

```
!unzip archive.zip -d archive
```

```
Archive:  archive.zip  
replace archive/README? [y]es, [n]o, [A]ll, [N]one, [r]ename: N
```

```
!pip3 install numpy  
!pip3 install pillow  
!pip3 install scikit-learn  
!pip3 install matplotlib
```

```
Requirement already satisfied: numpy in /usr/local/lib/python3.10/dist-packages (1.23.5)  
Requirement already satisfied: pillow in /usr/local/lib/python3.10/dist-packages (9.4.0)  
Requirement already satisfied: scikit-learn in /usr/local/lib/python3.10/dist-packages (1.2.2)  
Requirement already satisfied: numpy>=1.17.3 in /usr/local/lib/python3.10/dist-packages (from scikit-learn==1.2.2) (1.23.5)  
Requirement already satisfied: scipy>=1.3.2 in /usr/local/lib/python3.10/dist-packages (from scikit-learn==1.2.2) (1.10.1)  
Requirement already satisfied: joblib>=1.1.1 in /usr/local/lib/python3.10/dist-packages (from scikit-learn==1.2.2) (1.3.2)  
Requirement already satisfied: threadpoolctl>=2.0.0 in /usr/local/lib/python3.10/dist-packages (from scikit-learn==1.2.2) (3.2.0)  
Requirement already satisfied: matplotlib in /usr/local/lib/python3.10/dist-packages (3.7.1)  
Requirement already satisfied: contourpy>=1.0.1 in /usr/local/lib/python3.10/dist-packages (from matplotlib==3.7.1) (1.0.7)  
Requirement already satisfied: cycler>=0.10 in /usr/local/lib/python3.10/dist-packages (from matplotlib==3.7.1) (0.12.1)  
Requirement already satisfied: fonttools>=4.22.0 in /usr/local/lib/python3.10/dist-packages (from matplotlib==3.7.1) (4.22.0)  
Requirement already satisfied: kiwisolver>=1.0.1 in /usr/local/lib/python3.10/dist-packages (from matplotlib==3.7.1) (1.4.5)  
Requirement already satisfied: numpy>=1.20 in /usr/local/lib/python3.10/dist-packages (from matplotlib==3.7.1) (1.23.5)  
Requirement already satisfied: packaging>=20.0 in /usr/local/lib/python3.10/dist-packages (from matplotlib==3.7.1) (23.1)  
Requirement already satisfied: pillow>=6.2.0 in /usr/local/lib/python3.10/dist-packages (from pillow==9.4.0) (9.4.0)  
Requirement already satisfied: pyparsing>=2.3.1 in /usr/local/lib/python3.10/dist-packages (from pillow==9.4.0) (3.1.0)  
Requirement already satisfied: python-dateutil>=2.7 in /usr/local/lib/python3.10/dist-packages (from pillow==9.4.0) (2.8.2)  
Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.10/dist-packages (from pillow==9.4.0) (1.16.0)
```

```
import numpy as np  
import os  
from PIL import Image  
from sklearn.neighbors import KNeighborsClassifier  
from sklearn.metrics import accuracy_score  
import matplotlib.pyplot as plt  
  
# lists for storing the data matrix D and label vector y  
D = []  
y = []  
  
# 2) Generate the Data Matrix and the Label vector  
for subject in range(1, 41):  
    # every subject has 10 images, get 10 images per subject  
    imageCount = 0  
  
    for image in os.listdir(f'archive/s{subject}'):   
        temp = Image.open(f'archive/s{subject}/{image}')  
        vector = np.array(temp).flatten()  
  
        y.append(subject)  
        D.append(vector)  
  
# convert the dataMatrix and labels to numpy arrays  
D = np.array(D)  
y = np.array(y)
```

```
# 3) Split the data-set into Training and Test sets
```

```

training_data = D[:, :2]
testing_data = D[1::2]

training_labels = y[:, :2]
testing_labels = y[1::2]

# 4) Classification using PCA
# Calculate Projection Matrix U
training_mean = np.mean(training_data, axis=0)
training_std = np.std(training_data, axis=0)
training_standardized = (training_data - training_mean) / training_std

covariance_matrix = np.cov(training_standardized.T)
eigenvalues, eigenvectors = np.linalg.eig(covariance_matrix)
eigenvalues = eigenvalues.real
eigenvectors = eigenvectors.real

# index to sort the eigen values and eigen vectors in decreasing order of eigen values
idx = np.argsort(eigenvalues)[::-1]
sorted_eigenvalues = eigenvalues[idx]
sorted_eigenvectors = eigenvectors[:, idx]

# sum to get the variance fraction to choose how many dimension aka how many eigen vectors
cumulative_sum = np.cumsum(sorted_eigenvalues)

# alpha=[0.8,0.85,0.9,0.95]    loop on the array and mark accuracy
alphas = [0.8, 0.85, 0.9, 0.95] # for example

for alpha in alphas:
    num_eigenvectors = np.where(cumulative_sum >= alpha)[0][0] + 1
    # final eigen vectors chosen for projection
    U = sorted_eigenvectors[:, :num_eigenvectors]

    # project all the data on the eigen vectors
    D_train_pca = np.dot(training_data, U)
    D_test_pca = np.dot(testing_data, U)

    # training: fitting the points on the graph so the classifier can classify any new testing point
    # 5) Classifier Tuning
    knn_nums = [1, 3, 5, 7]
    accuracies = []
    for knn_num in knn_nums:
        knn = KNeighborsClassifier(n_neighbors=knn_num, weights='distance')
        knn.fit(D_train_pca, training_labels)

        # testing
        predicted_labels = knn.predict(D_test_pca)

        # accuracy
        accuracy = accuracy_score(testing_labels, predicted_labels)
        accuracies.append(accuracy)
        print(f'Accuracy of alpha={alpha}, K={knn_num}: {accuracy}')
```

```

plt.plot(knn_nums, accuracies)
plt.xlabel('Number of Neighbors (K)')
plt.ylabel(f'Accuracy of alpha={alpha}')

```

```
plt.title(f'Accuracy vs. Number of Neighbors for alpha={alpha}')  
plt.show()
```

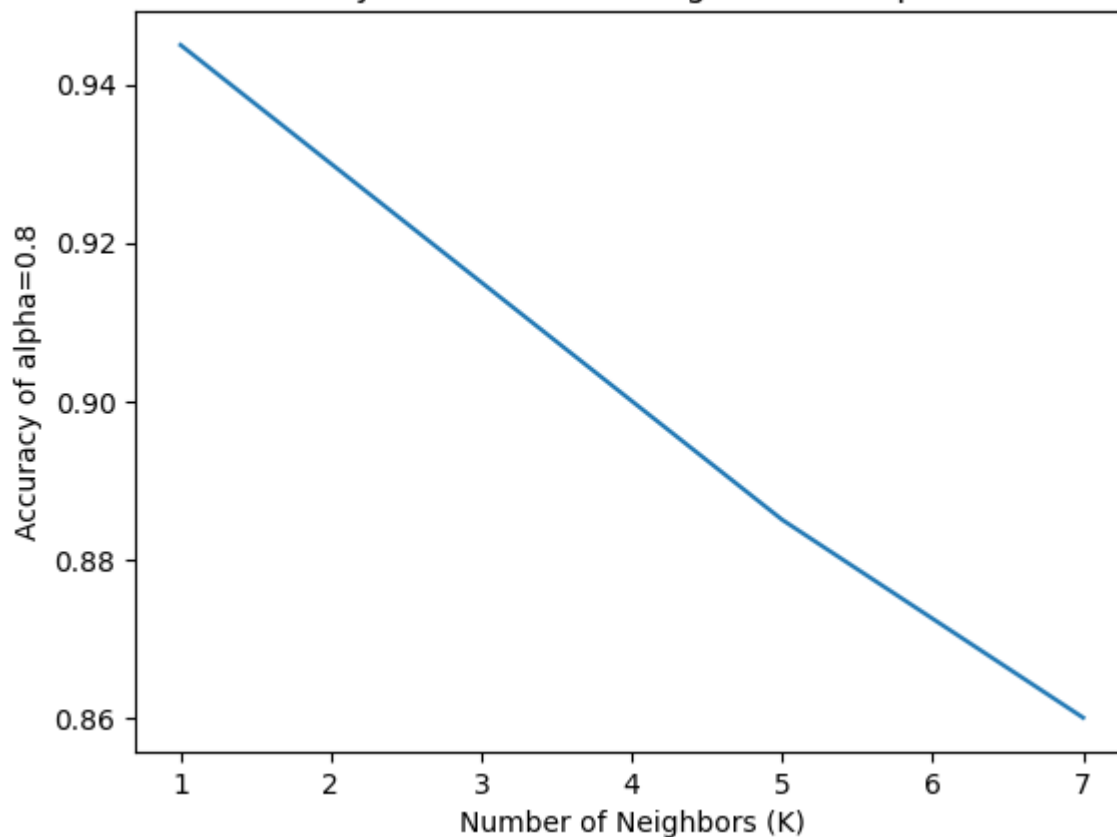
Accuracy of $\alpha=0.8$, $K=1$: 0.945

Accuracy of $\alpha=0.8$, $K=3$: 0.915

Accuracy of $\alpha=0.8$, $K=5$: 0.885

Accuracy of $\alpha=0.8$, $K=7$: 0.86

Accuracy vs. Number of Neighbors for $\alpha=0.8$



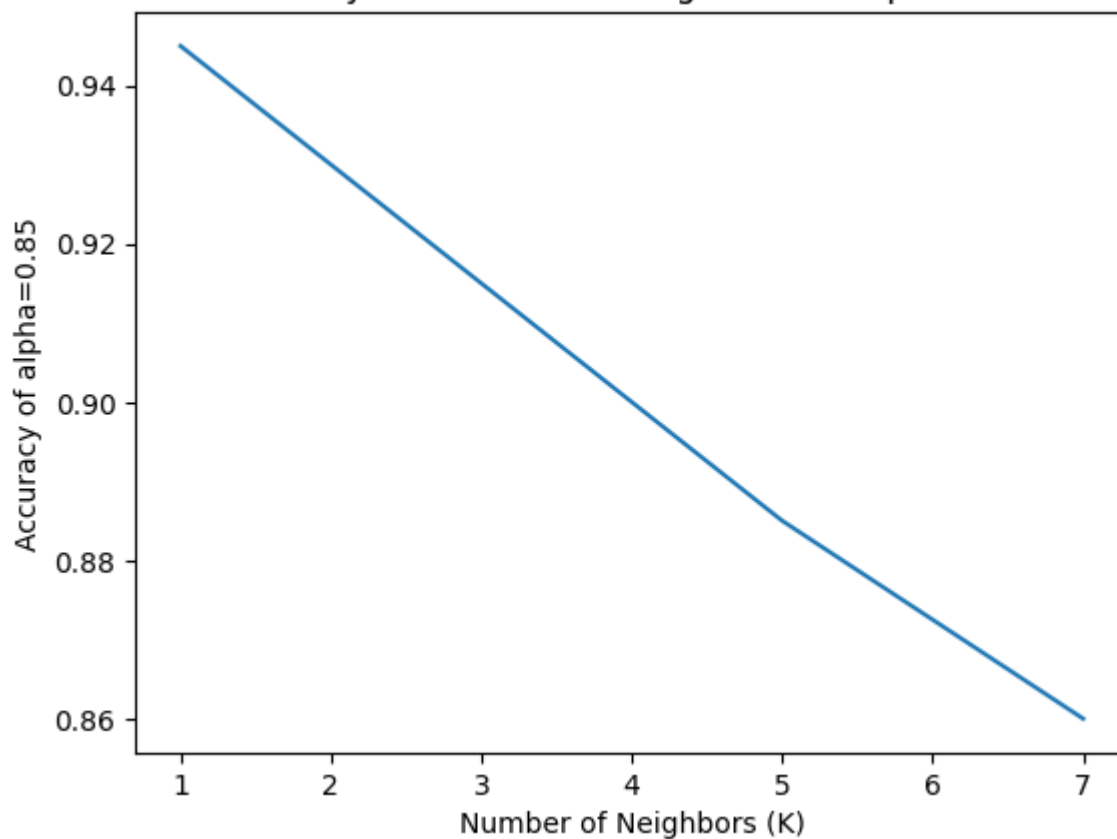
Accuracy of $\alpha=0.85$, $K=1$: 0.945

Accuracy of $\alpha=0.85$, $K=3$: 0.915

Accuracy of $\alpha=0.85$, $K=5$: 0.885

Accuracy of $\alpha=0.85$, $K=7$: 0.86

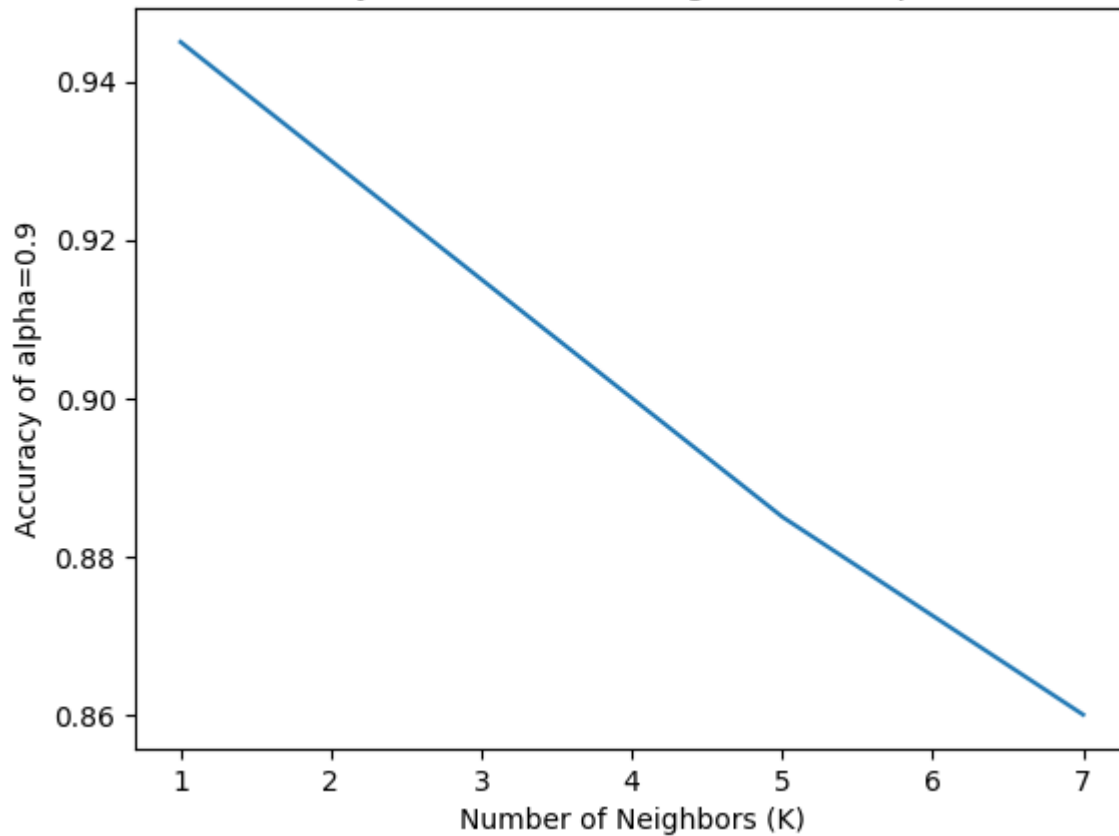
Accuracy vs. Number of Neighbors for $\alpha=0.85$



Accuracy of $\alpha=0.9$, $K=1$: 0.945

Accuracy of $\alpha=0.9$, $K=3$: 0.915
Accuracy of $\alpha=0.9$, $K=5$: 0.885
Accuracy of $\alpha=0.9$, $K=7$: 0.86

Accuracy vs. Number of Neighbors for $\alpha=0.9$



Accuracy of $\alpha=0.95$, $K=1$: 0.945
Accuracy of $\alpha=0.95$, $K=3$: 0.915
Accuracy of $\alpha=0.95$, $K=5$: 0.885
Accuracy of $\alpha=0.95$, $K=7$: 0.86

Accuracy vs. Number of Neighbors for $\alpha=0.95$

