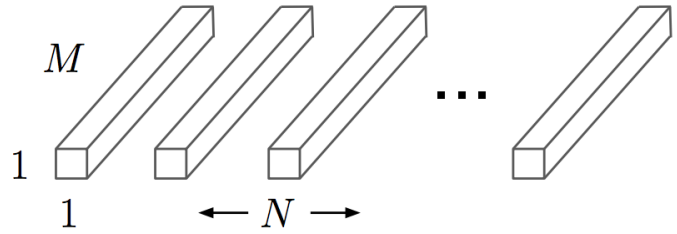
- Separable convolutions perform first channel-wise spatial convolution and then perform 1x1 convolution, whereas Inception performs the 1x1 convolution first.
- depthwise separable convolutions are usually implemented without non-linearities



(a) Standard Convolution Filters



(b) Depthwise Convolutional Filters



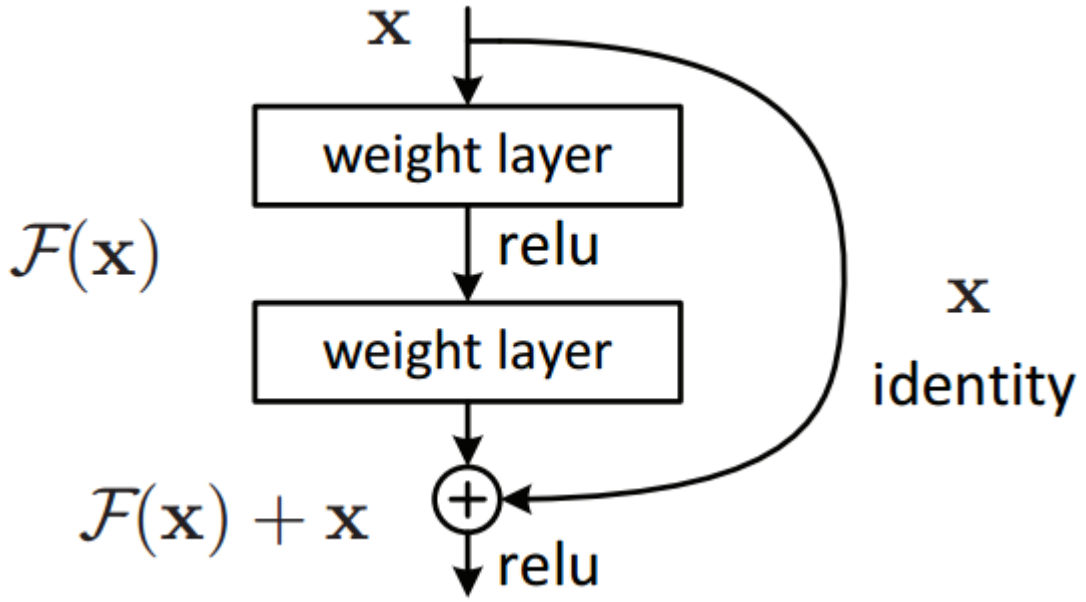
(c) 1×1 Convolutional Filters called Pointwise Convolution in the context of Depthwise Separable Convolution

❖ Using Depthwise convolution decreases the computation load of 3D-convolution

Residual Blocks

To avoid missing information and provide a solution for vanishing gradient

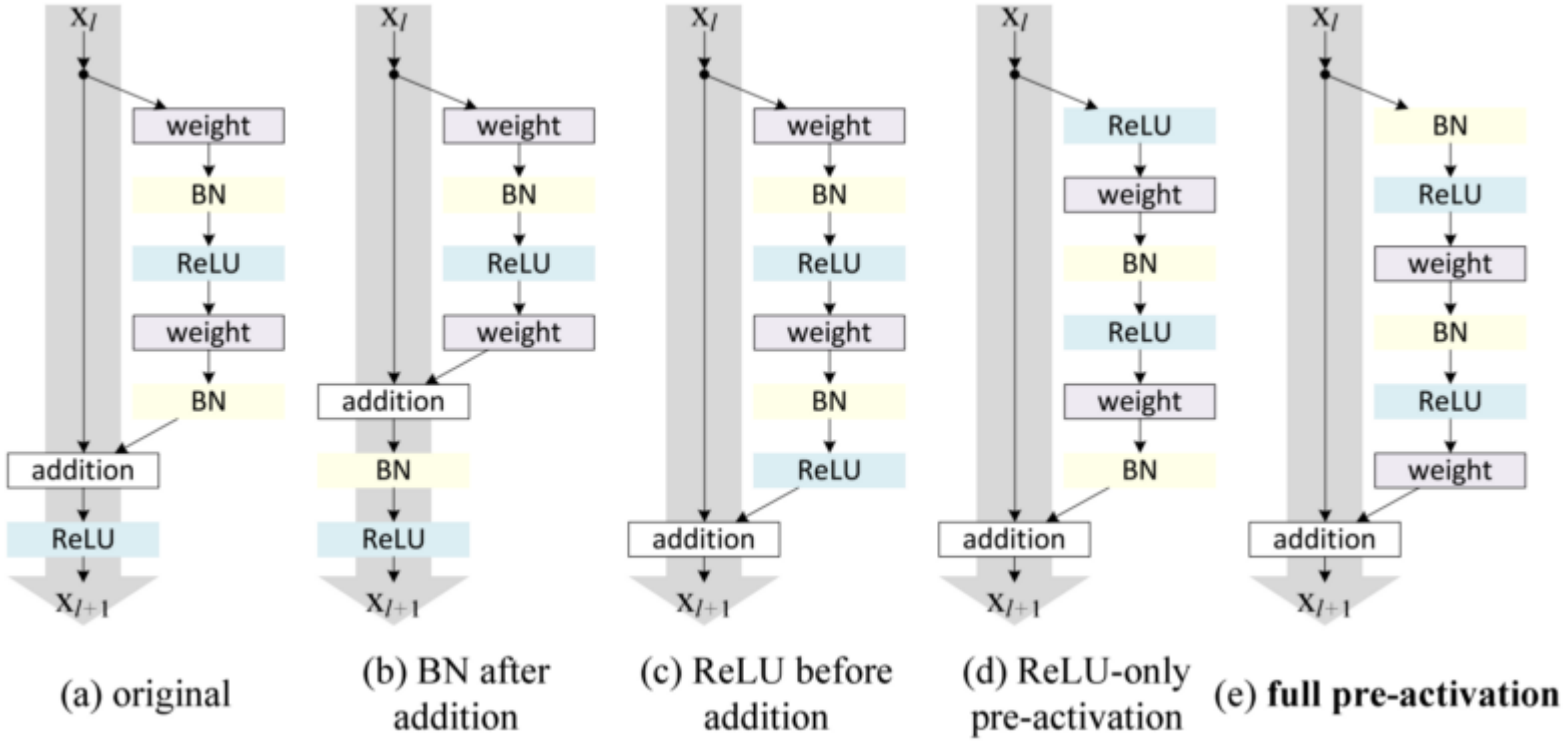
In traditional neural networks, each layer feeds into the next layer. In a network with residual blocks, each layer feeds into the next layer and directly into the layers about 2–3 hops away. That's it. But understanding the intuition behind why it was required in the first place, why it is so important, and how similar it looks to some other state-of-the-art architectures is where we are going to focus on. There is more than one interpretation of why residual blocks are awesome and how & why they are one of the key ideas that can make a neural network show state-of-the-art performances on a wide range of tasks.



❖ Applying an identity path to convolution, residual block causes that features to be captured in a difference evolving learning manner without missing information.

Different forms of residual blocks

The image below shows how to arrange the residual block and identity connections for the optimal gradient flow. It has been observed that pre-activations with batch normalizations generally give the best results (i.e., the right-most residual block in the image below gives the most promising results).



Grouped Convolutions

Grouped convolutions were initial mentioned in AlexNet, and later reused in ResNeXt. Main motivation of such convolutions is to reduce computational complexity while dividing features on groups.

The image below shows multiple interpretations of a residual block.

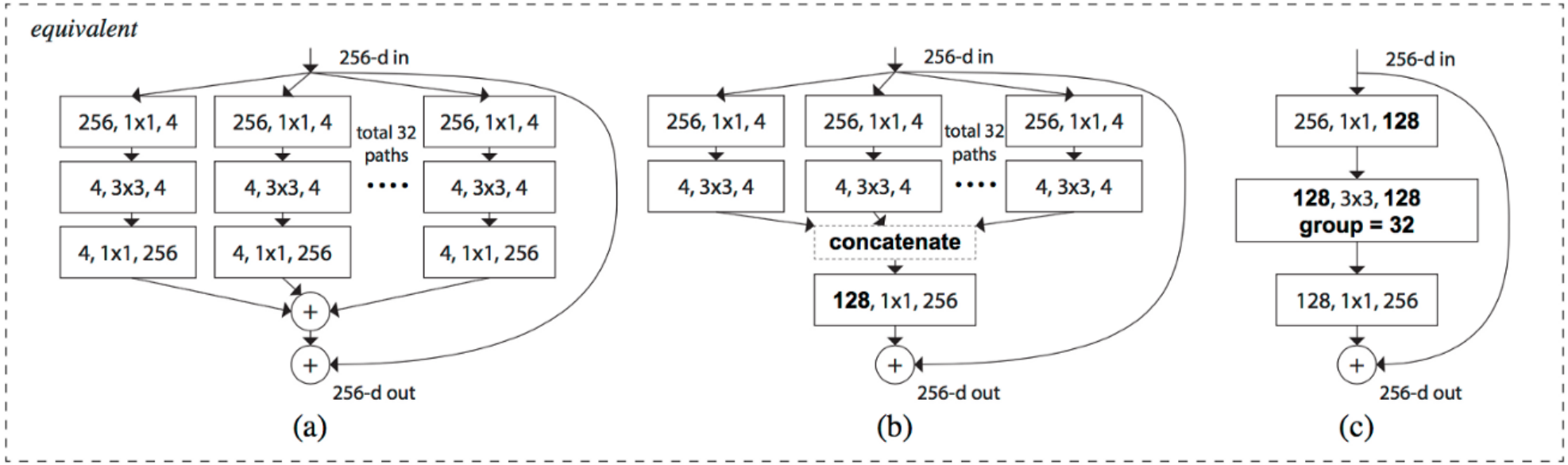


Figure 3. Equivalent building blocks of ResNeXt. **(a)**: Aggregated residual transformations, the same as Fig. 1 right. **(b)**: A block equivalent to (a), implemented as early concatenation. **(c)**: A block equivalent to (a,b), implemented as grouped convolutions [24]. Notations in **bold** text highlight the reformulation changes. A layer is denoted as (# input channels, filter size, # output channels).

Shuffled Grouped Convolutions

Shuffle Net proposed how to eliminate main side effect of the grouped convolutions that “outputs from a certain channel are only derived from a small fraction of input channels”.
They proposed shuffle channels in such way(layer with gg groups whose output has g×ng×n channels):

- reshape the output channel dimension into (g,n)(g,n)
- transpose output
- flatten output bac

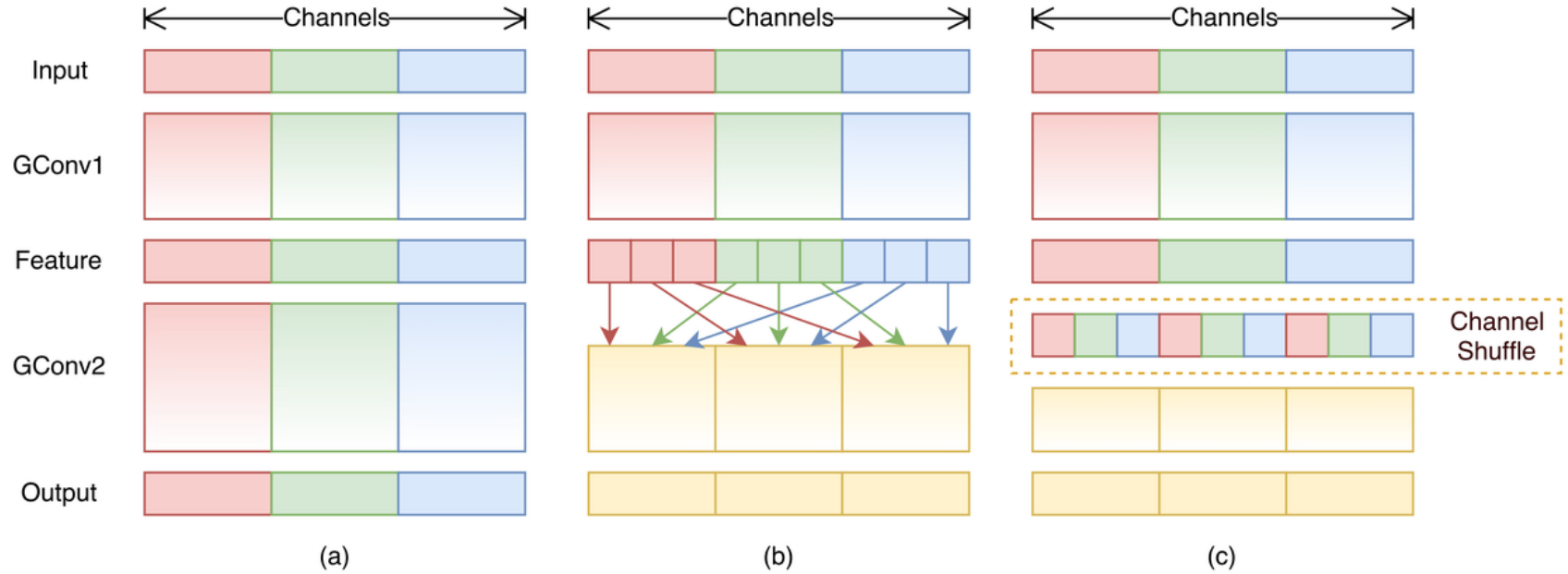


Figure 1: Channel shuffle with two stacked group convolutions. GConv stands for group convolution. a) two stacked convolution layers with the same number of groups. Each output channel only relates to the input channels within the group. No cross talk; b) input and output channels are fully related when GConv2 takes data from different groups after GConv1; c) an equivalent implementation to b) using channel shuffle.

Some notes about convolution layers

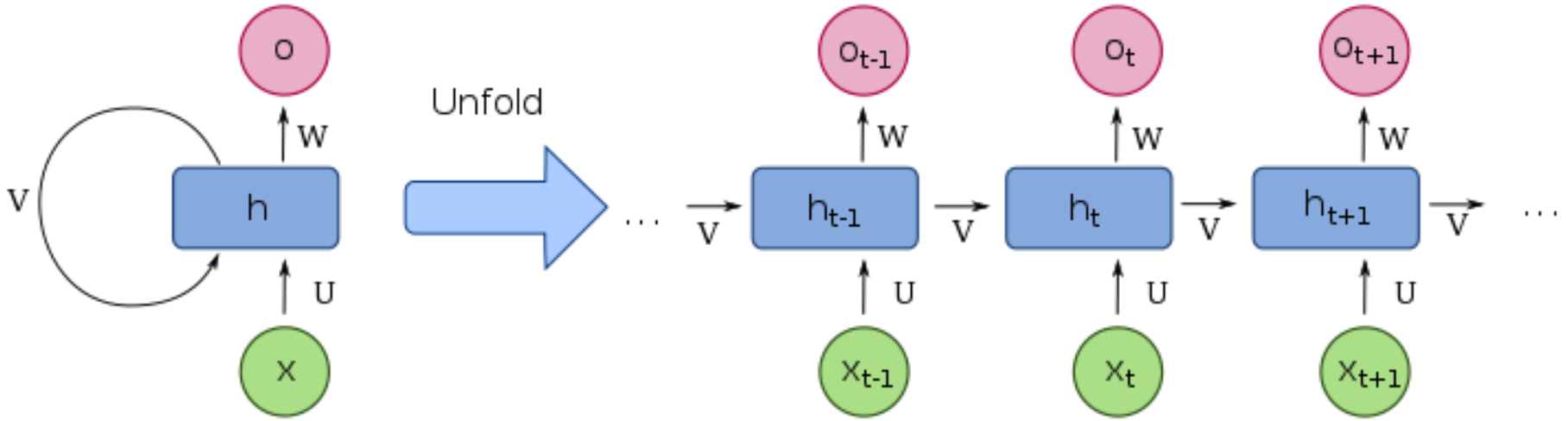
1. There are many extensions of simple convolutional layers.
2. Deconvolution layers are introduced as the backward pass of their corresponding convolution.
3. Residual blocks use a direct skip connection from inputs to outputs(as an identity function) to avoid missing information and to solve the problem of vanishing gradient. In addition, many other extended convolution layers use such skip connection in their structures.
4. Some convolutional layers such as "NiN" and flattened convolutions provide a considerable drop in computations by using point-wise and depth-wise convolution instead of using simple 3D convolution operations.
5. Some convolutional layers such as inception module by using some parallel convolutions with different resolutions have tried to provide better accuracy.
6. Grouped convolutions as well as shuffled grouped convolutions use several similar form and parallel convolution blocks (with an identity skip connection) in their structures. Each convolution block includes point-wise and depth-wise convolutions.

1.1.3 Recurrent Neural Networks

Ideal to retrieve short/long dependencies among the sequenced samples of a signals

- Simple RNN Module
- LSTM Module
- GRU Module
- Bidirectional RNN layer
- Bidirectional Deep RNNs
- TimeDistributed layer
- ConvLSTM layer

Simple RNN Module



$$\boldsymbol{h}_t = \mathbf{f}(\mathrm{V}\boldsymbol{h}_{t-1} + \mathrm{U}\boldsymbol{x}_t)$$

$$\boldsymbol{o}_t = \mathbf{g}(\mathrm{W}\boldsymbol{h}_t)$$

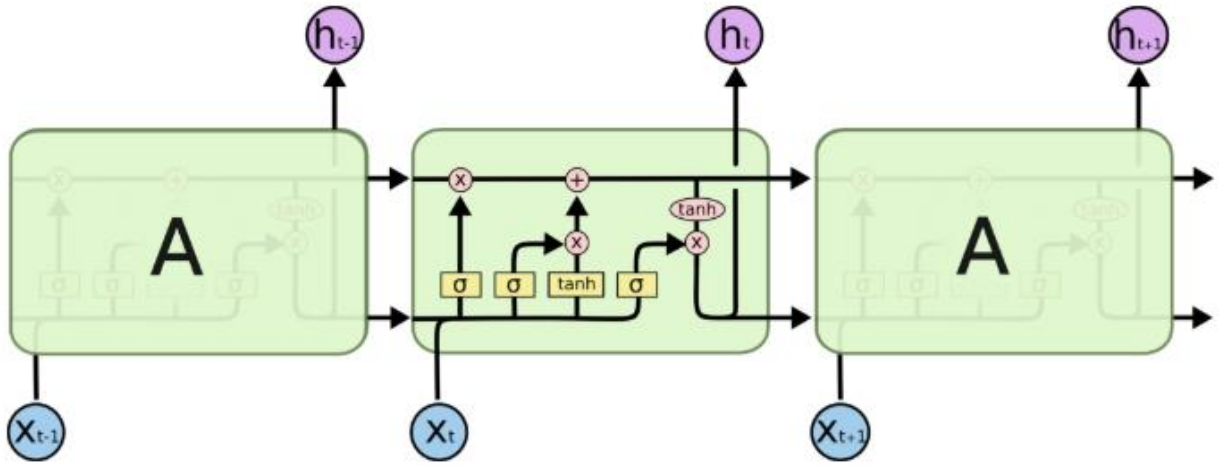
$$\boldsymbol{o}_t = \mathbf{g}\Big(\mathrm{W}\mathbf{f}\big(\mathrm{V}\mathbf{f}\big(\mathrm{V}\ldots(\mathrm{V}\mathbf{f}(\mathrm{V}\boldsymbol{h}_0 + \mathrm{U}\boldsymbol{x}_1)\ldots + \mathrm{U}\boldsymbol{x}_{t-1}\big)\big) + \mathrm{U}\boldsymbol{x}_t\big)\Big), t = 1,2,\cdots$$

Some notes

1. RNN actually make a set of nonlinear first order difference equations.
2. The current state $\boldsymbol{h}_t$ is affected by both exogenous input $\boldsymbol{x}_t$ and the former state $\boldsymbol{h}_{t-1}$.
3. The output $\boldsymbol{o}_t$ is a function of hidden state $\boldsymbol{h}_t$ at each time t .
4. Such equations can provide a memory from the short dependencies in a sequenced patterns
5. $Activation\ functions$: $f, g \epsilon \{Relu, tanh, sigm, sign, identity \ldots.\}$

LSTM (long short term memory)

Hochreitor & Shmidhuber 1997



$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] \; + \; b_f\right)$$

$$i_t = \sigma\left(W_i \cdot [h_{t-1}, x_t] \; + \; b_i\right)$$

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] \; + \; b_C)$$

$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

$$o_t = \sigma\left(W_o \; [h_{t-1}, x_t] \; + \; b_o\right)$$

$$h_t = o_t * \tanh\left(C_t\right)$$

$$\hat{y}_t = f(V.h_t + b_v)$$

Some notes:

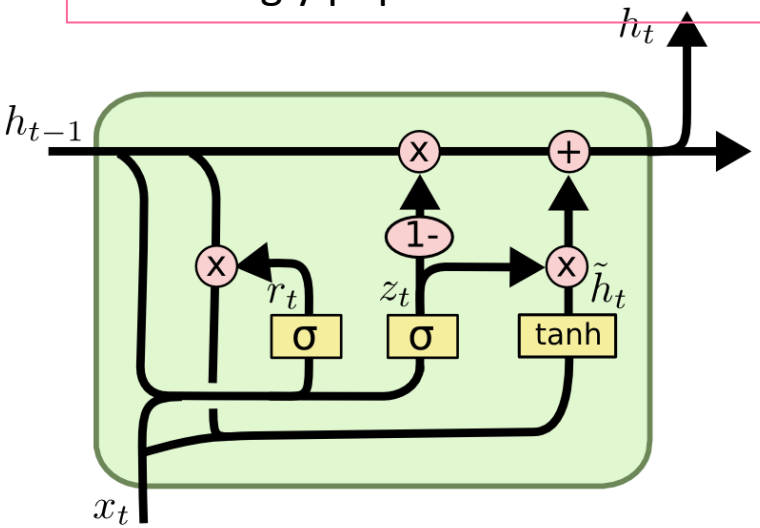
1. LSTM is a module of f*our interacted layers*.
2. A cell state is a key concept in a LSTM proving (packaging and carrying) all informative data required to save long/short dependencies among the sequenced patterns.
3. Using exogenous input and the hidden state, cell state interacts by three independent gates: forget, write, and read gates.
4. Some information on the cell state is forgotten by the forget gate.
5. Using exogenous input and the hidden state, a package of informative data is added to the cell state by write gate.
6. The hidden state is provided from the cell state by read gate.
7. The output is a function of the hidden state.

GRU (Gated Recurrent Unit)

Cho, et al. (2014)

Many extensions of the LSTM have been introduced. A slightly more dramatic variation on the LSTM is the Gated Recurrent Unit, or GRU.

GRU combines the forget and input gates into a single "update gate." It also merges the cell state and hidden state, and makes some other changes. The resulting model is simpler than standard LSTM models, and has been growing increasingly popular.



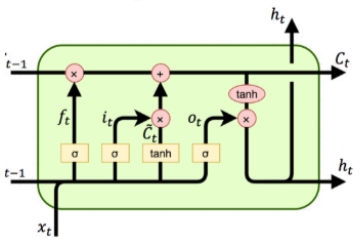
$$z_t = \sigma\left(W_z \cdot [h_{t-1}, x_t]\right)$$

$$r_t = \sigma\left(W_r \cdot [h_{t-1}, x_t]\right)$$

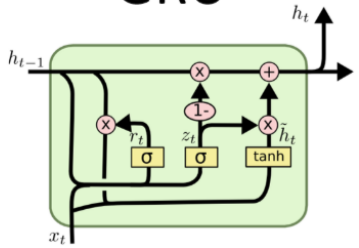
$$\tilde{h}_t = \tanh\left(W \cdot [r_t * h_{t-1}, x_t]\right)$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

LSTM



GRU

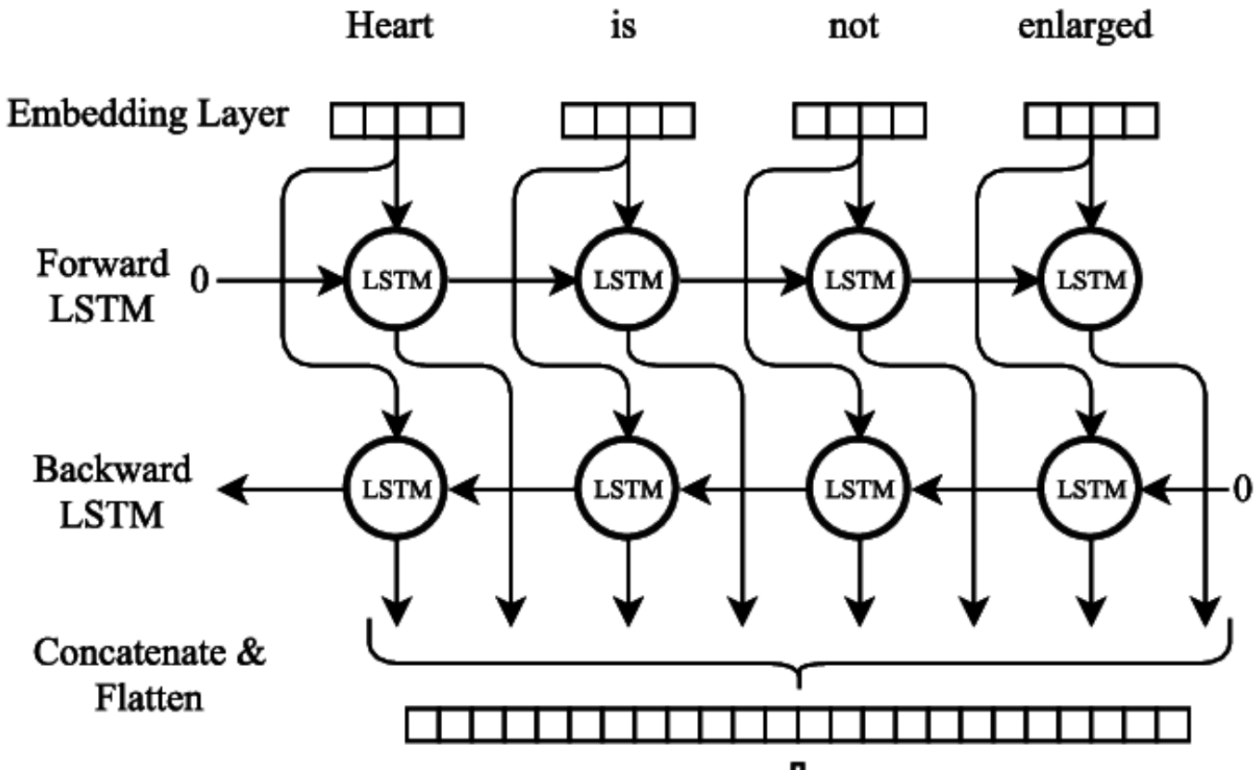


Bidirectional RNNs

A **Bidirectional LSTM**, or **biLSTM**, is a sequence processing model that consists of two LSTMs:

One taking the input in a forward direction, and the other in a backwards direction.
BiLSTMs effectively increase the amount of information available to the network, improving the context available to the algorithm (e.g. knowing what words immediately follow *and* precede a word in a sentence).

Image Source: Modelling Radiological Language with Bidirectional Long Short-Term Memory Networks, Cornegruta et al.

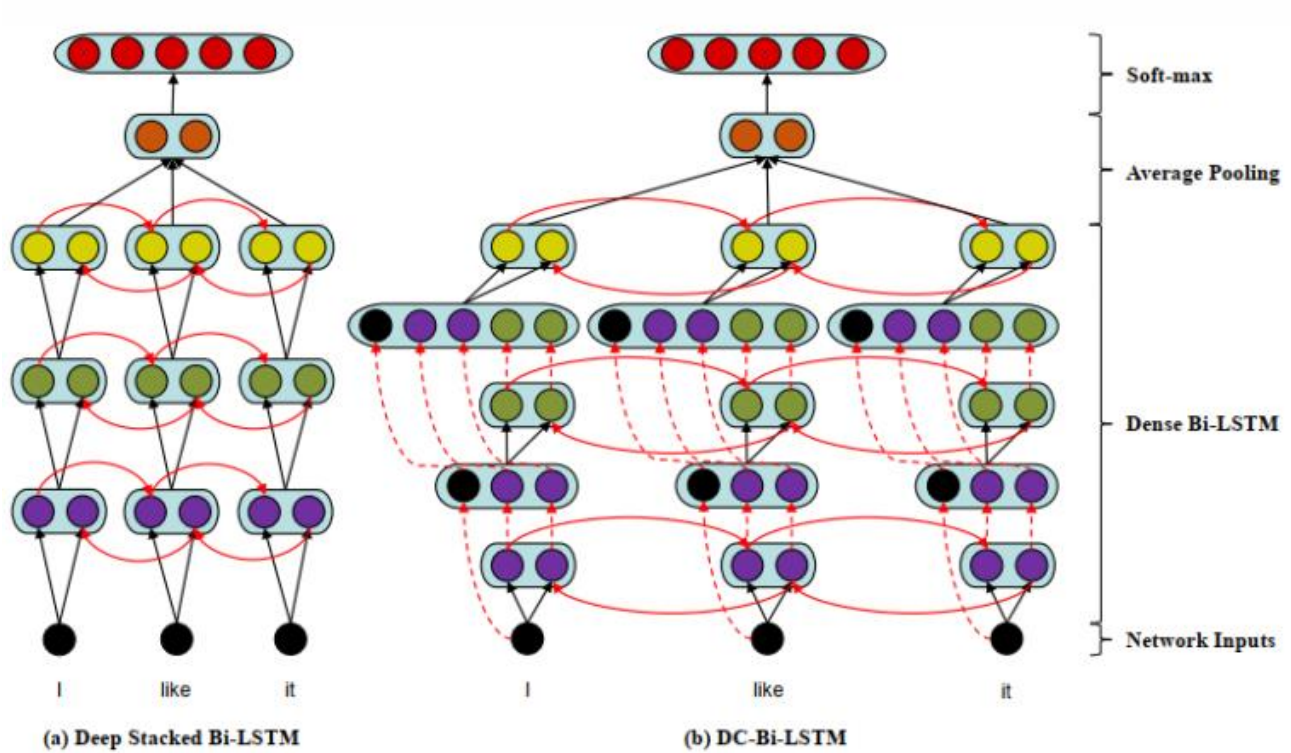


It can be used in categorization
Missed words prediction and so on.

Deep (Bidirectional) RNNs

A block of one or more than one LSTM or Bi-LSTM layers

- **Deep (Bidirectional) RNNs** are similar to Bidirectional RNNs, only that we now have multiple layers per time step. In practice this gives us a higher learning capacity (but we also need a lot of training data)



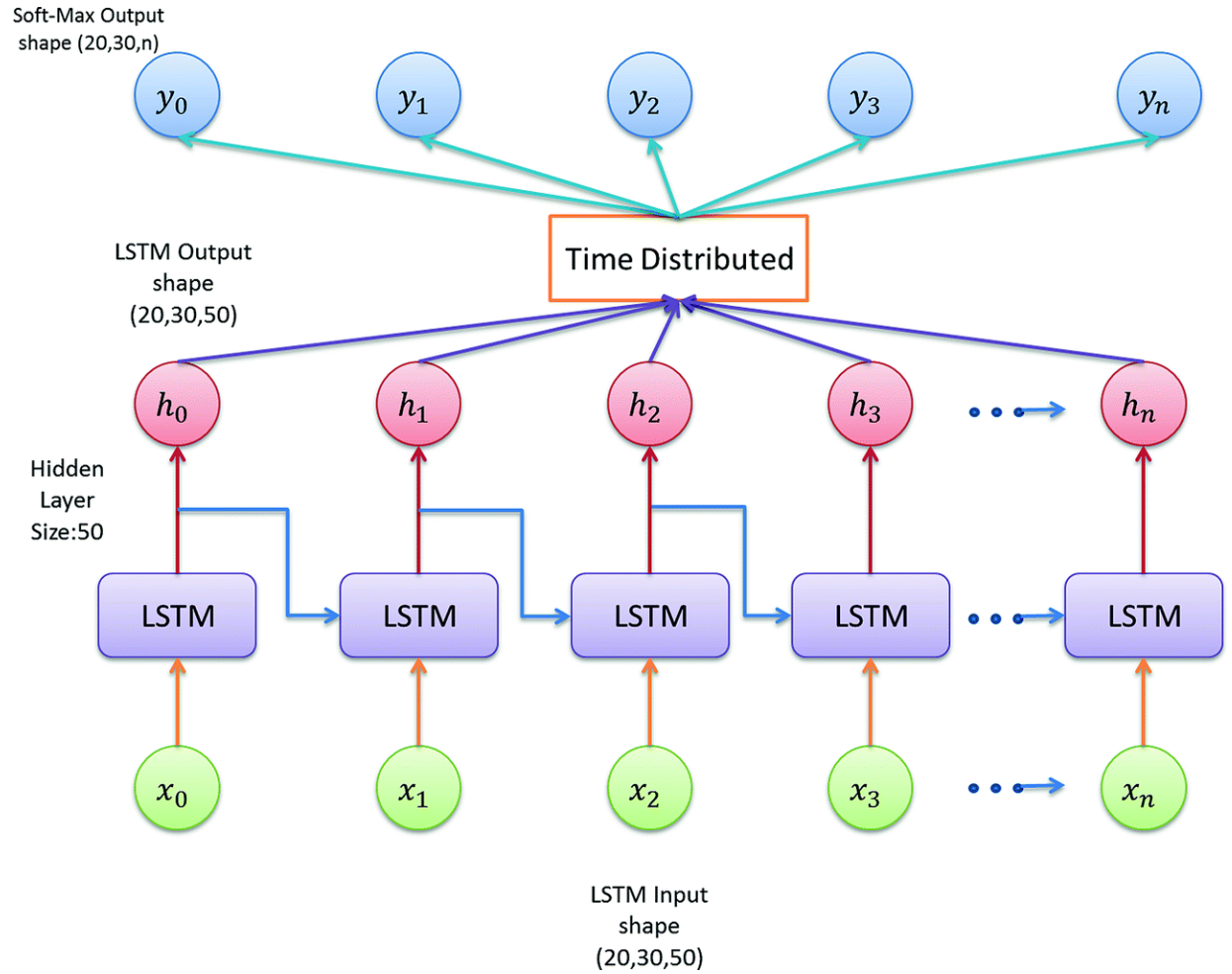
Deep Stacked Bi-LSTM

Densely Connected Bidirectional

Time distributed Layer

to reduce the required memory in processing multi sequenced samples(images) to predict the target

Time Distributed layer is very useful to work with time series data or video frames.
It allows **to use a layer for each input**. That means that instead of having several input "models", we can use "one model" applied to each input. Then GRU or LSTM can help to manage the data in "time".



Time step: **the number of past samples of a sequence which are used in a LSTM to predict the targets.**

ConvLSTM

Xingjian Shi Zhourong, et al (2015)

- To provide memory with sequential images, one approach is using **ConvLSTM** layers.
- **ConvLSTM** is a Recurrent layer, just like the LSTM, but internal matrix multiplications are exchanged with convolution operations. As a result, the data that flows through the ConvLSTM cells keeps the input dimension (3D in our case) instead of being just a 1D vector with features.
- Using shared weights, convolution provide more appropriate processing and less computations in comparison to matrix product.

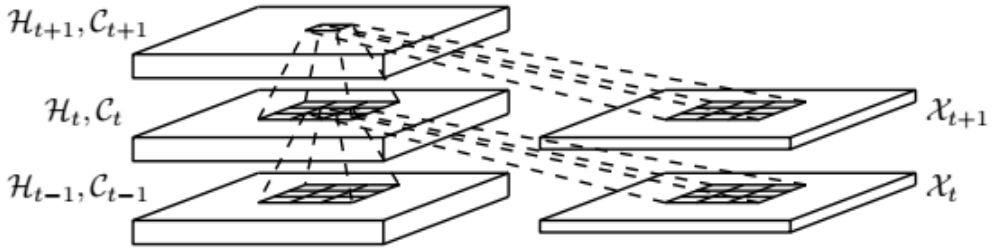
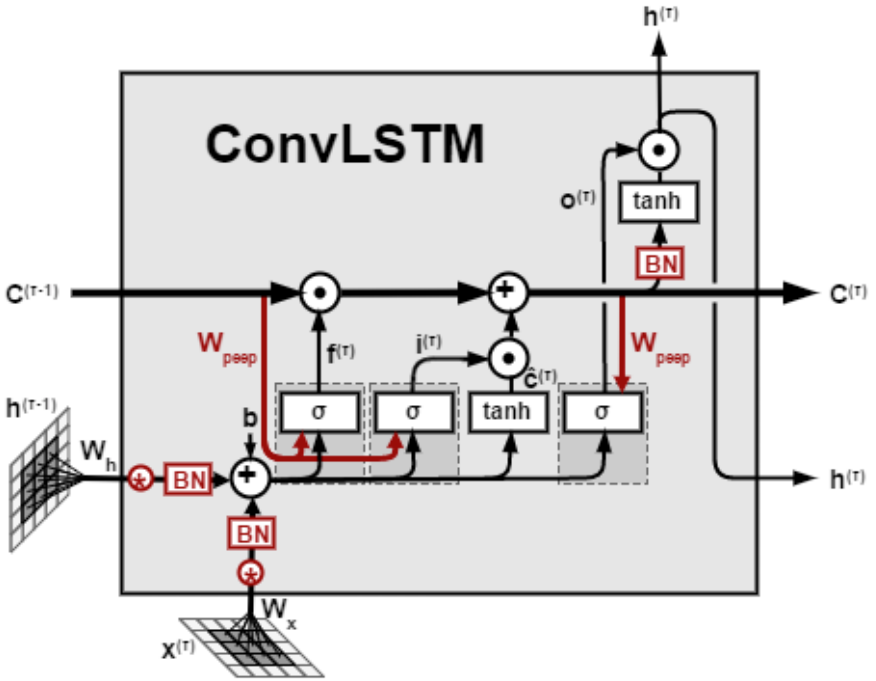


Figure 2: Inner structure of ConvLSTM

$$i_t = \sigma(W_{xi} * \mathcal{X}_t + W_{hi} * \mathcal{H}_{t-1} + W_{ci} \circ \mathcal{C}_{t-1} + b_i)$$
$$f_t = \sigma(W_{xf} * \mathcal{X}_t + W_{hf} * \mathcal{H}_{t-1} + W_{cf} \circ \mathcal{C}_{t-1} + b_f)$$
$$\mathcal{C}_t = f_t \circ \mathcal{C}_{t-1} + i_t \circ \tanh(W_{xc} * \mathcal{X}_t + W_{hc} * \mathcal{H}_{t-1} + b_c)$$
$$o_t = \sigma(W_{xo} * \mathcal{X}_t + W_{ho} * \mathcal{H}_{t-1} + W_{co} \circ \mathcal{C}_t + b_o)$$
$$\mathcal{H}_t = o_t \circ \tanh(\mathcal{C}_t)$$



where '$*$' denotes the convolution operator and '$\circ$', as before, denotes the Hadamard product (**element-wise product**)

ConvLSTM 2D,3D

1.1.4 Attention Layers-Modules

An improving mechanism for RNNs by applying an interface connecting the encoder and decoder

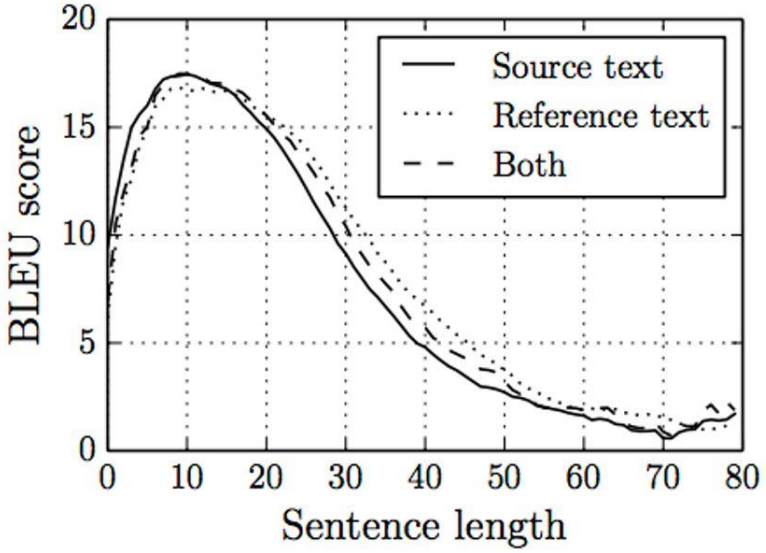
- In translation machines, LSTM/GRU as a seq2seq model can not predict successful translation for a sentence, when its length increases.

What is attention layer in Deep Learning?

- Every RNN/LSTM can be interpreted as an Encoder and Decoder.
  - Encoder encodes the input samples of a chronological signal to hidden state.
  - Decoder decodes the hidden state to the output.

Attention is an interface connecting the encoder and decoder that provides the decoder with information from every encoder hidden state.

With this framework, the model is able to selectively focus on valuable parts of the input sequence and hence, learn the association between them.



BLEU:
Bilingual Evaluation Understudy

*Neural Machine Translation by Jointly Learning to Align and Translate

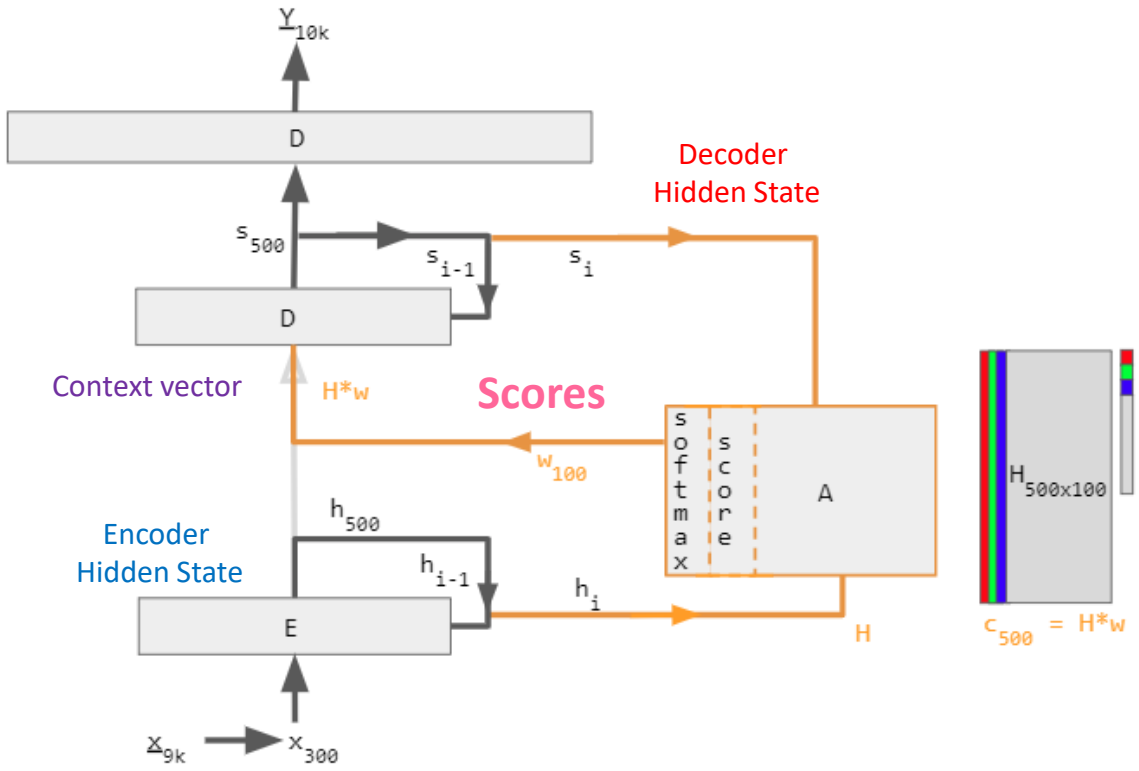
Dzmitry Bahdanau, Kyunghyun Cho, Yoshua Bengio

A language translation example

To build a machine that translates English-to-French (see the shown diagram), one starts with an Encoder-Decoder and grafts an attention unit to it. In the simplest case such as the shown example, the attention unit is just lots of dot products of recurrent layer states and does not need training. In practice, the attention unit consists of 3 fully connected neural network layers that needs to be trained. The 3 layers are called Query, Key, and Value.

Encoder-Decoder with attention. This diagram uses specific values to relieve an already cluttered notation alphabet soup. The left part (in black) is the Encoder-Decoder, the middle part (in orange) is the attention unit, and the right part (in grey & colors) is the computed data. Grey regions in H matrix and w vector are zero values.

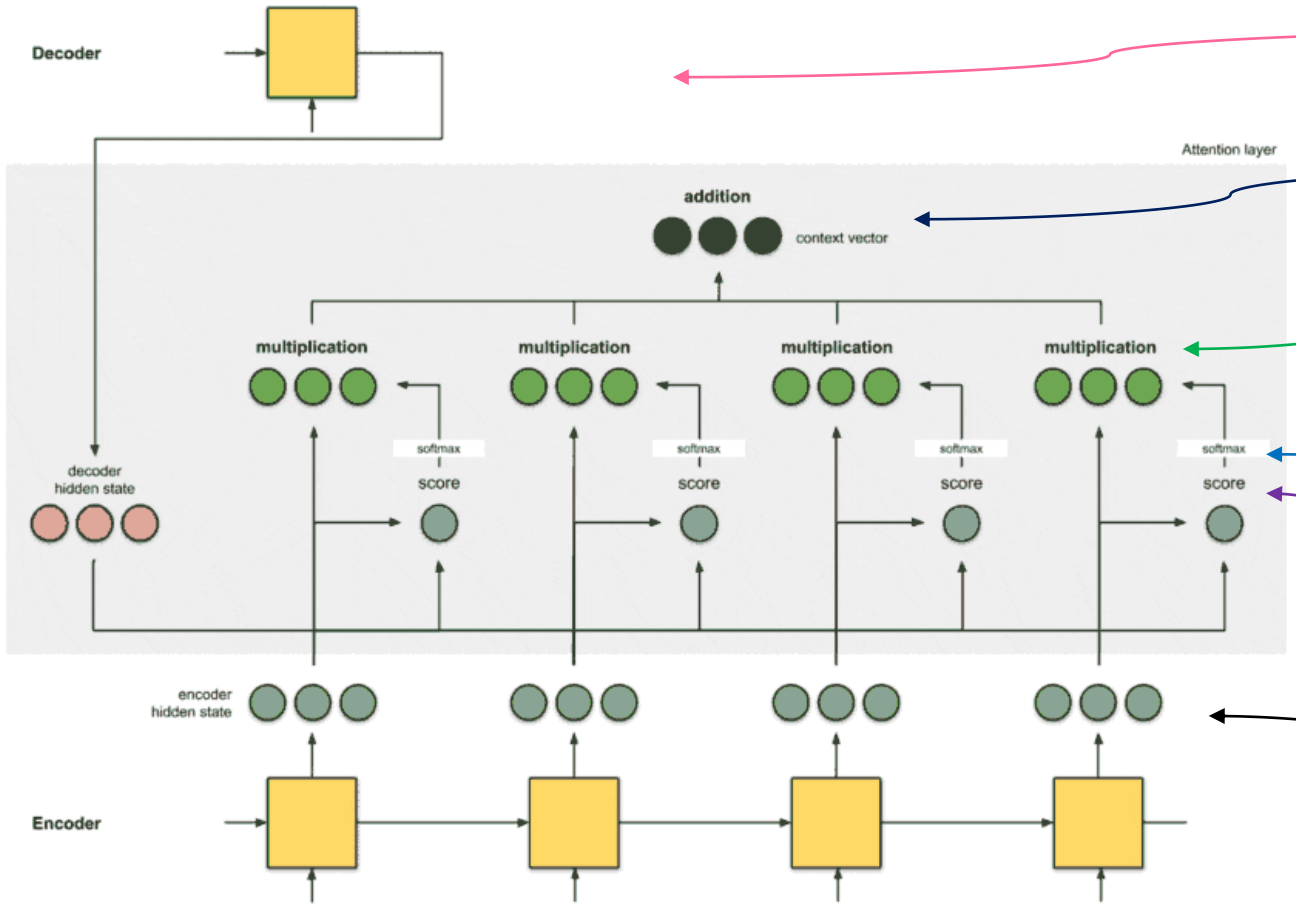
Numerical subscripts are examples of vector sizes. Lettered subscripts i and i-1 indicate time step.



label	description
100	max sentence length
300	embedding size (word dimension)
500	length of hidden vector
9k, 10k	dictionary size of input & output languages respectively.
x, Y	9k and 10k 1-hot dictionary vectors. x → x implemented as a lookup table rather than vector multiplication. Y is the 1-hot maximizer of the linear Decoder layer D; that is, it takes the argmax of D's linear layer output.
x	300-long word embedding vector. The vectors are usually pre-calculated from other projects such as GloVe or Word2Vec.
h	500-long encoder hidden vector. At each point in time, this vector summarizes all the preceding words before it. The final h can be viewed as a "sentence" vector, or a thought vector as Hinton calls it.
s	500-long decoder hidden state vector.
E	500 neuron RNN encoder. 500 outputs. Input count is 800–300 from source embedding + 500 from recurrent connections. The encoder feeds directly into the decoder only to initialize it, but not thereafter; hence, that direct connection is shown very faintly.
D	2-layer decoder. The recurrent layer has 500 neurons and the fully connected linear layer has 10k neurons (the size of the target vocabulary).[7] The linear layer alone has 5 million (500 * 10k) weights -- ~10 times more weights than the recurrent layer.
score	100-long alignment score
w	100-long vector attention weight. These are "soft" weights which changes during the forward pass, in contrast to "hard" neuronal weights that change during the learning phase.
A	Attention module — this can be a dot product of recurrent states, or the Query-Key-Value fully connected layers. The output is a 100-long vector w.
H	500x100. 100 hidden vectors h concatenated into a matrix
c	500-long context vector = H * w. c is a linear combination of h vectors weighted by w.

Unfolded attention layer

The below figure demonstrates an Encoder-Decoder architecture with an attention layer (All time steps).



5-Feed the context vector into the decoder.

4-Sum the alignment vectors (as context vector)

3- Multiply each encoder hidden state by its softmax score.

2-Run all the scores through a softmax layer

1-Obtain a score for every encoder hidden state.

0-Prepare hidden states.

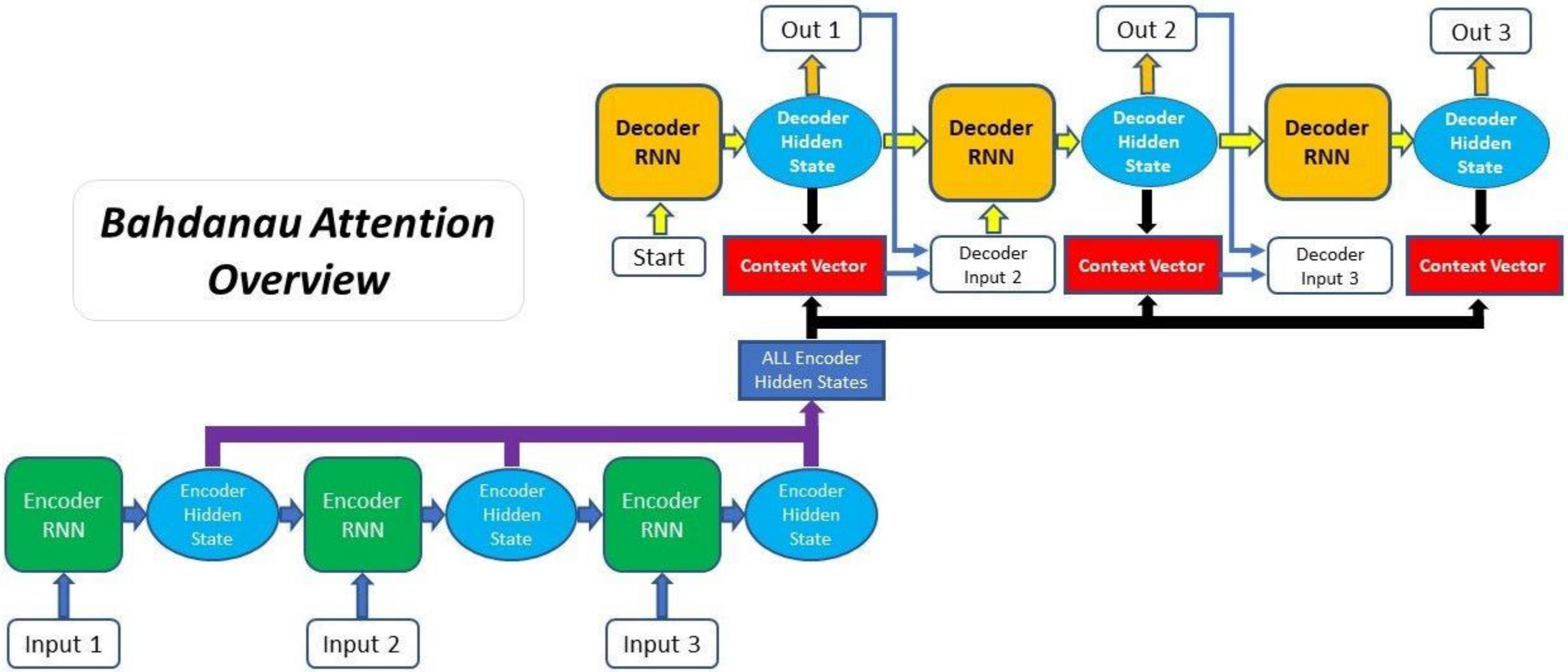
***Encoder-Decoder Recurrent Neural Network Models for Neural Machine Translation**
by **Jason Brownlee** on January 1, 2018 in **Deep Learning for Natural Language Processing**

The implementations of an attention layer can be broken down into 4 steps.

For each time step:

- **Step 0: Prepare hidden states.**
- First, prepare all the available encoder hidden states (green) and the first decoder hidden state (red). In our example, we have 4 encoder hidden states and the current decoder hidden state. (Note: the last consolidated encoder hidden state is fed as input to the first time step of the decoder. The output of this first time step of the decoder is called the first decoder hidden state.)
- **Step 1: Obtain a score for every encoder hidden state.**
- A score (scalar) is obtained by a score function (also known as alignment score function or alignment model). In this example, the score function is a dot product between the decoder and encoder hidden states.
- **Step 2: Run all the scores through a softmax layer.**
- We put the scores to a softmax layer so that the softmax scores (scalar) add up to 1. These softmax scores represent the attention distribution.
- **Step 3: Multiply each encoder hidden state by its softmax score.**
- By multiplying each encoder hidden state with its softmax score (scalar), we obtain the alignment vector or the annotation vector. This is exactly the mechanism where alignment takes place.
- **Step 4: Sum the alignment vectors.**
- The alignment vectors are summed up to produce the context vector. A context vector is an aggregated information of the alignment vectors from the previous step.
- **Step 5: Feed the context vector into the decoder.**

Bahdanau Attention Overview



*Neural Machine Translation by Jointly Learning to Align and Translate

Dzmitry Bahdanau, Kyunghyun Cho, Yoshua Bengio

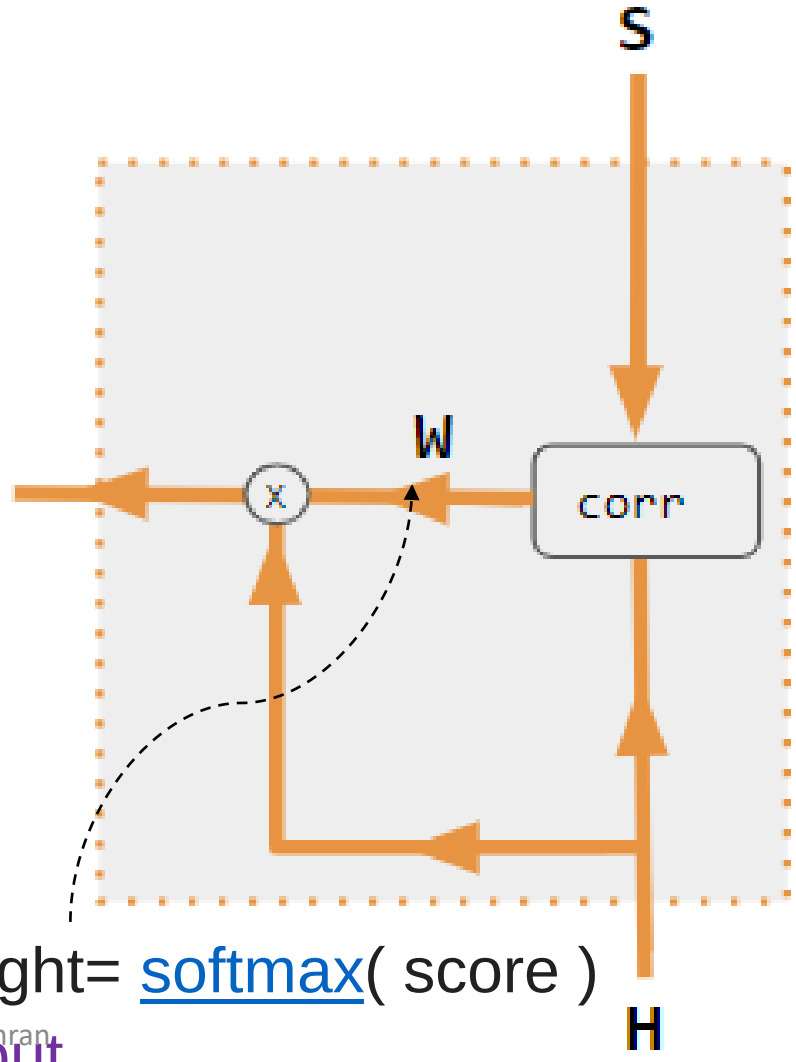
Attention variants

1. encoder-decoder dot product
2. encoder-decoder QKV (Query-Key-Value)
3. encoder-only dot product
4. encoder-only QKV
5. Pytorch tutorial

1. encoder-decoder dot product

s = decoder input to Attention
=Decoder hidden state

Both Encoder & Decoder are needed to calculate Attention.



c = context vector = H*w

w = attention weight= softmax(score)

H = encoder output

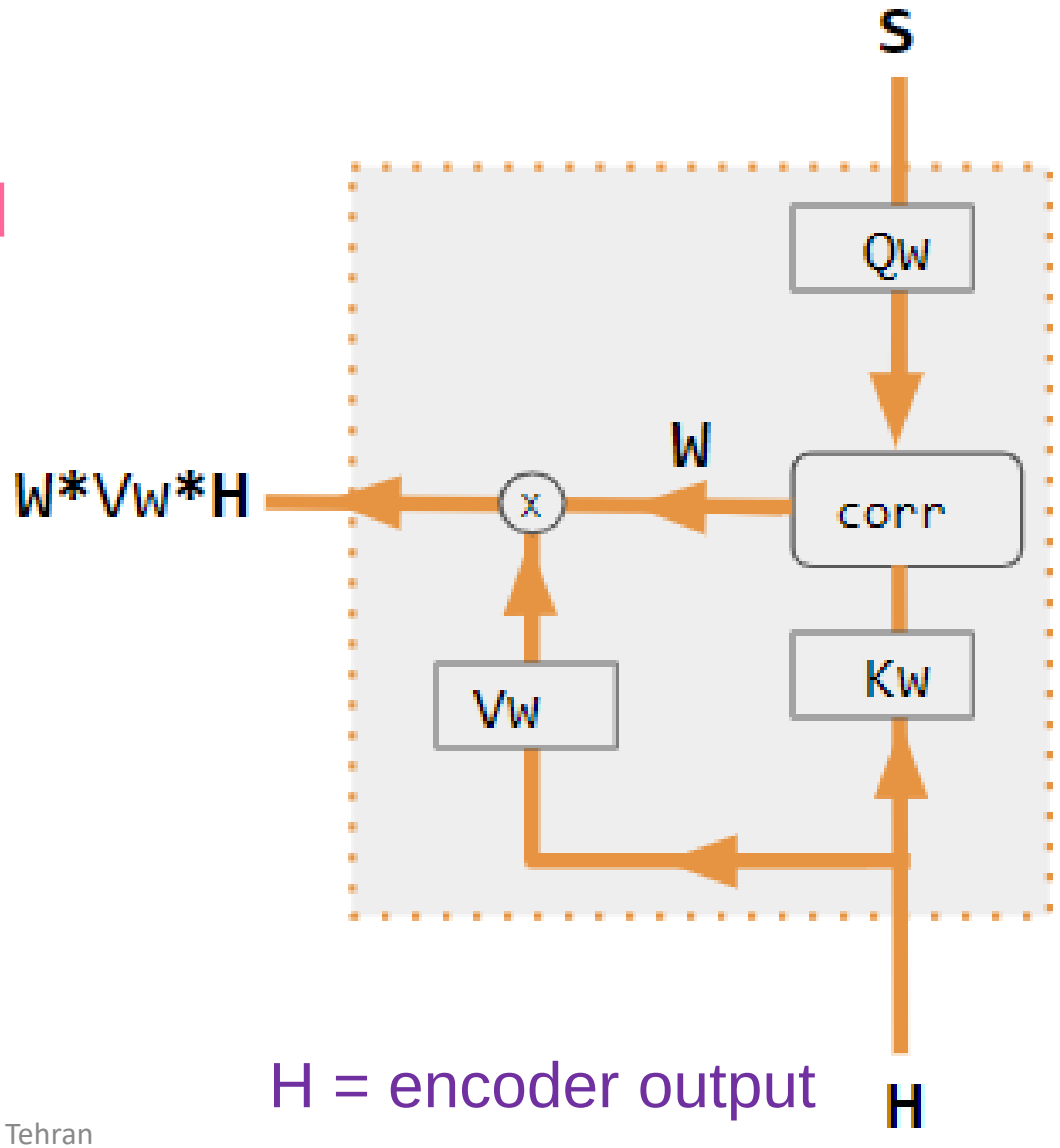
1.*Luong, Minh-Thang (2015-09-20). "Effective Approaches to Attention-based Neural Machine Translation". arXiv:1508.04025v5 [cs.CL].*

2. encoder-decoder QKV

s = decoder input to Attention

Both Encoder & Decoder are needed to calculate Attention.

c = context vector

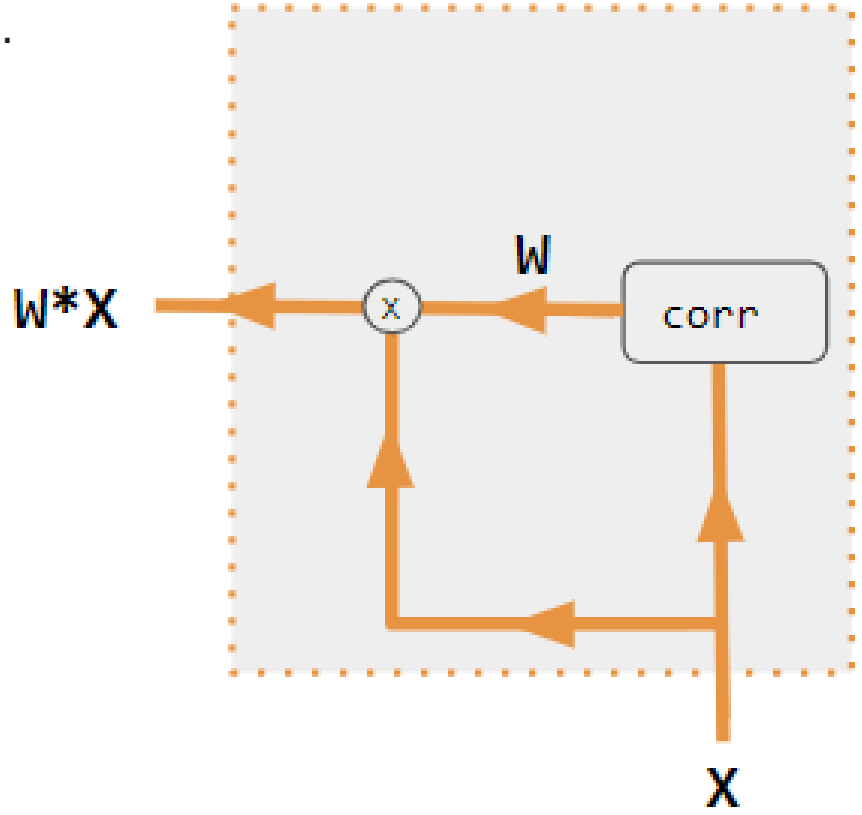


H = encoder output

1. *Neil Rhodes (2021). CS 152 NN—27: Attention: Keys, Queries, & Values. Event occurs at 06:30. Retrieved 2021-12-22.*

3. encoder-only dot product

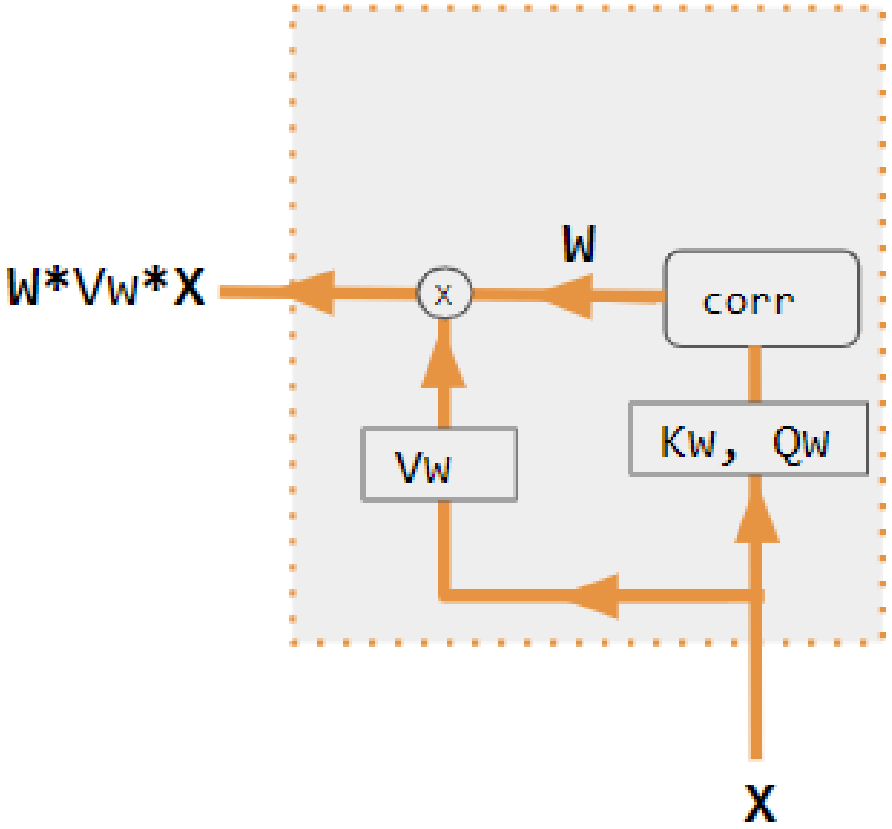
Decoder is NOT used to calculate Attention. With only 1 input into corr, W is an auto-correlation of dot products.
$w_{ij} = x_i * x_j$ [10]



1. *Alfredo Canziani & Yann Lecun (2021). NYU Deep Learning course, Spring 2020. Event occurs at 05:30. Retrieved 2021-12-22.*

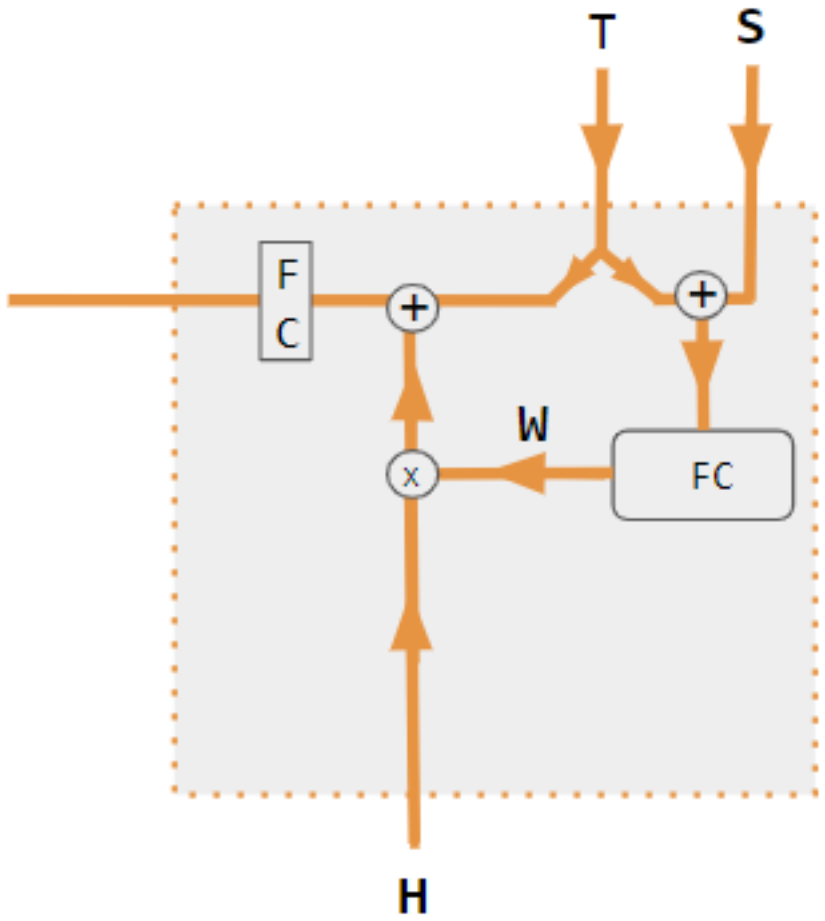
4. encoder-only QKV

Decoder is NOT used to calculate Attention.[11]



1. *Alfredo Canziani & Yann Lecun (2021). NYU Deep Learning course, Spring 2020. Event occurs at 20:15. Retrieved 2021-12-22.*

5. Pytorch tutorial



A FC layer is used to calculate Attention instead of dot product correlation.

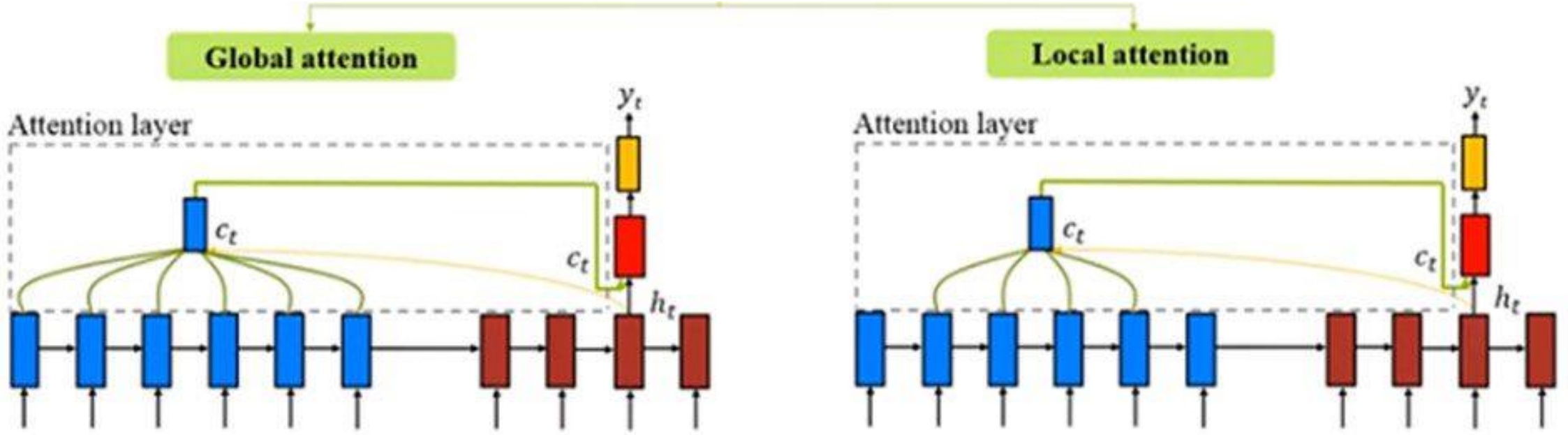
S = decoder hidden state, T = target word embedding.

H = encoder hidden state, X = input word embedding

1. *Robertson, Sean. "NLP From Scratch: Translation With a Sequence To Sequence Network and Attention". pytorch.org. Retrieved 2021-12-22.*

Types of attention

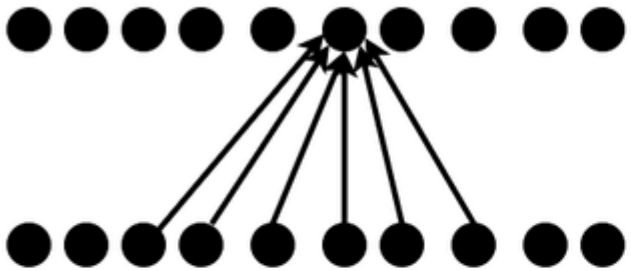
Depending on how many source states contribute while deriving the attention vector (α), there can be three types of attention mechanisms:



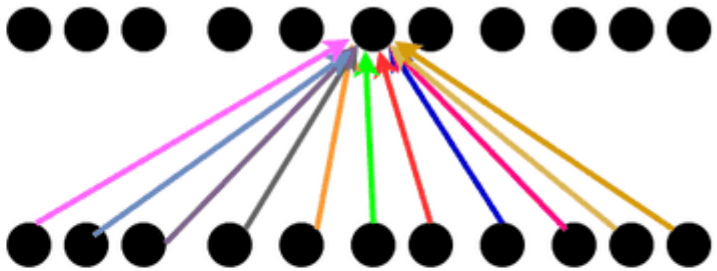
- **Global Attention**: When attention is placed on all source states. In global attention, we require as many weights as the source sentence length.
- **Local Attention**: When attention is placed on a few source states.
- **Hard Attention**: When attention is placed on only one source state.

You can check out my Kaggle notebook or GitHub repo to implement NMT with the attention mechanism using TensorFlow.

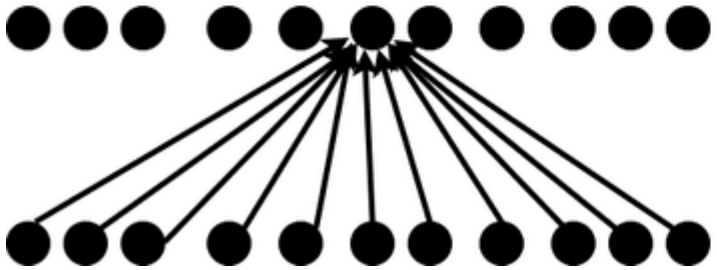
Convolution



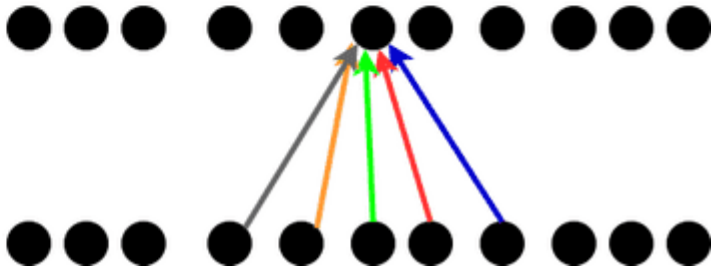
Global attention



Fully Connected layer



Local attention



1.1.5 Pooling layers

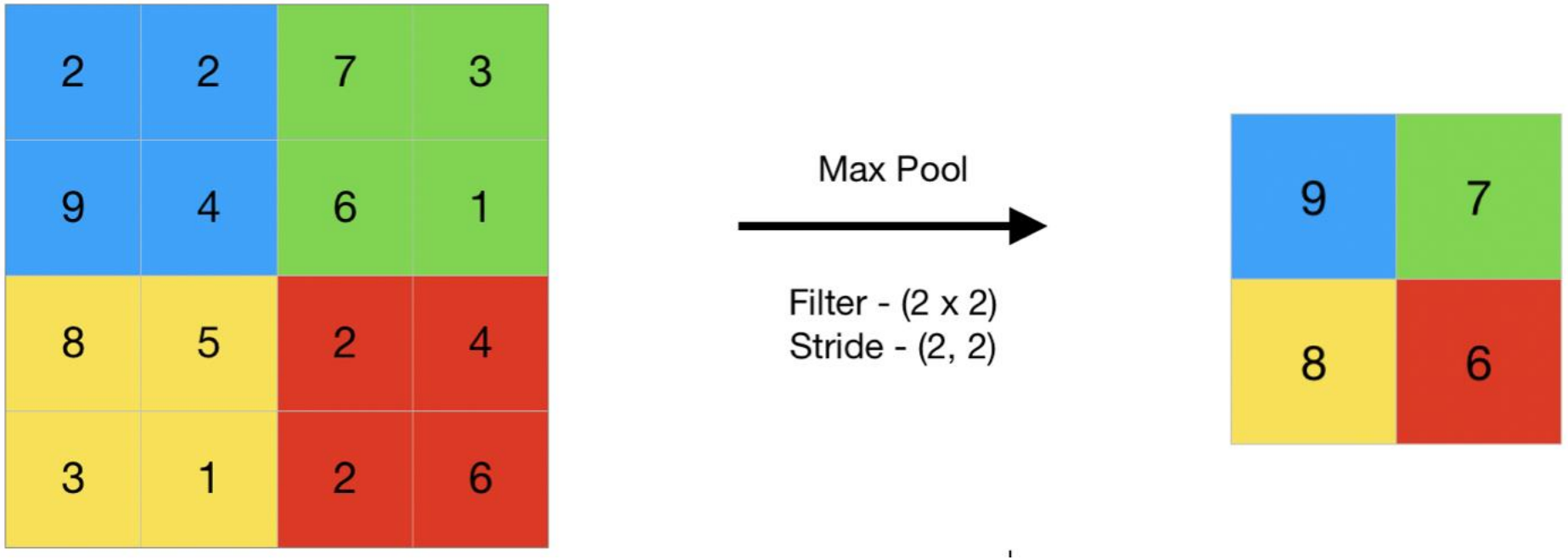
to reduce the spatial dimensions of the feature maps(subsampling) and to provide small spatial invariances

- Max pooling
- Min pooling
- Average pooling
- Global Pooling

Other pooling extensions

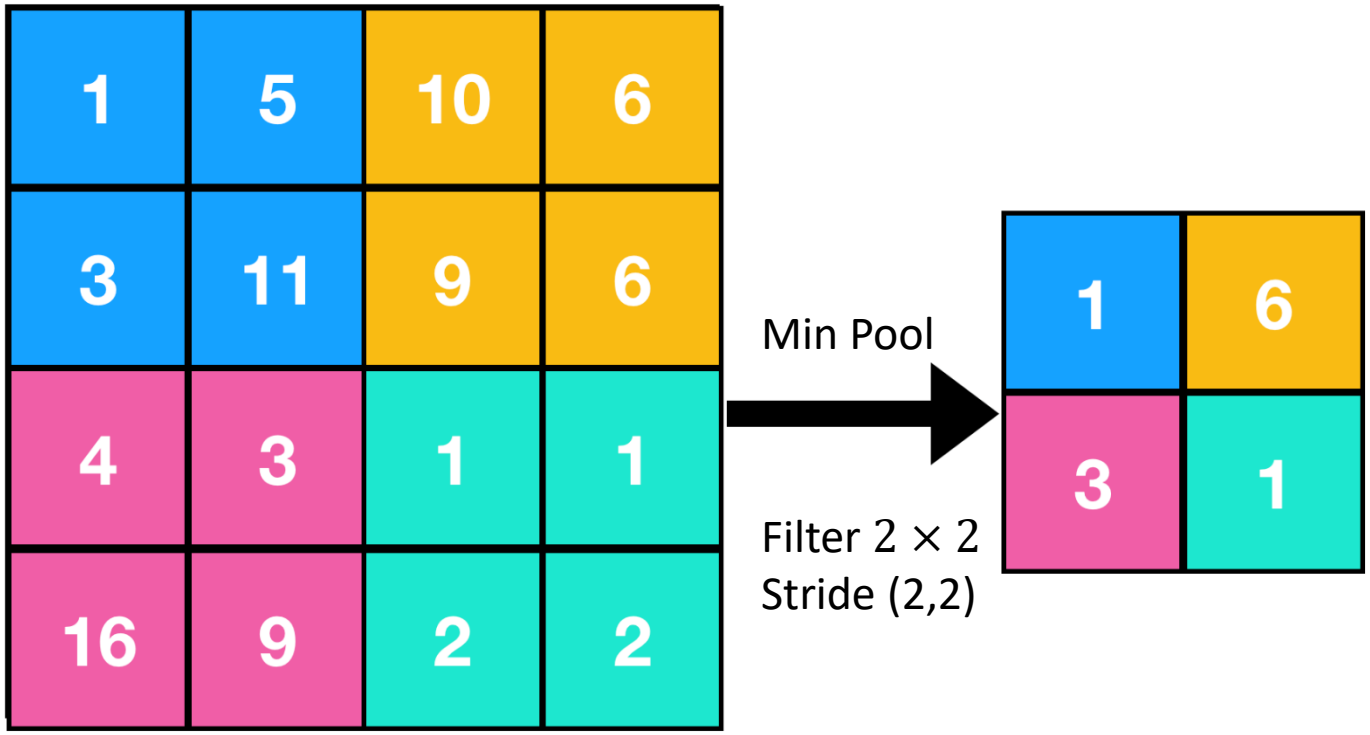
Mixed Pooling
Lp pooling
Stochastic pooling
Spatial Pyramid Pooling
Region of Interest Pooling
Multi-scale order-less pooling (MOP)
Super-pixel Pooling
PCA Networks
Compact Bilinear Pooling
Lead Asymmetric Pooling (LAP)
Edge-aware Pyramid Pooling
Spectral Pooling
Row-Wise Max-Pooling
Intermap Pooling
Per-pixel Pyramid Pooling
Rank-based Average Pooling
Weighted Pooling
Genetic-Based Pooling

Max pooling: The maximum pixel value of the batch is selected



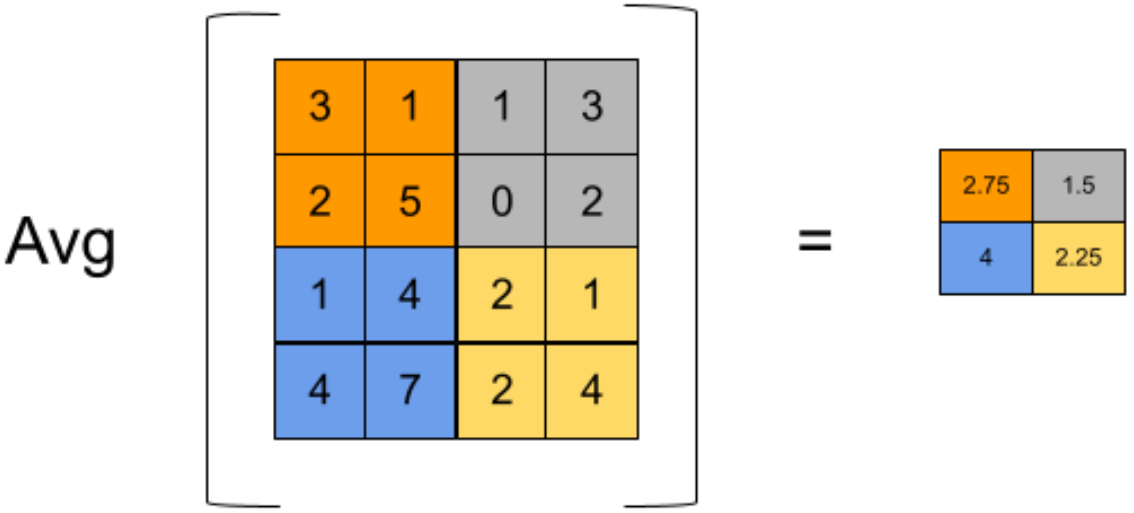
- Through Max Pooling, among units of a patch at each feature map, choose one which has the maximum similarity to the filter and ignore other ones.

Min pooling: The minimum pixel value of the batch is selected.



❖ It is mostly used when the image has a light background since min pooling will select darker pixels

Average pooling: The average value of all the pixels in the batch is selected.



Filter 2×2
Stride (2,2)

- Assuming all units of a patch are almost equal in information but with additive mean-zero noise, average pooling performs as a smooth function increasing the signal to noise ratio.

Global Pooling Layers

- Instead of down sampling patches of the input feature map, global pooling down samples the entire feature map to a single value.
- This would be the same as setting the *pool_size* to the size of the input feature map.
- Global pooling can be used in a model to aggressively summarize the presence of a feature in an image.
- It is also sometimes used in models as an alternative to using a fully connected layer to transition from feature maps to an output prediction for the model (**fully convolutional network like U-net**).
- Both global average pooling and global max pooling are defined.

1.1.6 Normalizing Layers

to speed up and stabilize the learning process

- Batch Normalization
- Weight Normalization
- Layer Normalization
- Group/Instance Normalization
- Weight Standarization

*Nilesh Vijayrania
Intrigued about Deep learning and all things ML.
Dec 10, 2020

Batch Normalization(BN)

A layer for standardization of inputs at each layer

Input: Values of x over a mini-batch: $\mathcal{B} = \{x_{1...m}\}$;
Parameters to be learned: γ, β
Output: $\{y_i = \mathrm{BN}_{\gamma,\beta}(x_i)\}$

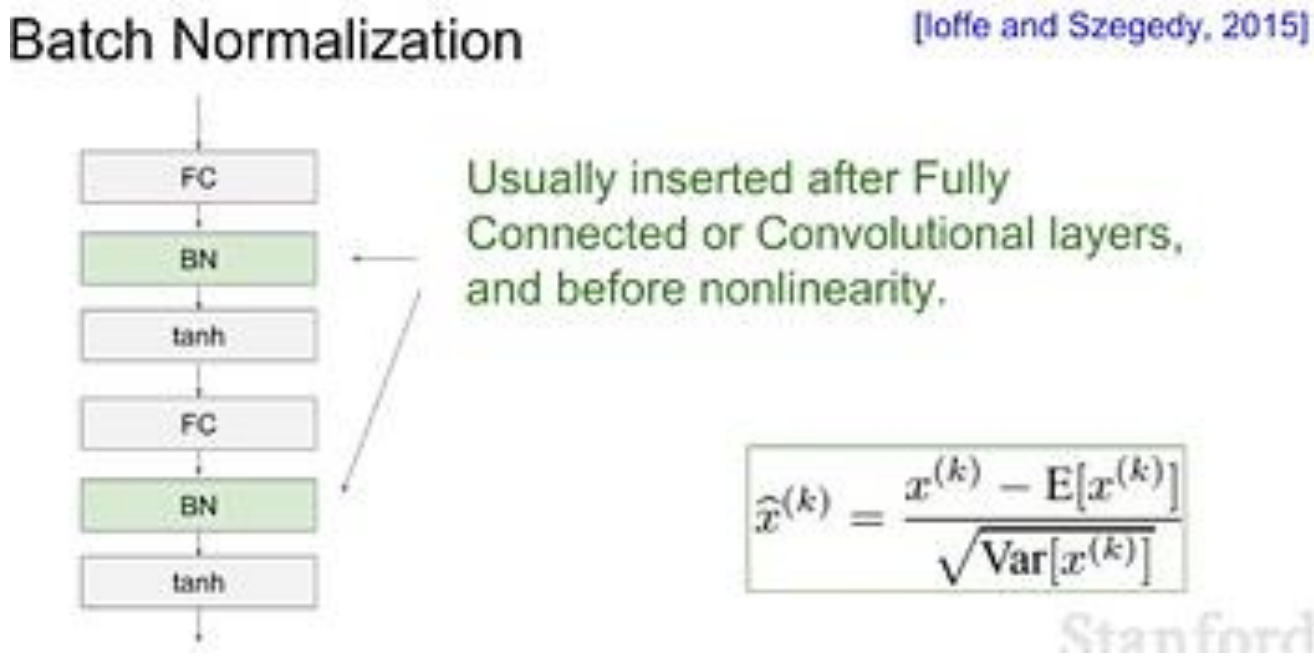
$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m}\sum_{i=1}^{m} x_i \qquad \text{// mini-batch mean}$$

$$\sigma^2_{\mathcal{B}} \leftarrow \frac{1}{m}\sum_{i=1}^{m}(x_i - \mu_{\mathcal{B}})^2 \qquad \text{// mini-batch variance}$$

$$\widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma^2_{\mathcal{B}} + \epsilon}} \qquad \text{// normalize}$$

$$y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv \mathrm{BN}_{\gamma,\beta}(x_i) \qquad \text{// scale and shift}$$

Algorithm 1: Batch Normalizing Transform, applied to activation x over a mini-batch.



The question is how BN helps NN training? since the layers are stacked one after the other, the data distribution of input to any particular layer changes too much due to slight update in weights of earlier layer, and hence the current gradient might produce suboptimal signals for the network. But BN restricts the distribution of the input data to any particular in the network, which helps the network to produce better gradients for weights update. Hence BN often provides a much stable and accelerated training regime

Weight Normalization(WN)

to decouple the length from the direction of the weight vector (Salimans, Tim, and Durk P. Kingma, 2016)

The authors of the Weight Normalization paper suggested using two parameters g(for length of the weight vector) and v(the direction of the weight vector) instead of w for gradient descent in the following manner.

$$\mathbf{w} = \frac{g}{||\mathbf{v}||}\mathbf{v}$$

- In weight normalization, the norm of the applied weights is constant (unitary) but the direction of the weights is free.
- Weight Normalization speeds up the training similar to batch normalization and unlike BN, it is applicable to RNNs as well.
- But the training of deep networks with Weight Normalization is significantly less stable compared to Batch Normalization and hence it is not widely used in practice.

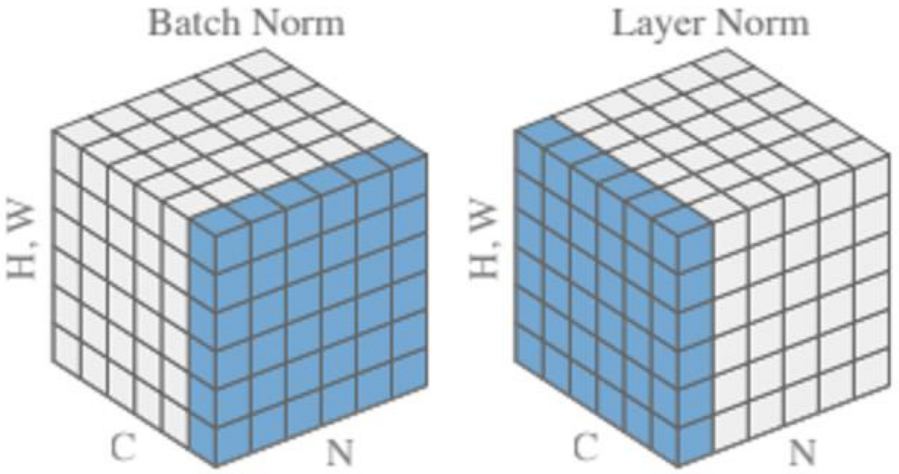
A Comparison between Batch Norm. and Wight Norm.

	BatchNorm: explicit normalization	WeightNorm: implicit normalization
Formula	$o_j = \frac{Wx-\mu_B}{\sigma_B^2}$	$o_j = \frac{Wx}{\|W\|_F}$
Goal	$\|o\|_2 \approx \text{const}$	$\|o\|_2 \approx \|x\|_2$
Assumptions	Batch is big enough	W is close to orthogonal matrix

Layer Normalization(LN)

Normalize a long feature maps rather than examples

- Layer Normalization normalizes the activations along the feature direction instead of mini-batch direction.
- This overcomes the cons of BN by removing the dependency on batches and makes it easier to apply for RNNs as well.
- In essence, Layer Normalization normalizes each feature of the activations to zero mean and unit variance.
- In batch normalization, **input values of the same neuron for all the data in the mini-batch are normalized**. Whereas in layer normalization, input values for all neurons in the same layer are normalized for each data sample.



(N, C, H, W)

N: number of data samples in Mini Batch

C: number of feature maps (channels)

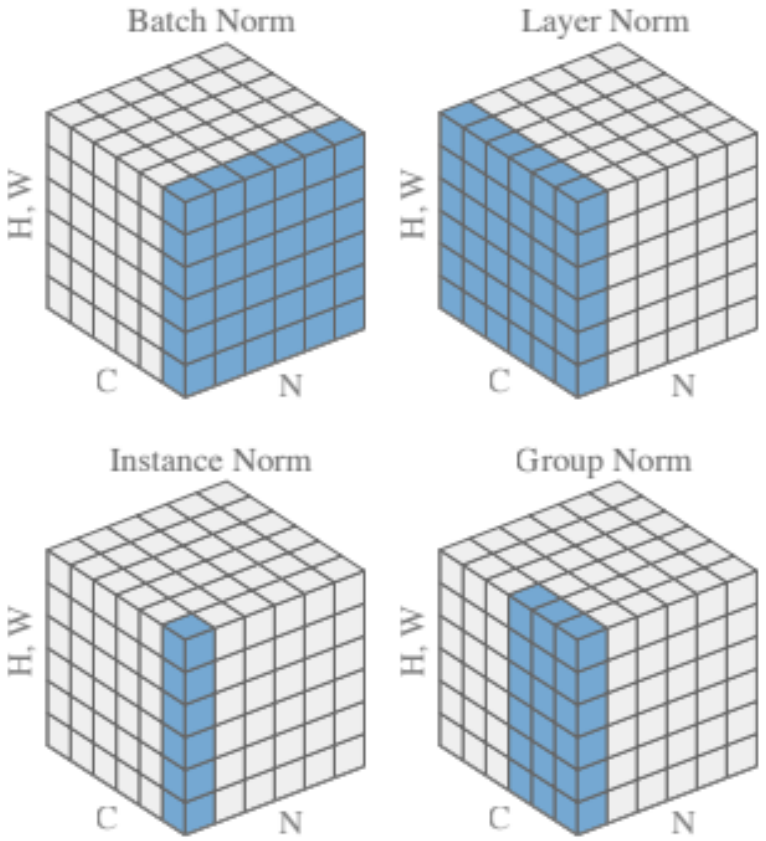
H,W: spatial size of feature maps

* Geoffrey Hinton et al. 2016

Group/Instance Normalization(GN)

normalize along a certain groups of feature maps and normalizes each group separately

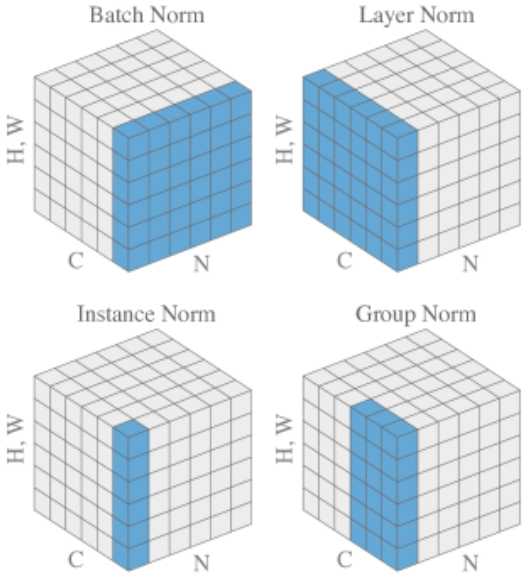
- Similar to layer Normalization, Group Normalization is also applied along the feature direction but unlike LN, it divides the features into certain groups and normalizes each group separately.
- In practice, Group normalization performs better than layer normalization.
- its parameter *num_groups* is tuned as a hyperparameter.
- In a case, when we choose one feature map to normalize, we have an instance normalization.

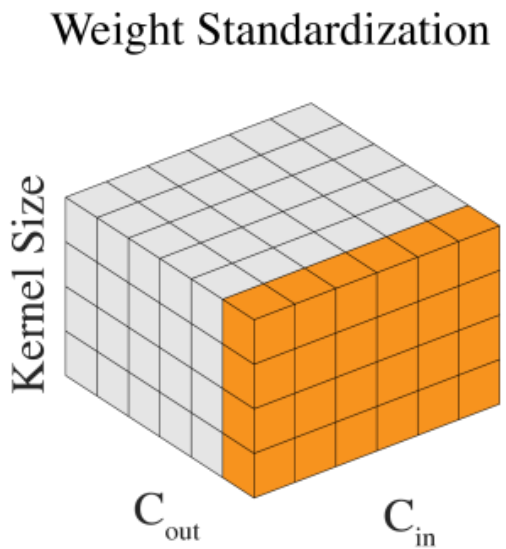


Weight standardization

to batch normalization of weights at a layer instead of data

Weight Standardization is transforming the weights of any layer to have zero mean and unit variance.
This layer could be a convolution layer, RNN layer or linear layer, etc.
For any given layer with shape(N, *) where * represents 1 or more dimensions, weight standardization, transforms the weights along the * dimension(s).





$$\hat{\boldsymbol{W}} = \left[\hat{\boldsymbol{W}}_{i,j} \mid \hat{\boldsymbol{W}}_{i,j} = \frac{\boldsymbol{W}_{i,j} - \mu_{\boldsymbol{W}_{i,\cdot}}}{\sigma_{\boldsymbol{W}_{i,\cdot}} + \epsilon}\right]$$

$$\boldsymbol{y} = \hat{\boldsymbol{W}} * \boldsymbol{x}$$

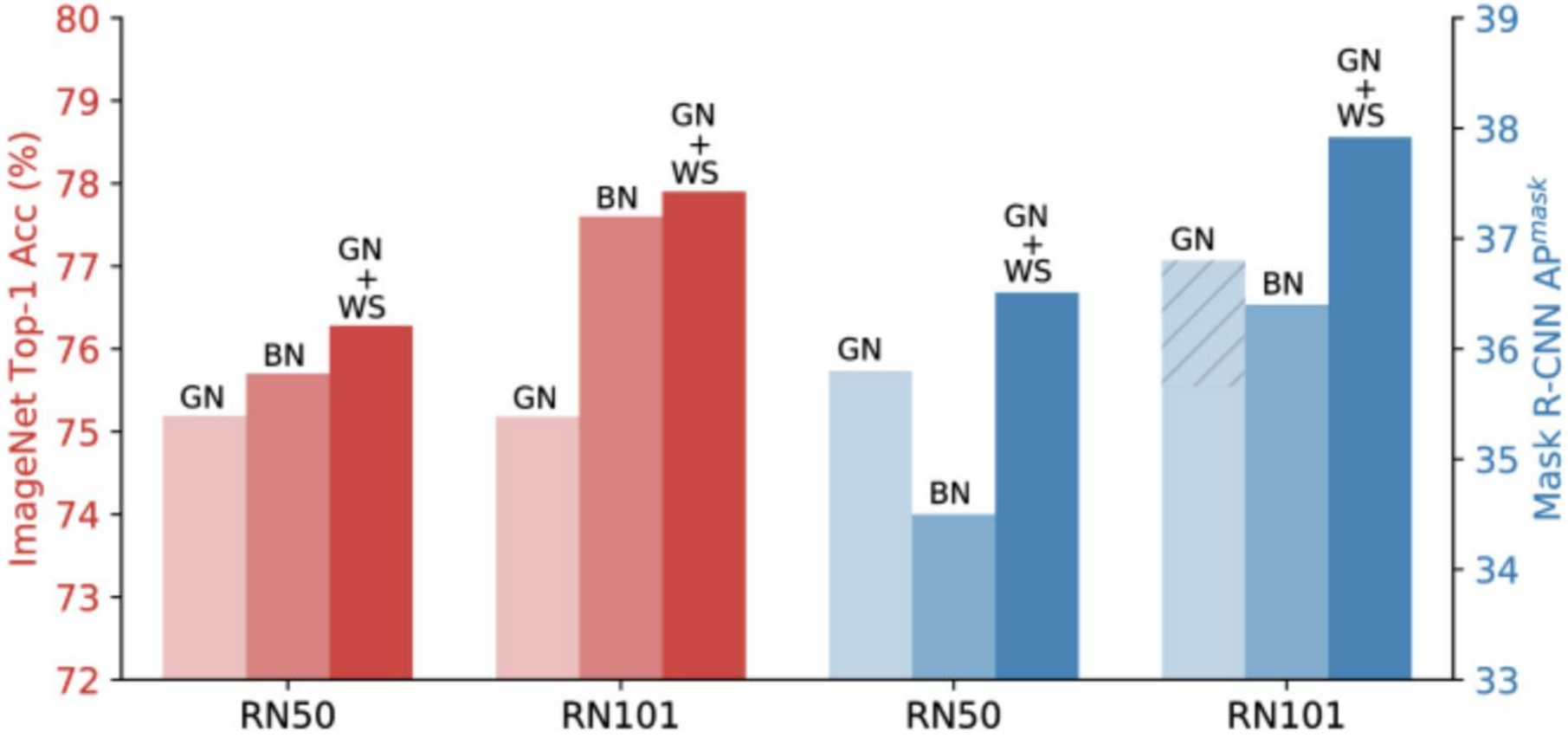
$$\mu_{\boldsymbol{W}_{i,\cdot}} = \frac{1}{I}\sum_{j=1}^{I} \boldsymbol{W}_{i,j}, \quad \sigma_{\boldsymbol{W}_{i,\cdot}} = \sqrt{\frac{1}{I}\sum_{i=1}^{I}(\boldsymbol{W}_{i,j} - \mu_{\boldsymbol{W}_{i,\cdot}})^2}$$

C_{in}: number of input channels
C_{out}: number of output channels
I: corresponds to the number of input channels within the kernel region of each output channel.

*Qiao, Siyuan, et al. 2019

Comparison of different normalization layers*

in Resnet50 and Resnet101 on ImageNet classification and MS COCO



*Siyuan Qiao et al. Weight Standardization. GN+WS effect on classification and object detection task[4]

1.2 Architectures

1.2.1 CNNs

1.2.2 R-CNNs

1.2.3 RNNs and Transformers

1.2.4 AEs and VAEs

1.2.5 GANs

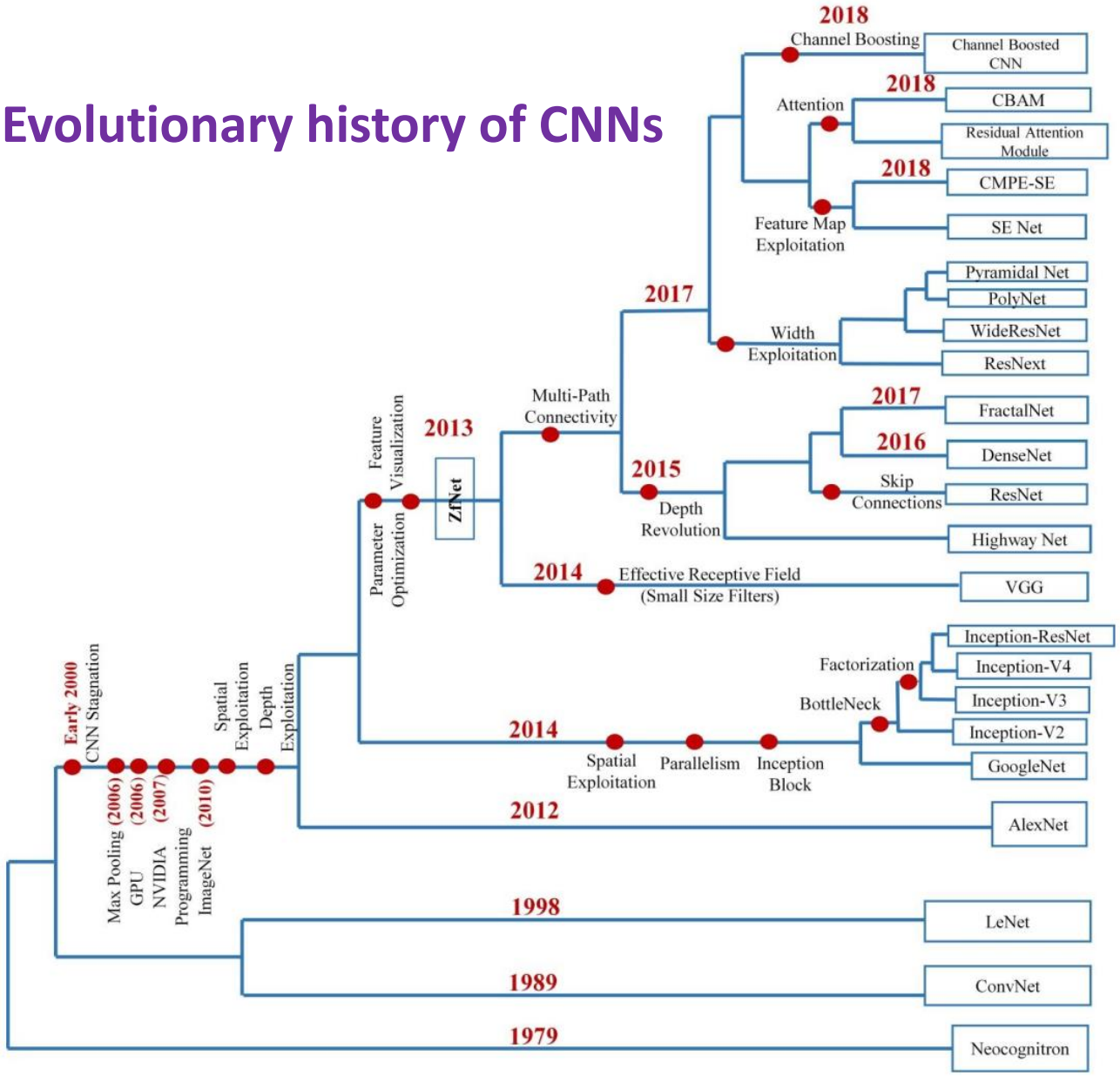
1.2.1 CNNs

ANNs which use convolution layers to filter and extract features from signals to solve a classification or regression problem.

In 1989, LeCuN et al. proposed the first multilayered CNN named ConvNet, whose origin rooted in Fukushima's Neocognitron (Fukushima and Miyake 1982; Fukushima 1988). **Japanese handwritten character recognition and oth pattern recognition tasks**

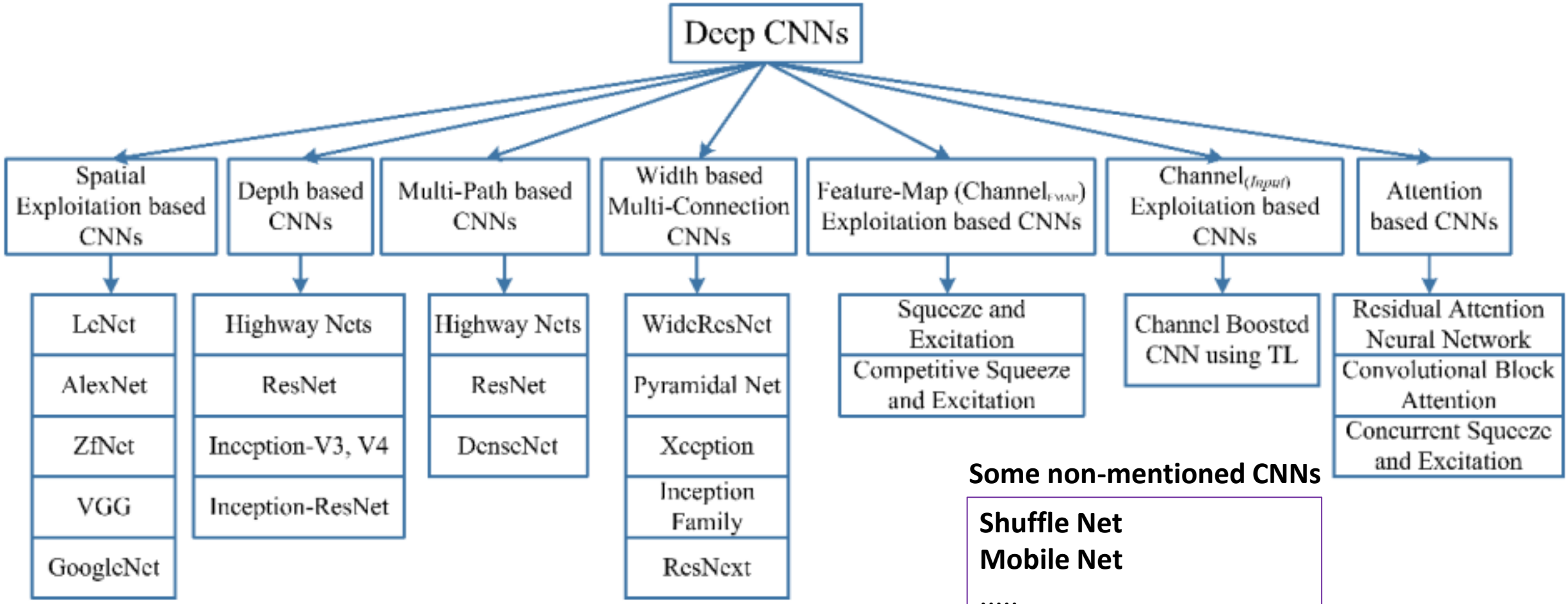
In 1998, LeCuN proposed an improved version of ConvNet, which was famously known as LeNet-5, and it started the use of CNN in classifying characters in a document recognition related applications (LeCun et al. 1995, 1998).

Evolutionary history of CNNs



*Assifullah khan, et al. 2020

Taxonomy of deep CNN architectures showing seven different categories



Some non-mentioned CNNs

Shuffle Net
Mobile Net
.....
Efficient Net
Transformer-CNN

Spatial Exploitation based CNNs

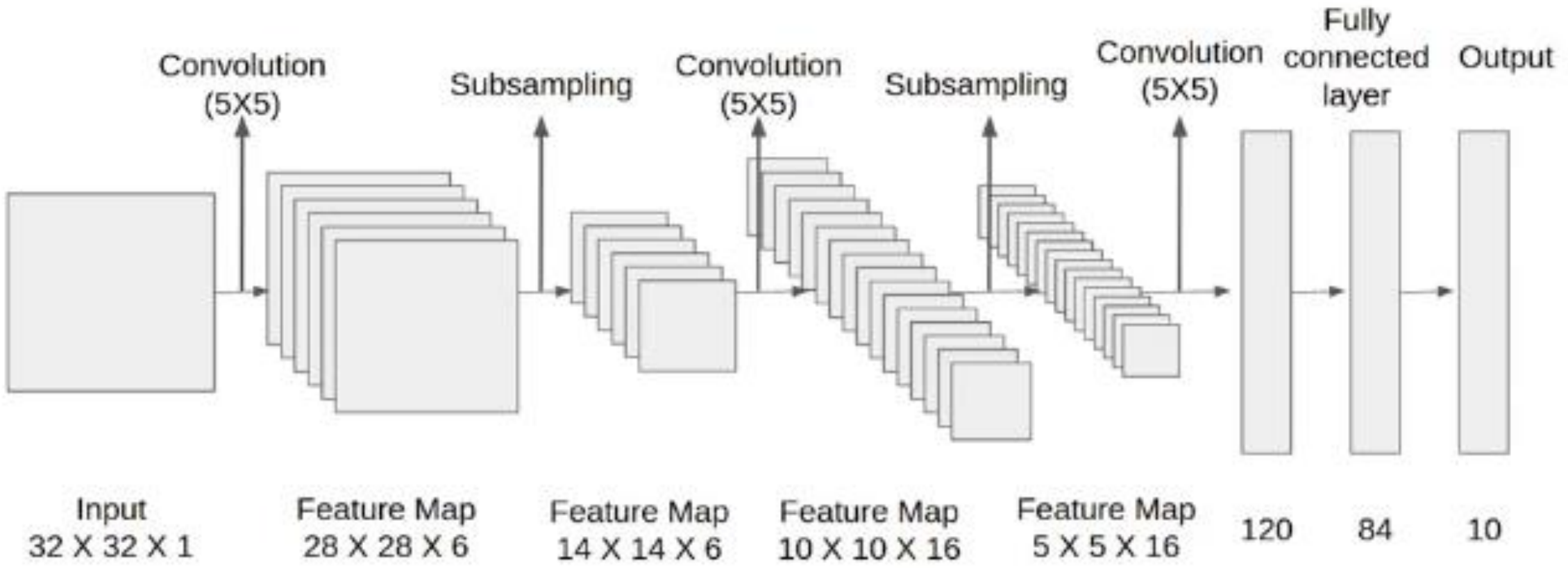
CNNs which improve themselves by exploring different levels of (spatial) correlation by employing different filter sizes

CNNs: LeNet AlexNet ZFNet VGG GoogleNet

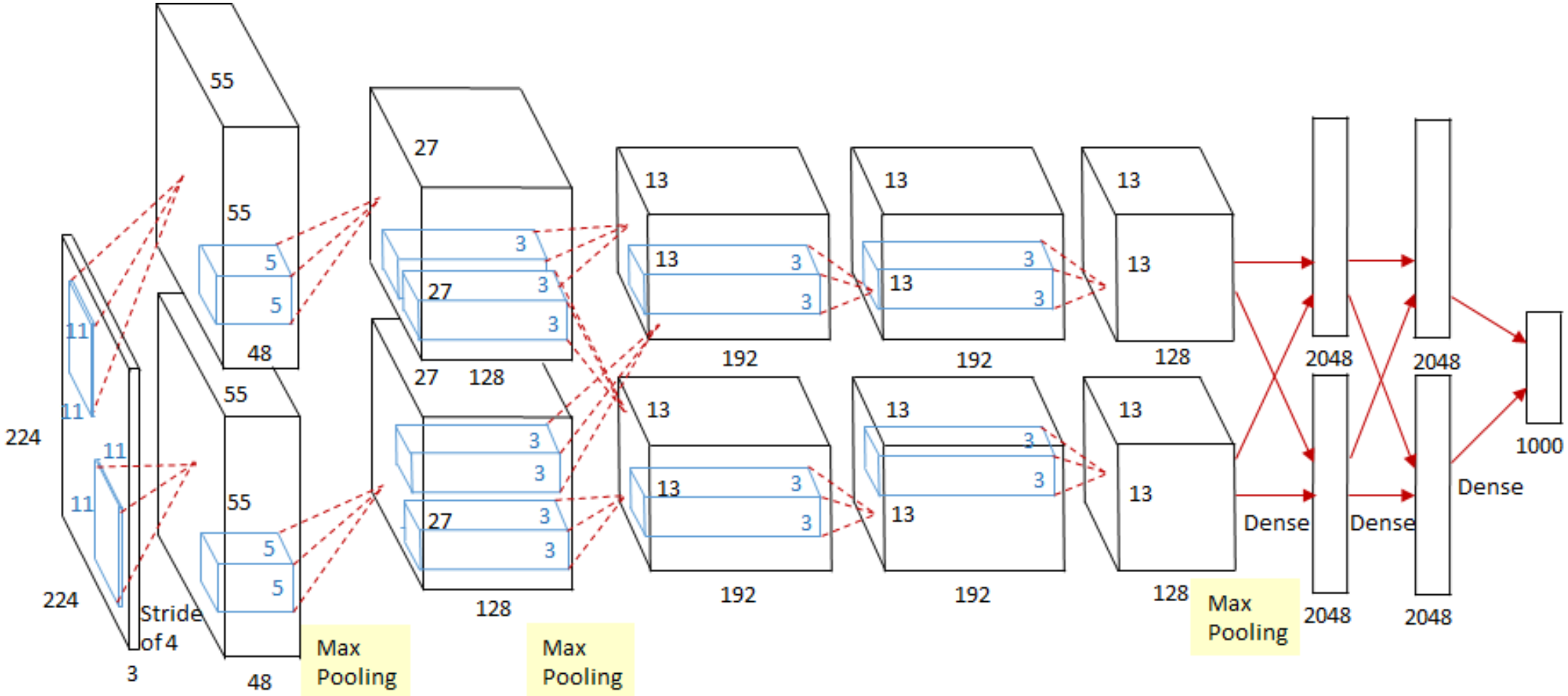
.

Architecture Name	Year	Main contribution	Parameters	Error Rate	Depth	Category	Reference
LeNet	1998	- First popular CNN architecture	0.060 M	[dist]MNIST: 0.8 MNIST: 0.95	5	Spatial Exploitation	(LeCun et al. 1995)
AlexNet	2012	- Deeper and wider than the LeNet - Uses Relu, dropout and overlap Pooling - GPUs NVIDIA GTX 580	60 M	ImageNet: 16.4	8	Spatial Exploitation	(Krizhevsky et al. 2012)
ZfNet	2014	-Visualization of intermediate layers	60 M	ImageNet: 11.7	8	Spatial Exploitation	(Zeiler and Fergus 2013)
VGG	2014	- Homogenous topology - Uses small size kernels	138 M	ImageNet: 7.3	19	Spatial Exploitation	(Simonyan and Zisserman 2015)
GoogLeNet	2015	- Introduced block concept - Split transform and merge idea	4 M	ImageNet: 6.7	22	Spatial Exploitation	(Szegedy et al. 2015)

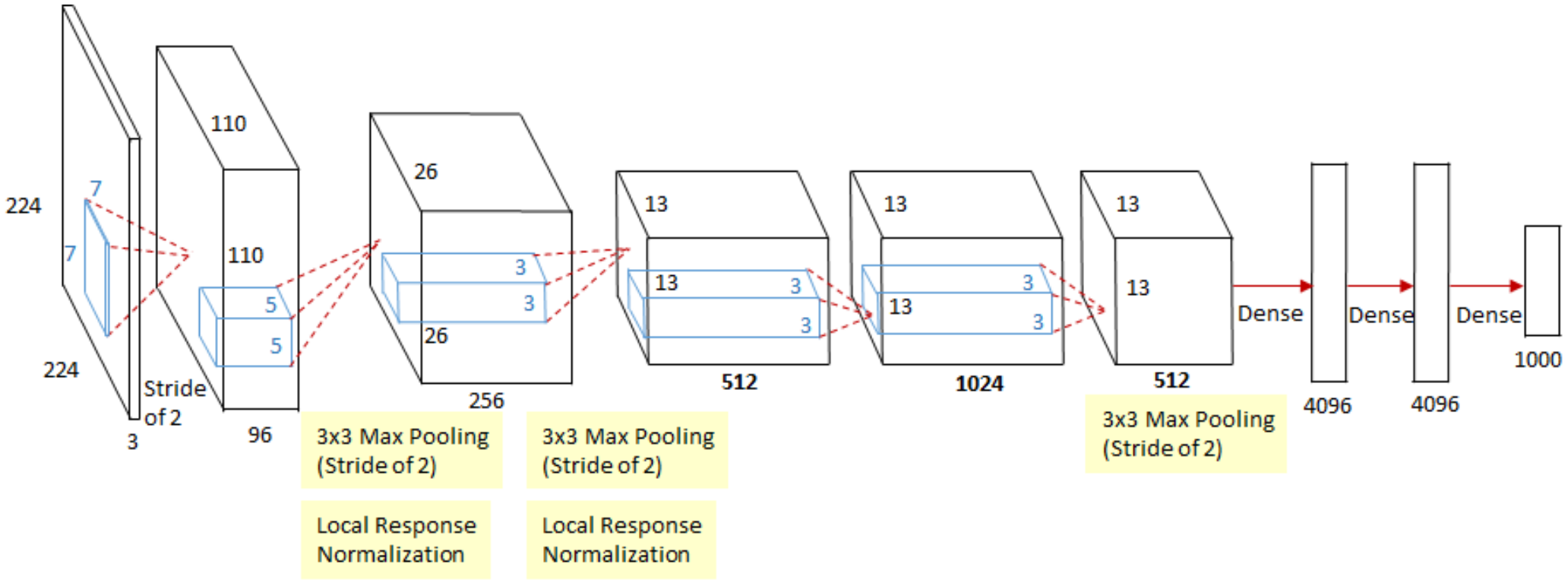
The final architecture of the Lenet-5 model.



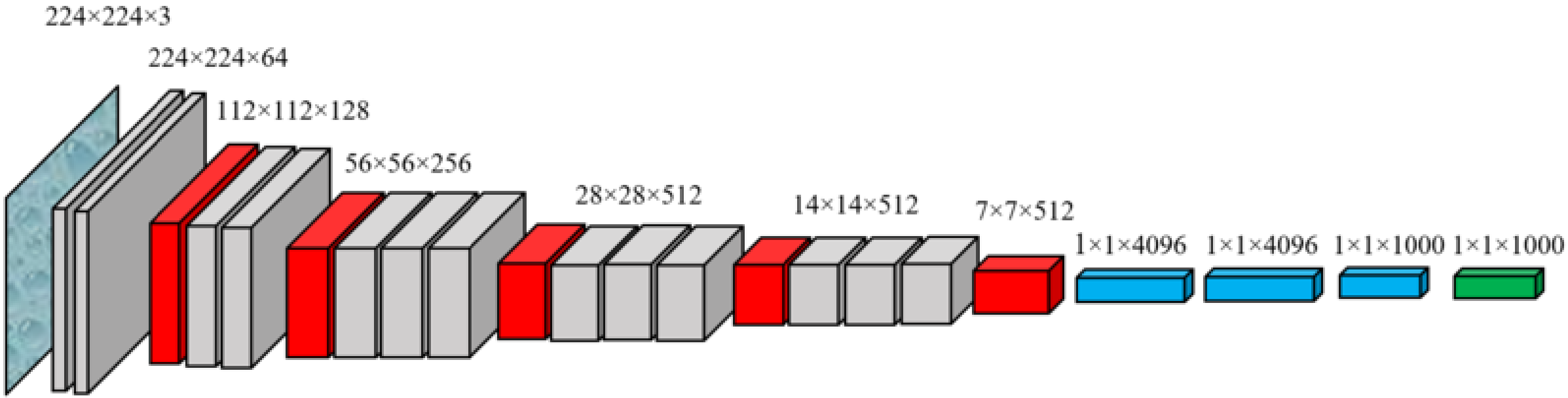
AlexNet

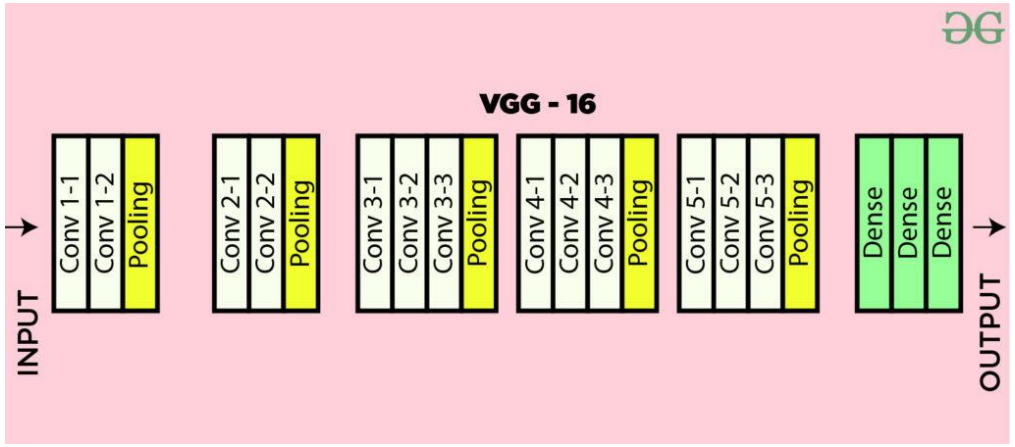

55
55
48
55
55
48
224
224
11
11
11
11
5
5
5
5
3
Stride of 4
27
27
27
128
128
3
13
13
13
13
13
13
192
192
192
192
128
128
2048
2048
2048
2048
1000
Dense
Dense
Dense
Max Pooling
Max Pooling
Local Response Normalization
Local Response Normalization

ZFNET

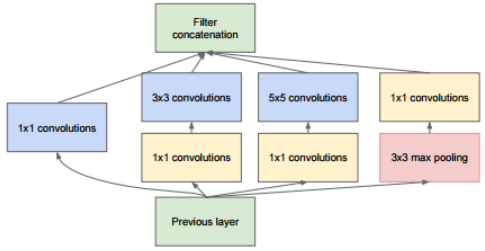

224
7
7
224
3
Stride
of 2
110
110
5
5
96
26
3
3
26
256
13
13
3
3
512
13
13
3
3
1024
13
13
512
Dense
Dense
Dense
1000
4096
4096
3x3 Max Pooling
(Stride of 2)
Local Response
Normalization
3x3 Max Pooling
(Stride of 2)
Local Response
Normalization
3x3 Max Pooling
(Stride of 2)

VGG


224×224×3
224×224×64
112×112×128
56×56×256
28×28×512
14×14×512
7×7×512
1×1×4096
1×1×4096
1×1×1000
1×1×1000


VGG - 16
INPUT
Conv 1-1
Conv 1-2
Pooling
Conv 2-1
Conv 2-2
Pooling
Conv 3-1
Conv 3-2
Conv 3-3
Pooling
Conv 4-1
Conv 4-2
Conv 4-3
Pooling
Conv 5-1
Conv 5-2
Conv 5-3
Pooling
Dense
Dense
Dense
OUTPUT

GoogLeNet



(b) Inception module with dimension reductions

Auxiliary Classifiers are type of architectural component that seek to improve the convergence of very deep networks.
They are classifier heads we attach to layers before the end of the network.
The motivation is to push useful gradients to the lower layers to make them immediately useful and improve the convergence during training by combatting the vanishing gradient problem.
They are notably used in the Inception family of convolutional neural networks.

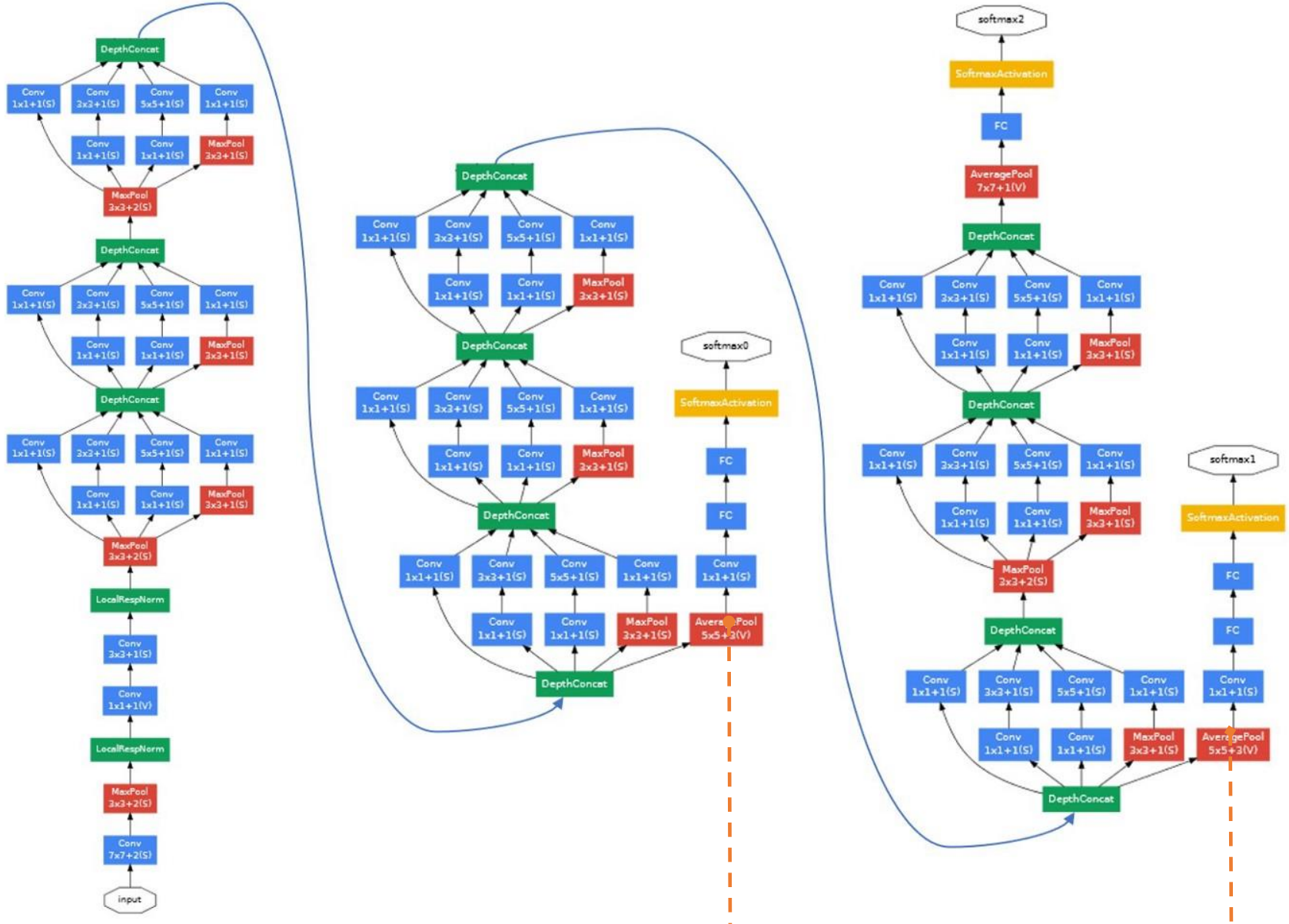


Table 5a Major challenges associated with implementation of Spatial exploitation based CNN architectures.

Spatial Exploitation	As convolutional operation considers the neighborhood (correlation) of input pixels, therefore different levels of correlation can be explored by using different filter sizes.	
Architecture	**Strength**	**Gaps**
LeNet	• Exploited spatial correlation to reduce the computation and number of parameters • Automatic learning of feature hierarchies	• Poor scaling to diverse classes of images • Large size filters • Low level feature extraction
AlexNet	• Low, mid and high-level feature extraction using large and small size filters on initial (5x5 and 11x11) and last layers (3x3) • Give an idea of deep and wide CNN architecture • Introduced regularization in CNN • Started parallel use of GPUs as an accelerator to deal with complex architectures	• Inactive neurons in the first and second layers • Aliasing artifacts in the learned feature-maps due to large filter size
ZfNet	• Introduced the idea of parameter tuning by visualizing the output of intermediate layers • Reduced both the filter size and stride in the first two layers of AlexNet	• Extra information processing is required for visualization
VGG	• Proposed an idea of effective receptive field • Gave the idea of simple and homogenous topology	• Use of computationally expensive fully connected layers
GoogLeNet	• Introduced the idea of using Mutiscale Filters within the layers • Gave a new idea of split, transform, and merge • Reduce the number of parameters by using bottleneck layer, global average-pooling at last layer and Sparse Connections • Use of auxiliary classifiers to improve the convergence rate	• Tedious parameter customization due to heterogeneous topology • May lose the useful information due to representational bottleneck

Depth based CNNs

CNNs which improve themselves by increasing the depth to utilize more cascaded filters and to achieve better feature representation

CNNs: **Highway Networks** **ResNet** **Inception-V3, V4** **Inception-ResNet**

Architecture Name	Year	Main contribution	Parameters	Error Rate	Depth	Category	Reference
Inception-V3	2015	- Handles the problem of a representational bottleneck - Replace large size filters with small filters	23.6 M	ImageNet: 3.5 Multi-Crop: 3.58 Single-Crop: 5.6	159	Depth + Width	(Szegedy et al. 2016b)
Highway Networks	2015	- Introduced an idea of Multi-path	2.3 M	CIFAR-10: 7.76	19	Depth + Multi-Path	(Srivastava et al. 2015a)
Inception-V4	2016	- Split transform and merge idea Uses asymmetric filters	35 M	ImageNet: 4.01	70	Depth +Width	(Szegedy et al. 2016a)
Inception-ResNet	2016	- Uses split transform merge idea and residual links	55.8M	ImageNet: 3.52	572	Depth + Width + Multi-Path	(Szegedy et al. 2016a)
ResNet	2016	- Residual learning - Identity mapping based skip connections	25.6 M 1.7 M	ImageNet: 3.6 CIFAR-10: 6.43	152 110	Depth + Multi-Path	(He et al. 2015a)