# The Mandelbrot Set Hybrid MPI/OpenMP Implementation

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May 2024

#### Introduction

The goal is to implement and analyze a **hybrid MPI/OpenMP** implementation of the computation of the Mandelbrot set, which is defined as:

$$\mathcal{M} = \{c \in \mathbb{C} : \lim_{n \to \infty} z_n < \infty\}$$

where 
$$z_{n+1} = z_n^2 + c$$
 and  $z_0 = 0$ .

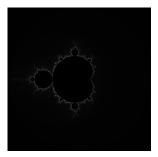


Figure: Rendering of the Mandelbrot set.

#### Encoding:

- each pixel represents a complex number c.
- the color of the pixel depends on the number of iterations before z<sub>n</sub> diverges.

## Computational architecture

## ORFEO cluster EPYC paritition

- ▶ 8 nodes
- 2x AMD EPYC 7742 64-Core Processor on each node
- ▶ 512 GB RAM

For our purposes we will use at most 2 nodes of the EPYC partition.

# Parallelization strategy

### We adopt a sequential fashion:

- using MPI, initialize P processes
- each process computes a portion of the image using T OpenMP threads (loop scheduling policy is set to dynamic)
- the master process uses MPI\_Gatherv to collect the results



Figure: Suppose to have 4 processes. Each process will compute a portion of the image.

Let  $N = n_x \times n_y$  be the total number of pixels. Each process will compute approximately N/P pixels.

## Experimental setup

#### MPI scaling

Set 
$$T = 1$$
 and vary  $P = 1, 2, 4, 8, \dots, 112, 128$ 

strong scaling:

$$n_{\rm x}=n_{\rm y}=4096$$

weak scaling:

$$\textit{n}_{x} = \textit{n}_{y} = 1024 \times \texttt{round}\{\sqrt{\textit{P}}\}$$

## OpenMP scaling

Set 
$$P = 1$$
 and vary  $T = 2, 4, 6, 8, \dots, 62, 64$ 

strong scaling:

$$n_{x}=n_{y}=4096$$

weak scaling:

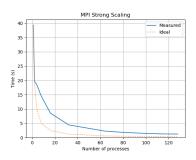
$$n_x = n_y = 1024 \times \text{round}\{\sqrt{T}\}$$

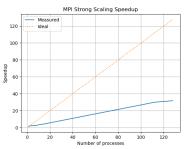


## Other parameters

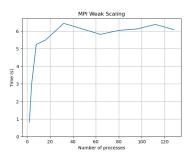
- ► For MPI, we set --map-by core and --bind-to socket
- For OpenMP, we set OMP\_PLACES=cores and no binding policy.

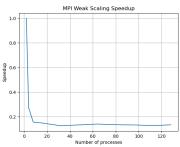
## MPI **strong** scaling results



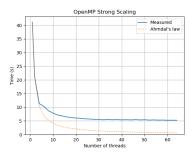


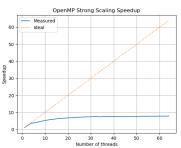
## MPI weak scaling results





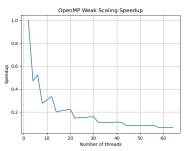
# OpenMP **strong** scaling results





# OpenMP weak scaling results





## Conclusions

- MPI scaling shows an expected behavior for both strong and weak scaling
- OpenMP strong scaling shows that we reach a bottleneck

#### OpenMP issues:

- load imbalance
- false sharing

#### Improvements:

- smarter load balancing strategy
- exploit symmetries
- exploit compiler optimizations