

A Choreographic Language for PRISM

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Abstract

This is the abstract

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1 Formal Language

In this section, we provide the formal definition of our choreographic language as well as process algebra representing PRISM [?].

1.1 PRISM

We start by describing PRISM semantics. Except from transforming some informal text in precise rules, Our formalisation closely follows that found on the PRISM website [?].

Syntax. Let \mathbf{p} range over a (possibly infinite) set of module names \mathcal{R} , a over a (possibly infinite) set of labels \mathcal{L} , x over a (possibly infinite) set of variables \mathbf{Var} , and v over a (possibly infinite) set of values \mathbf{Val} . Then, the syntax of PRISM is given by the following grammar:

(Networks)	$N, M ::=$	$\mathbf{0}$	empty network
		$\mathbf{p} : \{F_i\}_i$	module
		$M [A] M$	parallel composition
		M/A	action hiding
		σM	substitution
(Commands)	$F ::=$	$[a]g \rightarrow \Sigma_{i \in I} \{\lambda_i : u_i\}$	g is a boolean expression in E
(Assignment)	$u ::=$	$(x' = E)$	update x , element of \mathcal{V} , with E
		$A \& A$	multiple assignments
(Expr)	$E ::=$	$f(\tilde{E}) \mid x \mid v$	

Networks are the top syntactic category for system of modules composed together. The term $CEnd$ represent an empty network. A module $\mathbf{p} : \{F_i\}_i$ is identified by its name \mathbf{p} and a set of commands F_i . Networks can be composed in parallel, in a CSP style: a term like $M_1|[A]|M_2$ says that networks M_1 and M_2 can interact with each other using labels in the finite set A . The term M/A is the standard CSP/CCS hiding operator. Finally σM is equivalent to applying the substitution σ to all variables in x . A substitution is a function that given a variable returns a value. When we write σN we refer to the term obtained by replacing every free variable x in N with $\sigma(x)$. [Marco: Is this really the way substitution is used?](#)
[Where does it become important?](#)

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30 **Semantics.** We construct all the enables commands by applying a closure to the following
 31 rules.

$$\begin{array}{c}
 \frac{\llbracket E \rightarrow \{\lambda_i : x_i = E_i\}_{i \in I} \in \llbracket M_j \rrbracket \quad j \in \{1, 2\}}{\llbracket E \rightarrow \{\lambda_i : x_i = E_i\}_{i \in I} \in \llbracket M_1 \mid [A] \mid M_2 \rrbracket} \\
 \\
 \frac{[a]E \rightarrow \{\lambda_i : x_i = E_i\}_{i \in I} \in \llbracket M_j \rrbracket \quad a \notin A \quad j \in \{1, 2\}}{[a]E \rightarrow \{\lambda_i : x_i = E_i\}_{i \in I} \in \llbracket M_1 \mid [A] \mid M_2 \rrbracket} \\
 \\
 \frac{[a]E \rightarrow \{\lambda_j : x_i = E_i\}_{i \in I} \in \llbracket M_1 \rrbracket \quad [a]E' \rightarrow \{\lambda_j : x'_j = E'_j\}_{j \in J} \in \llbracket M_2 \rrbracket \quad a \in A}{[a]E \wedge E' \rightarrow \{\lambda_i * \lambda'_j : x_i = E_i \wedge x'_j = E'_j\}_{i \in I, j \in J} \in \llbracket M_1 \mid [A] \mid M_2 \rrbracket}
 \end{array}$$

33 That means that ones we have a set of executable rules, we can start building a transition
 34 system. In order to do so, we

$$W(M) = \{F \mid F \in \llbracket M \rrbracket\}$$

35 $X = \{x_1, \dots, x_n\}$

$$\sigma : X \rightarrow V$$

1.2 Choreographies

Syntax. Our choreographic language is defined by the following syntax:

$$(\text{Chor}) \quad C ::= \{p_i\}_{i \in I} + \{\lambda_j : x_j = E_j; C_j\}_{j \in J} \mid \text{if } E@p \text{ then } C_1 \text{ else } C_2 \mid X \mid 0$$

We briefly comment the various constructs. The syntactic category C denotes choreographic programmes. The term $\{p_i\}_{i \in I} + \{\lambda_j : x_j = E_j; C_j\}_{j \in J}$ denotes an interaction between the roles p_i . The value λ_j is a real number representing the rate. ...

1.3 Projection from Choreographies to PRISM

Mapping Choreographies to PRISM. We need to run some standard static checks because, since there is branching, some terms may not be projectable.

$$f : C \longrightarrow \text{network} \longrightarrow \text{network} \quad \text{network} : \mathcal{R} \longrightarrow \text{Set}(F)$$

$$f\left(p_1 \longrightarrow \{p_i\}_{i \in I} \oplus \{[\lambda_j]x_j = E_j : D_j\}_{j \in J}, \text{network}\right)$$

=

```
label = newlabel();
for  $p_k \in \text{roles}\{$ 
  for  $j \in J\{$ 
    network = add( $p_k, [label]s_{p_k} = \text{state}(p_k) \rightarrow \lambda_j : x_j = E_j \ \& \ s'_{p_k} = \text{genNewState}(p_k);$ 
  }
}
for  $j \in J\{$ 
  network =  $f(D_j, \text{network});$ 
}
return network
```

$$f\left(\text{if } E@p \text{ then } C_1 \text{ else } C_2, \text{network}\right)$$

=

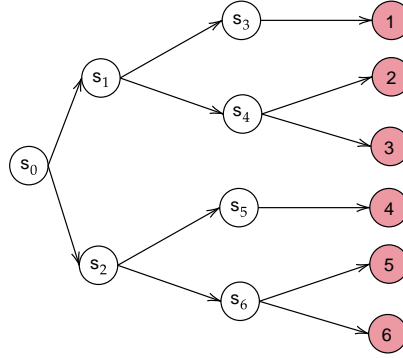
```
network = add( $p, []s_p = \text{state}(p) \ \& \ f(E);$ 
network =  $f(C_1, \text{network});$ 
network =  $f(C_2, \text{network});$ 
return network
```

2 Tests

We tested our language by various examples.

2.1 The Dice Program

The first example we present is the Dice Program¹ [4]. The following program models a die using only fair coins. Starting at the root vertex (state 0), one repeatedly tosses a coin. Every time heads appears, one takes the upper branch and when tails appears, the lower branch. This continues until the value of the die is decided.



We modelled the program using the choreographic language (Listing 1) and we were able to generate the corresponding PRISM program, reported in Listing 2.

```

57 preamble
58 "dtmc"
59 endpreamble
60
61
62 n = 1;
63 Dice → Dice : "d : [0..6] init 0;" ;
64
65 {
66 DiceProtocol0 := Dice → Dice : (+["0.5*1" " "&&" " . DiceProtocol1
67   +["0.5*1" " "&&" " . DiceProtocol2)
68
69 DiceProtocol1 := Dice → Dice : (+["0.5*1" " "&&" " .
70   Dice → Dice : (+["0.5*1" " "&&" " . DiceProtocol1
71   +["0.5*1" " "(d'=1)"&&" " . DiceProtocol3)
72   +["0.5*1" " "&&" " .
73   Dice → Dice : (+["0.5*1" " "(d'=2)"&&" " . DiceProtocol3
74   +["0.5*1" " "(d'=3)"&&" " . DiceProtocol3)
75
76 DiceProtocol2 := Dice → Dice : (+["0.5*1" " "&&" " .
77   Dice → Dice : (+["0.5*1" " "&&" " . DiceProtocol2
78   +["0.5*1" " "(d'=4)"&&" " . DiceProtocol3)
79   +["0.5*1" " "&&" " .
80   Dice → Dice : (+["0.5*1" " "(d'=5)"&&" " . DiceProtocol3
81   +["0.5*1" " "(d'=6)"&&" " . DiceProtocol3)

```

¹ <https://www.prismmodelchecker.org/casestudies/dice.php>

```

82
83 DiceProtocol3 := Dice → Dice : ([ "1*1" " "&&" ".DiceProtocol3)
84 }
85

```

■ **Listing 1** Choreographic language for the Dice Program.

```

86
87 dtmc
88
89 module Dice
90     Dice : [0..11] init 0;
91     d : [0..6] init 0;
92
93     [] (Dice=0) → 0.5 : (Dice'=2) + 0.5 : (Dice'=6);
94     [] (Dice=2) → 0.5 : (Dice'=3) + 0.5 : (Dice'=4);
95     [] (Dice=3) → 0.5 : (Dice'=2) + 0.5 : (d'=1)&(Dice'=10);
96     [] (Dice=4) → 0.5 : (d'=2)&(Dice'=10) + 0.5 : (d'=3)&(Dice'=10);
97     [] (Dice=6) → 0.5 : (Dice'=7) + 0.5 : (Dice'=8);
98     [] (Dice=7) → 0.5 : (Dice'=6) + 0.5 : (d'=4)&(Dice'=10);
99     [] (Dice=8) → 0.5 : (d'=5)&(Dice'=10) + 0.5 : (d'=6)&(Dice'=10);
100    [] (Dice=10) → 1 : (Dice'=10);
101
102 endmodule
103

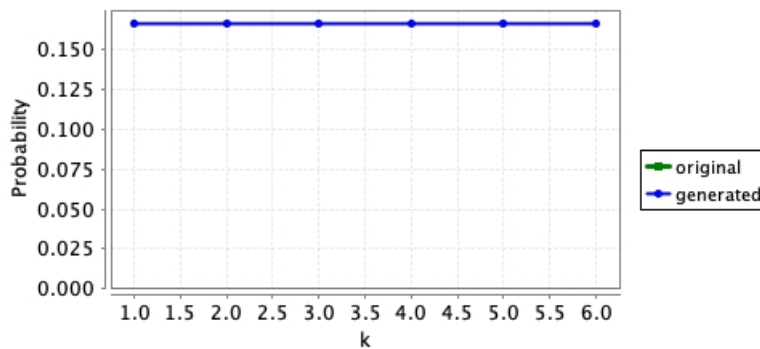
```

■ **Listing 2** Generated PRISM program for the Dice Program.

By comparing our model with the one presented in the PRISM documentation, we noticed that the difference is the number assumed by the variable `Dice`. In particular, the variable does not assume the values 1, 5 and 9. This is due to how the generation in presence of a branch is done. However, this does not cause any problems since the updates are done correctly. Moreover, to prove the generated program is correct, we show that the probability of reaching a state where

$$d=k \text{ for } k = 1, \dots, 6 \text{ is } 1/6.$$

104 The results are displayed in Figure 1, where also the results obtained with the original PRISM model are shown.



■ **Figure 1** Probability of reaching a state where $d = k$, for $k = 1, \dots, 6$.

2.2 Simple Peer-To-Peer Protocol

This case study describes a simple peer-to-peer protocol based on BitTorrent². The model comprises a set of clients trying to download a file that has been partitioned into K blocks. Initially, there is one client that has already obtained all of the blocks and N additional clients with no blocks. Each client can download a block from any of the others but they can only attempt four concurrent downloads for each block. The code we analyze with $k = 5$ and $N = 4$ is reported in Listing 3.

```

113 preamble
114 "ctmc"
115 "const double mu=2;"
116 "formula rate1=mu*(1+min(3,b11+b21+b31+b41));"
117 "formula rate2=mu*(1+min(3,b12+b22+b32+b42));"
118 "formula rate3=mu*(1+min(3,b13+b23+b33+b43));"
119 "formula rate4=mu*(1+min(3,b14+b24+b34+b44));"
120 "formula rate5=mu*(1+min(3,b15+b25+b35+b45));"
121 endpreamble
122
123
124 n = 4;
125 n = 4;
126
127 Client[i] → i in [1..n]
128 Client[i] : "b[i]1 : [0..1];", "b[i]2 : [0..1];", "b[i]3 : [0..1];", "b[i]4 :
129           [0..1];", "b[i]5 : [0..1];" ;
130
131 {
132 PeerToPeer := Client[i] → Client[i]:
133           (+["rate1*1"] "(b[i]1'=1)"&&" " . PeerToPeer
134           +["rate2*1"] "(b[i]2'=1)"&&" " . PeerToPeer
135           +["rate3*1"] "(b[i]3'=1)"&&" " . PeerToPeer
136           +["rate4*1"] "(b[i]4'=1)"&&" " . PeerToPeer
137           +["rate5*1"] "(b[i]5'=1)"&&" " . PeerToPeer)
138 }
139

```

■ Listing 3 Choreographic language for the Peer-To-Peer Protocol.

Part of the generated PRISM code is shown in Listing 4 and it is faithful with what reported in the PRISM documentation.

```

142 ctmc
143
144 const double mu=2;
145 formula rate1=mu*(1+min(3,b11+b21+b31+b41));
146 formula rate2=mu*(1+min(3,b12+b22+b32+b42));
147 formula rate3=mu*(1+min(3,b13+b23+b33+b43));
148 formula rate4=mu*(1+min(3,b14+b24+b34+b44));
149 formula rate5=mu*(1+min(3,b15+b25+b35+b45));
150
151 module Client1
152     Client1 : [0..1] init 0;
153     b11 : [0..1];
154     b12 : [0..1];
155     b13 : [0..1];

```

² <https://www.prismmodelchecker.org/casestudies/peer2peer.php>

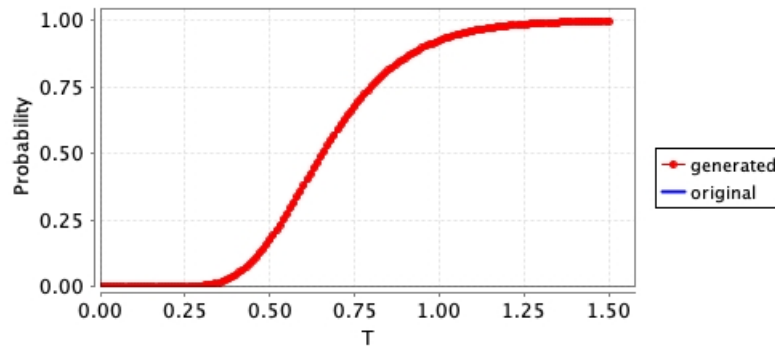
```

156      b14 : [0..1];
157      b15 : [0..1];
158
159      [] (Client1=0) → rate1 : (b11'=1)&(Client1'=0);
160      [] (Client1=0) → rate2 : (b12'=1)&(Client1'=0);
161      [] (Client1=0) → rate3 : (b13'=1)&(Client1'=0);
162      [] (Client1=0) → rate4 : (b14'=1)&(Client1'=0);
163      [] (Client1=0) → rate5 : (b15'=1)&(Client1'=0);
164
165  endmodule
166

```

■ **Listing 4** Generated PRISM program for the Peer-To-Peer Protocol.

167 In Figure 2, we compare the values obtained for the probability that all clients have
 168 received all blocks by time $0 \leq T \leq 1.5$ both for our generated model and the model reported
 in the documentation.



■ **Figure 2** Probability that clients received all the block before T , with $0 \leq T \leq 1.5$.

169

170 2.3 Proof of Work Bitcoin Protocol

171 This protocol represents the Proof of Work implemented in the Bitcoin blockchain. In[2],
 172 a Bitcoin system is the result of the parallel composition of n Miner processes, n *Hasher*
 173 processes and a process called *Network*. *Hasher* processes model the attempts of the miners
 174 to solve the cryptopuzzle, while the *Network* process model the broadcast communication
 175 among miners. We tested our system by considering a protocol with $n = 5$ miners and it is
 176 reported in Listing 5.

```

177  preamble
178  "ctmc"
179  "const T"
180  "const double r = 1;"
181  "const double mR = 1/600;"
182  "const double lR = 1-mR;"
183  "const double hR1 = 0.25;"
184  "const double hR2 = 0.25;"
185  "const double hR3 = 0.25;"
186  "const double hR4 = 0.25;"
187  "const double rB = 1/12.6;"
188  "const int N = 100;"
189  endpreamble
190

```

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```

191
192 n = 4;
193
194 Hasher[i] -> i in [1..n] ;
195
196 Miner[i] -> i in [1..n]
197 Miner[i] : "b[i] : block {m[i],0;genesis,0} ;", "B[i] : blockchain [{genesis,0;
198     genesis,0}];", "c[i] : [0..N] init 0;", "setMiner[i] : list [];" ;
199
200 Network ->
201 Network : "set1 : list [];", "set2 : list [];", "set3 : list [];" , "set4 : list
202     [];" ;
203
204 {
205 PoW := Hasher[i] → Miner[i] :
206 (+["mR*hr[i]" " "&&"(b[i]'=createB(b[i],B[i],c[i]))&(c[i]'=c[i]+1)" " .
207     Miner[i] → Network :
208         ([ "rB*1" " (B[i]'=addBlock(B[i],b[i]))" &&
209             foreach(k != i) "(set[k]'=addBlockSet(set[k],b[i]))" @Network .PoW
210 +["lR*hr[i]" " " && " " " .
211         if "!isEmpty(set[i])"@Miner[i] then {
212             ["r" " (b[i]'=extractBlock(set[i]))"@Miner[i] .
213             Miner[i] → Network :
214                 ([ "1*1" " (setMiner[i]' = addBlockSet(setMiner[i] , b[i]))"
215                 &&"(set[i]' = removeBlock(set[i],b[i]))" . PoW)
216         }
217         else{
218             if "canBeInserted(B[i],b[i])"@Miner[i] then {
219                 ["1" " (B[i]'=addBlock(B[i],b[i]))
220                 &(setMiner[i]'=removeBlock(setMiner[i],b[i]))"@Miner[i] . Pow
221             }
222             else{
223                 PoW
224             }
225         }
226     )
227 }
228

```

■ **Listing 5** Choreographic language for the Proof of Work Bitcoin Protocol.

Part of the generated PRISM code is shown in Listing 6.

```

229
230
231 ctmc
232 const T;
233 const double r = 1;
234 const double mR = 1/600;
235 const double lR = 1-mR;
236 const double hR1 = 0.25;
237 const double hR2 = 0.25;
238 const double hR3 = 0.25;
239 const double hR4 = 0.25;
240 const double rB = 1/12.6;
241 const int N = 100;
242
243 module Miner1
244 Miner1 : [0..7] init 0;

```



```

245 b1 : block {m1,0;genesis,0} ;
246 B1 : blockchain [{genesis,0;genesis,0}];
247 c1 : [0..N] init 0;
248 setMiner1 : list [];
249
250 [PZKYT] (Miner1=0) → hR1 : (b1'=createB(b1,B1,c1))&(c1'=c1+1)&(Miner1'=1);
251 [EUBVP] (Miner1=0) → hR1 : (Miner1'=2);
252 [HXYKO] (Miner1=1) → 1 : (B1'=addBlock(B1,b1))&(Miner1'=0);
253 [] (Miner1=2)&!isEmpty(set1) → r : (b1'=extractBlock(set1))&(Miner1'=4);
254 [SRKSV] (Miner1=4) → 1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Miner1'=0);
255 [] (Miner1=2)&!(isEmpty(set1)) → 1 : (Miner1'=5);
256 [] (Miner1=5)&canBeInserted(B1,b1) → 1 : (B1'=addBlock(B1,b1))
257           &(setMiner1'=removeBlock(setMiner1,b1))&(Miner1'=0);
258 [] (Miner1=5)&!(canBeInserted(B1,b1)) → 1 : (Miner1'=0);
259 endmodule
260 ...
261 module Network
262   Network : [0..1] init 0;
263   set1 : list [];
264   ...
265
266 [HXYKO] (Network=0) → 1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3
267   ))&(set4'=addBlockSet(set4,b4))&(Network'=0);
268 [SRKSV] (Network=0) → 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
269 ...
270
271 endmodule
272
273 module Hasher1
274   Hasher1 : [0..1] init 0;
275
276 [PZKYT] (Hasher1=0) → mR : (Hasher1'=0);
277 [EUBVP] (Hasher1=0) → lR : (Hasher1'=0);
278
279 endmodule
280

```

■ **Listing 6** Generated PRISM program for the Peer-To-Peer Protocol.

281 In Figure 3, we compare the values obtained for the probability that at least one miner
 282 has mined a block both for the generated model and the model presented in [2].

283 2.4 Random Graphs Protocol

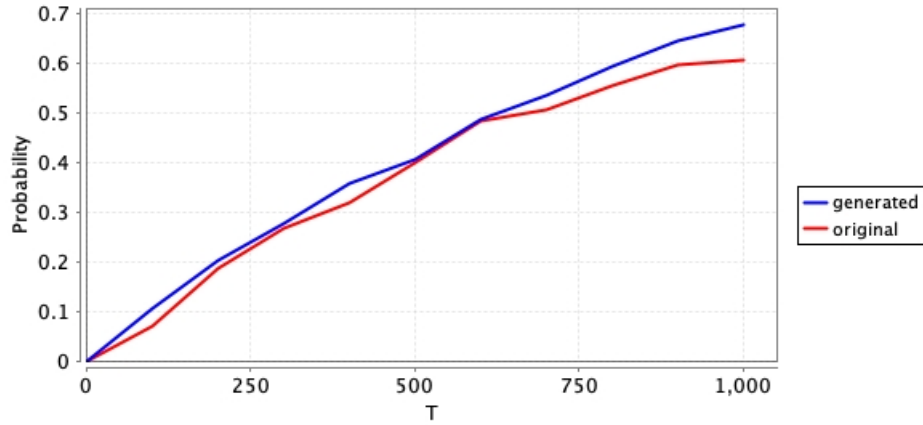
284 In this case study³ we investigate the likelihood that a pair of nodes are connected in a
 285 random graph. More precisely, we take into account the the set of random graphs $G(n, p)$,
 286 i.e. the set of random graphs with n nodes where the probability of there being an edge
 287 between any two nodes equals p .

```

288     preamble
289     "mdp"
290     "const double p;"
291     endpreamble
292

```

³ https://www.prismmodelchecker.org/casestudies/graph_connected.php



■ **Figure 3** Probability at least one miner has created a block.

```

293
294  n = 3;
295
296  PC ->
297  PC : " ";
298
299  M[i] -> i in [1..n]
300  Module[i] : "varM[i] : bool;";
301
302  P[i] -> i in [1..n]
303  P[i] : "varP[i] : bool;";
304
305  {
306  GraphConnected0 :=
307      PC -> M[i] : (+["1*p"] " "&&"(varM[i] '=true)". END
308                  +["1*(1-p)" " "&&"(varM[i] '=false)". END)
309      PC -> P[i] : (+["1*p"] " "&&"(varP[i] '=true)" . END
310                  +["1*(1-p)" " "&&"(varP[i] '=false)".
311                  if "(PC=6)&!varP[i]&((varP[i] & varM[i]) | (varM[i+1] & varP[
312                  i+2]))" "@P[i] then {
313                      ["1"] "(varP[i] '=true)"@P[i] . GraphConnected0
314                  })
315  }
316

```

■ **Listing 7** Choreographic language for the Random Graphs Protocol.

317 The model is divided in two parts: at the beginning the random graph is built. Then they
318 find nodes that have a path to node 2 by searching for nodes for which one can reach (in one
319 step) a node for which they have already found the existence of a path to node 2. Part of the
320 generated PRISM code is shown in Listing 8 (we do not report modules M2, M3, P2, P3).

```

321
322  mdp
323  const double p;
324
325  module PC
326      PC : [0..7] init 0;
327

```

```

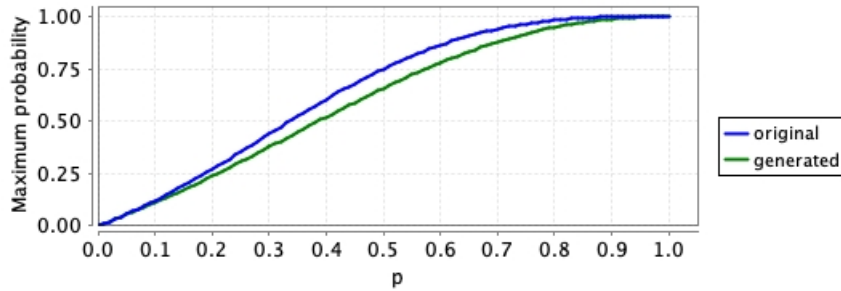
328 [DPPGR] (PC=0) → 1 : (PC'=1);
329 [YCJJG] (PC=1) → 1 : (PC'=2);
330 [TWGVA] (PC=2) → 1 : (PC'=3);
331 [NODPZ] (PC=3) → 1 : (PC'=4);
332 [FDALJ] (PC=4) → 1 : (PC'=5);
333 [DCKXC] (PC=5) → 1 : (PC'=6);
334 endmodule
335
336 module M1
337   M1 : [0..1] init 0;
338   varM1 : bool;
339
340   [DPPGR] (M1=0) → p : (varM1'=true)&(M1'=0) + (1-p) : (varM1'=false)&(M1'=0);
341 endmodule
342
343 ...
344
345 module P1
346   P1 : [0..3] init 0;
347   varP1 : bool;
348
349   [NODPZ] (P1=0) → p : (varP1'=true)&(P1'=0) + (1-p) : (varP1'=false)&(P1'=0);
350   [] (P1=0)&(PC=6)&!varP1&((varP1 & varM1) | (varM2& varP3))
351     → 1 : (varP1'=true)&(P1'=0);
352 endmodule
353

```

■ **Listing 8** Generated PRISM program for the Random Graphs Protocol.

354 The model is very similar to the one presented in the PRISM repository, the main
 355 difference is that we use state variables also for the modules P_i and M_i .

In Figure 4, we compare the results obtained with the two models.



■ **Figure 4** Probability that the nodes 1 and 2 are connected.

356

357 2.5 Hybrid Casper Protocol

358 The last case we study is the Hybrid Casper Protocol presented in [3]. The protocol models
 359 what happened in the Ethereum blockchain while it was implemented the hybrid Casper
 360 protocol: an hybrid protocol that includes features of the Proof of Work and the Proof of
 361 Stake protocols. The modeling language is reported in Listing 9 while (part of) the generated
 362 PRISM code can be found in Listing 8.

363 preamble
 364

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```

365 "ctmc"
366 "const int EpochSize = 2;"
367 "const k = 1;"
368 "const double rMw = 1/12.6;"
369 "const epochs = 0;"
370 "const double T;"
371 "const int N = 100;"
372 "const double rC = 1/(14*EpochSize);"
373 "const double mR = 1/14;"
374 "const double lR = 10;"
375 endpreamble
376
377 n = 5;
378
379 Validator[i] -> i in [1..n]
380 Validator[i] : "b[i] : block {m[i],0;genesis,0};", "lastJ[i] : block {m[i],0;
381     genesis,0};", "L[i] : blockchain [{genesis,0;genesis,0}];", "c[i] : [0..N]
382     init 0;", "setMiner[i] : list [];", "heightCheckpoint[i] : [0..N] init 0;", "
383     heightLast[i] : [0..N] init 0;", "lastFinalized[i] : block {genesis,0;genesis
384     ,0};", "lastJustified[i] : block {genesis,0;genesis,0};", "lastCheck[i] :
385     block {genesis,0;genesis,0};", "votes[i] : [0..1000] init 0;", "
386     listCheckpoints[i] : list []";
387
388 Network ->
389 Network : "set1 : list [];", "set2 : list [];", "set3 : list [];" , "set4 : list
390     [];" , "set5 : list []";
391
392 Vote_Manager ->
393 Vote_Manager : "Votes : hash [];" , "tot_stake : [0..120000] init 50;", "stake1 :
394     [0..N] init 10;", "stake2 : [0..N] init 10;", "stake3 : [0..N] init 10;", "
395     stake4 : [0..N] init 10;", "stake5 : [0..N] init 10;";
396
397 {
398 PoS := Validator[i] -> Validator[i] :
399     (+["mR*1"] " (b[i]'=createB(b[i],L[i],c[i]))&(c[i]'=c[i]+1)"&&" " .
400     if "!(mod(getHeight(b[i]),EpochSize)=0)"@Validator[i] then{
401         Validator[i] -> Network : ([ "1*1" ] " (L[i]'=addBlock(L[i],b[i]
402         ]))" && foreach(k!=i) "(set[k]'=addBlockSet(set[k],b[i]))"
403         "@Network .PoS)
404     }
405     else{
406         Validator[i] -> Network : ([ "1*1" ] " (L[i]'=addBlock(L[i],b[i]
407         ]))" && foreach(k!=i) "(set[k]'=addBlockSet(set[k],b[i]))"
408         "@Network .
409         Validator[i] -> Vote_Manager : ([ "1*1" ] " "&&"(Votes'=addVote(
410         Votes,b[i],stake[i]))".PoS))
411     }
412     +["lR*1"] " "&&" " .
413     if "isEmpty(set[i])"@Validator[i] then {
414         [ "1" ] " (b[i]'=extractBlock(set[i]))"@Validator[i] .
415         if "canBeInserted(L[i],b[i])"@Validator[i] then {
416             PoS
417         }
418         else{
419             if "!(mod(getHeight(b[i]),EpochSize)=0)"

```

```

420         @Validator[i] then {
421             Validator[i] -> Network : ([ "1*1" ] "(
422                 setMiner[i]' = addBlockSet(setMiner
423                     [i] , b[i]))"&&"(set[i]' =
424                     removeBlock(set[i],b[i]))" . PoS)
425         }
426     else{
427         Validator[i] -> Network : ([ "1*1" ] "(
428             setMiner[i]' = addBlockSet(setMiner
429                 [i] , b[i]))"&&"(set[i]' =
430                 removeBlock(set[i],b[i]))" .
431             Validator[i] -> Vote_Manager :
432             ([ "1*1" ] " "&&"(Votes'=addVote(
433                 Votes,b[i],stake[i]))".PoS ))
434     }
435 }
436 }
437 else{
438     PoS
439 }
440 +["rC*1"] "(lastCheck[i]'=extractCheckpoint(listCheckpoints[i],lastCheck[i
441 ]) )&(heightLast[i]'=getHeight(extractCheckpoint(listCheckpoints[i],
442 lastCheck[i]))&(votes[i]'=calcVotes(Votes,extractCheckpoint(
443 listCheckpoints[i],lastCheck[i])))"&&" " .
444     if "(heightLast[i]=heightCheckpoint[i]+EpochSize)&(votes[i]>=2/3*
445 tot_stake)"@Validator[i] then{
446         if "(heightLast[i]=heightCheckpoint[i]+EpochSize)"@Validator[
447 i] then{
448             ["1"] "(lastJ[i]'=b[i])&(L[i]'= updateHF(L[i],lastJ[i
449 ]) )" @Validator[i].Validator[i]->Vote_Manager
450             :([ "1*1" ] " "&&"(epoch'=height(lastF(L[i]))&(Stakes
451                 '=addVote(Votes,b[i],stake[i]))".PoS)
452         }
453     else{
454         ["1"] "(lastJ[i]'=b[i])"@Validator[i] . PoS
455     }
456 }
457 else{
458     PoS
459 }
460 )
461 }
462

```

■ Listing 9 Choreographic language for the Hybrid Casper Protocol.

```

463
464 module Validator1
465     ...
466
467 [] (Validator1=0) → mR : (b1'=createB(b1,L1,c1))&(c1'=c1+1)&(Validator1'=1);
468 [] (Validator1=0) → lR : (Validator1'=2);
469 [] (Validator1=0)&(!isEmpty(listCheckpoints1)) →
470     rC : (lastCheck1'=extractCheckpoint(listCheckpoints1,lastCheck1))&(
471         heightLast1'=getHeight(extractCheckpoint(listCheckpoints1,lastCheck1)))
472         &(votes1'=calcVotes(Votes,extractCheckpoint(listCheckpoints1,lastCheck1
473             )))&(Validator1'=3);

```

```

474 [NGRDF] (Validator1=1)&!(mod(getHeight(b1),EpochSize)=0) → 1 : (L1'=addBlock(
475   L1,b1))&(Validator1'=0);
476 [] (Validator1=1)&!(mod(getHeight(b1),EpochSize)=0) → 1 : (Validator1'=3);
477 [PCRLD] (Validator1=1)&!(mod(getHeight(b1),EpochSize)=0) →
478   1 : (L1'=addBlock(L1,b1))&(Validator1'=4);
479 [VSJBE] (Validator1=5) → 1 : (Validator1'=0);
480 [] (Validator1=2)&!isEmpty(set1) →
481   1 : (b1'=extractBlock(set1))&(Validator1'=4);
482 [] (Validator1=4)&!canBeInserted(L1,b1) → (Validator1'=0);
483 [] (Validator1=4)&!(canBeInserted(L1,b1)) → 1 : (Validator1'=6);
484 [MDDCF] (Validator1=6)&!(mod(getHeight(b1),EpochSize)=0) →
485   1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=0);
486 [] (Validator1=6)&!(mod(getHeight(b1),EpochSize)=0) → 1 : (Validator1'=8);
487 [IQVPA] (Validator1=6)&!(mod(getHeight(b1),EpochSize)=0) →
488   1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=9);
489 [IFNVZ] (Validator1=10) → 1 : (Validator1'=0);
490 [] (Validator1=2)&!isEmpty(set1) → 1 : (Validator1'=0);
491 [] (Validator1=3)&(heightLast1=heightCheckpoint1+EpochSize)&(votes1>=2/3*
492   tot_stake) → (Validator1'=4);
493 [] (Validator1=4)&(heightLast1=heightCheckpoint1+EpochSize) →
494   1 : (lastJ1'=b1)&(L1'= updateHF(L1,lastJ1))&(Validator1'=6);
495 [EQCYO] (Validator1=6) → 1 : (Validator1'=0);
496 [] (Validator1=4)&!(heightLast1=heightCheckpoint1+EpochSize) →
497   1 : (lastJ1'=b1)&(Validator1'=0);
498 [] (Validator1=3)&!(heightLast1=heightCheckpoint1+EpochSize)&(votes1>=2/3*
499   tot_stake)) → 1 : (Validator1'=0);
500 endmodule
501 ...
502 module Network
503   Network : [0..1] init 0;
504   set1 : list [];
505   set2 : list [];
506   set3 : list [];
507   set4 : list [];
508   set5 : list [];
509
510   [NGRDF] (Network=0) →
511     1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(set4'=
512       addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&(Network'=0);
513   [PCRLD] (Network=0) →
514     1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(set4'=
515       addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&(Network'=0);
516   [MDDCF] (Network=0) → 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
517   [IQVPA] (Network=0) → 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
518   ...
519 endmodule
520
521 module Vote_Manager
522   Vote_Manager : [0..1] init 0;
523   epoch : [0..10] init 0;
524   Votes : hash[];
525   tot_stake : [0..120000] init 50;
526   stake1 : [0..N] init 10;
527   stake2 : [0..N] init 10;
528   stake3 : [0..N] init 10;

```

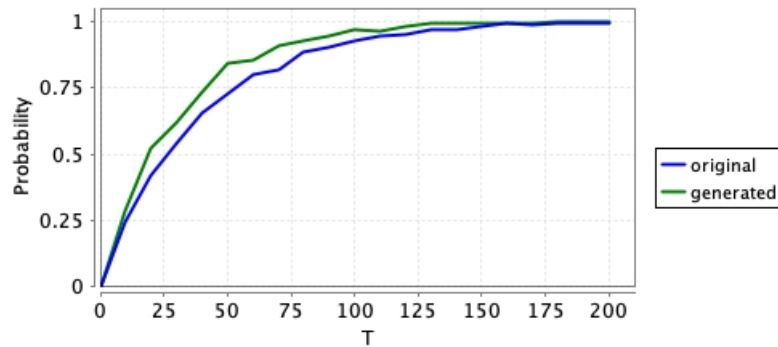
```

529     stake4 : [0..N] init 10;
530     stake5 : [0..N] init 10;
531
532     [VSJBE] (Vote_Manager=0) →
533         1 : (Votes'=addVote(Votes,b1,stake1))&(Vote_Manager'=0);
534     ...
535 endmodule

```

■ **Listing 10** Generated PRISM program for the Hybrid Casper Protocol.

537 The code is very similar to the one presented in [3], the main difference is the fact that
 538 our generated model has more lines of code. This is due to the fact that there are some
 539 commands that can be merged, but the compiler is not able to do it automatically. This
 540 discrepancy between the two models can be observed also in the simulations, reported in
 541 Figure 5. Although the results are similar, PRISM takes 39.016 seconds to run the simulations
 542 for the generated model, instead of 22.051 seconds needed for the original model.



■ **Figure 5** Probability that a block has been created.

543 2.6 Problems

544 While testing our choreographic language, we noticed that some of the case studies presented
 545 in the PRISM documentation [1] cannot be modeled by using our language. The reasons are
 546 various, in this section we try to outline the problems.

- 547 ■ **Asynchronous Leader Election**⁴: processes synchronize with the same label but the
 548 conditions are different. We include in our language the **it-then-else** statement but we
 549 do not allow the **if-then** (without the **else**). This is done because in this way, we do
 550 not incur in deadlock states.
- 551 ■ **Probabilistic Broadcast Protocols**⁵: also in this case, the problem are the labels
 552 of the synchronizations. In fact, all the processes synchronizes with the same label on
 553 every actions. This is not possible in our language, since a label is unique for every
 554 synchronization between two (or more) processes.

⁴ https://www.prismmodelchecker.org/casestudies/asynchronous_leader.php

⁵ https://www.prismmodelchecker.org/casestudies/prob_broadcast.php

555 ■ **Cyclic Server Polling System**⁶: in this model, the processes `stationi` do two different
 556 things in the same state. More precicely, at the state 0 ($s_i=0$), the processes may syn-
 557 chornize with the process `server` or may change their state without any synchronization.
 558 In out language, this cannot be formalized since the synchronization is a branch action,
 559 so there should be another option with a synchronization.

560 — References —

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 567 5:25, 2023. doi:10.1145/3571587.
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⁶ <https://www.prismmodelchecker.org/casestudies/polling.php>