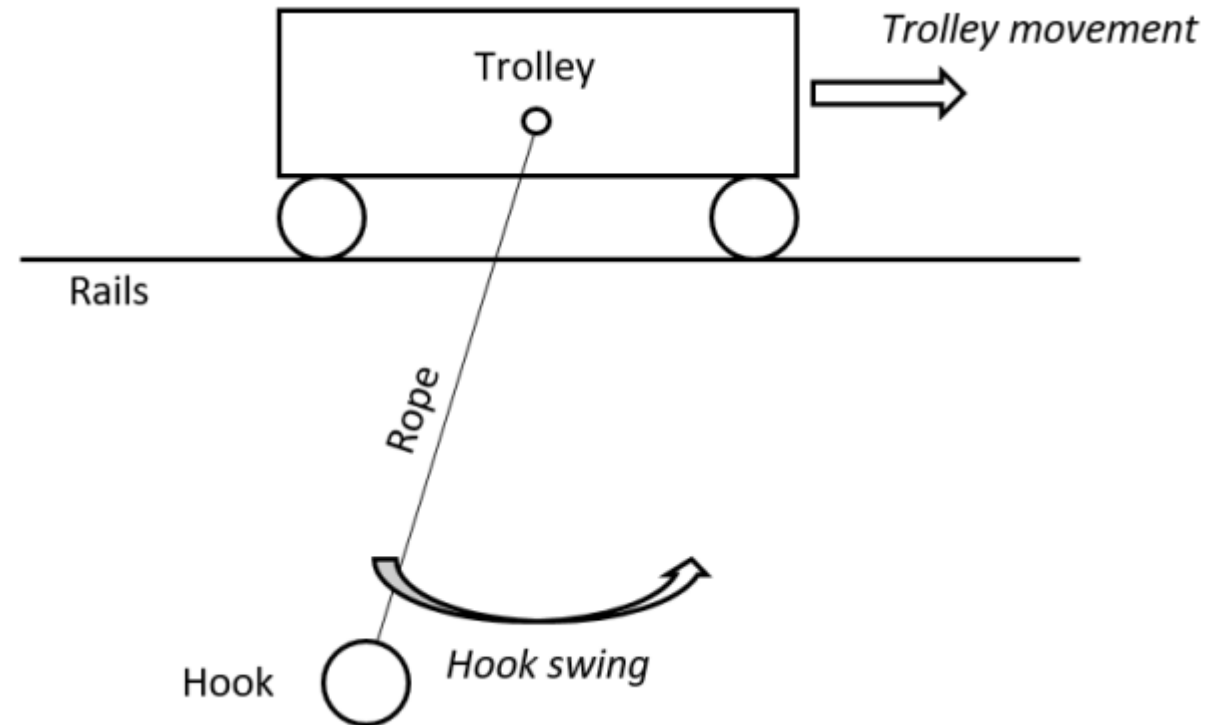


MEC-E5001 Mechatronic Machine Design Project Work

Crane Hook Sway Simulation and Control



1. Introduction and Numeric Modelling
2. CAD Modelling
3. Components
4. Simulation model and control
5. Closure



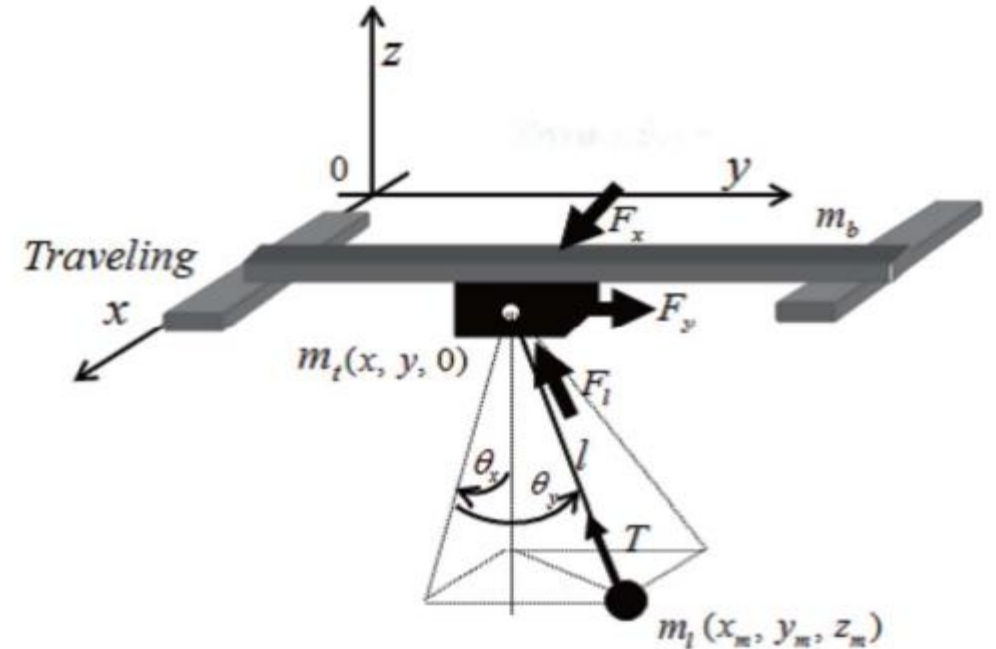
1. Introduction and Numeric Modelling

The non-linear dynamic model of crane is derived using Lagrange equations as follow:

$$(m_t + m_l)\ddot{y} + m_l l (\ddot{\theta}_y \cos \theta_y - \dot{\theta}_y^2 \sin \theta_y) = F_y$$
$$\cos \theta_y \ddot{y} + l \ddot{\theta}_y + g \sin \theta_y = 0$$

By assuming small motion of θ_y and $\theta = 0$ as the stable equilibrium of the system, the following linearized model of the crane is obtained:

$$(m_t + m_l)\ddot{y} + m_l l \ddot{\theta}_y = F_y$$
$$\ddot{y} + l \ddot{\theta}_y + g \theta_y = 0$$



1. Introduction and Numeric Modelling

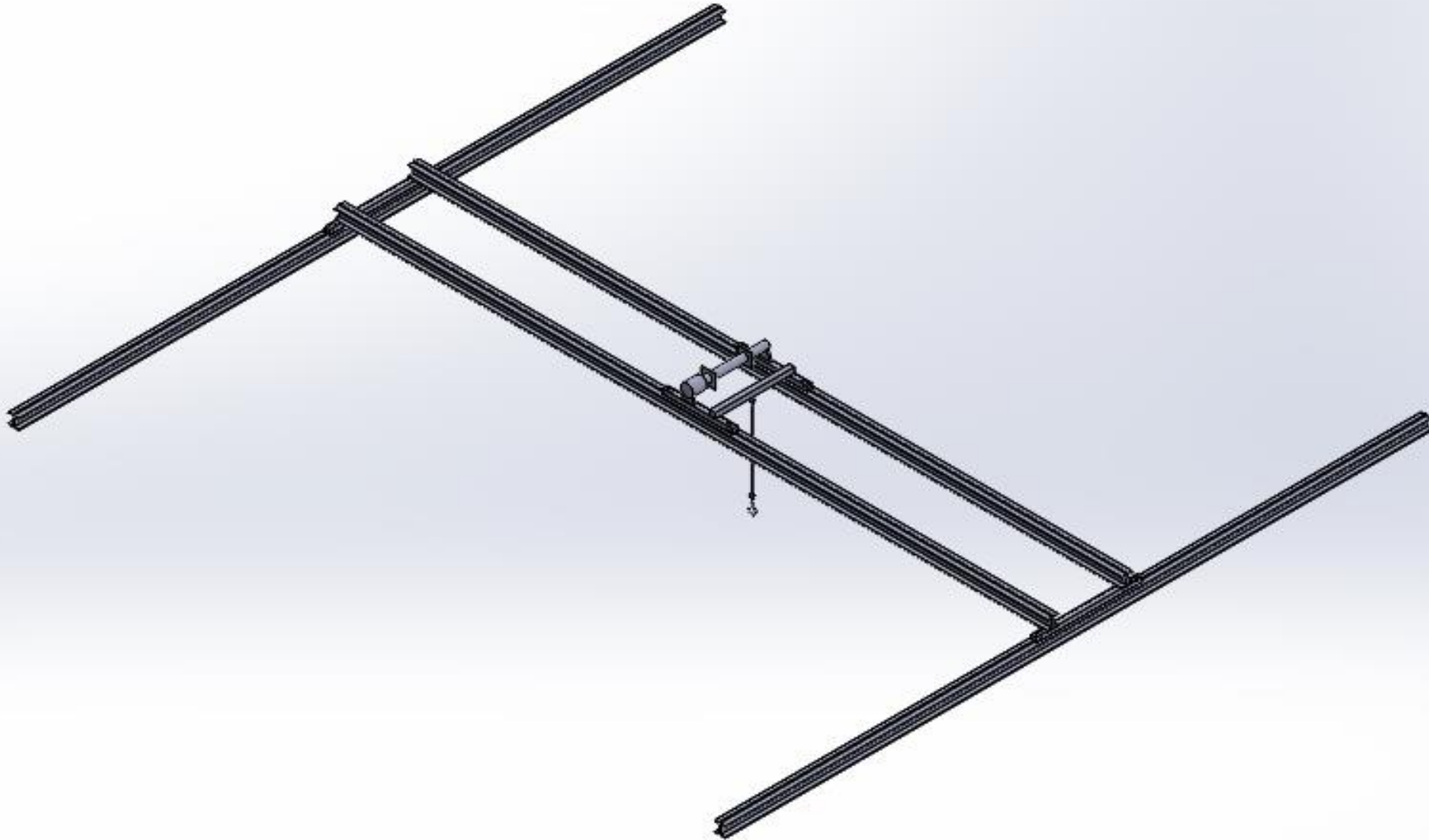
The state space model of the crane can be obtained as:

$$\dot{X} = Ax + Bu$$

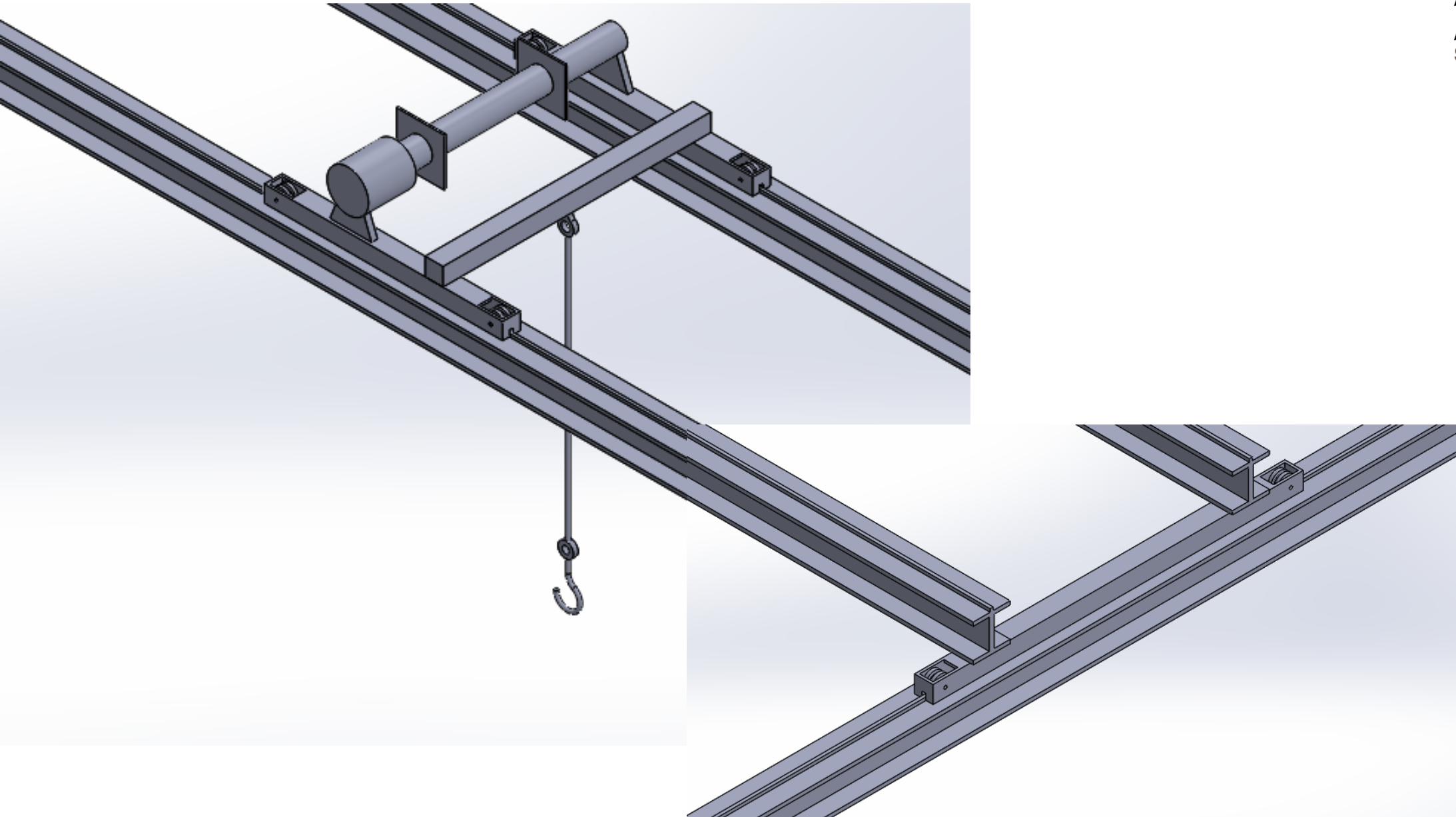
$$Y = Cx + Du$$

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{m_l g}{m_t} & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & -\frac{(m_t + m_l)g}{m_t l} & 0 \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ 1/m_t \\ 0 \\ -1/m_t l \end{bmatrix} \quad C = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \quad D = [0]$$

2. CAD Modelling



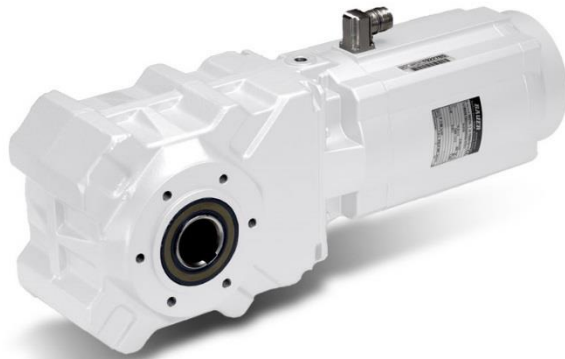
2. CAD Modelling



3. Components

AsepticDRIVE | Bauer Gear Motor

Power rating 0,37 -2,2 kW



The angle of the “rope” will be measured by using a **SeedStudio Grove Rotary Angle Sensor** and analog potentiometer.



Amerigear® Class I Gear | Ameridrives



CRANE® 44000 Electric Actuators



PLC Controller (CLESCRANE)



4. Simulation model and control

```
l=0.5 %:0.5:3.0 % rope length
v=20 % Trolly max speed [m/min]
L_2=9 % Trolly movement range [meters]
m_t=250 % Trolly weight [kg]
m_max=3200 % Lifting capacity
m_hook=5 % hook weight
m_l=m_max+m_hook;
g=9.81;
s=tf('s')
P_t=(l*s^2+g)/((m_t+m_l)*l*s^4+(m_t*g+m_l*g-m_l*l))
P_p=s^2/(m_l*l*s^4-(m_t+m_l)*l*s^2-(m_t*g+m_l*g))
```

```
P_t =

      0.5 s^2 + 9.81
-----
1728 s^4 + 3.229e04
```

Continuous-time transfer function.

```
P_p =

      s^2
-----
1603 s^4 - 1728 s^2 - 3.389e04
```

Continuous-time transfer function.

```
sys_tf =

From input "u" to output...
      0.5 s^2 + 9.81
x:  -----
1728 s^4 + 3.229e04

      s^2
phi: -----
1603 s^4 - 1728 s^2 - 3.389e04
```

Continuous-time transfer function.

```
controllability =
```

4

```
K =
```

```
70.7107 717.5049 345.3303 -1.8960
```

```
Nbar =
```

```
70.7107
```

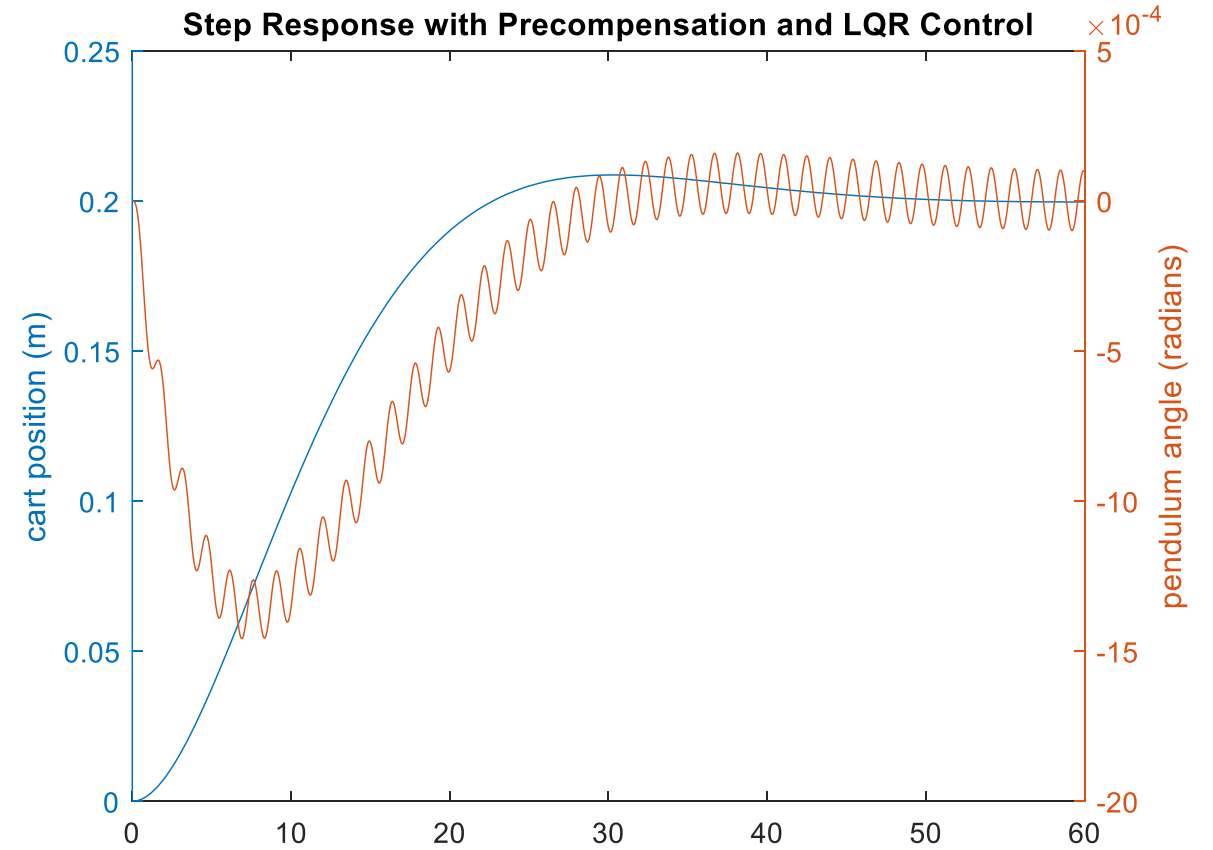
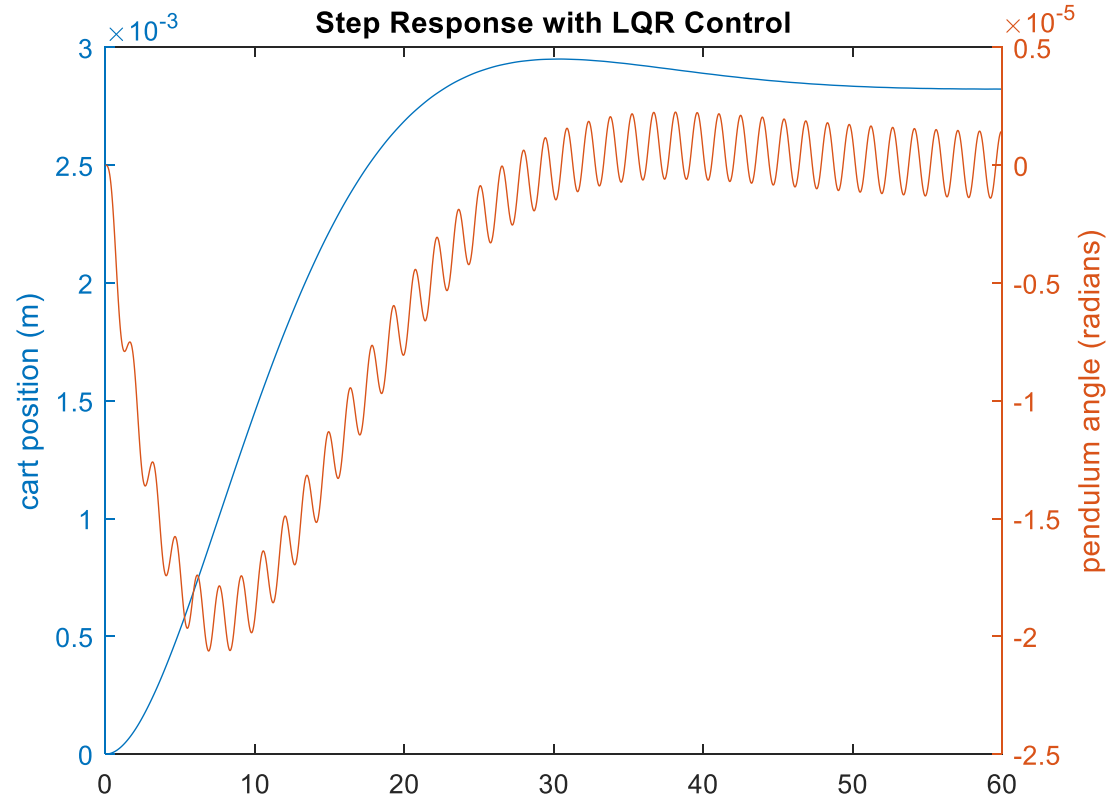
```
observability =
```

```
4
```

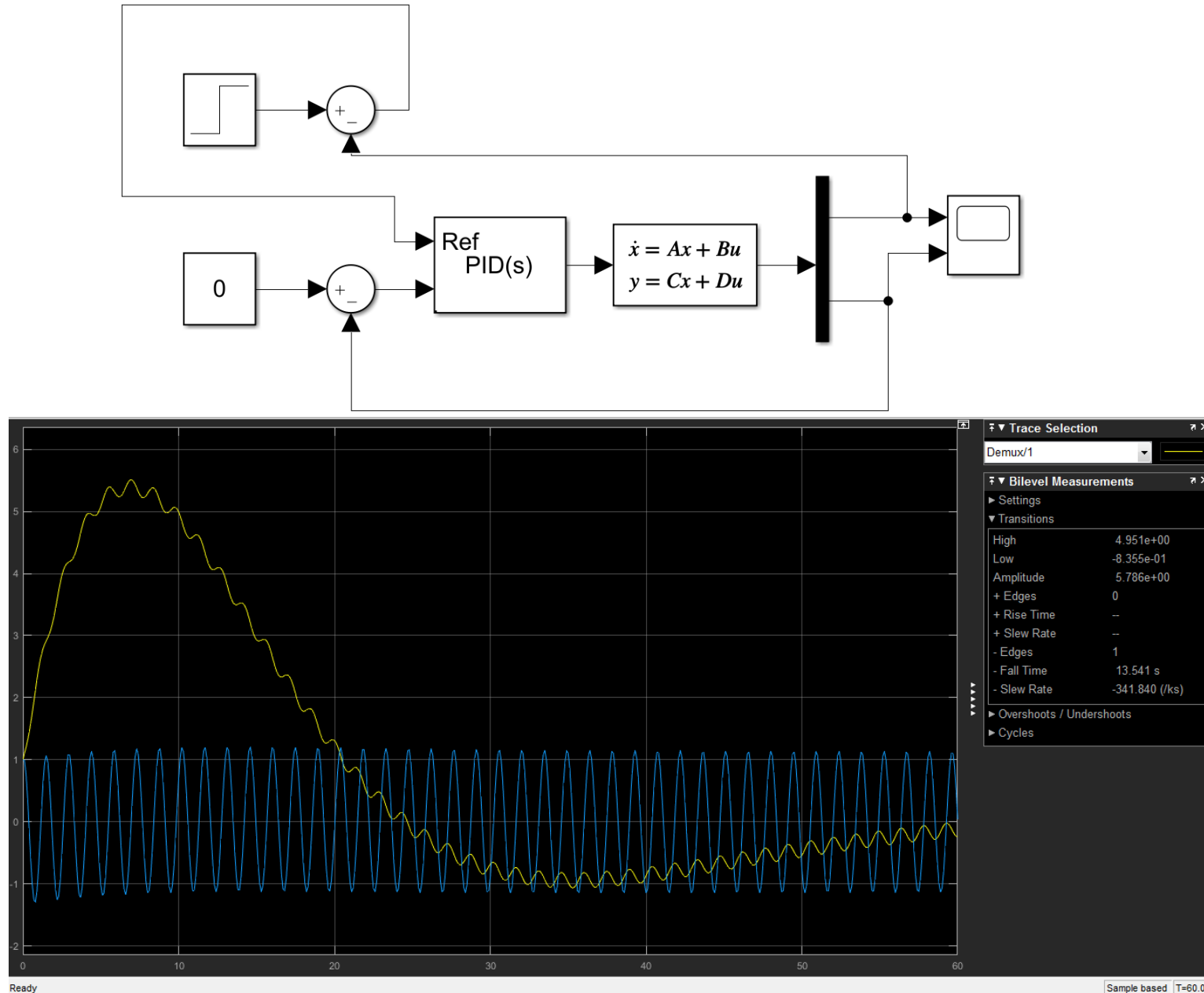
```
poles =
```

```
-0.1036 + 0.1036i
-0.1036 - 0.1036i
-0.0002 + 4.3235i
-0.0002 - 4.3235i
```


4. Simulation model and control



4. Simulation model and control



5. Closure

