

XI. SAMPLING β

According to [?], β is distributed as follows:

$$\beta = (\beta_1, \dots, \beta_K, \beta_u) \sim \text{Dir}(m_{.1}, \dots, m_{.K}, \gamma) \quad (79)$$

Where $m_{.k}$ represent the number of tables serving the dish k in all restaurants, in the chinese restaurant franchise. The sampling of the table configuration \mathbf{m} can be done using the unsigned Stirling numbers of the first kind $s(n, m)$ [?]:

$$\mathbf{p}(m_{ik} = m \mid Z, \mathbf{m}^{-jk}, \beta) = \frac{\Gamma(\alpha_0 \beta_k)}{\Gamma(\alpha_0 \beta_k + N_{jk})} s(n_{jk}, m) (\alpha_0 \beta_k)^m \quad (80)$$