# A Choreographic Language for PRISM

- ... Author: Please enter affiliation as second parameter of the author macro
- ... Author: Please enter affiliation as second parameter of the author macro

#### Abstract

- This is the abstract
- 2012 ACM Subject Classification Theory of computation  $\rightarrow$  Type theory; Computing methodologies
- $\rightarrow$  Distributed programming languages; Theory of computation  $\rightarrow$  Program verification
- Keywords and phrases Session types, PRISM, Model Checking
- Digital Object Identifier 10.4230/LIPIcs.ITP.2023.m
- Funding This work was supported by

# Formal Language

- In this section, we provide the formal definition of our choreographic language as well as
- process algebra representing PRISM [?].

#### 1.1 **PRISM**

- We start by describing PRISM semantics. Except from transforming some informal text in
- precise rules, Our formalisation closely follows that found on the PRISM website [?].
- Syntax. Let p range over a (possibly infinite) set of module names  $\mathcal{R}$ , a over a (possibly
- infinite) set of labels  $\mathcal{L}$ , x over a (possibly infinite) set of variables Var, and v over a (possibly
- infinite) set of values Val. Then, the syntax of PRISM is given by the following grammar:

$$(Networks) \qquad N, M \quad ::= \quad \mathbf{0} \qquad \qquad \text{empty network} \\ \mid \ \mathsf{p} : \{F_i\}_i \qquad \qquad \text{module} \\ \mid \ M \mid [A] \mid M \qquad \qquad \text{parallel composition} \\ \mid \ M/A \qquad \qquad \text{action hiding} \\ \mid \ \sigma M \qquad \qquad \text{substitution} \\ (Commands) \qquad F \quad ::= \qquad [a]g \to \Sigma_{i \in I} \{\lambda_i : u_i\} \quad g \text{ is a boolean expression in } E \\ (Assignment) \qquad u \quad ::= \qquad (x' = E) \qquad \qquad \text{update } x, \text{ element of } \mathcal{V}, \text{ with } E \\ \mid \ A\&A \qquad \qquad \text{multiple assignments} \\ (Expr) \qquad E \quad ::= \qquad f(\tilde{E}) \quad \mid \ x \quad \mid \ v$$

- Networks are the top syntactic category for system of modules composed together. The
- term CEnd represent an empty network. A module  $p:\{F_i\}_i$  is identified by its name p
- and a set of commands  $F_i$ . Networks can be composed in parallel, in a CSP style: a term
- like  $M_1[A]M_2$  says that networks  $M_1$  and  $M_2$  can interact with each other using labels in
- the finite set A. The term M/A is the standard CSP/CCS hiding operator. Finally  $\sigma M$  is
- equivalent to applying the substitution  $\sigma$  to all variables in x. A substitution is a function
- that given a variable returns a value. When we write  $\sigma N$  we refer to the term obtained by
- replacing every free variable x in N with  $\sigma(x)$ . Marco: Is this really the way substitution is used?
- Where does it become important?

#### m:2 A Choreographic Language for PRISM

Semantics. In order to give a probabilistic semantics to PRISM, we proceed by steps. First, we define {[-]}, as the closure of the following rules:

$$\frac{[]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_j]\} \quad j \in \{1,2\}}{[]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1|[A]|M_2]\}} \quad (\mathsf{Par}_1)}$$
 
$$\frac{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_j]\} \quad a \not\in A \quad j \in \{1,2\}}{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1|[A]|M_2]\}} \quad (\mathsf{Par}_2)}{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1]\} \quad [a]E' \to \{\lambda'_j : y_j = E'_j\}_{j \in J} \in \{[M_2]\} \quad a \in A} \quad (\mathsf{Par}_3)}$$
 
$$\frac{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1]\} \quad [a]E' \to \{\lambda'_j : y_j = E'_j\}_{j \in J} \in \{[M_2]\} \quad a \in A}{[BE \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}\}} \quad (\mathsf{Hide}_1)$$
 
$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \notin A}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \notin A} \quad (\mathsf{Hide}_2)}$$
 
$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in A}{[BE \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}\}} \quad (\mathsf{Subst}_1)}$$
 
$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \notin \mathsf{dom}(\sigma)}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}} \quad (\mathsf{Subst}_2)}$$
 
$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}{[\sigma a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}} \quad (\mathsf{Subst}_3)$$

The rules above work with modules, parallel composition, name hiding, and substitution. The idea is that given a network, we wish to collect all those commands F that are contained in the network, independently from which module they are being executed in. Intuitively, we can regard  $\{[N]\}$  as a set, where starting from all commands present in the syntax, we do some filtering and renaming, based on the structure of the network.

Now, given  $\{N\}$ , we define a transition system that shows how the system evolves. In order to do so, let state be a function that given a variable in Var returns a value in Val. Then, given an initial state  $\mathsf{state}_0$ , we can define a transition system where each of node is a (different)  $\mathsf{state}$  function. Then, we can move from  $\mathsf{state}_1$  to  $\mathsf{state}_2$  whenever

That means that ones we have a set of executable rules, we can start building a transition system. In order to do so, we

$$W(M)=\{F\mid F\in\{\![M]\!]\}$$
 
$$X=\{x_1,\ldots,x_n\}$$
 
$$\sigma:X o V$$

38

39

40

41

43

### 1.2 Choreographies

46 Syntax. Our choreographic language is defined by the following syntax:

```
(Chor) C ::= \{ \mathbf{p}_i \}_{i \in I} + \{ \lambda_j : x_j = E_j; \ C_j \}_{j \in J} \mid \text{if } E@\{\mathbf{p}_i \}_{i \in I} \text{ then } C_1 \text{ else } C_2 \mid X \mid \mathbf{0} \}
```

- 48 We briefly comment the various constructs. The syntactic category C denotes choreographic
- programmes. The term  $\{p_i\}_{i\in I}$   $+\{\lambda_j: x_j=E_j;\ C_j\}_{j\in J}$  denotes an interaction between the
- roles  $p_i$ . The value  $\lambda_j$  is a real number representing the rate. ...

# 1.3 Projection from Choreographies to PRISM

- 52 Mapping Choreographies to PRISM. We need to run some standard static checks
- because, since there is branching, some terms may not be projectable.

```
f: C \longrightarrow \operatorname{network} \longrightarrow \operatorname{network} \qquad \operatorname{network} : \mathcal{R} \longrightarrow \operatorname{Set}(F)
f\left(\operatorname{p}_1 \longrightarrow \{\operatorname{p}_i\}_{i \in I} + \{\lambda_j : x_j = E_j : C_j\}_{j \in J}, \operatorname{network}\right)
=
|\operatorname{label} = \operatorname{newlabel}();
\operatorname{for} \operatorname{p}_k \in \operatorname{roles}\{
\operatorname{for} j \in J\{
\operatorname{network} = \operatorname{add}(\operatorname{p}_k, [\operatorname{label}] s_{\operatorname{p}_k} = \operatorname{state}(\operatorname{p}_k) \rightarrow \lambda_j : x_j = E_j \ \& \ s'_{\operatorname{p}_k} = \operatorname{genNewState}(\operatorname{p}_k));
\}
f \cap j \in J\{
\operatorname{network} = f(C_j, \operatorname{network});
\operatorname{return} \operatorname{network}
f\left(\operatorname{if} E@\{\operatorname{p}_i\}_{i \in I} \operatorname{then} C_1 \operatorname{else} C_2, \operatorname{network}\right)
=
f \cap \operatorname{p}_k \in \operatorname{roles}\{
\operatorname{network} = \operatorname{add}(\operatorname{p}_k, [] s_{\operatorname{p}_k} = \operatorname{state}(\operatorname{p}_k) \ \& \ f(E));
\operatorname{network} = f(C_1, \operatorname{network});
\operatorname{network} = f(C_2, \operatorname{network});
\operatorname{network} = f(C_2, \operatorname{network});
\operatorname{return} \operatorname{network}
```

# 2 Tests

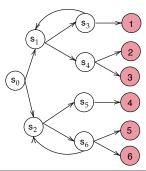
70

In this section we present our experimental evaluation of our language. We focus on four benchmarks: the dice program and the random graphs protocol that we compare with the test cases reported in the PRISM repository<sup>1</sup>; the Bitcoin proof of work protocol and the Hybrid Casper protocol, presented in [2, 4].

# 2.1 The Dice Program

The first test case we focus on the Dice Program<sup>2</sup>[5]. The following program models a die using only fair coins. Starting at the root vertex (state  $s_0$ ), one repeatedly tosses a coin. Every time heads appears, one takes the upper branch and when tails appears, the lower branch. This continues until the value of the die is decided.

In Listing 1, we report the modelled program using the choreographic language while in Listing 2 the generated PRISM program is shown.



```
preamble
     "dtmc"
75
     endpreamble
76
77
     n = 1;
78
79
     Dice \rightarrow Dice : "d : [0..6] init 0;";
80
81
82
     {\tt DiceProtocol}_0 \; \coloneqq \; {\tt Dice} \; \to \; {\tt Dice} \; : \; (\texttt{+["0.5*1"]} \;\; \texttt{" "&\&" "} \;\; . \;\; {\tt DiceProtocol}_1
                                               +["0.5*1"] " "&&" " . DiceProtocol<sub>2</sub>)
     {	t DiceProtocol}_1 \coloneqq {	t Dice} 	o {	t Dice} : (+["0.5*1"] " "&&" "
86
                                 Dice \rightarrow Dice : (+["0.5*1"] " "&&" " . DiceProtocol_1
87
88
                                                    +["0.5*1"] "(d'=1)"&&" " . DiceProtocol3)
                                              +["0.5*1"] " "&&" "
89
                                 Dice \rightarrow Dice : (+["0.5*1"] "(d'=2)"&&" " . DiceProtocol_3
90
                                                     +["0.5*1"] "(d'=3)"&&" " . DiceProtocol3))
91
92
     {	t DiceProtocol}_2 \coloneqq {	t Dice} 	o {	t Dice} : (+["0.5*1"] " "&&" "
93
                                 Dice \rightarrow Dice : (+["0.5*1"] " "&&" " . DiceProtocol_2
                                                     +["0.5*1"] "(d'=4)"&&" " . DiceProtocol_3)
95
                                            +["0.5*1"] " "&&" " .
                                 Dice \rightarrow Dice : (+["0.5*1"] "(d'=5)"&&" " . DiceProtocol_3
97
                                                    +["0.5*1"] "(d'=6)"&&" " . DiceProtocol3))
     DiceProtocol_3 := Dice \rightarrow Dice : (["1*1"] " "&&" ".DiceProtocol_3)
100
     }
101
```

 $<sup>^{1}</sup>$  https://www.prismmodelchecker.org/casestudies/

https://www.prismmodelchecker.org/casestudies/dice.php

102

**Listing 1** Choreographic language for the Dice Program.

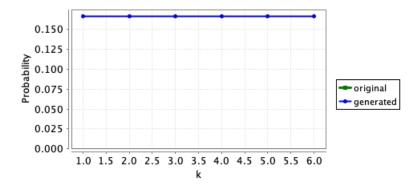
```
dtmc
104
105
     module Dice
106
              Dice : [0..11] init 0;
107
              d : [0..6] init 0;
108
109
                 (Dice=0) \rightarrow 0.5 : (Dice'=2) + 0.5 : (Dice'=6);
110
111
                 (Dice=2) \rightarrow 0.5 : (Dice'=3) + 0.5 : (Dice'=4);
                            \rightarrow 0.5 : (Dice'=2) + 0.5 : (d'=1)&(Dice'=10);
112
                  (Dice=4) \rightarrow 0.5 : (d'=2) & (Dice'=10) + 0.5 : (d'=3) & (Dice'=10);
113
              (Dice=6) \rightarrow 0.5 : (Dice'=7) + 0.5 : (Dice'=8);
114
              (Dice=7) \rightarrow 0.5 : (Dice'=6) + 0.5 : (d'=4)&(Dice'=10);
115
                 (Dice=8) \rightarrow 0.5 : (d'=5) & (Dice'=10) + 0.5 : (d'=6) & (Dice'=10);
              Г٦
116
              [] (Dice=10) \rightarrow 1 : (Dice'=10);
117
118
     endmodule
119
```

**Listing 2** Generated PRISM program for the Dice Program.

By comparing our model with the one presented in the PRISM documentation, we notice that the difference is the number assumed by the variable Dice. In particular, the variable assumes different values and this is due to how the generation in presence of a branch is done. However, this does not cause any problems since the updates are done correctly and the states are unique. Moreover, to prove the generated program is correct, we show that the probability of reaching a state where

$$d=k \text{ for } k = 1, \dots, 6 \text{ is } 1/6.$$

The results are displayed in Figure 1, where we compare the probability we obtain with our generated model and the one obtained with the original PRISM model. As expected, the results are equivalent.



**Figure 1** Probability of reaching a state where d = k, for k = 1, ..., 6.

123

125

126

127

128

129

130

131

132

134

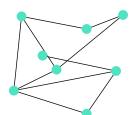
135

136

137

138

# 2.2 Random Graphs Protocol



The second case study we report is the random graphs protocol presented in the PRISM documentation<sup>3</sup>. It investigates the likelihood that a pair of nodes are connected in a random graph. More precisely, we take into account the the set of random graphs G(n,p), i.e. the set of random graphs with n nodes where the probability of there being an edge between any two nodes equals p.

The model is divided in two parts: at the beginning the random graph is built. Then the algorithm finds nodes that have a path to node 2 by searching for nodes for which one can reach (in one step) a node for which the existence of a path to node 2 has already been found.

The choreographic model is shown in Listing 3, while in Listing 4, we report only part of the generated PRISM module (the modules  $M_2$ ,  $M_3$  and  $P_2$ ,  $P_3$  are equivalent to, respectively,  $M_1$  and  $P_2$  and can be found in the repository<sup>4</sup>).

```
139
     preamble
140
     "mdp"
141
     "const double p;"
142
143
     endpreamble
144
    n = 3;
145
146
    PC -> PC : " ";
147
    M[i] -> i in [1...n] M[i] : "varM[i] : bool;";
148
    P[i] -> i in [1...n] P[i] : "varP[i] : bool;";
149
150
151
    GraphConnected0 :=
152
             PC -> M[i] : (+["1*p"] " "&&"(varM[i]'=true)". END
153
                              +["1*(1-p)"] " "&&"(varM[i]'=false)". END)
154
             PC -> P[i] : (+["1*p"] " "&&"(varP[i]'=true)" . END
155
                              +["1*(1-p)"] " "&&"(varP[i]'=false)".
156
                              if "(PC=6)&!varP[i]&((varP[i] & varM[i]) | (varM[i+1] & varP[
157
158
                                   \hookrightarrow i+2])) "@P[i] then {
                                      ["1"]"(varP[i]'=true)"@P[i] . GraphConnectedO
159
160
                              })
    }
\frac{161}{162}
```

**Listing 3** Choreographic language for the Random Graphs Protocol.

```
163
164
mdp
165 const double p;
166
167 module PC
168 PC: [0..7] init 0;
169
```

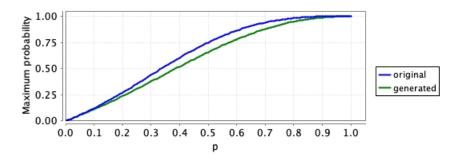
 $<sup>^3</sup>$  https://www.prismmodelchecker.org/casestudies/graph\_connected.php

 $<sup>^4</sup>$  https://github.com/adeleveschetti/choreography-to-PRISM

```
170
         [DPPGR] (PC=0) \rightarrow 1 : (PC'=1);
         [YCJJG] (PC=1) \rightarrow 1 : (PC'=2);
171
         [TWGVA] (PC=2) \rightarrow 1 : (PC'=3);
172
         [NODPZ] (PC=3) \rightarrow 1 : (PC'=4);
173
         [FDALJ] (PC=4) \rightarrow 1 : (PC'=5);
174
         [DCKXC] (PC=5) \rightarrow 1 : (PC'=6);
175
     endmodule
176
177
     module M1
178
        M1 : [0..1] init 0;
179
        varM1 : bool;
180
181
         [DPPGR] (M1=0) \rightarrow p :(varM1'=true)&(M1'=0) + (1-p) :(varM1'=false)&(M1'=0);
182
     endmodule
183
184
185
186
     module P1
187
        P1 : [0..3] init 0;
188
        varP1 : bool;
189
190
         [NODPZ] (P1=0) \rightarrow p:(varP1'=true)&(P1'=0) + (1-p):(varP1'=false)&(P1'=0);
191
         [] (P1=0)&(PC=6)&!varP1&((varP1 & varM1) | (varM2& varP3))
192
                                         \rightarrow 1 : (varP1'=true)&(P1'=0);
193
194
     endmodule
195
196
```

Listing 4 Generated PRISM program for the Random Graphs Protocol.

The model is very similar to the one presented in the PRISM repository, the main difference is that we use state variables also for the modules  $P_i$  and  $M_i$ , where in the original model they were not requires. However, this does not affect the behaviour of the model, as the reader can notice from the results of the probability that nodes 1 and 2 are connected showed in Figure 2.



**Figure 2** Probability that the nodes 1 and 2 are connected.

201

199

205

206

207

208

210

215

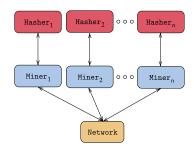
216

#### 2.3 Proof of Work Bitcoin Protocol

In [2], the authors decided to extend the PRISM model checker with dynamic data types in order to model the Proof of Work protocol implemented in the Bitcoin blockchain [6].

The Bitcoin system is the result of the parallel composition of n Miner processes, n Hasher processes and a process called Network. In particular:

- The *Miner* processes model the blockchain mainers that create new blocks and add them to their local ledger;
- the *Hasher* processes model the attempts of the miners to solve the cryptopuzzle;
- the Network process model the broadcast communication among miners.



Since we are not interested in the properties obtained by analyzing the protocol, we decided to consider n = 4 miner and hasher processes; the model can be found in Listing 5.

```
217
    preamble
218
219
    endpreamble
220
221
    n = 4;
222
223
224
225
226
    PoW := Hasher[i] -> Miner[i] :
227
    (+["mR*hR[i]"] " "\&\&"(b[i]'=createB(b[i],B[i],c[i]))\&(c[i]'=c[i]+1)".
228
           Miner[i] -> Network :
229
                   (["rB*1"] "(B[i]'=addBlock(B[i],b[i]))" &&
230
                  foreach(k != i) "(set[k], addBlockSet(set[k], b[i]))" @Network .PoW)
231
     +["lR*hR[i]"] " " && " " .
232
           if "!isEmpty(set[i])"@Miner[i] then {
233
                   ["r"] "(b[i]'=extractBlock(set[i]))"@Miner[i] .
234
                          Miner[i] -> Network :
235
                          (["1*1"] "(setMiner[i]' = addBlockSet(setMiner[i] , b[i]))"&&
236
                              237
           }
238
           else{
239
                   if "canBeInserted(B[i],b[i])"@Miner[i] then {
240
                          ["1"] "(B[i]'=addBlock(B[i],b[i]))&&(setMiner[i]'=removeBlock
241
                              242
                  }
243
                  else{
244
                          PoW
245
                  }
246
           }
247
248
    }
249
```

**Listing 5** Choreographic language for the Proof of Work Bitcoin Protocol.

Part of the generated PRISM code is shown in Listing 6, the modules  $Miner_2$ ,  $Miner_3$ ,  $Miner_4$  and  $Hasher_2$ ,  $Hasher_3$ ,  $Hasher_4$  are equivalent to  $Miner_1$  and  $Hasher_1$ , respectively. Our generated PRISM model is more verbose than the one presented in [2], this is due to the fact that for the if-then-else expression, we always generate the else branch. and this leads to having more instructions

252

253

255

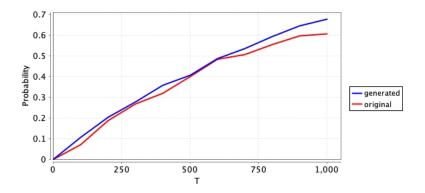
300

```
256
257
258
     module Miner1
259
         Miner1 : [0..7] init 0;
         b1 : block {m1,0;genesis,0} ;
261
         B1 : blockchain [{genesis,0;genesis,0}];
262
         c1 : [0..N] init 0;
263
         setMiner1 : list [];
264
265
         [PZKYT] (Miner1=0) \rightarrow hR1 : (b1'=createB(b1,B1,c1))&(c1'=c1+1)&(Miner1'=1);
266
         [EUBVP] (Miner1=0) \rightarrow hR1 : (Miner1'=2);
267
         [HXYKO] (Miner1=1) \rightarrow 1 : (B1'=addBlock(B1,b1))&(Miner1'=0);
268
         \label{eq:miner1} \begin{tabular}{ll} \begin{tabular}{ll} $($Miner1=2)\&!isEmpty(set1)$ $\rightarrow$ $r:(b1'=extractBlock(set1))\&(Miner1'=4)$; \end{tabular}
269
         [SRKSV] (Miner1=4) \rightarrow 1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Miner1'=0)
270
              \hookrightarrow ;
271
         [] (Miner1=2)\&!(!isEmpty(set1)) \rightarrow 1 : (Miner1'=5);
         [] (Miner1=5)\&canBeInserted(B1,b1) \rightarrow 1 : (B1'=addBlock(B1,b1))\&(setMiner1'=balanceInserted(B1,b1))

    removeBlock(setMiner1,b1))&(Miner1'=0);
274
         [] (Miner1=5)&!(canBeInserted(B1,b1)) \rightarrow 1 : (Miner1'=0);
275
276
     endmodule
277
278
     module Network
279
     Network : [0..1] init 0;
280
         set1 : list [];
281
         [HXYK0] (Network=0) \rightarrow 1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,
              \rightarrow b3))&(set4'=addBlockSet(set4,b4))&(Network'=0);
         [SRKSV] (Network=0) \rightarrow 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
286
287
288
     endmodule
289
290
     module Hasher1
291
     Hasher1 : [0..1] init 0;
292
293
      [PZKYT] (Hasher1=0) \rightarrow mR : (Hasher1'=0);
294
      [EUBVP] (Hasher1=0) \rightarrow 1R : (Hasher1'=0);
295
     endmodule
297
298
```

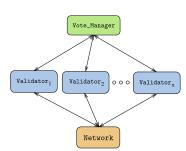
**Listing 6** Generated PRISM program for the Peer-To-Peer Protocol.

However, for this particular test case, the results of the experiments are not affected, as shown Figure 3 where the results are compared. In this example, since we are comparing the results of two simulations, the two probabilities are slightly different, but it has nothing to do with the model itself.



**Figure 3** Probability at least one miner has created a block.

# 2.4 Hybrid Casper Protocol



305

306

308

309

310

311

312

313

314

316

317

The last case we study we present is the Hybrid Casper Protocol modelled in PRISM in [4]. The Hybrid Capser protocol is an hybrid blockchain consenus protocol that includes features of the Proof of Work and the Proof of Stake protocols. It was implemented in the Ethereum blockchain [3] as a testing phase before switching to Proof of Stake protocol.

The approach is very similar to the one used for the Proof of Work Bitcoin protocol, so they model Hybrid Casper in PRISM as the parallel composition of n Validator modules

and the module Vote\_Manager and Network. The module Validator is very similar to the module Miner of the previous protocol and the only module that requires an explaination is the Vote\_Manager that stores the tables containing the votes for each checkpoint and calculates the rewards/penalties.

The modeling language is reported in Listing 7 while (part of) the generated PRISM code can be found in Listing 8.

```
319
    preamble
320
321
    endpreamble
322
    n = 5;
323
324
     . . .
     ₹
325
    PoS := Validator[i] -> Validator[i] :
326
        (+["mR*1"] "(b[i]'=createB(b[i],L[i],c[i]))\&(c[i]'=c[i]+1)"\&\&" "
327
       if "!(mod(getHeight(b[i]),EpochSize)=0)"@Validator[i] then{
328
          Validator[i] -> Network : (["1*1"] "(L[i]'=addBlock(L[i],b[i]))" && foreach(k
329
              \hookrightarrow !=i) "(set[k]'=addBlockSet(set[k],b[i]))"@Network .PoS)
330
       }
331
       else{
332
          Validator[i] -> Network : (["1*1"] "(L[i]'=addBlock(L[i],b[i]))" && foreach(k
333

→ !=i) "(set[k]'=addBlockSet(set[k],b[i]))"@Network . Validator[i] ->

334

→ Vote_Manager :(["1*1"] " "&&"(Votes'=addVote(Votes,b[i],stake[i]))".PoS

335
              \hookrightarrow ))
336
337
        +["lR*1"] " "&&" " . if "!isEmpty(set[i])"@Validator[i] then {
338
```

```
["1"] "(b[i]'=extractBlock(set[i]))"@Validator[i] .
339
            if "!canBeInserted(L[i],b[i])"@Validator[i] then {
               PoS
341
           }
342
           else{
343
           if "!(mod(getHeight(b[i]),EpochSize)=0)"@Validator[i] then {
344
            Validator[i] -> Network : (["1*1"] "(setMiner[i]' = addBlockSet(setMiner[i])
345
                 \hookrightarrow , b[i]))"&&"(set[i]' = removeBlock(set[i],b[i]))" . PoS)
346
          }
347
          else{
348
            Validator[i] -> Network : (["1*1"] "(setMiner[i]' = addBlockSet(setMiner[i]
349
                 → , b[i]))"&&"(set[i]' = removeBlock(set[i],b[i]))" . Validator[i] ->
                 → Vote_Manager : (["1*1"] " "&&"(Votes'=addVote(Votes,b[i],stake[i]))
351
                 → ".PoS ))
352
          }
353
        }
354
      }
355
      else{PoS}
356
       +["rC*1"] "(lastCheck[i]'=extractCheckpoint(listCheckpoints[i],lastCheck[i]))&(
357
            → heightLast[i] '=getHeight(extractCheckpoint(listCheckpoints[i],lastCheck[i
358
            \hookrightarrow \texttt{])))\&(votes[i]'=calcVotes(Votes,extractCheckpoint(listCheckpoints[i],extractCheckpoints[i])))}
359
            → lastCheck[i])))"&&" " .
360
          if "(heightLast[i]=heightCheckpoint[i]+EpochSize)&(votes[i]>=2/3*tot_stake)"
361

→ @Validator[i] then{
36
            if "(heightLast[i]=heightCheckpoint[i]+EpochSize)"@Validator[i] then{
363
              ["1"] "(lastJ[i]'=b[i])&(L[i]'= updateHF(L[i],lastJ[i]))" @Validator[i].
36
                   → Validator[i]->Vote_Manager :(["1*1"]" "&&"(epoch'=height(lastF(L[i
365
                  → ]))&(Stakes'=addVote(Votes,b[i],stake[i]))".PoS)
366
367
           else{["1"] "(lastJ[i]'=b[i])"@Validator[i] . PoS}
368
369
          else{PoS}
370
371
    }
372
373
```

Listing 7 Choreographic language for the Hybrid Casper Protocol.

```
374
     module Validator1
375
376
377
        [] (Validator1=0) \rightarrow mR : (b1'=createB(b1,L1,c1))&(c1'=c1+1)&(Validator1'=1);
378
        [] (Validator1=0) \rightarrow 1R : (Validator1'=2);
379
        [] (Validator1=0)&(!isEmpty(listCheckpoints1)) \rightarrow
             rC : (lastCheck1'=extractCheckpoint(listCheckpoints1,lastCheck1))&(
38

→ heightLast1'=getHeight(extractCheckpoint(listCheckpoints1,lastCheck1))
382
                  → )))&(votes1'=calcVotes(Votes,extractCheckpoint(listCheckpoints1,
383

    lastCheck1)))&(Validator1'=3);
384
        [NGRDF] (Validator1=1)&!(mod(getHeight(b1), EpochSize)=0) \rightarrow 1 : (L1'=addBlock(
385
             \hookrightarrow L1,b1))&(Validator1'=0);
386
        [] (Validator1=1)\&!(!(mod(getHeight(b1),EpochSize)=0)) \rightarrow 1 : (Validator1'=3);
387
        [PCRLD] (Validator1=1)&!(mod(getHeight(b1),EpochSize)=0) \rightarrow
388
             1 : (L1'=addBlock(L1,b1))&(Validator1'=4);
389
        [VSJBE] (Validator1=5) \rightarrow 1 : (Validator1'=0);
390
        [] (Validator1=2)&!isEmpty(set1) \rightarrow
391
```

```
1 : (b1'=extractBlock(set1))&(Validator1'=4);
392
        [] (Validator1=4)&!canBeInserted(L1,b1) \rightarrow (Validator1'=0);
393
        [] (Validator1=4)&!(!canBeInserted(L1,b1)) \rightarrow 1 : (Validator1'=6);
394
        [MDDCF] (Validator1=6)&!(mod(getHeight(b1),EpochSize)=0) \rightarrow
395
             1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=0);
396
        [] (Validator1=6)&!(!(mod(getHeight(b1),EpochSize)=0)) → 1 : (Validator1'=8);
397
        [IQVPA] (Validator1=6)&!(mod(getHeight(b1),EpochSize)=0) \rightarrow
398
             1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=9);
300
        [IFNVZ] (Validator1=10) \rightarrow 1 : (Validator1'=0);
400
        [] (Validator1=2)&!(!isEmpty(set1)) \rightarrow 1 : (Validator1'=0);
401
        [] (Validator1=3)&(heightLast1=heightCheckpoint1+EpochSize)&(votes1>=2/3*
402
             \hookrightarrow tot_stake) \rightarrow (Validator1'=4);
403
        [] (Validator1=4)&(heightLast1=heightCheckpoint1+EpochSize) \rightarrow
404
             1 : (lastJ1'=b1)&(L1'= updateHF(L1,lastJ1))&(Validator1'=6);
405
        [EQCYO] (Validator1=6) \rightarrow 1 : (Validator1'=0);
406
        [] (Validator1=4)&!((heightLast1=heightCheckpoint1+EpochSize)) \rightarrow
407
             1 : (lastJ1'=b1)&(Validator1'=0);
408
        [] (Validator1=3)&!((heightLast1=heightCheckpoint1+EpochSize)&(votes1>=2/3*
409
             \hookrightarrow tot_stake)) \rightarrow 1 : (Validator1'=0);
410
     endmodule
411
412
    module Network
413
        Network : [0..1] init 0;
414
        set1 : list [];
415
        set2 : list [];
416
        set3 : list [];
417
        set4 : list [];
418
        set5 : list [];
419
420
        [NGRDF] (Network=0) \rightarrow
421
             1: (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(set4'=
422
                  \hookrightarrow addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&(Network'=0);
423
        [PCRLD] (Network=0) \rightarrow
424
             1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(set4'=
425
                  \hookrightarrow addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&(Network'=0);
426
        [MDDCF] (Network=0) \rightarrow 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
427
        [IQVPA] (Network=0) \rightarrow 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
429
     endmodule
430
431
    module Vote_Manager
432
        Vote Manager : [0..1] init 0;
433
        epoch : [0..10] init 0;
434
        Votes : hash[];
435
        tot_stake : [0..120000] init 50;
436
        stake1 : [0..N] init 10;
437
        stake2 : [0..N] init 10;
438
        stake3 : [0..N] init 10;
439
        stake4 : [0..N] init 10;
440
        stake5 : [0..N] init 10;
441
442
        [VSJBE] (Vote_Manager=0) \rightarrow
443
             1 : (Votes'=addVote(Votes,b1,stake1))&(Vote_Manager'=0);
444
445
     endmodule
446
```

447

450

452

457

458

459

460

461

462

463

464

465

466

467

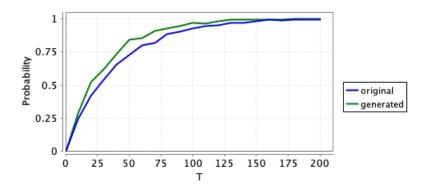
468

469

470

# **Listing 8** Generated PRISM program for the Hybrid Casper Protocol.

The code is very similar to the one presented in [4], the main difference is the fact that our generated model has more lines of code. This is due to the fact that there are some commands that can be merged, but the compiler is not able to do it automatically. This discrepancy between the two models can be observed also in the simulations, reported in Figure 4. Although the results are similar, PRISM takes 39.016 seconds to run the simulations for the generated model, instead of 22.051 seconds needed for the original model.



**Figure 4** Probability that a block has been created.

#### 2.5 Problems

While testing our choreographic language, we noticed that some of the case studies presented in the PRISM documentation [1] cannot be modeled by using our language. The reasons are various, in this section we try to outline the problems.

- Asynchronous Leader Election<sup>5</sup>: processes synchronize with the same label but the conditions are different. We include in our language the it-then-else statement but we do not allow the if-then (without the else). This is done because in this way, we do not incur in deadlock states.
- Probabilistic Broadcast Protocols<sup>6</sup>: also in this case, the problem are the labels of the synchronizations. In fact, all the processes synchronize with the same label on every actions. This is not possible in our language, since a label is unique for every synchronization between two (or more) processes.
- Cyclic Server Polling System<sup>7</sup>: in this model, the processes  $station_i$  do two different things in the same state. More precicely, at the state 0 ( $s_i$ =0), the processes may synchronize with the process server or may change their state without any synchronization. In out language, this cannot be formalized since the synchronization is a branch action, so there should be another option with a synchronization.

https://www.prismmodelchecker.org/casestudies/asynchronous\_leader.php

 $<sup>^6</sup>$  https://www.prismmodelchecker.org/casestudies/prob\_broadcast.php

<sup>7</sup> https://www.prismmodelchecker.org/casestudies/polling.php

#### m:14 A Choreographic Language for PRISM

#### ---- References

- Prism documentation. https://www.prismmodelchecker.org/. Accessed: 2023-09-05.
- Stefano Bistarelli, Rocco De Nicola, Letterio Galletta, Cosimo Laneve, Ivan Mercanti, and Adele Veschetti. Stochastic modeling and analysis of the bitcoin protocol in the presence of block communication delays. Concurr. Comput. Pract. Exp., 35(16), 2023. doi:10.1002/cpe.6749.
- Vitalik Buterin. Ethereum white paper. https://github.com/ethereum/wiki/wiki/
  White-Paper, 2013.
- Letterio Galletta, Cosimo Laneve, Ivan Mercanti, and Adele Veschetti. Resilience of hybrid casper under varying values of parameters. *Distributed Ledger Technol. Res. Pract.*, 2(1):5:1–5:25, 2023. doi:10.1145/3571587.
- D. Knuth and A. Yao. Algorithms and Complexity: New Directions and Recent Results, chapter The complexity of nonuniform random number generation. Academic Press, 1976.
- Satoshi Nakamoto. Bitcoin: A peer-to-peer electronic cash system. https://bitcoin.org/bitcoin.pdf, 2008.