

The weight and systolic blood pressure of 26 randomly selected males in the age group 25-30 are shown below. Assume that weight and blood pressure are jointly normally distributed.

- Find a regression line relating systolic Blood pressure to Weight
- Estimate the correlation coefficient
- Test the hypothesis that correlation coefficient (ρ) = 0.
- Find a 95% confidence interval for correlation coefficient.

Run the file to Load the dataframe

```
df = data.frame(subject=c(1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,24,25,26),
                 weight=c(165,167,180,155,212,175,190,210,200,149,158,169,170,172,159,168,174,183,215,195,180,143,240,235,192,187),
                 systolic_BP=c(130,133,150,128,151,146,150,140,148,125,133,135,150,153,128,132,149,158,150,163,156,124,170,165,160,159))
```

A) Find a regression line relating systolic Blood pressure to Weight

To visualize the dataframe as a Table

View(df)

```
model1 <- lm(systolic_BP~weight,data=df)
model1
```

```
##
```

```
## Call:
```

```
## lm(formula = systolic_BP ~ weight, data = df)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)      weight
```

```
##      69.1044      0.4194
```

Hence, the regression equation of systolic BP on weight is: $\text{Systolic_BP} = 69.1044 + 0.4194 * \text{weight}$

B) Estimate the correlation coefficient

```
cor(df$weight, df$systolic_BP)
```

```
## [1] 0.7734903
```

We can observe that Weight and Systolic BP are highly correlated.

C) Test the hypothesis that correlation coefficient (ρ) = 0.

```
model1 <- lm(systolic_BP~weight,data=df)
summary(model1)
```

```
##
## Call:
## lm(formula = systolic_BP ~ weight, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -17.182  -6.485  -2.519   8.926  12.143
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 69.10437    12.91013   5.353 1.71e-05 ***
## weight      0.41942     0.07015   5.979 3.59e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.681 on 24 degrees of freedom
## Multiple R-squared:  0.5983, Adjusted R-squared:  0.5815
## F-statistic: 35.74 on 1 and 24 DF,  p-value: 3.591e-06

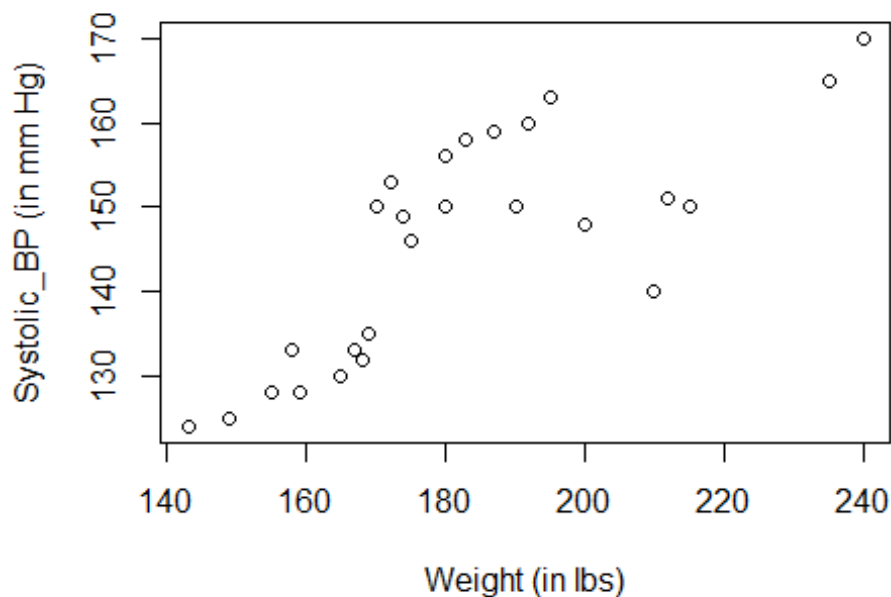
fitted(model1)

##           1           2           3           4           5           6           7           8
## 138.3079 139.1467 144.5991 134.1137 158.0204 142.5020 148.7933 157.1816
##           9          10          11          12          13          14          15          16
## 152.9874 131.5972 135.3720 139.9855 140.4050 141.2438 135.7914 139.5661
##          17          18          19          20          21          22          23          24
## 142.0826 145.8574 159.2786 150.8903 144.5991 129.0807 169.7640 167.6669
##          25          26
## 149.6321 147.5350

residuals(model1)

##           1           2           3           4           5           6
## -8.3078813 -6.1467117  5.4008907 -6.1137292 -7.0203958  3.4979667
##           7           8           9          10          11          12
##  1.2067387 -17.1815654 -4.9874134 -6.5972380 -2.3719749 -4.9855421
##          13          14          15          16          17          18
##  9.5950427 11.7562123 -7.7913901 -7.5661269  6.9173819 12.1426451
##          19          20          21          22          23          24
## -9.2786414 12.1096626 11.4008907 -5.0807468  0.2359785 -2.6669455
##          25          26
## 10.3679082 11.4649843

plot(df$weight,df$systolic_BP,
      xlab = "Weight (in lbs)",
      ylab = "Systolic_BP (in mm Hg)")
```



```
c = cor.test(df$weight,df$systolic_BP)
c

##
## Pearson's product-moment correlation
##
## data: df$weight and df$systolic_BP
## t = 5.9786, df = 24, p-value = 3.591e-06
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.5513214 0.8932215
## sample estimates:
## cor
## 0.7734903
```

Default confidence interval: 95%

D) Find a 95% confidence interval for correlation coefficient.

```
d = cor.test(df$weight,df$systolic_BP,level=0.95)
d

##
## Pearson's product-moment correlation
##
## data: df$weight and df$systolic_BP
## t = 5.9786, df = 24, p-value = 3.591e-06
```

```
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
##  0.5513214 0.8932215
## sample estimates:
##          cor
## 0.7734903
```