A Choreographic Language for PRISM

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Abstract. The abstract should briefly summarize the contents of the paper in 150–250 words.

Keywords: First keyword \cdot Second keyword \cdot Another keyword.

1 Introduction

This is the introduction

Contributions and Overview. Our contributions can be categorised as follows:

_

2 The Prism Language

We start by describing the PRISM language syntax and semantics. To the best of our knowledge, the only formalisation of a semantics for PRISM can be found on the PRISM website [?]. Our approach starts from this and attempts to make more precise some informal assumptions and definitions.

Syntax. Let p range over a (possibly infinite) set of module names \mathcal{R} , a over a (possibly infinite) set of labels \mathcal{L} , x over a (possibly infinite) set of variables Var , and v over a (possibly infinite) set of values Val . Then, the syntax of the PRISM language is given by the following grammar:

Networks are the top syntactic category for system of modules composed together. The term **0** represent an empty network. A module is meant to represent a process running in the system, and is denoted by its variables and its commands. Formally, a module $p : \{F_i\}_i$ is identified by its name p and a set of commands F_i . Networks can be composed in parallel, in a CSP style: a term like $M_1|[A]|M_2$ says that networks M_1 and M_2 can interact with each other using labels in the finite set A. The term M/A is the standard CSP/CCS hiding operator. Finally σM is equivalent to applying the substitution σ to all variables in x. A substitution is a function that given a variable returns a value. When we write σN we refer to the term obtained by replacing every free variable x in N with $\sigma(x)$. Marco: Is this really the way substitution is used? Where does it become important? Commands in a module have the form $[a]g \to \Sigma_{i \in I}\{\lambda_i : u_i\}$. The label a is used for synchronisation (it is a condition that allows the command to be executed when all other modules having a command on the same label also execute). The term q is a guard on the current variable state. If both label and the guards are enabled, then the command executes in a probabilistic way one of the branches. Depending on the model we are going to use, the value λ_i is either a real number representing a rate (when adapting an exponential distribution) or a probability. If we are using probabilities, then we assume that terms in every choice are such that the sum of the probabilities is equal to 1.

Semantics. In order to give a probabilistic semantics to PRISM, we have two possibilities: we can either proceed denotationally, following the approach given on the PRISM website [?] or define an operational semantics in the style of Plotkin [?] and Bookes et al. [?]. Since the semantics of the choreographic language we present is purely operational, we will opt for the second choice.

[HERE WE NEED FORMAL DEFINITIONS OF TRANSITION SYSTEM, Markov Chain, etc. But perhaps not because of space reason we can just claim that our semeantics is a Markov chain/process/whatever]

Definition 1 (Discrete Time Markov Chain (DTMC)). A Discrete Time Markov Chain (DTMC) is a pair (S, P) where

```
- S is a set of states
```

 $-P: S \times S \rightarrow [0,1]$ is the probability transition matrix such that, for all $s \in S$, $\sum_{s' \in S} P(s,s') = 1$.

Definition 2 (Continuous Time Markov Chain (CTMC)). A Continuous Time Markov Chain (DTMC) is a pair (S, R) where

```
- S is a set of states
```

 $⁻P: S \times S \to R^{\geq 0}$ is the rate transition matrix.

We now define the operational semantics as the minimum relation \longrightarrow satisfying the following rules:

$$\frac{|E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_j]\} \quad j \in \{1, 2\}}{|E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_1|[A]|M_2]\}} \quad (\mathsf{Par}_1) }$$

$$\frac{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_j]\} \quad a \not\in A \quad j \in \{1, 2\}}{|a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1|[A]|M_2]\}} \quad (\mathsf{Par}_2) }$$

$$\frac{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1]\} \quad [a]E' \to \{\lambda'_j : y_j = E'_j\}_{j \in J} \in \{[M_2]\} \quad a \in A}{|E \wedge E' \to \{\lambda_i * \lambda'_j : x_i = E_i \wedge y_j = E'_j\}_{i \in I, j \in J} \in \{[M_1|[A]|M_2]\}} \quad (\mathsf{Par}_3) }$$

$$\frac{[B \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}\} \quad (\mathsf{Hide}_1)}{|E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}} \quad a \not\in A}{|a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}} \quad (\mathsf{Hide}_2) }$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in A}{|E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}} \quad (\mathsf{Subst}_1) }$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \not\in \mathsf{dom}(\sigma)}{|a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}} \quad (\mathsf{Subst}_1) }$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \not\in \mathsf{dom}(\sigma)}{|a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}}{|a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}{|a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}}$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}{|a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}}$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}{|a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}}$$

3 Choreographic Language

We now give syntax and semantics for our choreographic language. **Syntax.** Our choreographic language is defined by the following syntax:

(Chor)
$$C ::= \mathbf{p} \to \{\mathbf{p}_1, \dots, \mathbf{p}_n\} \Sigma_{i \in J} \lambda_i : x_i = E_i; C_i \mid \text{if } E@\mathbf{p} \text{ then } C_1 \text{ else } C_2 \mid X \mid \mathbf{0}$$

We comment the various constructs. The syntactic category C denotes choreographic programmes. The term $\mathbf{p} \to \{\mathbf{p}_1,\dots,\mathbf{p}_n\} \Sigma \{\lambda_j: x_j=E_j; C_j\}_{j\in J}$ denotes an interaction initiated by role \mathbf{p} with roles \mathbf{p}_i . Unlike in PRISM, a choreography specifies what interaction must be executed next, shifting the focus from what can happen to what must happen. When the synchronisation happens then, in a probabilistic way, one of the branches is selected as a continuation. The term if $E@\mathbf{p}$ then C_1 else C_2 factors in some local choices for some particular roles. [write a bit more about procedure calls, recursion and the zero process]

Semantics. Similarly to how we did for the PRISM language, we consider the state space Val^n where n is the number of variables present in the choreography. We then inductively define the transition function for the state space as follows:

$$\begin{split} &(\sigma,\mathsf{p}\to\{\mathsf{p}_1,\ldots,\mathsf{p}_n\}\,\varSigma_{j\in J}\lambda_j:x_j\!=\!E_j;\ C_j)\ \longrightarrow_{\lambda_j}\ (\sigma[\sigma(E_j)/x_j],C_j)\\ &(\sigma,\mathsf{if}\ E@\mathsf{p}\ \mathsf{then}\ C_1\ \mathsf{else}\ C_2)\ \longrightarrow\ (\sigma,C_1)\\ &X\stackrel{\mathsf{def}}{=}\ C\ \Rightarrow\ (\sigma,X)\ \longrightarrow\ (\sigma,C) \end{split}$$

4 M. Carbone and A. Veschetti

From the transition relation above, we can immediately define an LTS on the state space. Given an initial state σ_0 and a choreography C, the LTS is given by all the states reachable from the pair (σ_0, C) . I.e., for all derivations $(\sigma_0, C) \longrightarrow_{\lambda_0} \ldots \longrightarrow_{\lambda_n} (\sigma_n, C_n)$ and i < n, we have that $(\sigma_i, \sigma_{i+1}) \in \delta$ [adjust once the definition of probabilistic LTS is in].

3.1 Projection from Choreographies to PRISM

Mapping Choreographies to PRISM. We need to run some standard static checks because, since there is branching, some terms may not be projectable.

$$\begin{aligned} & \big(q \in \{ \mathsf{p}, \mathsf{p}_1, \dots, \mathsf{p}_n \}, J = \{ 1, 2 \}, \ l_1, l_2 \ \mathrm{fresh} \big) \\ & \mathsf{proj}(q, \mathsf{p} \to \{ \mathsf{p}_1, \dots, \mathsf{p}_n \} \ \varSigma_{j \in J} \lambda_j : x_j = E_j; \ C_j, s) = \\ & \quad \{ [l_1] s_{\mathsf{p}_1} = s \to \lambda_1 : s_{\mathsf{p}_1} = s_{\mathsf{p}_1} + 1, \ [l_2] s_{\mathsf{p}_1} = s \to \lambda_2 : s_{\mathsf{p}_1} = s_{\mathsf{p}_1} + 2 \} \quad \cup \\ & \quad \mathsf{proj}(\mathsf{p}_1, C_1, s + 1) \quad \cup \quad \mathsf{proj}(\mathsf{p}_1, C_2, s + \mathsf{nodes}(C_1)) \end{aligned}$$

$$\begin{aligned} & \big(q \notin \{ \mathsf{p}, \mathsf{p}_1, \dots, \mathsf{p}_n \} \big) \\ & \quad \mathsf{proj}(q, \mathsf{p} \to \{ \mathsf{p}_1, \dots, \mathsf{p}_n \} \ \varSigma_{j \in J} \lambda_j : x_j = E_j; \ C_j, s) = \ \mathsf{proj}(\mathsf{p}_1, C_1, s) \ \cup \ \mathsf{proj}(\mathsf{p}_1, C_2, s + \mathsf{nodes}(C_1)) \end{aligned}$$

$$\begin{aligned} & \big(q = \mathsf{p} \big) \\ & \quad \mathsf{proj}(q, \mathsf{if} \ E @ \mathsf{p} \ \mathsf{then} \ C_1 \ \mathsf{else} \ C_2, s) = \\ & \quad \{ [] s_{\mathsf{p}_1} = s \& E \to \varSigma_{i \in I} \{ \lambda_i ::_i \} s_{\mathsf{p}_1} = s_{\mathsf{p}_1} + 1, [] s_{\mathsf{p}_1} = s \& \mathsf{not}(E) \to \varSigma_{i \in I} \{ \lambda_i ::_i \} s_{\mathsf{p}_1} = s_{\mathsf{p}_1} + 1 \} \quad \cup \\ & \quad \mathsf{proj}(\mathsf{p}_1, C_1, s + 1) \quad \cup \quad \mathsf{proj}(\mathsf{p}_1, C_2, s + \mathsf{nodes}(C_1)) \end{aligned}$$

4 Tests

In this section we present the implementation and our experimental evaluation of our language. We focus on four benchmarks: the dice program and the random graphs protocol that we compare with the test cases reported in the PRISM repository³; the Bitcoin proof of work protocol and the Hybrid Casper protocol, presented in [3, 5].

4.1 Implementation

AV: To be finished

We implemented our language in 1246 lines of Java. We defined the grammar of our language and generated both the parser and the visitor components with ANTLR [1]. Each abstract syntax tree (AST) node, such as ActionNode, IfThenElseNode, BranchNode, InternalActionNode, LoopNode, MessageNode, ModuleNode, PreambleNode, ProtocolNode, RecNode, RoleNode, and ProgramNode, was encapsulated in a corresponding Node class. The methods of these classes were then utilized to generate PRISM code.

Listing 1.1. The generateCode function.

The generateCode function generates the projection from our language to PRISM. The input parameters for the projection function include:

- mods: a list containing the choreography modules. As new commands are generated, they are appended to the set of commands for the respective module;
- index and maxIndex: indices used to keep track of the currently analyzed role:
- isCtmc: a boolean flag indicating whether a Continuous-Time Markov Chain (CTMC) is being generated. This flag is crucial as the projection generation logic depends on it;
- labels: the pre-existing labels. This parameter is necessary for checking the uniqueness of a label;
- prot: the name of the protocol currently under analysis.

The projection function operates recursively on each command in the choreographic language, systematically generating PRISM code based on the type of command being analyzed. While most code generations are straightforward, the focal point lies in how new states are created. Each module maintains its set of states, and when a new state is to be generated, the function examines the last available state for the corresponding module and increments it by one.

³ https://www.prismmodelchecker.org/casestudies/

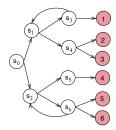
Recursion follows a similar pattern: every module possesses a table that accumulates recursion protocols, along with the first and last states associated with each recursion. This recursive approach ensures a systematic and coherent generation of states within the modules, enhancing the overall efficiency and clarity of the projection function.

4.2 The Dice Program

AV: Ricontrollare e tagliare

The first test case we focus on the Dice Program⁴[6]. The following program models a die using only fair coins. Starting at the root vertex (state s_0), one repeatedly tosses a coin. Every time heads appears, one takes the upper branch and when tails appears, the lower branch. This continues until the value of the die is decided.

In Listing 1.2, we report the modelled program using the choreographic language while in Listing 1.3 the generated PRISM program is shown.



```
preamble
"dtmc"
endpreamble
n = 1;
Dice \rightarrow Dice : "d : [0..6] init 0;";
{\tt DiceProtocol}_0 \; \coloneqq \; {\tt Dice} \; \to \; {\tt Dice} \; : \; (\texttt{+["0.5*1"]} \;\; "\; \&\&" \;\; " \;\; . \;  \, {\tt DiceProtocol}_1
                                             +["0.5*1"] " "&&" " . DiceProtocol<sub>2</sub>)
DiceProtocol_1 := Dice \rightarrow Dice : (+["0.5*1"] " "&&" " .
                              Dice \rightarrow Dice : (+["0.5*1"] " "&&" " . DiceProtocol_1
                                                   +["0.5*1"] "(d'=1)"&&" " .
                                                        DiceProtocol3)
                                            +["0.5*1"] " "&&" " .
                              Dice \rightarrow Dice : (+["0.5*1"] "(d'=2)"&&" " .
                                    {\tt DiceProtocol}_3
                                                    +["0.5*1"] "(d'=3)"&&" " .
                                                          DiceProtocol3))
\mathsf{DiceProtocol}_2 \coloneqq \mathsf{Dice} \, 	o \, \mathsf{Dice} \, : \, (+["0.5*1"] \; " \; "\&\&" \; " \; .
                              Dice \rightarrow Dice : (+["0.5*1"] " "&&" " . DiceProtocol_2
```

 $^{^4\ \}mathtt{https://www.prismmodelchecker.org/casestudies/dice.php}$

```
+["0.5*1"] "(d'=4)"&&" " .

DiceProtocol<sub>3</sub>)

+["0.5*1"] " "&&" " .

Dice → Dice : (+["0.5*1"] "(d'=5)"&&" " .

DiceProtocol<sub>3</sub>

+["0.5*1"] "(d'=6)"&&" " .

DiceProtocol<sub>3</sub>))

DiceProtocol<sub>3</sub> := Dice → Dice : (["1*1"] " "&&" ".DiceProtocol<sub>3</sub>)

}
```

Listing 1.2. Choreographic language for the Dice Program.

```
dtmc

module Dice
    Dice : [0..11] init 0;
    d : [0..6] init 0;

[] (Dice=0) → 0.5 : (Dice'=2) + 0.5 : (Dice'=6);
    [] (Dice=2) → 0.5 : (Dice'=3) + 0.5 : (Dice'=4);
    [] (Dice=3) → 0.5 : (Dice'=2) + 0.5 : (d'=1)&(Dice'=10);
    [] (Dice=4) → 0.5 : (d'=2)&(Dice'=10) + 0.5 : (d'=3)&(Dice'=10);
    [] (Dice=6) → 0.5 : (Dice'=7) + 0.5 : (Dice'=8);
    [] (Dice=7) → 0.5 : (Dice'=6) + 0.5 : (d'=4)&(Dice'=10);
    [] (Dice=8) → 0.5 : (d'=5)&(Dice'=10) + 0.5 : (d'=6)&(Dice'=10);
    [] (Dice=10) → 1 : (Dice'=10);
endmodule
```

Listing 1.3. Generated PRISM program for the Dice Program.

By comparing our model with the one presented in the PRISM documentation, we notice that the difference is the number assumed by the variable Dice. In particular, the variable assumes different values and this is due to how the generation in presence of a branch is done. However, this does not cause any problems since the updates are done correctly and the states are unique. Moreover, to prove the generated program is correct, we show that the probability of reaching a state where

```
d=k \text{ for } k = 1, \dots, 6 \text{ is } 1/6.
```

The results are displayed in Figure 1, where we compare the probability we obtain with our generated model and the one obtained with the original PRISM model. As expected, the results are equivalent.

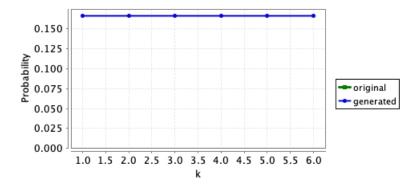
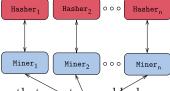


Fig. 1. Probability of reaching a state where d = k, for k = 1, ..., 6.

4.3 Proof of Work Bitcoin Protocol

In [3], the authors decided to extend the PRISM model checker with dynamic data types in order to model the Proof of Work protocol implemented in the Bitcoin blockchain [7].

The Bitcoin system is the result of the parallel composition of n Miner processes, n Hasher processes and a process called Network. In particular:



- The *Miner* processes model the blockchain mainers that create new blocks and add them to their local ledger;
- the *Hasher* processes model the attempts of the miners to solve the cryptopuzzle;
- the *Network* process model the broadcast communication among miners.

Since we are not interested in the properties obtained by analyzing the protocol, we decided to consider n=4 miner and hasher processes; the model can be found in Listing 1.4.

```
(["rB*1"] "(B[i]'=addBlock(B[i],b[i]))" &&
               foreach(k != i) "(set[k]', addBlockSet(set[k], b[i]))"
                   → @Network .PoW)
 +["lR*hR[i]"] " " && " " .
       if "!isEmpty(set[i])"@Miner[i] then {
               ["r"] "(b[i]'=extractBlock(set[i]))"@Miner[i] .
                      Miner[i] -> Network :
                      (["1*1"] "(setMiner[i]' = addBlockSet(setMiner[i])

    b[i]))"&&"(set[i]' = removeBlock(set[i],b[i])

                          → ]))" . PoW)
       else{
               if "canBeInserted(B[i],b[i])"@Miner[i] then {
                      ["1"] "(B[i]'=addBlock(B[i],b[i]))&&(setMiner[i]'=
                          → removeBlock(setMiner[i],b[i]))"@Miner[i] .
               }
               else{
                      PoW
       }
)
}
```

Listing 1.4. Choreographic language for the Proof of Work Bitcoin Protocol.

Part of the generated PRISM code is shown in Listing 1.5, the modules $Miner_2$, $Miner_3$, $Miner_4$ and $Hasher_2$, $Hasher_3$, $Hasher_4$ are equivalent to $Miner_1$ and $Hasher_1$, respectively. Our generated PRISM model is more verbose than the one presented in [3], this is due to the fact that for the if-then-else expression, we always generate the else branch. and this leads to having more instructions

```
[SRKSV] (Miner1=4) \rightarrow 1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(
        \hookrightarrow Miner1'=0);
   [] (Miner1=2)\&!(!isEmpty(set1)) \rightarrow 1 : (Miner1'=5);
   [] (Miner1=5)\&canBeInserted(B1,b1) \rightarrow 1 : (B1'=addBlock(B1,b1))\&(

    setMiner1'=removeBlock(setMiner1,b1))&(Miner1'=0);

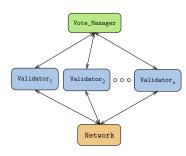
   [] (Miner1=5)&!(canBeInserted(B1,b1)) \rightarrow 1 : (Miner1'=0);
endmodule
module Network
Network : [0..1] init 0;
   set1 : list [];
   [HXYKO] (Network=0) \rightarrow 1 : (set2'=addBlockSet(set2,b2))&(set3'=

→ addBlockSet(set3,b3))&(set4'=addBlockSet(set4,b4))&(Network'=0)
   [SRKSV] (Network=0) \rightarrow 1 : (set1' = removeBlock(set1,b1))&(Network'=0)
        \hookrightarrow :
endmodule
module Hasher1
Hasher1 : [0..1] init 0;
[PZKYT] (Hasher1=0) \rightarrow mR : (Hasher1'=0);
[EUBVP] (Hasher1=0) \rightarrow 1R : (Hasher1'=0);
endmodule
```

Listing 1.5. Generated PRISM program for the Peer-To-Peer Protocol.

However, for this particular test case, the results of the experiments are not affected, as shown Figure 2 where the results are compared. In this example, since we are comparing the results of two simulations, the two probabilities are slightly different, but it has nothing to do with the model itself.

4.4 Hybrid Casper Protocol



The last case we study we present is the Hybrid Casper Protocol modelled in PRISM in [5]. The Hybrid Capser protocol is an hybrid blockchain consenus protocol that includes features of the Proof of Work and the Proof of Stake protocols. It was implemented in the Ethereum blockchain [4] as a testing phase before switching to Proof of Stake protocol.

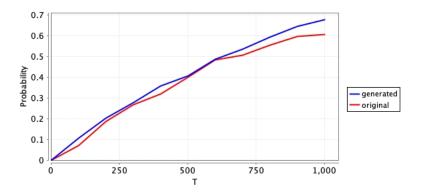


Fig. 2. Probability at least one miner has created a block.

The approach is very similat to the one used for the Proof of Work Bitcoin protocol, so they model Hybrid Casper in PRISM as the parallel composition of n Validator modules and the modules Vote_Manager and Network. The module Validator is very similar to the module Miner of the previous protocol and the only module that requires an explaination is the Vote_Manager that stores the tables containing the votes for each checkpoint and calculates the rewards/penalties.

The modeling language is reported in Listing 1.6 while (part of) the generated PRISM code can be found in Listing 1.7.

```
preamble
endpreamble
n = 5;
PoS := Validator[i] -> Validator[i] :
   (+["mR*1"] "(b[i]'=createB(b[i],L[i],c[i]))&(c[i]'=c[i]+1)"&&" ".
  if "!(mod(getHeight(b[i]),EpochSize)=0)"@Validator[i] then{
    Validator[i] -> Network : (["1*1"] "(L[i]'=addBlock(L[i],b[i]))" &&

    foreach(k!=i) "(set[k]'=addBlockSet(set[k],b[i]))"@Network .

         → PoS)
  }
  else{
    Validator[i] -> Network : (["1*1"] "(L[i]'=addBlock(L[i],b[i]))" &&

    foreach(k!=i) "(set[k]'=addBlockSet(set[k],b[i]))"@Network .

         → Validator[i] -> Vote_Manager :(["1*1"] " "&&"(Votes'=addVote(
         → Votes,b[i],stake[i]))".PoS))
   +["lR*1"] " "&&" " . if "!isEmpty(set[i])"@Validator[i] then {
     ["1"] "(b[i]'=extractBlock(set[i]))"@Validator[i] .
      if "!canBeInserted(L[i],b[i])"@Validator[i] then {
```

```
PoS
      }
      else{
     if "!(mod(getHeight(b[i]),EpochSize)=0)"@Validator[i] then {
       Validator[i] -> Network : (["1*1"] "(setMiner[i]' = addBlockSet(

    setMiner[i] , b[i]))"&&"(set[i]' = removeBlock(set[i],b[i])

            → ]))" . PoS)
     }
     else{
       Validator[i] -> Network : (["1*1"] "(setMiner[i]' = addBlockSet(

    setMiner[i] , b[i]))"&&"(set[i]' = removeBlock(set[i],b[i])

            → ]))" . Validator[i] -> Vote_Manager : (["1*1"] " "&&"(
            → Votes'=addVote(Votes,b[i],stake[i]))".PoS ))
     }
   }
  }
  else{PoS}
  +["rC*1"] "(lastCheck[i]'=extractCheckpoint(listCheckpoints[i],
       → lastCheck[i]))&(heightLast[i]'=getHeight(extractCheckpoint())
       → listCheckpoints[i],lastCheck[i])))&(votes[i]'=calcVotes(Votes,
       \hookrightarrow \texttt{extractCheckpoint(listCheckpoints[i],lastCheck[i]))}"\&\&"~"~.
    if "(heightLast[i]=heightCheckpoint[i]+EpochSize)&(votes[i]>=2/3*
         → tot_stake)"@Validator[i] then{
      if "(heightLast[i]=heightCheckpoint[i]+EpochSize)"@Validator[i]
           \hookrightarrow then{
        ["1"] "(lastJ[i]'=b[i])&(L[i]'= updateHF(L[i],lastJ[i]))"
            → @Validator[i].Validator[i]->Vote_Manager :(["1*1"]" "&&"(

→ epoch'=height(lastF(L[i]))&(Stakes'=addVote(Votes,b[i],
            → stake[i]))".PoS)
      else{["1"] "(lastJ[i]'=b[i])"@Validator[i] . PoS}
    else{PoS}
)
}
```

Listing 1.6. Choreographic language for the Hybrid Casper Protocol.

```
    extractCheckpoint(listCheckpoints1,lastCheck1)))&(
            → Validator1'=3);
   [NGRDF] (Validator1=1) &! (mod(getHeight(b1), EpochSize)=0) \rightarrow 1 : (L1'=

    addBlock(L1,b1))&(Validator1'=0);
   [] (Validator1=1)&!(!(mod(getHeight(b1),EpochSize)=0)) \rightarrow 1 : (
       → Validator1'=3);
   [PCRLD] (Validator1=1) \&! (mod(getHeight(b1), EpochSize)=0) \rightarrow
        1 : (L1'=addBlock(L1,b1))&(Validator1'=4);
   [VSJBE] (Validator1=5) \rightarrow 1 : (Validator1'=0);
   [] (Validator1=2)&!isEmpty(set1) →
        1 : (b1'=extractBlock(set1))&(Validator1'=4);
   [] (Validator1=4)&!canBeInserted(L1,b1) → (Validator1'=0);
   [] (Validator1=4)\&!(!canBeInserted(L1,b1)) \rightarrow 1 : (Validator1'=6);
   [MDDCF] (Validator1=6) &! (mod(getHeight(b1), EpochSize)=0) →
        1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=0);
   [] (Validator1=6)&!(!(mod(getHeight(b1),EpochSize)=0)) \rightarrow 1 : (
       → Validator1'=8);
   [IQVPA] (Validator1=6) \&! (mod(getHeight(b1), EpochSize)=0) \rightarrow
        1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=9);
   [IFNVZ] (Validator1=10) \rightarrow 1 : (Validator1'=0);
   [] (Validator1=2)\&!(!isEmpty(set1)) \rightarrow 1 : (Validator1'=0);
   [] (Validator1=3)&(heightLast1=heightCheckpoint1+EpochSize)&(votes1>=
       \hookrightarrow 2/3*tot_stake) \rightarrow (Validator1'=4);
   [] (Validator1=4)&(heightLast1=heightCheckpoint1+EpochSize) \rightarrow
        1 : (lastJ1'=b1)&(L1'= updateHF(L1,lastJ1))&(Validator1'=6);
   [EQCY0] (Validator1=6) \rightarrow 1 : (Validator1'=0);
   [] (Validator1=4)&!((heightLast1=heightCheckpoint1+EpochSize)) \rightarrow
        1 : (lastJ1'=b1)&(Validator1'=0);
   [] (Validator1=3)&!((heightLast1=heightCheckpoint1+EpochSize)&(votes1
       \hookrightarrow >=2/3*tot_stake)) \rightarrow 1 : (Validator1'=0);
endmodule
module Network
  Network : [0..1] init 0;
   set1 : list [];
   set2 : list [];
  set3 : list [];
   set4 : list [];
   set5 : list [];
   [NGRDF] (Network=0) \rightarrow
        1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(

    set4'=addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&
            [PCRLD] (Network=0) \rightarrow
        1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(

    set4'=addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&
            \hookrightarrow (Network'=0);
   [MDDCF] (Network=0) \rightarrow 1 : (set1', = removeBlock(set1,b1)) & (Network'=0)
```

Listing 1.7. Generated PRISM program for the Hybrid Casper Protocol.

The code is very similar to the one presented in [5], the main difference is the fact that our generated model has more lines of code. This is due to the fact that there are some commands that can be merged, but the compiler is not able to do it automatically. This discrepancy between the two models can be observed also in the simulations, reported in Figure 3. Although the results are similar, PRISM takes 39.016 seconds to run the simulations for the generated model, instead of 22.051 seconds needed for the original model.

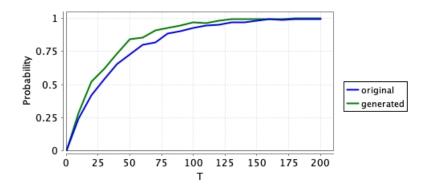


Fig. 3. Probability that a block has been created.

4.5 Problems

While testing our choreographic language, we noticed that some of the case studies presented in the PRISM documentation [2] cannot be modeled by using our language. The reasons are various, in this section we try to outline the problems.

- Asynchronous Leader Election⁵: processes synchronize with the same label but the conditions are different. We include in our language the it-then-else statement but we do not allow the if-then (without the else). This is done because in this way, we do not incur in deadlock states.
- Probabilistic Broadcast Protocols⁶: also in this case, the problem are the labels of the synchronizations. In fact, all the processes synchronize with the same label on every actions. This is not possible in our language, since a label is unique for every synchronization between two (or more) processes.
- Cyclic Server Polling System⁷: in this model, the processes $\mathtt{station}_i$ do two different things in the same state. More precicely, at the state 0 (\mathtt{s}_i =0), the processes may synchronize with the process \mathtt{server} or may change their state without any synchronization. In out language, this cannot be formalized since the synchronization is a branch action, so there should be another option with a synchronization.

5 Discussion

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References

- 1. ANTLR another tool for language recognition. https://www.antlr.org/
- Prism documentation. https://www.prismmodelchecker.org/, accessed: 2023-09-05
- 3. Bistarelli, S., Nicola, R.D., Galletta, L., Laneve, C., Mercanti, I., Veschetti, A.: Stochastic modeling and analysis of the bitcoin protocol in the presence of block communication delays. Concurr. Comput. Pract. Exp. 35(16) (2023). https://doi.org/10.1002/cpe.6749, https://doi.org/10.1002/cpe.6749
- 4. Buterin, V.: Ethereum white paper. https://github.com/ethereum/wiki/wiki/White-Paper (2013)
- Galletta, L., Laneve, C., Mercanti, I., Veschetti, A.: Resilience of hybrid casper under varying values of parameters. Distributed Ledger Technol. Res. Pract. 2(1), 5:1–5:25 (2023). https://doi.org/10.1145/3571587, https://doi.org/10.1145/3571587

⁵ https://www.prismmodelchecker.org/casestudies/asynchronous_leader.php

 $^{^{6}\ \}mathtt{https://www.prismmodelchecker.org/casestudies/prob_broadcast.php}$

⁷ https://www.prismmodelchecker.org/casestudies/polling.php

M. Carbone and A. Veschetti

16

- 6. Knuth, D., Yao, A.: Algorithms and Complexity: New Directions and Recent Results, chap. The complexity of nonuniform random number generation. Academic Press (1976)
- 7. Nakamoto, S.: Bitcoin: A peer-to-peer electronic cash system. https://bitcoin.org/bitcoin.pdf (2008)

A A denotational semantics for PRISM

We proceed by steps. First, we define $\{-\}$, as the closure of the following rules:

$$\frac{|E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_j]\} \quad j \in \{1, 2\}}{|E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_1|[A]|M_2]\}} \quad (\mathsf{Par}_1)}{|E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_1|[A]|M_2]\}} \quad (\mathsf{Par}_1)}$$

$$\frac{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_j]\} \quad a \not\in A \quad j \in \{1, 2\}}{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_1|[A]|M_2]\}} \quad (\mathsf{Par}_2)}{|B \to \{\lambda_i : x_i = E_i\}_{i \in I} \in [M_1]\} \quad [a]E' \to \{\lambda'_j : y_j = E'_j\}_{j \in J} \in [M_2]\} \quad a \in A}{|B \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}} \quad (\mathsf{Par}_3)}$$

$$\frac{|B \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}}{|B \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}} \quad (\mathsf{Hide}_1) \qquad \frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\} \quad a \not\in A}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}} \quad (\mathsf{Hide}_2)}{|B \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}} \quad (\mathsf{Subst}_1)$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\} \quad a \not\in \mathsf{dom}(\sigma)}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}} \quad (\mathsf{Subst}_2)$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\} \quad a \in \mathsf{dom}(\sigma)}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}} \quad (\mathsf{Subst}_2)$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\} \quad a \in \mathsf{dom}(\sigma)}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in [M]\}} \quad (\mathsf{Subst}_3)$$

The rules above work with modules, parallel composition, name hiding, and substitution. The idea is that given a network, we wish to collect all those commands F that are contained in the network, independently from which module they are being executed in. Intuitively, we can regard $\{N\}$ as a set, where starting from all commands present in the syntax, we do some filtering and renaming, based on the structure of the network.

Now, given $\{[N]\}$, we define a transition system that shows how the system evolves. Let state be a function that given a variable in Var returns a value in Val. Then, given an initial state state_0 , we can define a transition system where each of node is a (different) state function. Then, we can move from state_1 to state_2 .