

# 微分方程

## Exercise Miscellaneous (Chapter 2)

1. In each exercise, find a set of solutions, unless the statement of the exercise stipulates otherwise.

3.  $(3xy + 3y - 4) dx + (x + 1)^2 dy = 0$ .

7.  $y' = x^3 - 2xy$ ; when  $x = 1$ ,  $y = 2$ .

11.  $(1 + x^2)y' = x^4y^4$ .

15.  $xy(dx - dy) = x^2 dy + y^2 dx$ .

19.  $(x^3 + y^3) dx + y^2(3x + ky) dy = 0$ ;  $k$  a constant.

23.  $y' + ay = b$ ;  $a$  and  $b$  constants. Solve by two methods.

27.  $(2y \cos x + \sin^4 x) dx = \sin x dy$ ; when  $x = \frac{1}{2}\pi$ ,  $y = 1$ .

37.  $y' = y \tan x + \cos x$ .

41.  $y = \sec x - y \tan x$ .

45.  $y dx = (3x + y^3 - y^2) dy$ ; when  $x = 1$ ,  $y = -1$ .

49. Find that solution of  $y' = 3x + y$  which passes through the point  $(-1, 0)$ .

53.  $(3x^4y - 1) dx + x^5 dy = 0$ ; when  $x = 1$ ,  $y = 1$ .