A Choreographic Language for PRISM

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Abstract

- This is the abstract
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Formal Language

- In this section, we provide the formal definition of our choreographic language as well as
- process algebra representing PRISM [?].

1.1 **PRISM**

- We start by describing PRISM semantics. Except from transforming some informal text in
- precise rules, Our formalisation closely follows that found on the PRISM website [?].
- Syntax. Let p range over a (possibly infinite) set of module names \mathcal{R} , a over a (possibly
- infinite) set of labels \mathcal{L} , x over a (possibly infinite) set of variables Var, and v over a (possibly
- infinite) set of values Val. Then, the syntax of PRISM is given by the following grammar:

$$(Networks) \qquad N, M \quad ::= \quad \mathbf{0} \qquad \qquad \text{empty network} \\ \mid \ \mathsf{p} : \{F_i\}_i \qquad \qquad \text{module} \\ \mid \ M \mid [A] \mid M \qquad \qquad \text{parallel composition} \\ \mid \ M/A \qquad \qquad \text{action hiding} \\ \mid \ \sigma M \qquad \qquad \text{substitution} \\ (Commands) \qquad F \quad ::= \qquad [a]g \to \Sigma_{i \in I} \{\lambda_i : u_i\} \quad g \text{ is a boolean expression in } E \\ (Assignment) \qquad u \quad ::= \qquad (x' = E) \qquad \qquad \text{update } x, \text{ element of } \mathcal{V}, \text{ with } E \\ \mid \ A\&A \qquad \qquad \text{multiple assignments} \\ (Expr) \qquad E \quad ::= \qquad f(\tilde{E}) \quad \mid \ x \quad \mid \ v$$

- Networks are the top syntactic category for system of modules composed together. The
- term CEnd represent an empty network. A module $p:\{F_i\}_i$ is identified by its name p
- and a set of commands F_i . Networks can be composed in parallel, in a CSP style: a term
- like $M_1[A]M_2$ says that networks M_1 and M_2 can interact with each other using labels in
- the finite set A. The term M/A is the standard CSP/CCS hiding operator. Finally σM is
- equivalent to applying the substitution σ to all variables in x. A substitution is a function
- that given a variable returns a value. When we write σN we refer to the term obtained by
- replacing every free variable x in N with $\sigma(x)$. Marco: Is this really the way substitution is used?
- Where does it become important?

m:2 A Choreographic Language for PRISM

Semantics. In order to give a probabilistic semantics to PRISM, we proceed by steps. First, we define {[-]}, as the closure of the following rules:

$$\frac{[]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_j]\} \quad j \in \{1,2\}}{[]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1|[A]|M_2]\}} \quad (\mathsf{Par}_1)}$$

$$\frac{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_j]\} \quad a \not\in A \quad j \in \{1,2\}}{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1|[A]|M_2]\}} \quad (\mathsf{Par}_2)}{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1]\} \quad [a]E' \to \{\lambda'_j : y_j = E'_j\}_{j \in J} \in \{[M_2]\} \quad a \in A} \quad (\mathsf{Par}_3)}$$

$$\frac{[a]E \to \{\lambda_i : x_i = E_i\}_{i \in I} \in \{[M_1]\} \quad [a]E' \to \{\lambda'_j : y_j = E'_j\}_{j \in J} \in \{[M_2]\} \quad a \in A}{[BE \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}\}} \quad (\mathsf{Hide}_1)$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \notin A}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \notin A} \quad (\mathsf{Hide}_2)}$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in A}{[BE \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}\}} \quad (\mathsf{Subst}_1)}$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \notin \mathsf{dom}(\sigma)}{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\}} \quad (\mathsf{Subst}_2)}$$

$$\frac{[a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}{[\sigma a]E \to \{\lambda_j : x_i = E_i\}_{i \in I} \in \{[M]\} \quad a \in \mathsf{dom}(\sigma)}} \quad (\mathsf{Subst}_3)$$

The rules above work with modules, parallel composition, name hiding, and substitution. The idea is that given a network, we wish to collect all those commands F that are contained in the network, independently from which module they are being executed in. Intuitively, we can regard $\{[N]\}$ as a set, where starting from all commands present in the syntax, we do some filtering and renaming, based on the structure of the network.

Now, given $\{N\}$, we define a transition system that shows how the system evolves. In order to do so, let state be a function that given a variable in Var returns a value in Val. Then, given an initial state state_0 , we can define a transition system where each of node is a (different) state function. Then, we can move from state_1 to state_2 whenever

That means that ones we have a set of executable rules, we can start building a transition system. In order to do so, we

$$W(M)=\{F\mid F\in\{\![M]\!]\}$$

$$X=\{x_1,\ldots,x_n\}$$

$$\sigma:X o V$$

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45 1.2 Choreographies

46 Syntax. Our choreographic language is defined by the following syntax:

```
(Chor) C ::= \{ \mathbf{p}_i \}_{i \in I} + \{ \lambda_j : x_j = E_j; \ C_j \}_{j \in J} \mid \text{if } E@\{\mathbf{p}_i \}_{i \in I} \text{ then } C_1 \text{ else } C_2 \mid X \mid \mathbf{0} \}
```

- 48 We briefly comment the various constructs. The syntactic category C denotes choreographic
- programmes. The term $\{p_i\}_{i\in I} + \{\lambda_i : x_j = E_j; C_i\}_{j\in J}$ denotes an interaction between the
- roles p_i . The value λ_j is a real number representing the rate. ...

1.3 Projection from Choreographies to PRISM

- 52 Mapping Choreographies to PRISM. We need to run some standard static checks
- because, since there is branching, some terms may not be projectable.

```
f: C \times \mathtt{network} \times States \times Labels \longrightarrow \mathtt{network} \quad \mathtt{network} : \mathcal{R} \longrightarrow \mathrm{Set}(F)
54
               f\Big( \ \mathsf{p}_1 \longrightarrow \{\mathsf{p}_i\}_{i \in I} + \{\lambda_j : x_j = E_j : C_j\}_{j \in J}, \mathtt{network}, \overline{s}, \ell \Big)
                \text{ for } \mathsf{p}_k \in \mathbf{roles} \{
                    for j \in J\{
                         \mathtt{network} = \mathtt{add}(\mathsf{p}_k, [\ell] \ s_{\mathsf{p}_k} = s_k \rightarrow \ \lambda_j : x_j = E_j \ \& \ s'_{\mathsf{p}_k} = s_k + 1);
                for j \in J\{
                    network = f(C_j, network, \overline{s}', genLabel(\ell));
                return network
              where \overline{s} = (s_1, \dots, s_n) and \overline{s}' = (s_1 + 1, \dots, s_n + 1) for n = |\mathbf{roles}|.
56
               f\Big( \text{ if } E@\{\mathbf{p}_i\}_{i\in I} \text{ then } C_1 \text{ else } C_2, \mathtt{network}, \overline{s}, \ell \Big)
                for p_k \in \mathbf{roles}\{
                    \mathtt{network} = \mathtt{add}(\mathsf{p}_k, [\;] \; s_{\mathsf{p}_k} = s_k \; \& \; f(E)) + f(C_1, \mathtt{network}, \overline{s}, \ell);
                    \mathtt{network} = \mathtt{add}(\mathsf{p}_k, [\ ]\ s_{\mathsf{p}_k} = s_k\ \&\ !f(E)) + f(C_1, \mathtt{network}, \overline{s}, \ell);
                }
                return network
```

2 Tests

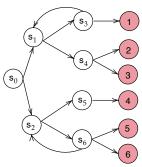
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In this section we present our experimental evaluation of our language. We focus on four benchmarks: the dice program and the random graphs protocol that we compare with the test cases reported in the PRISM repository¹; the Bitcoin proof of work protocol and the Hybrid Casper protocol, presented in [2, 4].

3 2.1 The Dice Program

The first test case we focus on the Dice Program²[5]. The following program models a die using only fair coins. Starting at the root vertex (state s_0), one repeatedly tosses a coin. Every time heads appears, one takes the upper branch and when tails appears, the lower branch. This continues until the value of the die is decided.

In Listing 1, we report the modelled program using the choreographic language while in Listing 2 the generated PRISM program is shown.



```
preamble
     "dtmc"
76
     endpreamble
77
78
     n = 1;
79
80
     Dice \rightarrow Dice : "d : [0..6] init 0;";
81
82
83
     {\tt DiceProtocol}_0 \; \coloneqq \; {\tt Dice} \; \to \; {\tt Dice} \; : \; (\texttt{+["0.5*1"]} \;\; \texttt{" "&\&" "} \;\; . \;\; {\tt DiceProtocol}_1
                                               +["0.5*1"] " "&&" " . DiceProtocol<sub>2</sub>)
86
     {	t DiceProtocol}_1 \coloneqq {	t Dice} 	o {	t Dice} : (+["0.5*1"] " "&&" "
87
                                 Dice \rightarrow Dice : (+["0.5*1"] " "&&" " . DiceProtocol_1
88
89
                                                    +["0.5*1"] "(d'=1)"&&" " . DiceProtocol3)
                                              +["0.5*1"] " "&&" "
90
                                 Dice \rightarrow Dice : (+["0.5*1"] "(d'=2)"&&" " . DiceProtocol_3
91
                                                     +["0.5*1"] "(d'=3)"&&" " . DiceProtocol3))
92
93
     {	t DiceProtocol}_2 \coloneqq {	t Dice} 	o {	t Dice} : (+["0.5*1"] " "&&" "
                                 Dice \rightarrow Dice : (+["0.5*1"] " "&&" " . DiceProtocol_2
                                                     +["0.5*1"] "(d'=4)"&&" " . DiceProtocol_3)
                                            +["0.5*1"] " "&&" " .
                                 Dice \rightarrow Dice : (+["0.5*1"] "(d'=5)"&&" " . DiceProtocol_3
                                                    +["0.5*1"] "(d'=6)"&&" " . DiceProtocol3))
100
     DiceProtocol_3 := Dice \rightarrow Dice : (["1*1"] " "&&" ".DiceProtocol_3)
101
     }
102
```

 $^{^{1}}$ https://www.prismmodelchecker.org/casestudies/

² https://www.prismmodelchecker.org/casestudies/dice.php

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Listing 1 Choreographic language for the Dice Program.

```
dtmc
105
106
     module Dice
107
              Dice : [0..11] init 0;
108
              d : [0..6] init 0;
109
110
                  (Dice=0) \rightarrow 0.5 : (Dice'=2) + 0.5 : (Dice'=6);
111
112
                  (Dice=2) \rightarrow 0.5 : (Dice'=3) + 0.5 : (Dice'=4);
                             \rightarrow 0.5 : (Dice'=2) + 0.5 : (d'=1)&(Dice'=10);
113
                  (Dice=4) \rightarrow 0.5 : (d'=2) & (Dice'=10) + 0.5 : (d'=3) & (Dice'=10);
114
               (Dice=6) \rightarrow 0.5 : (Dice'=7) + 0.5 : (Dice'=8);
115
               (Dice=7) \rightarrow 0.5 : (Dice'=6) + 0.5 : (d'=4)&(Dice'=10);
116
                  (Dice=8) \rightarrow 0.5 : (d'=5) & (Dice'=10) + 0.5 : (d'=6) & (Dice'=10);
               Г٦
117
              [] (Dice=10) \rightarrow 1 : (Dice'=10);
118
119
     endmodule
120
121
```

Listing 2 Generated PRISM program for the Dice Program.

By comparing our model with the one presented in the PRISM documentation, we notice that the difference is the number assumed by the variable Dice. In particular, the variable assumes different values and this is due to how the generation in presence of a branch is done. However, this does not cause any problems since the updates are done correctly and the states are unique. Moreover, to prove the generated program is correct, we show that the probability of reaching a state where

$$d=k \text{ for } k = 1, \dots, 6 \text{ is } 1/6.$$

The results are displayed in Figure 1, where we compare the probability we obtain with our generated model and the one obtained with the original PRISM model. As expected, the results are equivalent.

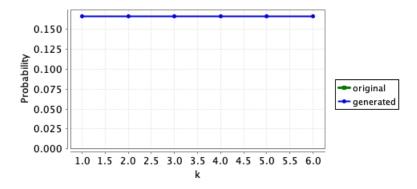


Figure 1 Probability of reaching a state where d = k, for k = 1, ..., 6.

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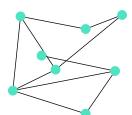
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2.2 Random Graphs Protocol



The second case study we report is the random graphs protocol presented in the PRISM documentation³. It investigates the likelihood that a pair of nodes are connected in a random graph. More precisely, we take into account the the set of random graphs G(n,p), i.e. the set of random graphs with n nodes where the probability of there being an edge between any two nodes equals p.

The model is divided in two parts: at the beginning the random graph is built. Then the algorithm finds nodes that have a path to node 2 by searching for nodes for which one can reach (in one step) a node for which the existence of a path to node 2 has already been found.

The choreographic model is shown in Listing 3, while in Listing 4, we report only part of the generated PRISM module (the modules M_2 , M_3 and P_2 , P_3 are equivalent to, respectively, M_1 and P_2 and can be found in the repository⁴).

```
140
     preamble
141
     "mdp"
142
     "const double p;"
143
144
     endpreamble
145
    n = 3;
146
147
    PC -> PC : " ";
148
    M[i] -> i in [1...n] M[i] : "varM[i] : bool;";
149
    P[i] -> i in [1...n] P[i] : "varP[i] : bool;";
150
151
152
    GraphConnected0 :=
153
             PC -> M[i] : (+["1*p"] " "&&"(varM[i]'=true)". END
154
                             +["1*(1-p)"] " "&&"(varM[i]'=false)". END)
155
             PC -> P[i] : (+["1*p"] " "&&"(varP[i]'=true)" . END
156
                             +["1*(1-p)"] " "&&"(varP[i]'=false)".
157
                             if "(PC=6)&!varP[i]&((varP[i] & varM[i]) | (varM[i+1] & varP[
158
159
                                  \hookrightarrow i+2])) "@P[i] then {
                                      ["1"]"(varP[i]'=true)"@P[i] . GraphConnectedO
160
161
                             })
    }
162
163
```

Listing 3 Choreographic language for the Random Graphs Protocol.

```
164
165 mdp
166 const double p;
167
168 module PC
169 PC: [0..7] init 0;
```

 $^{^3}$ https://www.prismmodelchecker.org/casestudies/graph_connected.php

 $^{^4}$ https://github.com/adeleveschetti/choreography-to-PRISM

```
171
         [DPPGR] (PC=0) \rightarrow 1 : (PC'=1);
         [YCJJG] (PC=1) \rightarrow 1 : (PC'=2);
172
         [TWGVA] (PC=2) \rightarrow 1 : (PC'=3);
173
         [NODPZ] (PC=3) \rightarrow 1 : (PC'=4);
174
         [FDALJ] (PC=4) \rightarrow 1 : (PC'=5);
175
         [DCKXC] (PC=5) \rightarrow 1 : (PC'=6);
176
     endmodule
177
178
     module M1
179
        M1 : [0..1] init 0;
180
        varM1 : bool;
181
182
         [DPPGR] (M1=0) \rightarrow p :(varM1'=true)&(M1'=0) + (1-p) :(varM1'=false)&(M1'=0);
183
     endmodule
184
185
186
187
     module P1
188
        P1 : [0..3] init 0;
189
        varP1 : bool;
190
191
         [NODPZ] (P1=0) \rightarrow p:(varP1'=true)&(P1'=0) + (1-p):(varP1'=false)&(P1'=0);
192
         [] (P1=0)&(PC=6)&!varP1&((varP1 & varM1) | (varM2& varP3))
193
                                         \rightarrow 1 : (varP1'=true)&(P1'=0);
194
195
     endmodule
189
```

Listing 4 Generated PRISM program for the Random Graphs Protocol.

The model is very similar to the one presented in the PRISM repository, the main difference is that we use state variables also for the modules P_i and M_i , where in the original model they were not requires. However, this does not affect the behaviour of the model, as the reader can notice from the results of the probability that nodes 1 and 2 are connected showed in Figure 2.

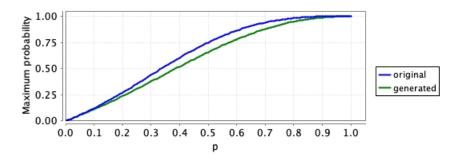


Figure 2 Probability that the nodes 1 and 2 are connected.

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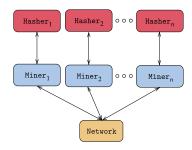
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2.3 Proof of Work Bitcoin Protocol

In [2], the authors decided to extend the PRISM model checker with dynamic data types in order to model the Proof of Work protocol implemented in the Bitcoin blockchain [6].

The Bitcoin system is the result of the parallel composition of n Miner processes, n Hasher processes and a process called Network. In particular:

- The *Miner* processes model the blockchain mainers that create new blocks and add them to their local ledger;
- the *Hasher* processes model the attempts of the miners to solve the cryptopuzzle;
- the Network process model the broadcast communication among miners.



Since we are not interested in the properties obtained by analyzing the protocol, we decided to consider n = 4 miner and hasher processes; the model can be found in Listing 5.

```
218
    preamble
219
220
    endpreamble
221
222
    n = 4;
223
224
225
226
227
    PoW := Hasher[i] -> Miner[i] :
228
    (+["mR*hR[i]"] " "\&\&"(b[i]'=createB(b[i],B[i],c[i]))\&(c[i]'=c[i]+1)".
229
           Miner[i] -> Network :
230
                   (["rB*1"] "(B[i]'=addBlock(B[i],b[i]))" &&
231
                   foreach(k != i) "(set[k], addBlockSet(set[k], b[i]))" @Network .PoW)
232
     +["lR*hR[i]"] " " && " " .
233
           if "!isEmpty(set[i])"@Miner[i] then {
234
                   ["r"] "(b[i]'=extractBlock(set[i]))"@Miner[i] .
235
                          Miner[i] -> Network :
236
                          (["1*1"] "(setMiner[i]' = addBlockSet(setMiner[i] , b[i]))"&&
237
                              238
           }
239
           else{
240
                   if "canBeInserted(B[i],b[i])"@Miner[i] then {
241
                          ["1"] "(B[i]'=addBlock(B[i],b[i]))&&(setMiner[i]'=removeBlock
242
                              243
                   }
244
                   else{
245
                          PoW
246
                   }
247
           }
248
249
    }
250
251
```

Listing 5 Choreographic language for the Proof of Work Bitcoin Protocol.

Part of the generated PRISM code is shown in Listing 6, the modules $Miner_2$, $Miner_3$, $Miner_4$ and $Hasher_2$, $Hasher_3$, $Hasher_4$ are equivalent to $Miner_1$ and $Hasher_1$, respectively. Our generated PRISM model is more verbose than the one presented in [2], this is due to the fact that for the if-then-else expression, we always generate the else branch. and this leads to having more instructions

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```
257
258
259
     module Miner1
260
         Miner1 : [0..7] init 0;
         b1 : block {m1,0;genesis,0} ;
262
         B1 : blockchain [{genesis,0;genesis,0}];
263
         c1 : [0..N] init 0;
264
         setMiner1 : list [];
265
266
         [PZKYT] (Miner1=0) \rightarrow hR1 : (b1'=createB(b1,B1,c1))&(c1'=c1+1)&(Miner1'=1);
267
         [EUBVP] (Miner1=0) \rightarrow hR1 : (Miner1'=2);
268
         [HXYKO] (Miner1=1) \rightarrow 1 : (B1'=addBlock(B1,b1))&(Miner1'=0);
269
         \label{eq:miner1} \begin{tabular}{ll} \begin{tabular}{ll} $($Miner1=2)\&!isEmpty(set1)$ $\rightarrow$ $r:(b1'=extractBlock(set1))\&(Miner1'=4)$; \end{tabular}
270
         [SRKSV] (Miner1=4) \rightarrow 1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Miner1'=0)
271
              \hookrightarrow ;
272
         [] (Miner1=2)\&!(!isEmpty(set1)) \rightarrow 1 : (Miner1'=5);
         [] (Miner1=5)\&canBeInserted(B1,b1) \rightarrow 1 : (B1'=addBlock(B1,b1))\&(setMiner1'=balanceInserted(B1,b1))

    removeBlock(setMiner1,b1))&(Miner1'=0);
275
         [] (Miner1=5)&!(canBeInserted(B1,b1)) \rightarrow 1 : (Miner1'=0);
276
277
     endmodule
278
279
     module Network
280
     Network : [0..1] init 0;
281
         set1 : list [];
282
         [HXYK0] (Network=0) \rightarrow 1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,
              \rightarrow b3))&(set4'=addBlockSet(set4,b4))&(Network'=0);
         [SRKSV] (Network=0) \rightarrow 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
287
288
289
     endmodule
290
291
     module Hasher1
292
     Hasher1 : [0..1] init 0;
293
294
      [PZKYT] (Hasher1=0) \rightarrow mR : (Hasher1'=0);
295
      [EUBVP] (Hasher1=0) \rightarrow 1R : (Hasher1'=0);
296
     endmodule
298
299
```

Listing 6 Generated PRISM program for the Peer-To-Peer Protocol.

However, for this particular test case, the results of the experiments are not affected, as shown Figure 3 where the results are compared. In this example, since we are comparing the results of two simulations, the two probabilities are slightly different, but it has nothing to do with the model itself.

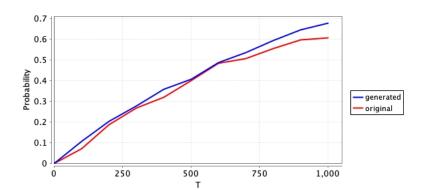
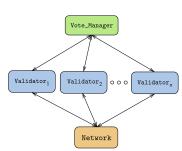


Figure 3 Probability at least one miner has created a block.

2.4 Hybrid Casper Protocol



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The last case we study we present is the Hybrid Casper Protocol modelled in PRISM in [4]. The Hybrid Capser protocol is an hybrid blockchain consenus protocol that includes features of the Proof of Work and the Proof of Stake protocols. It was implemented in the Ethereum blockchain [3] as a testing phase before switching to Proof of Stake protocol.

The approach is very similar to the one used for the Proof of Work Bitcoin protocol, so they model Hybrid Casper in PRISM as the parallel composition of n Validator modules

and the module Vote_Manager and Network. The module Validator is very similar to the module Miner of the previous protocol and the only module that requires an explaination is the Vote_Manager that stores the tables containing the votes for each checkpoint and calculates the rewards/penalties.

The modeling language is reported in Listing 7 while (part of) the generated PRISM code can be found in Listing 8.

```
320
    preamble
321
322
    endpreamble
323
    n = 5;
324
325
     . . .
     ₹
326
    PoS := Validator[i] -> Validator[i] :
327
        (+["mR*1"] "(b[i]'=createB(b[i],L[i],c[i]))\&(c[i]'=c[i]+1)"\&\&" "
328
       if "!(mod(getHeight(b[i]),EpochSize)=0)"@Validator[i] then{
329
          Validator[i] -> Network : (["1*1"] "(L[i]'=addBlock(L[i],b[i]))" && foreach(k
330
              \hookrightarrow !=i) "(set[k]'=addBlockSet(set[k],b[i]))"@Network .PoS)
331
       }
332
       else{
333
          Validator[i] -> Network : (["1*1"] "(L[i]'=addBlock(L[i],b[i]))" && foreach(k
334

→ !=i) "(set[k]'=addBlockSet(set[k],b[i]))"@Network . Validator[i] ->

335

→ Vote_Manager :(["1*1"] " "&&"(Votes'=addVote(Votes,b[i],stake[i]))".PoS

336
              \hookrightarrow ))
337
338
        +["lR*1"] " "&&" " . if "!isEmpty(set[i])"@Validator[i] then {
339
```

```
["1"] "(b[i]'=extractBlock(set[i]))"@Validator[i] .
340
            if "!canBeInserted(L[i],b[i])"@Validator[i] then {
               PoS
342
           }
343
           else{
344
           if "!(mod(getHeight(b[i]),EpochSize)=0)"@Validator[i] then {
345
            Validator[i] -> Network : (["1*1"] "(setMiner[i]' = addBlockSet(setMiner[i])
346
                 \hookrightarrow , b[i]))"&&"(set[i]' = removeBlock(set[i],b[i]))" . PoS)
347
          }
348
          else{
349
            Validator[i] -> Network : (["1*1"] "(setMiner[i]' = addBlockSet(setMiner[i])
350
                 → , b[i]))"&&"(set[i]' = removeBlock(set[i],b[i]))" . Validator[i] ->
                 → Vote_Manager : (["1*1"] " "&&"(Votes'=addVote(Votes,b[i],stake[i]))
352
                 → ".PoS ))
353
          }
354
        }
355
      }
356
      else{PoS}
357
       +["rC*1"] "(lastCheck[i]'=extractCheckpoint(listCheckpoints[i],lastCheck[i]))&(
358
            → heightLast[i] '=getHeight(extractCheckpoint(listCheckpoints[i],lastCheck[i
359
            \hookrightarrow \texttt{])))\&(votes[i]'=calcVotes(Votes,extractCheckpoint(listCheckpoints[i],extractCheckpoints[i])))}
360
            → lastCheck[i])))"&&" " .
361
          if "(heightLast[i]=heightCheckpoint[i]+EpochSize)&(votes[i]>=2/3*tot_stake)"
362

→ @Validator[i] then{
36
            if "(heightLast[i]=heightCheckpoint[i]+EpochSize)"@Validator[i] then{
36
              ["1"] "(lastJ[i]'=b[i])&(L[i]'= updateHF(L[i],lastJ[i]))" @Validator[i].
365
                   → Validator[i]->Vote_Manager :(["1*1"]" "&&"(epoch'=height(lastF(L[i
366
                  → ]))&(Stakes'=addVote(Votes,b[i],stake[i]))".PoS)
367
368
           else{["1"] "(lastJ[i]'=b[i])"@Validator[i] . PoS}
369
370
          else{PoS}
371
372
    }
373
374
```

Listing 7 Choreographic language for the Hybrid Casper Protocol.

```
375
     module Validator1
376
377
378
        [] (Validator1=0) \rightarrow mR : (b1'=createB(b1,L1,c1))&(c1'=c1+1)&(Validator1'=1);
379
        [] (Validator1=0) \rightarrow 1R : (Validator1'=2);
380
        [] (Validator1=0)&(!isEmpty(listCheckpoints1)) \rightarrow
381
             rC : (lastCheck1'=extractCheckpoint(listCheckpoints1,lastCheck1))&(
382

→ heightLast1'=getHeight(extractCheckpoint(listCheckpoints1,lastCheck1))
383
                  → )))&(votes1'=calcVotes(Votes,extractCheckpoint(listCheckpoints1,
38

    lastCheck1)))&(Validator1'=3);
385
        [NGRDF] (Validator1=1)&!(mod(getHeight(b1), EpochSize)=0) \rightarrow 1 : (L1'=addBlock(
386
             \hookrightarrow L1,b1))&(Validator1'=0);
387
        [] (Validator1=1)\&!(!(mod(getHeight(b1),EpochSize)=0)) \rightarrow 1 : (Validator1'=3);
388
        [PCRLD] (Validator1=1)&!(mod(getHeight(b1),EpochSize)=0) \rightarrow
389
             1 : (L1'=addBlock(L1,b1))&(Validator1'=4);
390
        [VSJBE] (Validator1=5) \rightarrow 1 : (Validator1'=0);
391
        [] (Validator1=2)&!isEmpty(set1) \rightarrow
392
```

```
1 : (b1'=extractBlock(set1))&(Validator1'=4);
393
        [] (Validator1=4)&!canBeInserted(L1,b1) \rightarrow (Validator1'=0);
        [] (Validator1=4)&!(!canBeInserted(L1,b1)) \rightarrow 1 : (Validator1'=6);
395
        [MDDCF] (Validator1=6)&!(mod(getHeight(b1),EpochSize)=0) \rightarrow
396
             1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=0);
397
        [] (Validator1=6)&!(!(mod(getHeight(b1),EpochSize)=0)) → 1 : (Validator1'=8);
398
        [IQVPA] (Validator1=6)&!(mod(getHeight(b1),EpochSize)=0) \rightarrow
399
             1 : (setMiner1' = addBlockSet(setMiner1 , b1))&(Validator1'=9);
400
        [IFNVZ] (Validator1=10) \rightarrow 1 : (Validator1'=0);
401
        [] (Validator1=2)&!(!isEmpty(set1)) \rightarrow 1 : (Validator1'=0);
402
        [] (Validator1=3)&(heightLast1=heightCheckpoint1+EpochSize)&(votes1>=2/3*
403
             \hookrightarrow tot_stake) \rightarrow (Validator1'=4);
404
        [] (Validator1=4)&(heightLast1=heightCheckpoint1+EpochSize) \rightarrow
405
             1 : (lastJ1'=b1)&(L1'= updateHF(L1,lastJ1))&(Validator1'=6);
406
        [EQCYO] (Validator1=6) \rightarrow 1 : (Validator1'=0);
407
        [] (Validator1=4)&!((heightLast1=heightCheckpoint1+EpochSize)) \rightarrow
408
             1 : (lastJ1'=b1)&(Validator1'=0);
409
        [] (Validator1=3)&!((heightLast1=heightCheckpoint1+EpochSize)&(votes1>=2/3*
410
             \hookrightarrow tot_stake)) \rightarrow 1 : (Validator1'=0);
411
     endmodule
412
413
    module Network
414
        Network : [0..1] init 0;
415
        set1 : list [];
416
        set2 : list [];
417
        set3 : list [];
418
        set4 : list [];
419
        set5 : list [];
420
421
        [NGRDF] (Network=0) \rightarrow
422
             1: (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(set4'=
423
                  \hookrightarrow addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&(Network'=0);
424
        [PCRLD] (Network=0) \rightarrow
425
             1 : (set2'=addBlockSet(set2,b2))&(set3'=addBlockSet(set3,b3))&(set4'=
426
                  \hookrightarrow addBlockSet(set4,b4))&(set5'=addBlockSet(set5,b5))&(Network'=0);
427
        [MDDCF] (Network=0) \rightarrow 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
        [IQVPA] (Network=0) \rightarrow 1 : (set1' = removeBlock(set1,b1))&(Network'=0);
430
     endmodule
431
432
    module Vote_Manager
433
        Vote Manager : [0..1] init 0;
434
        epoch : [0..10] init 0;
435
        Votes : hash[];
436
        tot_stake : [0..120000] init 50;
437
        stake1 : [0..N] init 10;
438
        stake2 : [0..N] init 10;
439
        stake3 : [0..N] init 10;
440
        stake4 : [0..N] init 10;
441
        stake5 : [0..N] init 10;
442
443
        [VSJBE] (Vote_Manager=0) \rightarrow
444
             1 : (Votes'=addVote(Votes,b1,stake1))&(Vote_Manager'=0);
445
446
     endmodule
447
```

448

451

453

458

459

460

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462

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465

466

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469

471

Listing 8 Generated PRISM program for the Hybrid Casper Protocol.

The code is very similar to the one presented in [4], the main difference is the fact that our generated model has more lines of code. This is due to the fact that there are some commands that can be merged, but the compiler is not able to do it automatically. This discrepancy between the two models can be observed also in the simulations, reported in Figure 4. Although the results are similar, PRISM takes 39.016 seconds to run the simulations for the generated model, instead of 22.051 seconds needed for the original model.

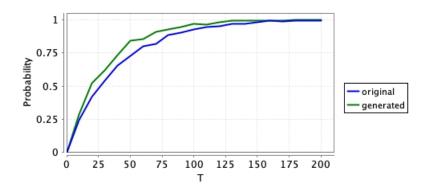


Figure 4 Probability that a block has been created.

2.5 Problems

While testing our choreographic language, we noticed that some of the case studies presented in the PRISM documentation [1] cannot be modeled by using our language. The reasons are various, in this section we try to outline the problems.

- Asynchronous Leader Election⁵: processes synchronize with the same label but the conditions are different. We include in our language the it-then-else statement but we do not allow the if-then (without the else). This is done because in this way, we do not incur in deadlock states.
- Probabilistic Broadcast Protocols⁶: also in this case, the problem are the labels of the synchronizations. In fact, all the processes synchronize with the same label on every actions. This is not possible in our language, since a label is unique for every synchronization between two (or more) processes.
- **Cyclic Server Polling System**⁷: in this model, the processes $\mathtt{station}_i$ do two different things in the same state. More precicely, at the state 0 (\mathtt{s}_i =0), the processes may synchronize with the process \mathtt{server} or may change their state without any synchronization. In out language, this cannot be formalized since the synchronization is a branch action, so there should be another option with a synchronization.

https://www.prismmodelchecker.org/casestudies/asynchronous_leader.php

 $^{^6}$ https://www.prismmodelchecker.org/casestudies/prob_broadcast.php

https://www.prismmodelchecker.org/casestudies/polling.php

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