

APPLICATION OF MULTIPLE REGRESSION ANALYSIS OF BASE BALL GAME

TESTING FOR WHICH VARIABLE CORRELATE WITH
RUN_SCORE

PERFORM MULTIPLE REGRESSION BETWEEN RUNS-SCORE IN A BASE BALL GAME AND OTHER
EXPLANATORY VARIABLES AS EXPLANINED IN THIS REPORT

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ADVANCE MATHS PROJECT

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INTRODUCTION

- MOTIVATION

The main motive behind this report is to analyze and predict the RUN-SCORE of 30 MLB teams of a base game within certain period using explanatory variables. Additionally, I want to know which explanatory variable has strong correlation with the RUN-SCORE variable and how relevant is this variable to the prediction of the response variable. Also, other statistical test will be carried out to validate the result.

- EXPLANATION OF THE PROJECT

This project consists of data from baseball games of 30 MLB teams. One of the tests is to predict which variable correlate strongly with the response variable. The data shows the runs score bats, batting-average etc. To start with, descriptive statistic like DATA COLLECTION, EXPLAINATION OF VARIABLES will be explained etc. Followed by STATISTICAL ANALYSIS such as statistical test, analysis etc. The project will be rounded up with a result summarizing all the analytical work.

DESCRIPTIVE STATISTICS

- DATA COLLECTION

Data was collected from www.statcrunch.com. The data consist of RUN-SCORE as a response variable (dependent variable) and four independent variable; BATTING-AVG, OBP, SLG, OPS. Each variable will be discussed in the subsequent heading.

- EXPLANATION OF A VARIABLE

As mentioned above, the following are the variables used in this project with their respective meaning:

- RUNS-SCORE

This is the total number of all runs the baseball team scored by the end of the season (dependent variable) *represent as y*

- BATTING-AVG

This is equal to the number of hits divided by bats *represent as x_1*

- OBP

On base percentage *represent as x_2*

- SLG (SLUGGING)

Weights hits to first base as 1 point *represent as x_3*

- OPS

On base plus slugging. *represent as x_4*

- DISCRIPTIVE STATISTICS

- GETTING THE MEAN, NUMBER, MINIMUM AND MAXIMUM VALUE FOR EACH VARIABLE

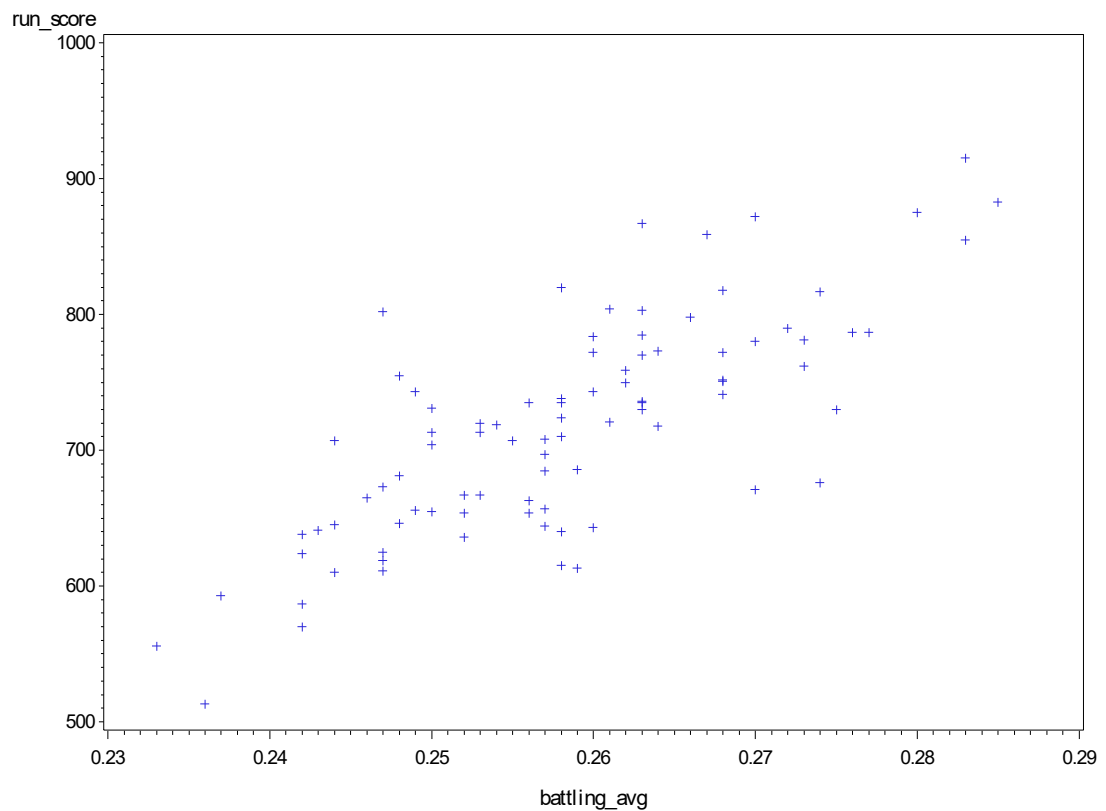
Conducting a descriptive test on each variable, starting with total number for each variable using proc mean.

| Variable | N | Mean | Median | Minimum | Maximum |
|--------------|----|--------|--------|---------|---------|
| run_score | 90 | 717.06 | 719.50 | 513.00 | 915.00 |
| battling_avg | 90 | 0.26 | 0.26 | 0.23 | 0.29 |
| obp | 90 | 0.33 | 0.33 | 0.29 | 0.36 |
| slg | 90 | 0.41 | 0.41 | 0.34 | 0.48 |
| ops | 90 | 0.73 | 0.73 | 0.64 | 0.84 |

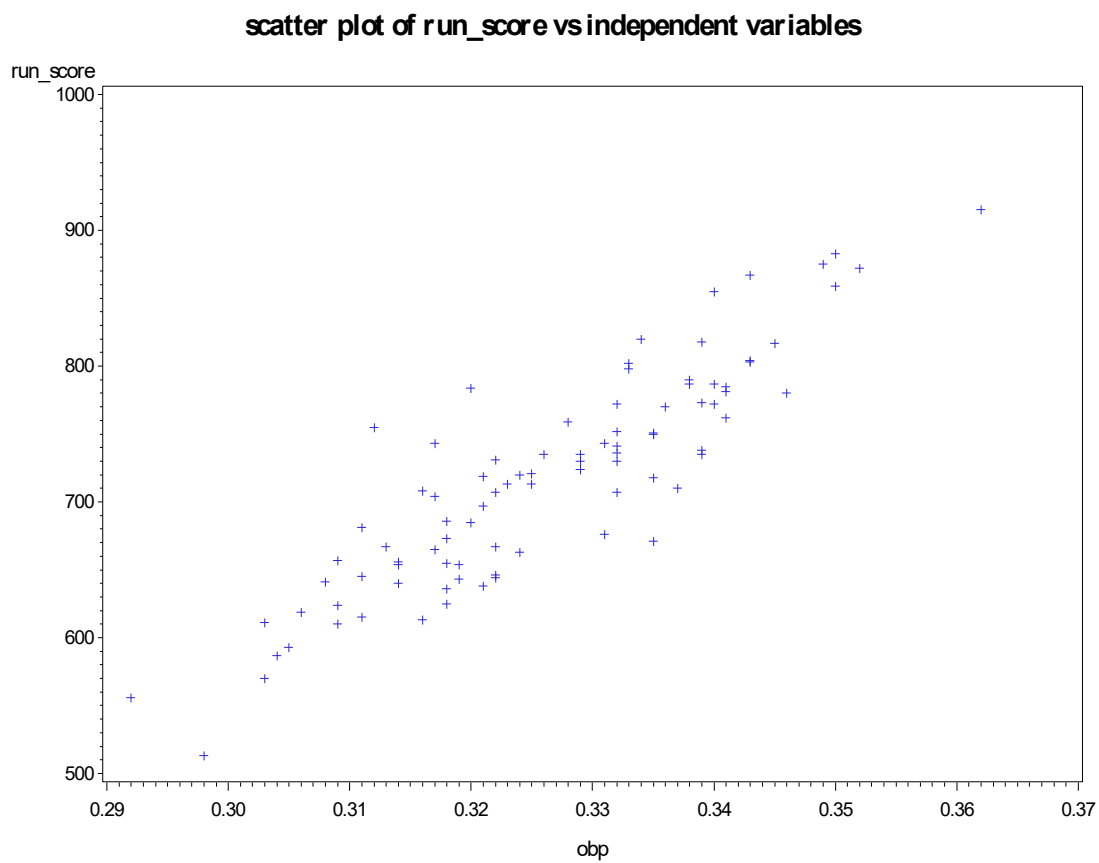
From the data above, it is shown that all explanatory variables have equal mean and median except for the response variable whose mean differs from the median. This means that the distribution of each explanatory variable is symmetrical and that their respective distribution will have a zero skewness.

- SCATTER DIAGRAM BETWEEN RUN-SCORE AND THE EXPLANATORY VARIABLES

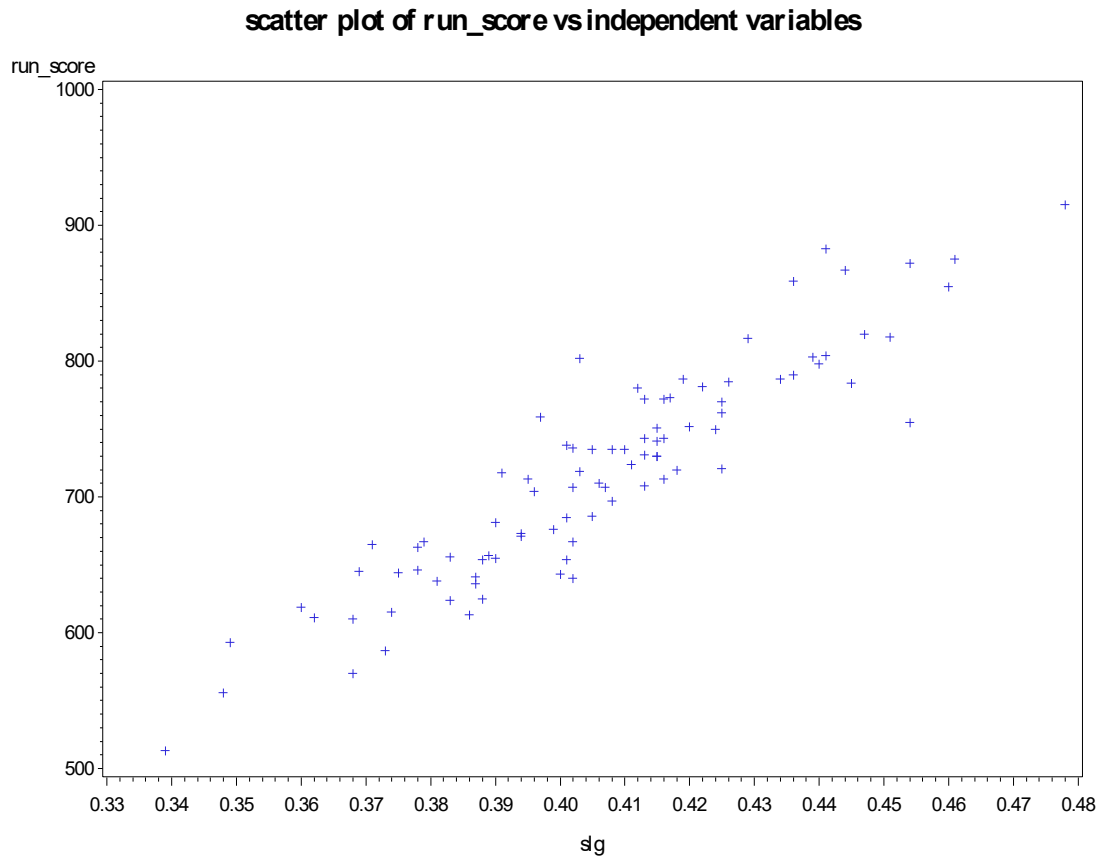
scatter plot of run_score vs independent variables



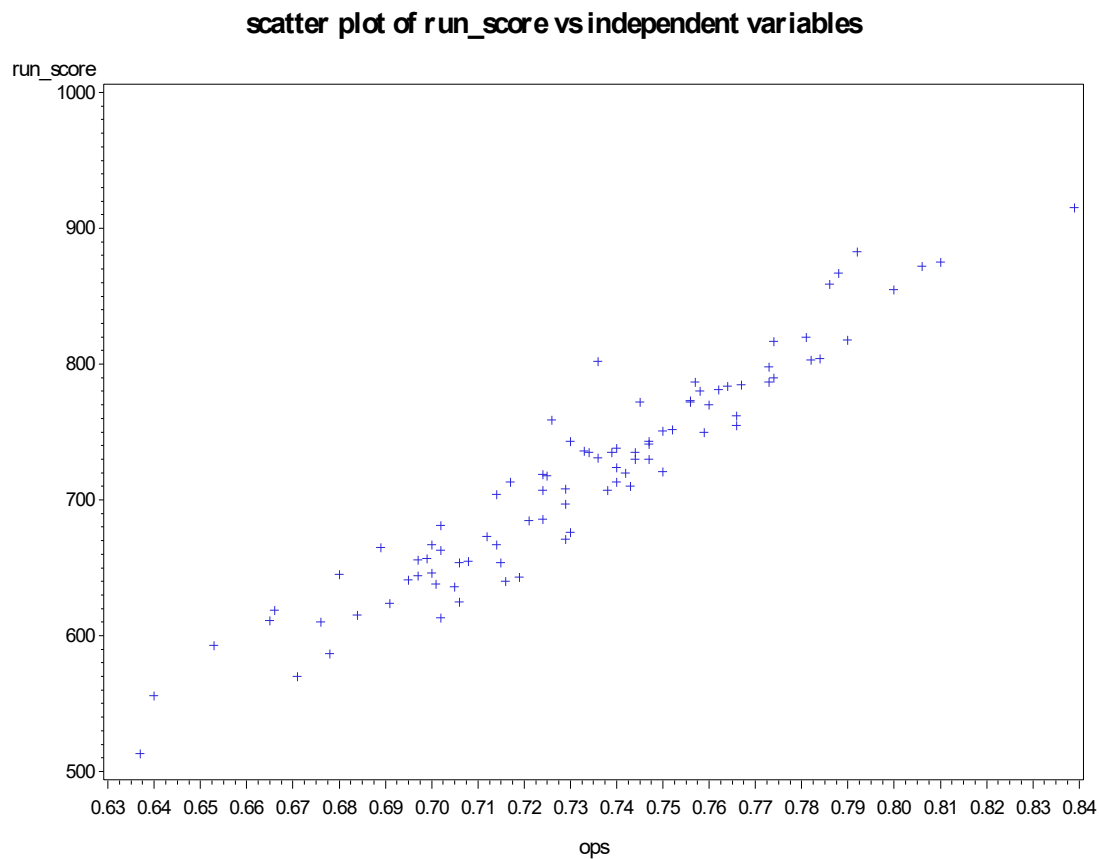
For scatter plot of RUN_SCORE Vs BATTLING_AVG, a moderate positive correlation exist between the two variables



As shown above, there appears to be a moderate positive correlation between the RUN_SCORE Vs OBP



The scatter plot of RUN_SCORE Vs SLG appear to be positively correlated.



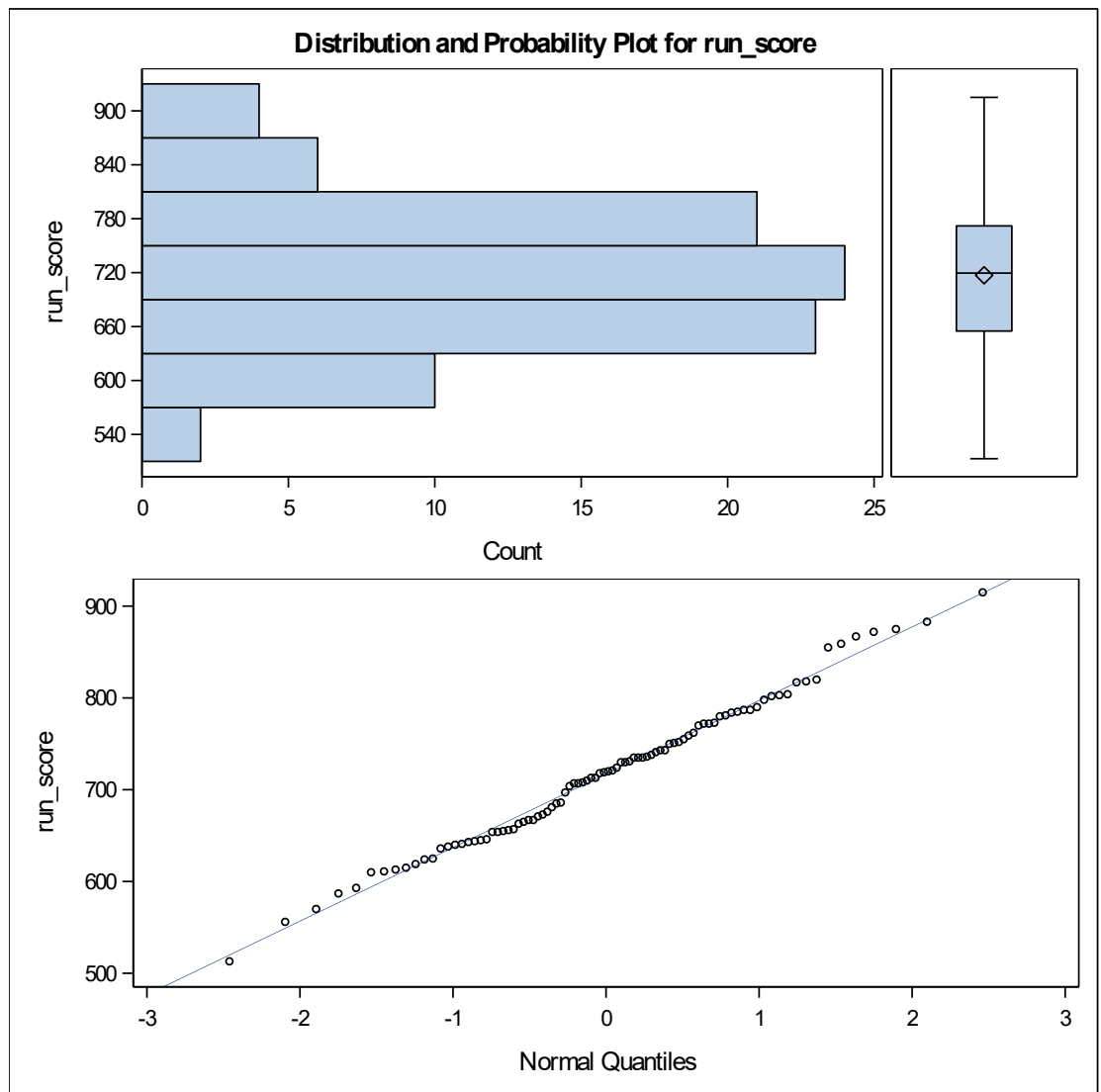
Likewise, the scatter plot between RUN_SCORE and OPS appears to be positively correlated.

From all the scatter plots above, relationship between RUNS_SCORE and all independent variables appear to be linear, so there is no need for transformation of data during multiple regression analysis.

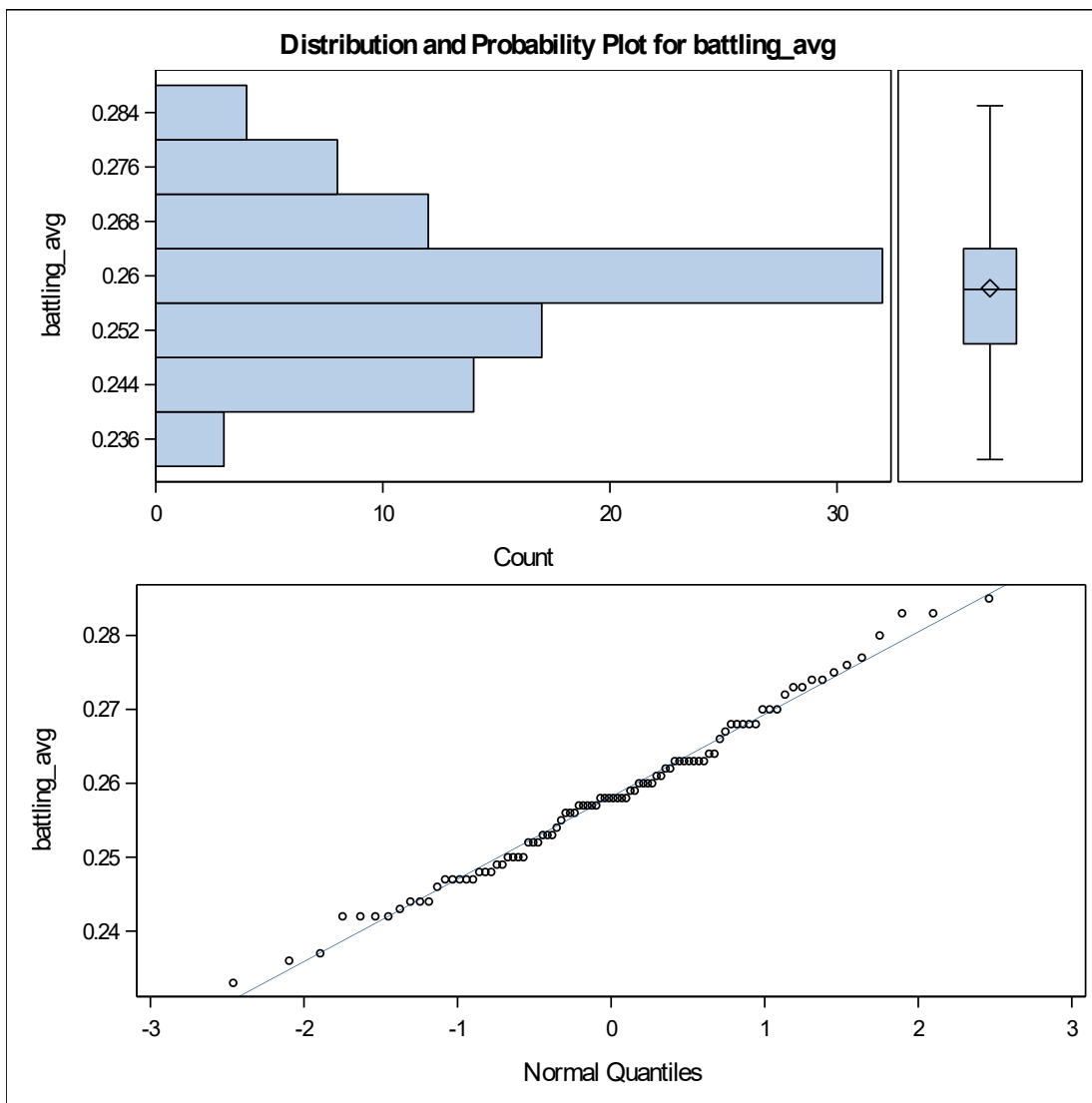
- GRAPHS

NORMAL PLOT

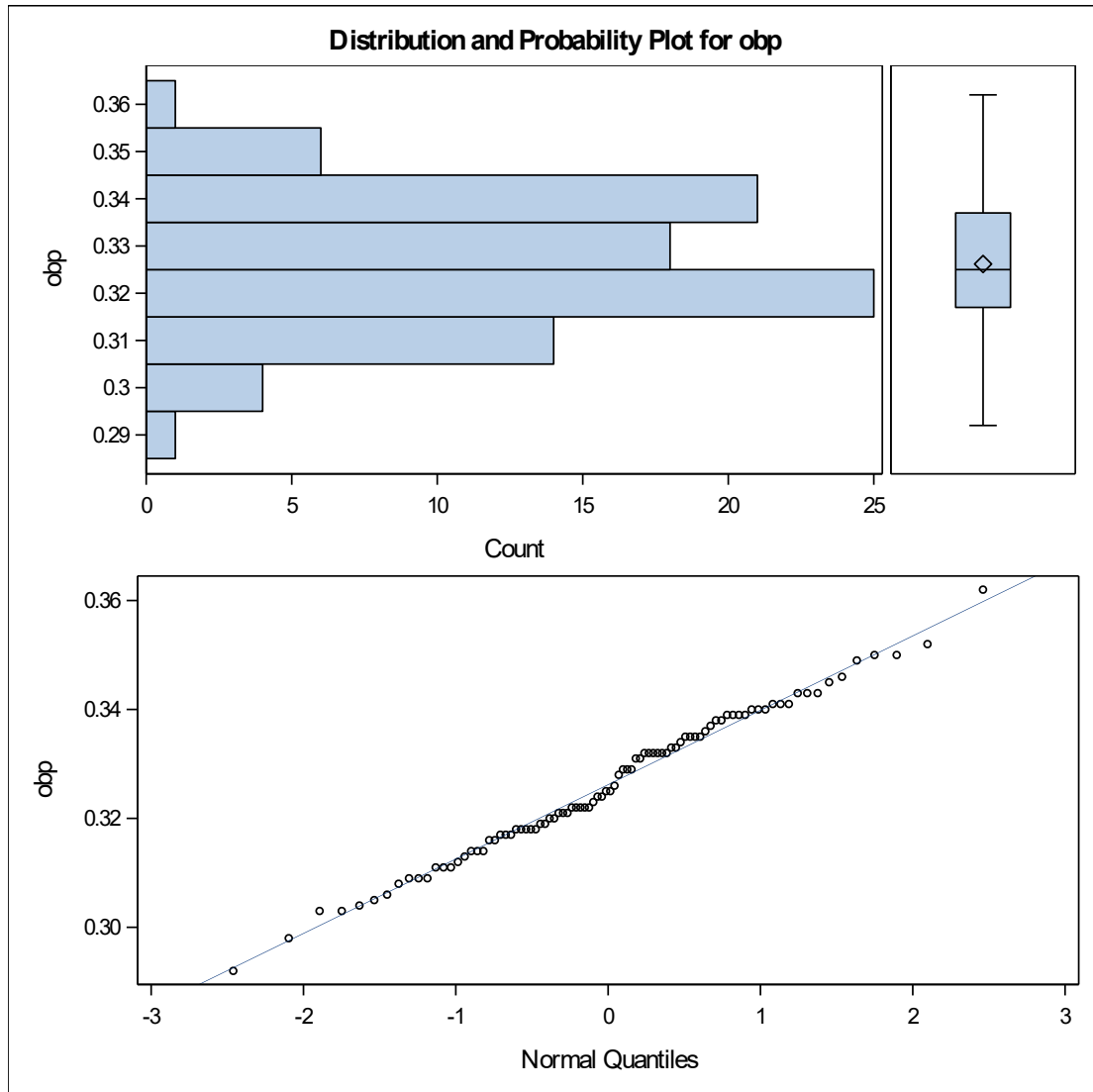
Testing for normality of all variables, we have:



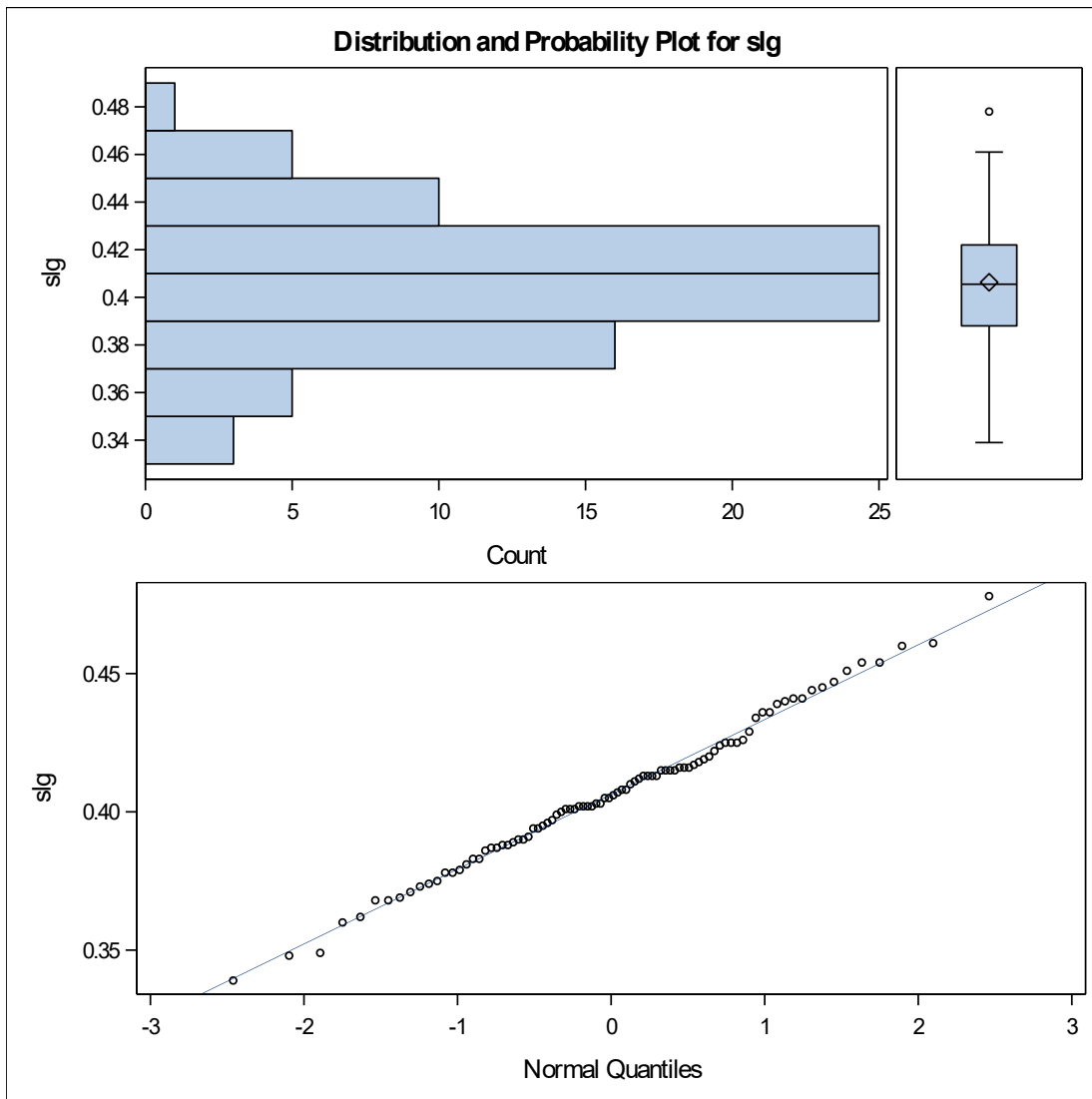
The points in this plot form a linear pattern. Its shows that the normal distribution is a good model for this data set



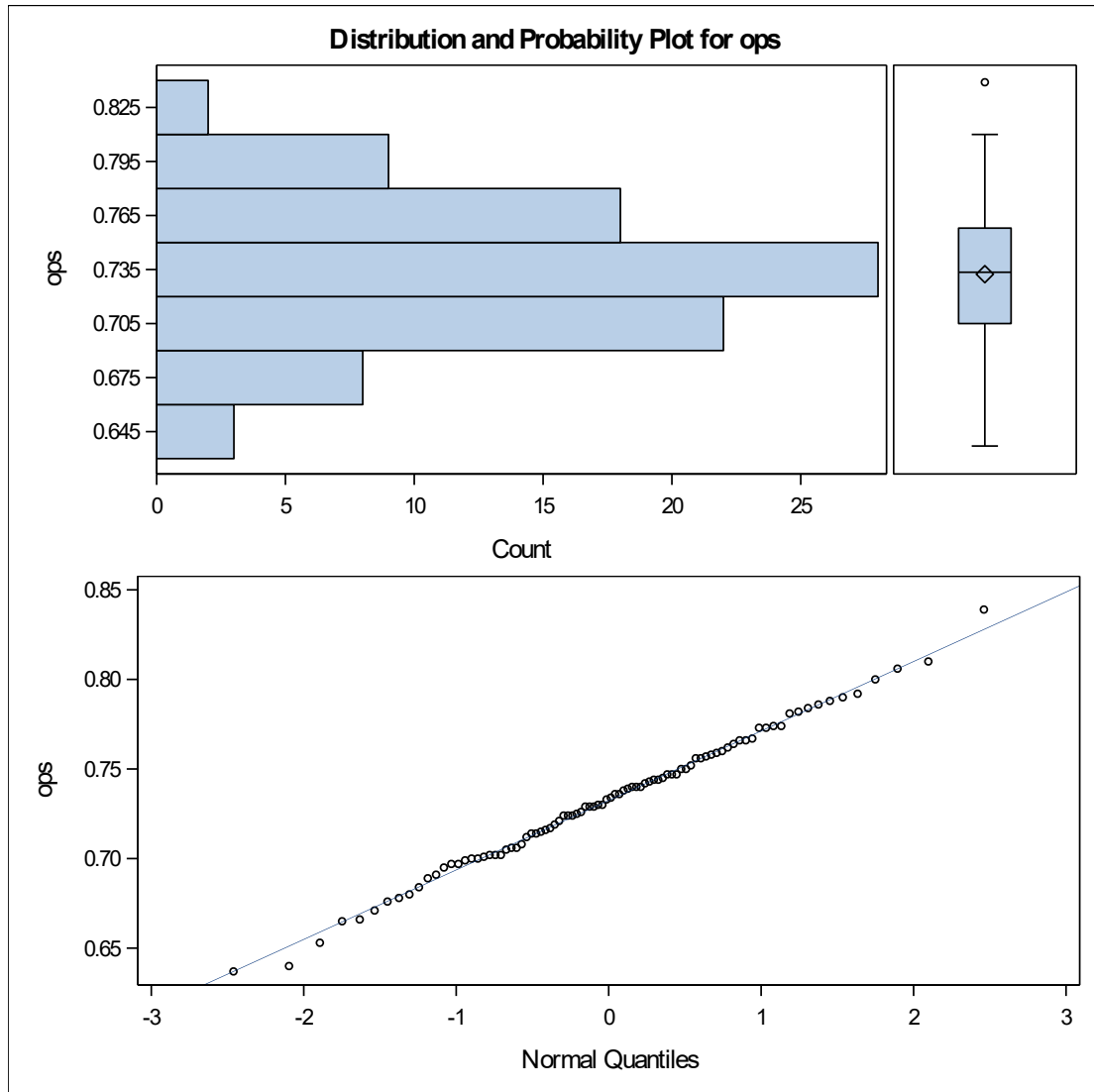
Likewise, **BATTLING_AVG** data form a linear pattern. It shows that the data is normally distributed.



For the OBP data, all points form a nearly pattern. It shows that the normal distribution is good model for this data set.



This data is normally distributed and all points form a moderately linear pattern.



For OPS variables, all values are normally distributed. The points on this plot form a nearly linear pattern.

STATISTICAL TEST

The following test will be carried out for analysis

- FITTING MULTIPLE REGRESSION MODEL AND TEST FOR VARIABILITY
- STATISTICAL INFERENCE ON MULTIPLE REGRESSION
- REGRESSION DIAGNOSIS
- RESIDUALS ANALYSIS
- MULTICOLLINEARITY
- VARIABLE SELECTION METHODS

JUSTIFICATION

The reason for using all this test for analysis is to test which of the predictive variable will have high correlation with the independent variable (RUN_SCORE).

STATISTICAL ANALYSIS

In this section, statistical analysis will be carried out on the response variable vs the explanatory variables using multiple regression analysis. Also, a test to know which variable has a greater correlation with the response variable will be conducted. Testing which explanatory variable fits the model will too and several other test.

- FITTING MULTIPLE REGRESSION MODEL AND TEST FOR VARIABILITY

To predict the RUNS-SCORE, a model is developed. The model is

$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4$. A PROC REG of SAS software will be used to fit the model as follows:

$$y = -786.01 - 789.47x_1 - 7839.50x_2 - 9173.3x_3 + 10911x_4$$

Where $\beta_0 = -786.01, \beta_1 = -789.4, \beta_2 = -7839.50, \beta_3 = -9173.3, \beta_4 = 10911$

All these are all coefficients of multiple regression.

| | | | |
|-----------------------|-----------|-----------------|--------|
| Root MSE | 21.99046 | R-Square | 0.9281 |
| Dependent Mean | 717.05556 | Adj R-Sq | 0.9247 |
| Coeff Var | 3.06677 | | |

Also from the table above, about 92.8% in RUN_SCORE IS accounted for by BATLLING_AVG, OBP, SLG and OPS.

- STATISTICAL INFERENCE FOR MULTIPLE REGRESSION

After fitting a multiple regression, the next is to determine which explanatory variables (BATLLING_AVG, OBP, SLG and OPS.) have a statistically significant effect on the response variable (RUN_SCORE).

This can be done by testing the hypothesis $H_{0j} : \beta_j = 0$ Vs $H_{1j} : \beta_j \neq 0$ for each β_j .

That is, test for $H_0 : \beta_1 = \beta_2 = \beta_3 = \beta_4 = 0$ Vs

$H_1 : \beta_1 \neq \beta_2 \neq \beta_3 \neq \beta_4 \neq 0$

Using PROC REG in SAS, derive analysis of variance (ANOVA) for this test as follows:

| Analysis of Variance | | | | | |
|----------------------|----|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 4 | 530482 | 132621 | 274.25 | <.0001 |
| Error | 85 | 41104 | 483.58041 | | |
| Corrected Total | 89 | 571587 | | | |

From SAS output, we can see that the F-statistic for testing at $\alpha = 0.05$ significant level.
 $H_0 : \beta_1 = \beta_2 = \beta_3 = \beta_4 = 0$ equals $274.25 > f_{4,85,0.05} = 2.479$
 This shows that one or all of $\beta_1, \beta_2, \beta_3, \beta_4$ non zero

Next we test the significance of individual terms

That is $H_{01} : \beta_1 = 0, H_{02} : \beta_2 = 0, H_{03} : \beta_3 = 0, H_{04} : \beta_4 = 0$

| Parameter Estimates | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| Intercept | 1 | -786.01473 | 60.31856 | -13.03 | <.0001 |
| battling_avg | 1 | -789.46564 | 397.51178 | -1.99 | 0.0503 |
| obp | 1 | -7839.49410 | 4212.63339 | -1.86 | 0.0662 |
| slg | 1 | -9173.65474 | 4250.71303 | -2.16 | 0.0337 |
| ops | 1 | 10911 | 4237.86669 | 2.57 | 0.0118 |

testing for $t_{85,0.025} = 1.99$ at $\alpha = 0.05$. If we use the T – statistic of each variable as shown in the table above, we have the following

for $\beta_1; |t| = 1.99 = 1.99$, accept H_{01} no significant different and reject x_1

for $\beta_2; |t| = 1.86 < 1.99$, accept H_{02} No significant different and reject x_2

for $\beta_3; |t| = 2.16 > 1.99$, reject H_{03} There is significant different and accept x_3

for $\beta_4; |t| = 2.57 > 1.99$, reject H_{04} . There is significant different and accept x_4

Also, the P – Value shows that x_1 and x_2 should be removed from the model, leaving behind x_3 and x_4

We can now compute 95% CI for β_3 and β_4 . that is

$$CI \text{ for } \beta_3: [\hat{\beta}_3 \pm t_{85,0.025}SE(\hat{\beta}_3)] = [-9173.65 \pm 1.99 \times 4250.71] = [17632.56, -714.74]$$

$$CI \text{ for } \beta_4: [\hat{\beta}_4 \pm t_{85,0.025}SE(\hat{\beta}_4)] = [10911 \pm 1.99 \times 4237.84] = [2477.64, 19344.36]$$

We may now refit the rectify model.

| Parameter Estimates | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| Intercept | 1 | -820.35086 | 59.49940 | -13.79 | <.0001 |
| slg | 1 | -947.95439 | 414.65213 | -2.29 | 0.0247 |
| ops | 1 | 2624.96315 | 289.22612 | 9.08 | <.0001 |

Thus we have $y = \beta_0 + \beta_3x_3 + \beta_4x_4 = -820.35 - 947.95x_3 + 2624.96x_4$

▪ REGRESSION DIAGNOSTICS OF THE NEW MODEL

RESIDUAL ANALYSIS

With the new fitted model, I want to test if there is an influential and an outliers' observations.

Using *INFLUENCE* option of *PROC REG*, we derive the following table.

| Output Statistics | | | | | | | | |
|-------------------|----------|----------|---------------|--------------|---------|-----------|---------|---------|
| Obs | Residual | RStudent | Hat Diag H | Cov Ratio | DFFITS | DFBETAS | | |
| | | | | | | Intercept | slg | ops |
| 1 | 10.8831 | 0.4825 | 0.0172 | 1.0449 | 0.0639 | 0.0228 | 0.0378 | -0.0359 |
| 2 | 3.8598 | 0.1724 | 0.0343 | 1.0710 | 0.0325 | 0.0272 | 0.0198 | -0.0232 |
| 3 | 6.2579 | 0.2802 | 0.0384 | 1.0737 | 0.0560 | 0.0337 | 0.0471 | -0.0466 |
| 4 | 6.1377 | 0.2776 | 0.0572 | 1.0951 | 0.0684 | -0.0388 | 0.0095 | 0.0037 |
| 5 | -22.3681 | -1.0014 | 0.0277 | 1.0284 | -0.1692 | -0.1198 | -0.1217 | 0.1293 |
| 6 | -11.0668 | -0.4904 | 0.0164 | 1.0437 | -0.0632 | -0.0274 | 0.0029 | 0.0048 |
| 7 | 15.3933 | 0.6813 | 0.0113 | 1.0303 | 0.0727 | 0.0055 | 0.0076 | -0.0068 |
| 8 | 25.5171 | 1.1370 | 0.0153 | 1.0054 | 0.1418 | 0.0790 | 0.0468 | -0.0580 |
| 9 | 4.1644 | 0.1839 | 0.0117 | 1.0463 | 0.0200 | -0.0035 | -0.0027 | 0.0034 |
| 10 | -10.3335 | -0.4595 | 0.0234 | 1.0523 | -0.0711 | 0.0372 | -0.0003 | -0.0108 |
| 11 | -40.0668 | -1.8064 | 0.0164 | 0.9413 | -0.2330 | -0.1011 | 0.0107 | 0.0178 |
| 12 | -5.5890 | -0.2490 | 0.0288 | 1.0637 | -0.0429 | -0.0286 | -0.0031 | 0.0102 |
| 13 | -9.2207 | -0.4076 | 0.0123 | 1.0422 | -0.0455 | 0.0043 | -0.0059 | 0.0030 |
| 14 | -5.7952 | -0.2592 | 0.0363 | 1.0718 | -0.0503 | -0.0369 | -0.0398 | 0.0417 |
| 15 | -9.7656 | -0.4374 | 0.0378 | 1.0688 | -0.0867 | 0.0031 | 0.0587 | -0.0481 |
| 16 | -24.4909 | -1.0981 | 0.0285 | 1.0220 | -0.1880 | -0.0522 | -0.1367 | 0.1220 |
| 17 | 32.3890 | 1.4724 | 0.0445 | 1.0055 | 0.3176 | 0.1958 | -0.0294 | -0.0298 |
| 18 | 5.9027 | 0.2655 | 0.0468 | 1.0835 | 0.0588 | -0.0277 | -0.0511 | 0.0487 |
| 19 | 39.7716 | 1.8097 | 0.0342 | 0.9583 | 0.3405 | -0.2096 | -0.0064 | 0.0661 |
| 20 | 30.1711 | 1.3607 | 0.0325 | 1.0038 | 0.2494 | 0.1307 | -0.0406 | -0.0027 |
| 21 | 25.6943 | 1.1438 | 0.0131 | 1.0026 | 0.1318 | 0.0308 | -0.0172 | 0.0064 |
| 22 | 4.7230 | 0.2111 | 0.0349 | 1.0711 | 0.0401 | 0.0265 | 0.0005 | -0.0076 |
| 23 | 30.0860 | 1.3781 | 0.0617 | 1.0334 | 0.3534 | 0.1874 | -0.0836 | 0.0155 |
| 24 | 26.2626 | 1.2134 | 0.0822 | 1.0720 | 0.3631 | 0.3189 | 0.1078 | -0.1738 |
| 25 | -22.1522 | -0.9998 | 0.0435 | 1.0455 | -0.2131 | -0.1778 | -0.0660 | 0.1012 |
| 26 | -25.4903 | -1.1418 | 0.0254 | 1.0154 | -0.1845 | 0.1335 | 0.0889 | -0.1096 |
| 27 | 7.9552 | 0.3516 | 0.0123 | 1.0437 | 0.0393 | 0.0136 | 0.0092 | -0.0107 |

| Output Statistics | | | | | | | | |
|-------------------|----------|----------|---------------|--------------|---------|-----------|---------|---------|
| Obs | Residual | RStudent | Hat Diag H | Cov Ratio | DFFITS | DFBETAS | | |
| | | | | | | Intercept | slg | ops |
| 28 | 11.4394 | 0.5200 | 0.0648 | 1.0966 | 0.1368 | -0.0249 | 0.0751 | -0.0521 |
| 29 | 38.6329 | 1.7562 | 0.0344 | 0.9646 | 0.3314 | 0.1926 | 0.2724 | -0.2687 |
| 30 | -6.4322 | -0.2871 | 0.0320 | 1.0664 | -0.0522 | -0.0433 | -0.0262 | 0.0326 |
| 31 | -14.7729 | -0.6560 | 0.0184 | 1.0390 | -0.0897 | -0.0277 | -0.0547 | 0.0505 |
| 32 | -3.9922 | -0.1796 | 0.0484 | 1.0867 | -0.0405 | 0.0250 | 0.0353 | -0.0353 |
| 33 | -43.4629 | -1.9679 | 0.0181 | 0.9238 | -0.2670 | -0.1438 | -0.0147 | 0.0498 |
| 34 | -7.8426 | -0.3526 | 0.0458 | 1.0803 | -0.0773 | 0.0185 | -0.0360 | 0.0230 |
| 35 | -7.1179 | -0.3148 | 0.0141 | 1.0465 | -0.0377 | -0.0181 | -0.0143 | 0.0161 |
| 36 | -3.4806 | -0.1539 | 0.0140 | 1.0491 | -0.0183 | 0.0050 | -0.0010 | -0.0008 |
| 37 | -8.0625 | -0.3586 | 0.0246 | 1.0567 | -0.0570 | 0.0241 | -0.0090 | -0.0001 |
| 38 | -12.7966 | -0.5719 | 0.0320 | 1.0574 | -0.1039 | 0.0011 | 0.0663 | -0.0537 |
| 39 | -1.7405 | -0.0770 | 0.0168 | 1.0528 | -0.0101 | 0.0042 | 0.0002 | -0.0014 |
| 40 | -3.9704 | -0.1758 | 0.0171 | 1.0521 | -0.0232 | 0.0127 | 0.0107 | -0.0123 |
| 41 | 20.9032 | 0.9283 | 0.0136 | 1.0186 | 0.1090 | 0.0471 | 0.0413 | -0.0450 |
| 42 | 28.9098 | 1.3120 | 0.0459 | 1.0225 | 0.2879 | 0.2200 | 0.0397 | -0.0918 |
| 43 | -41.6384 | -1.8857 | 0.0219 | 0.9374 | -0.2824 | 0.1102 | 0.1980 | -0.1907 |
| 44 | 28.3289 | 1.2706 | 0.0245 | 1.0037 | 0.2015 | 0.1540 | 0.1037 | -0.1242 |
| 45 | 9.1514 | 0.4078 | 0.0281 | 1.0591 | 0.0694 | 0.0041 | -0.0396 | 0.0308 |
| 46 | -20.0635 | -0.8920 | 0.0165 | 1.0239 | -0.1154 | 0.0506 | 0.0071 | -0.0209 |
| 47 | 1.1657 | 0.0518 | 0.0244 | 1.0610 | 0.0082 | -0.0058 | -0.0043 | 0.0051 |
| 48 | 9.8181 | 0.4359 | 0.0207 | 1.0502 | 0.0634 | 0.0386 | 0.0066 | -0.0155 |
| 49 | 29.4379 | 1.3380 | 0.0482 | 1.0225 | 0.3010 | -0.2580 | -0.1714 | 0.2104 |
| 50 | -1.0465 | -0.0468 | 0.0373 | 1.0754 | -0.0092 | 0.0011 | 0.0066 | -0.0056 |
| 51 | 28.2585 | 1.2602 | 0.0135 | 0.9934 | 0.1474 | -0.0563 | -0.0439 | 0.0523 |
| 52 | -18.7872 | -0.8441 | 0.0380 | 1.0498 | -0.1677 | -0.1395 | -0.0592 | 0.0852 |
| 53 | 28.4423 | 1.2837 | 0.0362 | 1.0147 | 0.2489 | 0.0351 | -0.1373 | 0.1009 |
| 54 | -17.3941 | -0.7993 | 0.0809 | 1.1017 | -0.2372 | -0.1465 | 0.0352 | 0.0122 |

| Output Statistics | | | | | | | | |
|-------------------|----------|----------|---------------|--------------|---------|-----------|---------|---------|
| Obs | Residual | RStudent | Hat Diag H | Cov Ratio | DFFITS | DFBETAS | | |
| | | | | | | Intercept | slg | ops |
| 55 | -9.4819 | -0.4201 | 0.0166 | 1.0463 | -0.0546 | -0.0249 | -0.0311 | 0.0312 |
| 56 | 13.3305 | 0.5918 | 0.0186 | 1.0421 | 0.0814 | -0.0315 | -0.0516 | 0.0506 |
| 57 | 72.4036 | 3.4261 | 0.0223 | 0.7214 | 0.5177 | -0.2472 | -0.3653 | 0.3641 |
| 58 | 17.4466 | 0.7767 | 0.0212 | 1.0357 | 0.1142 | -0.0746 | -0.0585 | 0.0684 |
| 59 | -4.9996 | -0.2494 | 0.2256 | 1.3340 | -0.1346 | -0.0645 | -0.1287 | 0.1201 |
| 60 | -13.4208 | -0.5949 | 0.0156 | 1.0388 | -0.0749 | -0.0353 | -0.0035 | 0.0120 |
| 61 | -11.1269 | -0.4942 | 0.0207 | 1.0482 | -0.0718 | -0.0226 | -0.0471 | 0.0432 |
| 62 | -13.7002 | -0.6152 | 0.0405 | 1.0649 | -0.1265 | 0.0809 | 0.1059 | -0.1077 |
| 63 | -6.0955 | -0.2694 | 0.0132 | 1.0465 | -0.0312 | 0.0111 | 0.0062 | -0.0084 |
| 64 | 7.0018 | 0.3161 | 0.0536 | 1.0901 | 0.0752 | -0.0579 | -0.0146 | 0.0282 |
| 65 | -24.0545 | -1.0706 | 0.0146 | 1.0097 | -0.1304 | 0.0478 | 0.0616 | -0.0637 |
| 66 | -8.5126 | -0.3761 | 0.0116 | 1.0423 | -0.0408 | 0.0065 | 0.0034 | -0.0050 |
| 67 | -2.1289 | -0.0942 | 0.0151 | 1.0508 | -0.0116 | -0.0062 | -0.0028 | 0.0038 |
| 68 | 4.1757 | 0.1856 | 0.0250 | 1.0605 | 0.0297 | -0.0204 | -0.0185 | 0.0207 |
| 69 | -15.5724 | -0.6963 | 0.0311 | 1.0506 | -0.1247 | 0.0769 | 0.0060 | -0.0272 |
| 70 | -3.1476 | -0.1390 | 0.0127 | 1.0479 | -0.0158 | 0.0041 | 0.0007 | -0.0018 |
| 71 | 2.2277 | 0.0992 | 0.0289 | 1.0658 | 0.0171 | -0.0121 | -0.0118 | 0.0129 |
| 72 | -44.8159 | -2.0289 | 0.0151 | 0.9136 | -0.2514 | -0.1341 | -0.1056 | 0.1192 |
| 73 | -10.2009 | -0.4524 | 0.0182 | 1.0470 | -0.0615 | -0.0338 | -0.0369 | 0.0383 |
| 74 | 42.4279 | 1.9517 | 0.0494 | 0.9563 | 0.4447 | -0.3800 | -0.2167 | 0.2815 |
| 75 | 1.1860 | 0.0538 | 0.0623 | 1.1039 | 0.0138 | -0.0104 | -0.0119 | 0.0125 |
| 76 | -4.1673 | -0.1853 | 0.0251 | 1.0607 | -0.0297 | 0.0213 | 0.0133 | -0.0168 |
| 77 | 12.3018 | 0.5505 | 0.0347 | 1.0613 | 0.1044 | -0.0836 | -0.0580 | 0.0702 |
| 78 | -48.7533 | -2.2528 | 0.0446 | 0.9124 | -0.4870 | 0.2461 | 0.4215 | -0.4071 |
| 79 | -13.8710 | -0.6419 | 0.0963 | 1.1293 | -0.2095 | 0.1546 | 0.0116 | -0.0534 |
| 80 | 49.9655 | 2.2808 | 0.0196 | 0.8854 | 0.3226 | -0.0942 | -0.2086 | 0.1951 |
| 81 | 13.9902 | 0.6308 | 0.0480 | 1.0725 | 0.1416 | -0.0047 | 0.0897 | -0.0692 |

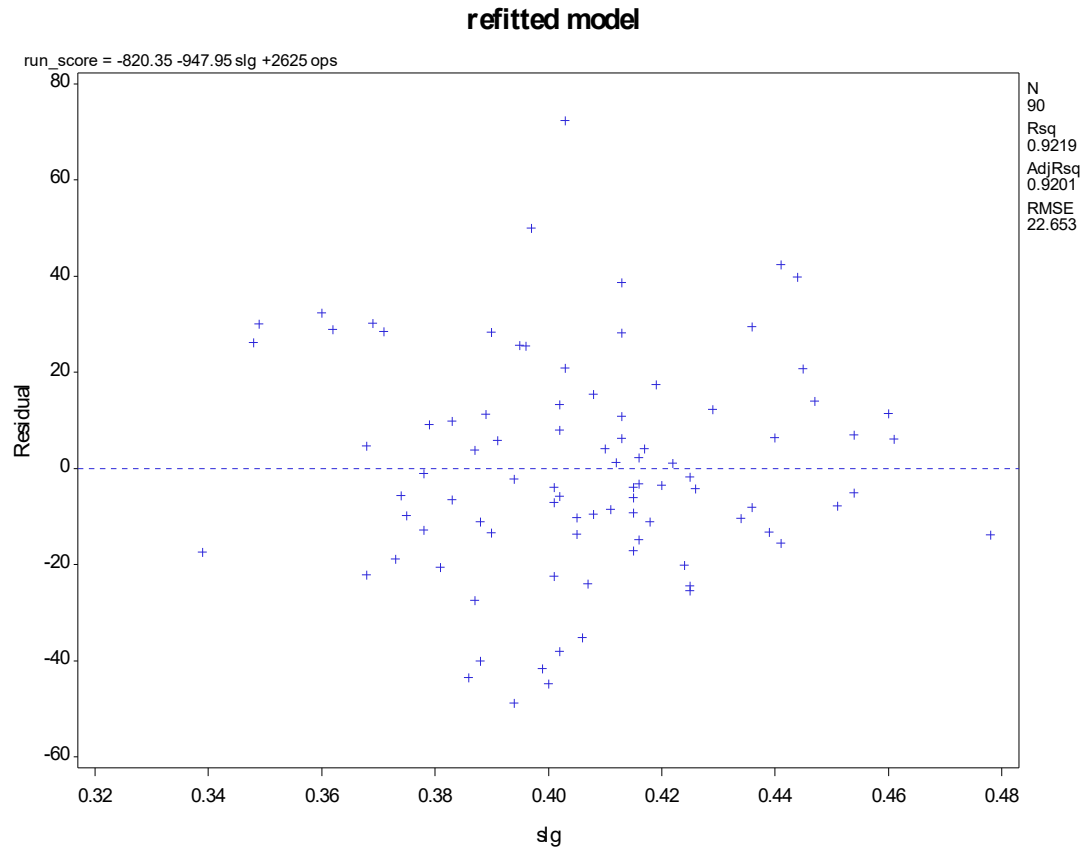
| Output Statistics | | | | | | | | |
|-------------------|----------|----------|---------------|--------------|---------|-----------|---------|---------|
| Obs | Residual | RStudent | Hat Diag H | Cov Ratio | DFFITS | DFBETAS | | |
| | | | | | | Intercept | slg | ops |
| 82 | -27.3898 | -1.2229 | 0.0169 | 1.0000 | -0.1602 | -0.0664 | 0.0144 | 0.0057 |
| 83 | -20.5777 | -0.9185 | 0.0236 | 1.0297 | -0.1428 | -0.0218 | 0.0666 | -0.0479 |
| 84 | -38.0451 | -1.7235 | 0.0289 | 0.9629 | -0.2974 | -0.2093 | -0.2198 | 0.2315 |
| 85 | 11.2559 | 0.5022 | 0.0294 | 1.0573 | 0.0874 | 0.0705 | 0.0508 | -0.0596 |
| 86 | -17.0955 | -0.7578 | 0.0132 | 1.0284 | -0.0877 | 0.0313 | 0.0175 | -0.0236 |
| 87 | -13.2184 | -0.5902 | 0.0299 | 1.0543 | -0.1036 | 0.0672 | 0.0121 | -0.0292 |
| 88 | 20.7187 | 0.9731 | 0.1172 | 1.1349 | 0.3547 | 0.1465 | 0.3254 | -0.2987 |
| 89 | 6.3543 | 0.2841 | 0.0356 | 1.0705 | 0.0546 | -0.0026 | 0.0319 | -0.0243 |
| 90 | -35.1273 | -1.5889 | 0.0309 | 0.9795 | -0.2839 | 0.1725 | 0.2225 | -0.2273 |

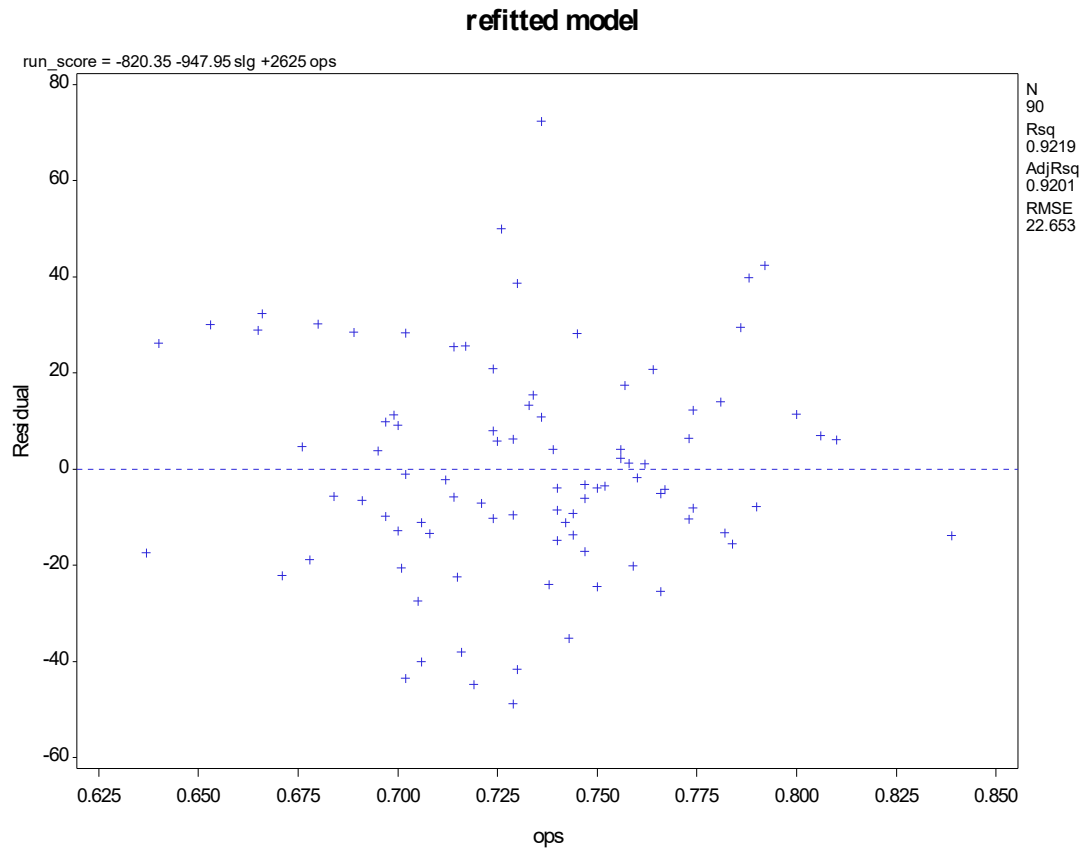
From the above table, we can test if there is an influential observations using the following formula;

if $h_{ii} > \frac{2(k+1)}{n}$ then we have an influential observation.

For influential observation, we have observation 24, 54 and 79.

PLOTS OF RESIDUALS AGAINST INDIVIDUAL PREDICTORS VARIABLES FOR THE NEW
FITTED MODEL



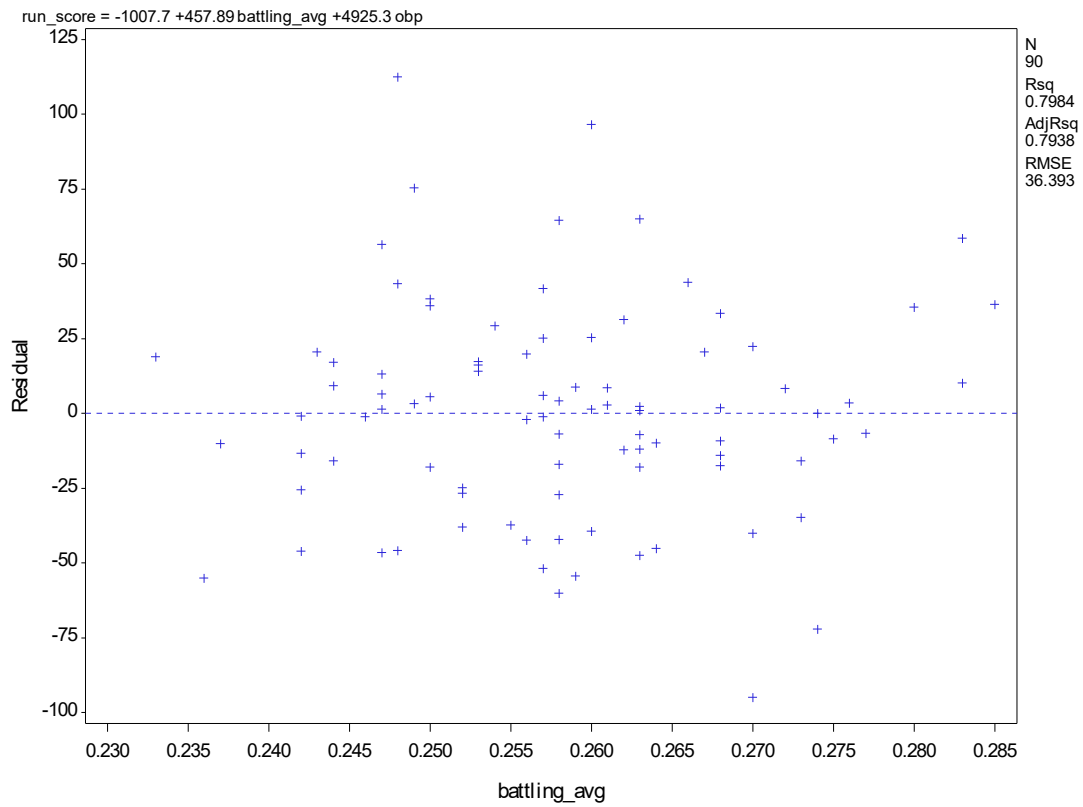


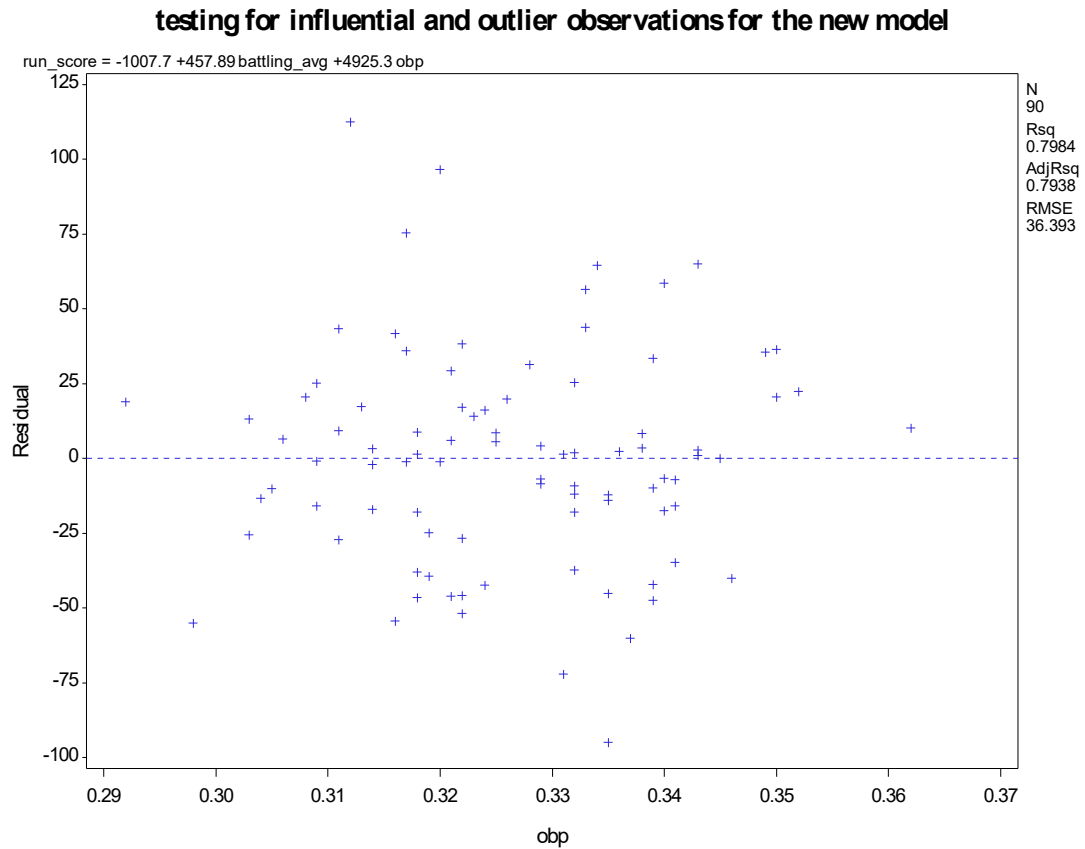
For each predictor variable, each plots are randomly dispersed.

PLOTS OF RESIDUALS AGAINST ANY OMITTED PREDICTOR VAIRABLES

This test is done to show if the excluded predictor variables BATTLING_AVG and OBP is worth included in the data. The two plots show points to be randomly scatter though out both plots and also a systematic pattern.

testing for influential and outlier observations for the new model





The two omitted variables look to be included in the model. But to test this further, we shall test for multicollinearity.

MULTICOLLINEARITY

Multicollinearity occurs when predictor variables are linearly related.

Going back to the first model, we can also use multicollinearity to test which variables should be excluded. This will also be used to test the first assumption of omitting BATTLING_AVG and OBP variables in the first place.

MEASURES OF MULTICOLLINEARITY

Use VIF option of PROC REG to measure MULTICOLLINEARITY.

| Parameter Estimates | | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|--------------------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t | Variance Inflation |
| Intercept | 1 | -786.01473 | 60.31856 | -13.03 | <.0001 | 0 |
| battling_avg | 1 | -789.46564 | 397.51178 | -1.99 | 0.0503 | 3.61502 |
| obp | 1 | -7839.49410 | 4212.63339 | -1.86 | 0.0662 | 609.24717 |
| slg | 1 | -9173.65474 | 4250.71303 | -2.16 | 0.0337 | 2433.21401 |
| ops | 1 | 10911 | 4237.86669 | 2.57 | 0.0118 | 4971.00404 |

From the table above, there are large VIF values, we can assume there are serious COLLINEARITY problems.

STANDARDIZED REGRESSION COEFFICIENTS

Comparing predictors variables magnitudes of their effects on the response variable. In order to do this effectively, I used STB option of PROC REG in SAS. The output is given as follows

| Parameter Estimates | | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|-----------------------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t | Standardized Estimate |
| Intercept | 1 | -786.01473 | 60.31856 | -13.03 | <.0001 | 0 |
| battling_avg | 1 | -789.46564 | 397.51178 | -1.99 | 0.0503 | -0.10983 |
| obp | 1 | -7839.49410 | 4212.63339 | -1.86 | 0.0662 | -1.33606 |
| slg | 1 | -9173.65474 | 4250.71303 | -2.16 | 0.0337 | -3.09645 |
| ops | 1 | 10911 | 4237.86669 | 2.57 | 0.0118 | 5.28002 |

From the table above, variable OPS seems to have larger effect on RUN_SCORE than any other variables.

VARIABLE SELECTION METHOD

STEPWISE REGRESSION

This is used for variable selection into the model. To know which variable deserves to be in the model. So I use stepwise regression of SAS solve the problem.

| Summary of Stepwise Selection | | | | | | | | |
|-------------------------------|------------------|------------------|----------------|------------------|----------------|---------|---------|--------|
| Step | Variable Entered | Variable Removed | Number Vars In | Partial R-Square | Model R-Square | C(p) | F Value | Pr > F |
| 1 | ops | | 1 | 0.9172 | 0.9172 | 11.8708 | 974.78 | <.0001 |
| 2 | slg | | 2 | 0.0047 | 0.9219 | 8.3245 | 5.23 | 0.0247 |
| 3 | battling_avg | | 3 | 0.0033 | 0.9252 | 6.4631 | 3.75 | 0.0560 |
| 4 | obp | | 4 | 0.0029 | 0.9281 | 5.0000 | 3.46 | 0.0662 |

Its shows that all variables seem to have entered the model. Known was removed at 0.015 significant level.

▪ ASSUMPTIONS

The following are the assumptions from this analysis:

1. All predictive variables are normally distributed. This shown from the normal plot above.
2. At the initial part of this variable, we tested for hypothesis to know whether each coefficient is significant. Some variables were rejected as a result of this.
3. It is possible to accept the rejected explanatory variables earlier rejected if a residual plot between the predictive variables show a regular pattern
4. Using VIF, we see that variable OBP has a high magnitude influence on RUN_SCORE than any other variables.
5. Using STEPWISE REGRESSION, we see that all variables are included in the model. .

RESULTS

From the above analysis, It is clear that variable OPS has a strong influence to predict the RUN_SCORE of the BASE BALL in the future. Also, there is a strong correlation between RUN_SCORE and all the four variables.

In conclusion, the RUN_SCORE for the MLS players can be predicted by all the variables but OBP has a strongest CORRELATION between it and RUN_SCORE. Variable OPS can influence the prediction of RUN_SCORE in the future.