Financial Derivatives Lecture 5: Option trading strategies



Douglas Chung

National Chengchi University

1 Option strategies

In this notebook, we will demonstrate how to use Python to construct payoff diagrams for option strategies. We need the numpy package for a few useful mathematical functions, the matplotlib package for plotting payoff diagrams, and the scipy package for statistical distributions.

```
[2]: import numpy as np
import matplotlib.pyplot as plt
from scipy import stats
```

1.1 Specify option payoffs

In this section, we need to specify payoff functions for options using Python function (def).

```
[3]: def call_payoff(S, K):
    payoff = np.maximum(S - K, 0)
    return payoff

def put_payoff(S, K):
    payoff = np.maximum(K - S, 0)
    return payoff

def digital_call_payoff(S, K):
    payoff = 1*(S>K)
    return payoff

def digital_put_payoff(S, K):
    payoff = 1*(S<K)
    return payoff</pre>
```

```
def risk_free_payoff(S, P):
   payoff = [P] * len(S)
   return payoff
```

1.2 Black-Scholes model

 \rightarrow cdf(-d1,0.0,1.0) return Put

To estimate the profit and loss, we also have to specify the Black-Scholes option pricing model.

```
C_{t} = S\mathcal{N}(d_{1}) - K \exp^{-rt} \mathcal{N}(d_{2})
P_{t} = K \exp^{-rt} \mathcal{N}(-d_{2}) - S\mathcal{N}(-d_{1})
d_{1} = \frac{\ln(\frac{S}{K}) + (r + \frac{1}{2}\sigma^{2})t}{\sigma\sqrt{t}}
d_{2} = d_{1} - \sigma\sqrt{t}
[4]: \det BS_{-} \text{call}(S, K, r, t, Sigma): \\ d_{1} = (\text{np.log}(S/K) + (r + 0.5 * Sigma**2)*t)/(Sigma * \text{np.sqrt}(t))
d_{2} = d_{1} - Sigma * \text{np.sqrt}(t)
Call = S * \text{stats.norm.cdf}(d_{1}, 0.0, 1.0) - K * \text{np.exp}(-r*t) * \text{stats.norm.}
\Rightarrow \text{cdf}(d_{2}, 0.0, 1.0)
\text{return Call}
\det BS_{-} \text{put}(S, K, r, t, Sigma): \\ d_{1} = (\text{np.log}(S/K) + (r + 0.5 * Sigma**2)*t)/(Sigma * \text{np.sqrt}(t))
d_{2} = d_{1} - Sigma * \text{np.sqrt}(t)
\text{Put} = K * \text{np.exp}(-r*t) * \text{stats.norm.cdf}(-d_{2}, 0.0, 1.0) - S * \text{stats.norm.}
```

1.3 Payoff and profit diagram for call option

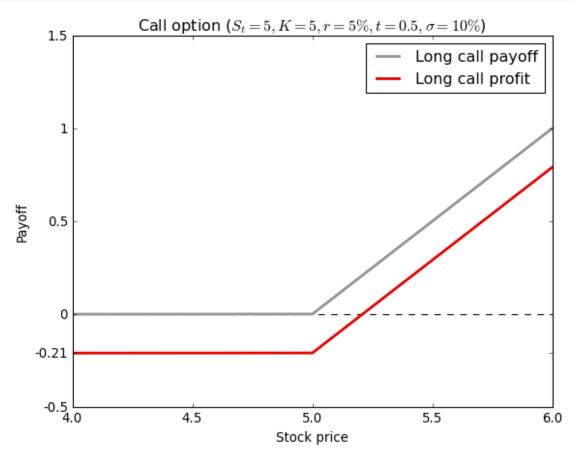
```
[9]: plt.style.use('classic')

S_t = 5
K = 5
r = 0.05
t = 0.5
Sigma = 0.1
Call_price = BS_call(S_t, K, r, t, Sigma)

S = np.linspace(0.0001, S_t*2, 10000, endpoint=True)

fig, ax = plt.subplots()
fig.patch.set_facecolor('white')
plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
plt.title('Call option ($S_t = 5, K = 5, r = 5\%, t = 0.5, \sigma = 10\%$)')
plt.ylabel('Payoff')
```

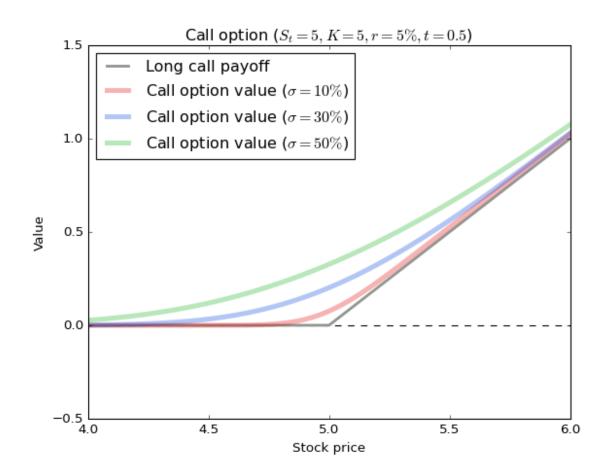




1.4 Volatility and option value

```
[5]: plt.style.use('classic')
     S_t = 5
     K = 5
     r = 0.05
     t = 0.5
     Sigma = 0.1
     Call_price = BS_call(S_t, K, r, t, Sigma)
     S = np.linspace(0.0001, S_t*2, 10000, endpoint=True)
     fig, ax = plt.subplots()
     fig.patch.set_facecolor('white')
     plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
     plt.title('Call option (S_t = 5, K = 5, r = 5\%, t = 0.5$)')
     plt.ylabel('Value')
     plt.xlabel('Stock price')
     plt.plot(S, call_payoff(S, K), color='xkcd:gray', linewidth=2.5)
     plt.plot(S, BS_call(S, K, r, 0.1, Sigma), color='xkcd:red', linewidth=4.5,
     ⇒alpha=0.3)
     plt.plot(S, BS_call(S, K, r, 0.1, 0.3), color='xkcd:blue', linewidth=4.5,
     \rightarrowalpha=0.3)
     plt.plot(S, BS_call(S, K, r, 0.1, 0.5), color='xkcd:green', linewidth=4.5,
     →alpha=0.3)
     plt.xlim(4,6)
     plt.ylim(-0.5, 1.5)
     plt.legend(['Long call payoff', 'Call option value ($\sigma=10\\%$)', 'Call_\_
     'Call option value ($\sigma=50\\\$)'], loc='best')
     #plt.savefig('call_vola.png', bbox_inches="tight", dpi=600)
     plt.show()
```





1.5 Time to maturity and option value

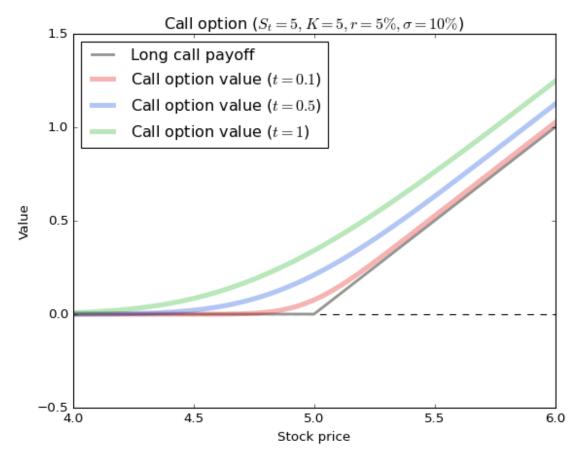
```
[6]: plt.style.use('classic')

S_t = 5
K = 5
r = 0.05
t = 0.5
Sigma = 0.1
Call_price = BS_call(S_t, K, r, t, Sigma)

S = np.linspace(0.0001, S_t*2, 10000, endpoint=True)

fig, ax = plt.subplots()
fig.patch.set_facecolor('white')
plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
plt.title('Call option ($S_t = 5, K = 5, r = 5\%, \sigma = 10\%$)')
plt.ylabel('Value')
plt.xlabel('Stock price')
```

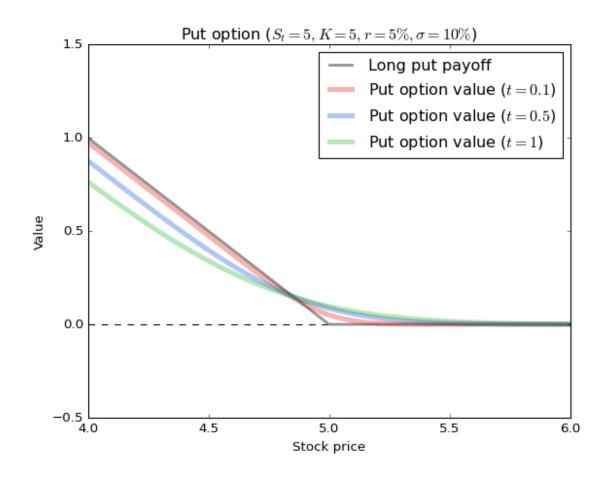






```
[7]: plt.style.use('classic')
     S_t = 5
     K = 5
     r = 0.05
     t = 0.5
     Sigma = 0.1
     S = np.linspace(0.0001, S_t*2, 10000, endpoint=True)
     fig, ax = plt.subplots()
     fig.patch.set_facecolor('white')
     plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
     plt.title('Put option (S_t = 5, K = 5, r = 5\%, \sigma = 10\%$)')
     plt.ylabel('Value')
     plt.xlabel('Stock price')
     plt.plot(S, put_payoff(S, K), color='xkcd:gray', linewidth=2.5)
     plt.plot(S, BS_put(S, K, r, 0.1, Sigma), color='xkcd:red', linewidth=4.5,_
     \rightarrowalpha=0.3)
     plt.plot(S, BS_put(S, K, r, 0.5, Sigma), color='xkcd:blue', linewidth=4.5,_
     \rightarrowalpha=0.3)
     plt.plot(S, BS_put(S, K, r, 1, Sigma), color='xkcd:green', linewidth=4.5,__
      ⇒alpha=0.3)
     plt.xlim(4,6)
     plt.ylim(-0.5, 1.5)
     plt.legend(['Long put payoff', 'Put option value ($t=0.1$)', 'Put option value⊔
     \hookrightarrow ($t=0.5$)',
                 'Put option value ($t=1$)'], loc='best')
     #plt.savefig('put_ttm.png', bbox_inches="tight", dpi=600)
     plt.show()
```





1.6 Covered calls

```
[8]: plt.style.use('classic')

S = 5
S = np.linspace(0, S*2, 10000, endpoint=True)

fig, ax = plt.subplots()
fig.patch.set_facecolor('white')
plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
plt.title('Covered call')
plt.ylabel('Payoff/Profit')
plt.xlabel('Payoff/Profit')
plt.xlabel('Stock price')

Payoff = S - call_payoff(S, 5)
plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)

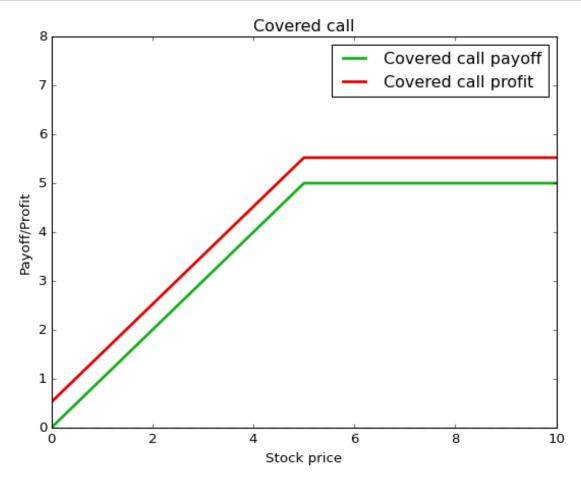
S_t = 5
r = 0.05
```



```
t = 1
Sigma = 0.2

Cost = -BS_call(S_t, 5, r, t, Sigma)
plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)

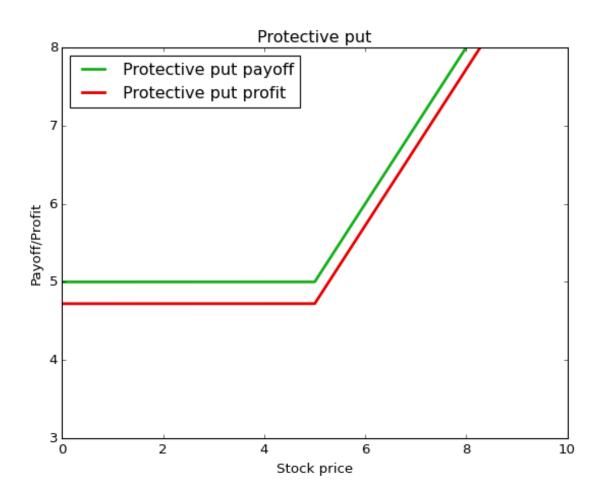
plt.xlim(0,10)
plt.ylim(0,8)
plt.legend(['Covered call payoff', 'Covered call profit'], loc='best')
#plt.savefig('Covered_call.png', bbox_inches="tight", dpi=600)
plt.show()
```



1.7 Protective puts

```
[9]: plt.style.use('classic')
     S = 5
     S = np.linspace(0, S*2, 10000, endpoint=True)
     fig, ax = plt.subplots()
     fig.patch.set_facecolor('white')
     plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
     plt.title('Protective put')
     plt.ylabel('Payoff/Profit')
     plt.xlabel('Stock price')
     Payoff = S + put_payoff(S, 5)
     plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
     S_t = 5
     r = 0.05
     t = 1
     Sigma = 0.2
     Cost = BS_put(S_t, 5, r, t, Sigma)
     plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
     plt.xlim(0,10)
     plt.ylim(3,8)
     plt.legend(['Protective put payoff', 'Protective put profit'], loc='best')
     #plt.savefig('Protective_put.png', bbox_inches="tight", dpi=600)
     plt.show()
```



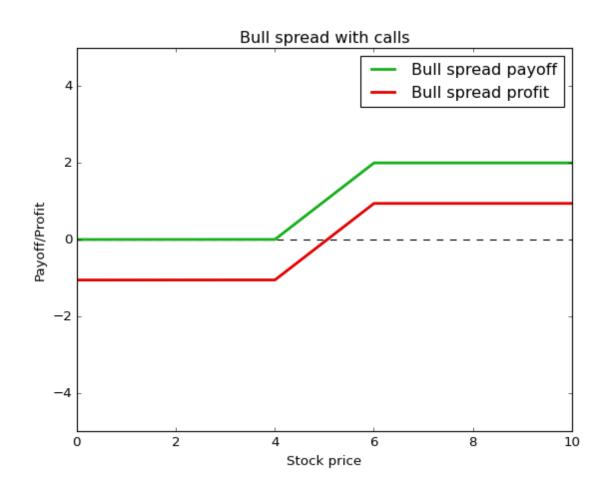




1.8 Bull spread with calls

```
[10]: plt.style.use('classic')
      S = 5
      S = np.linspace(0, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Bull spread with calls')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      Payoff = call_payoff(S, 4) - call_payoff(S, 6)
      plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      S_t = 5
      r = 0.05
      t = 0.5
      Sigma = 0.2
      Cost = BS_call(S_t, 4, r, t, Sigma) - BS_call(S_t, 6, r, t, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Bull spread payoff', 'Bull spread profit'], loc='best')
      #plt.savefig('Bull_spread_call.png', bbox_inches="tight", dpi=600)
      plt.show()
```





1.9 Bull spread with puts

```
[11]: plt.style.use('classic')

S = 5

S = np.linspace(0, S*2, 10000, endpoint=True)

fig, ax = plt.subplots()
  fig.patch.set_facecolor('white')
  plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
  plt.title('Bull spread with puts')
  plt.ylabel('Payoff/Profit')
  plt.xlabel('Stock price')

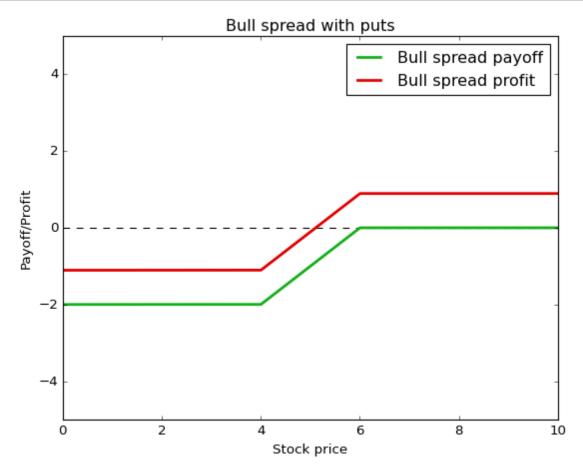
Payoff = put_payoff(S, 4) - put_payoff(S, 6)
  plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
```



```
S_t = 5
r = 0.05
t = 0.5
Sigma = 0.2

Cost = BS_put(S_t, 4, r, t, Sigma) - BS_put(S_t, 6, r, t, Sigma)
plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)

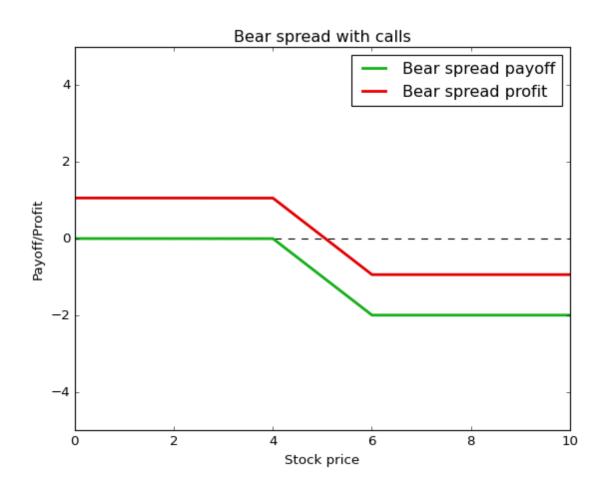
plt.xlim(0,10)
plt.ylim(-5,5)
plt.legend(['Bull spread payoff', 'Bull spread profit'], loc='best')
#plt.savefig('Bull_spread_put.png', bbox_inches="tight", dpi=600)
plt.show()
```



1.10 Bear spread with calls

```
[12]: plt.style.use('classic')
      S = 5
      S = np.linspace(0, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Bear spread with calls')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      Payoff = call_payoff(S, 6) - call_payoff(S, 4)
      plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      S_t = 5
      r = 0.05
      t = 0.5
      Sigma = 0.2
      Cost = BS_call(S_t, 6, r, t, Sigma) - BS_call(S_t, 4, r, t, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Bear spread payoff', 'Bear spread profit'], loc='best')
      #plt.savefig('Bear_spread_call.png', bbox_inches="tight", dpi=600)
      plt.show()
```





1.11 Bear spread with puts

```
[13]: plt.style.use('classic')

S = 5

S = np.linspace(0, S*2, 10000, endpoint=True)

fig, ax = plt.subplots()
  fig.patch.set_facecolor('white')
  plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
  plt.title('Bear spread with puts')
  plt.ylabel('Payoff/Profit')
  plt.xlabel('Stock price')

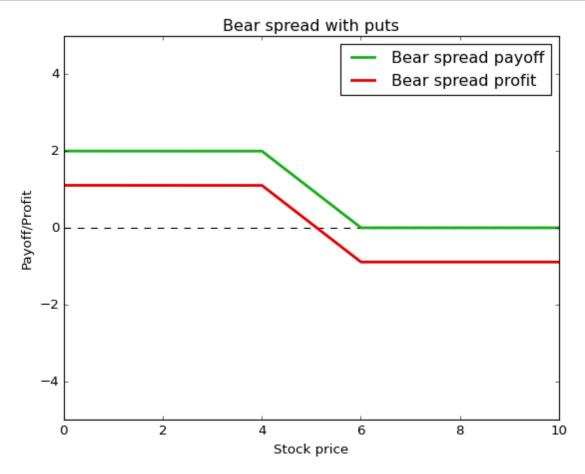
Payoff = put_payoff(S, 6) - put_payoff(S, 4)
  plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
```



```
S_t = 5
r = 0.05
t = 0.5
Sigma = 0.2

Cost = BS_put(S_t, 6, r, t, Sigma) - BS_put(S_t, 4, r, t, Sigma)
plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)

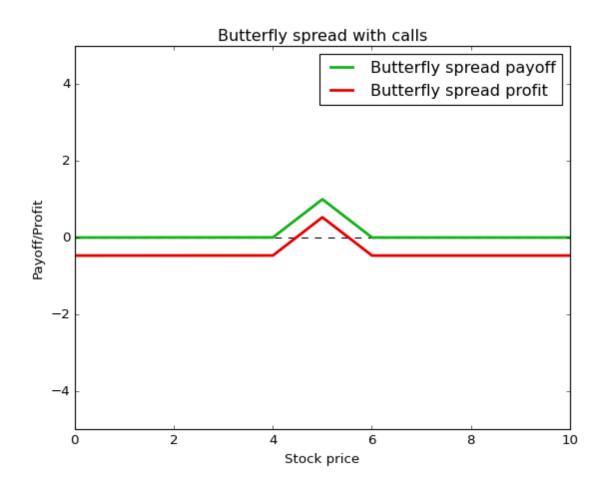
plt.xlim(0,10)
plt.ylim(-5,5)
plt.legend(['Bear spread payoff', 'Bear spread profit'], loc='best')
#plt.savefig('Bear_spread_put.png', bbox_inches="tight", dpi=600)
plt.show()
```



1.12 Butterfly spread with calls

```
[14]: plt.style.use('classic')
      S = 5
      S = np.linspace(0, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Butterfly spread with calls')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      Payoff = call_payoff(S, 4) - 2*call_payoff(S, 5) + call_payoff(S,6)
      plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      S_t = 5
      r = 0.05
      t = 0.5
      Sigma = 0.2
      Cost = BS_call(S_t, 4, r, t, Sigma) - 2*BS_call(S_t, 5, r, t, Sigma) + U
      →BS_call(S_t, 6, r, t, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Butterfly spread payoff', 'Butterfly spread profit'], loc='best')
      #plt.savefig('Butterfly_spread_call.png', bbox_inches="tight", dpi=600)
      plt.show()
```





1.13 Butterfly spread with puts

```
[15]: plt.style.use('classic')

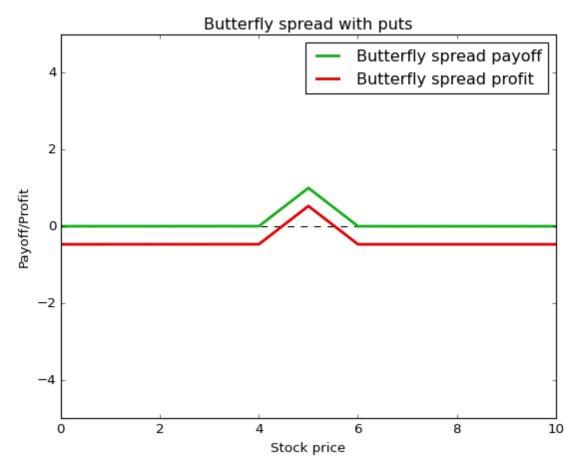
S = 5

S = np.linspace(0, S*2, 10000, endpoint=True)

fig, ax = plt.subplots()
  fig.patch.set_facecolor('white')
  plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
  plt.title('Butterfly spread with puts')
  plt.ylabel('Payoff/Profit')
  plt.xlabel('Stock price')

Payoff = put_payoff(S, 4) - 2*put_payoff(S, 5) + put_payoff(S, 6)
  plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
```

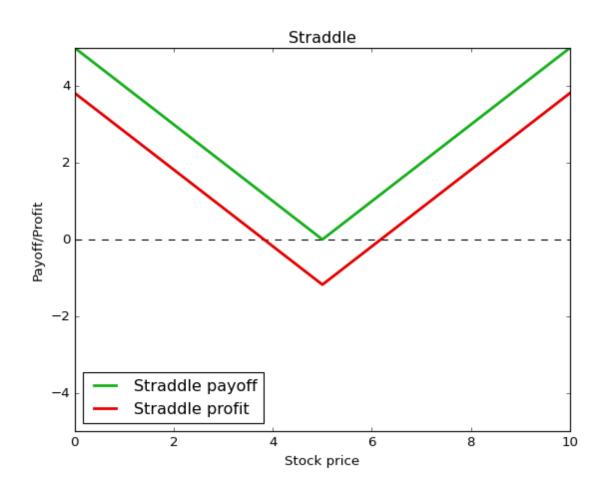




1.14 Straddles

```
[16]: plt.style.use('classic')
      S = 5
      S = np.linspace(0, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Straddle')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      Payoff = call_payoff(S, 5) + put_payoff(S, 5)
      plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      S_t = 5
      r = 0.05
      t = 1
      Sigma = 0.3
      Cost = BS_call(S_t, 5, r, t, Sigma) + BS_put(S_t, 5, r, t, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Straddle payoff', 'Straddle profit'], loc='best')
      #plt.savefig('Straddle.png', bbox_inches="tight", dpi=600)
      plt.show()
```





1.15 Strangles

```
[17]: plt.style.use('classic')

S = 5
S = np.linspace(0, S*2, 10000, endpoint=True)

fig, ax = plt.subplots()
fig.patch.set_facecolor('white')
plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
plt.title('Strangle')
plt.ylabel('Payoff/Profit')
plt.xlabel('Stock price')

Payoff = call_payoff(S, 6) + put_payoff(S, 4)
plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)

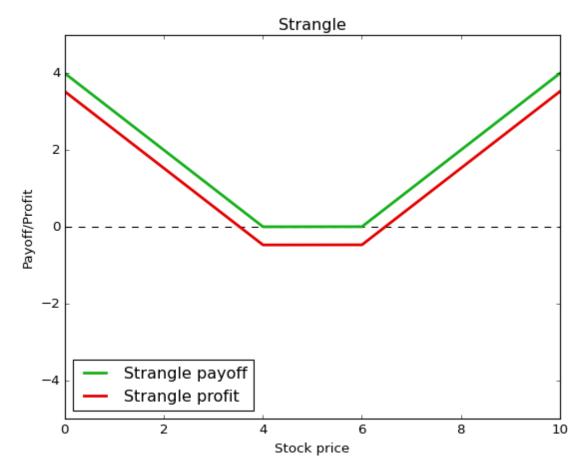
S_t = 5
```



```
r = 0.05
t = 1
Sigma = 0.3

Cost = BS_call(S_t, 6, r, t, Sigma) + BS_put(S_t, 4, r, t, Sigma)
plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)

plt.xlim(0,10)
plt.ylim(-5,5)
plt.legend(['Strangle payoff', 'Strangle profit'], loc='best')
#plt.savefig('Strangle.png', bbox_inches="tight", dpi=600)
plt.show()
```

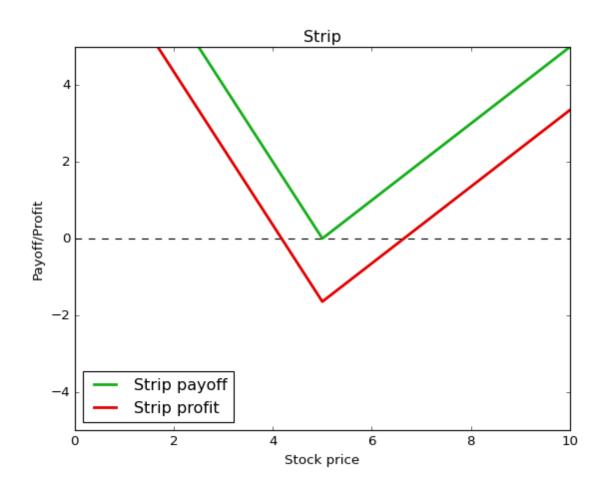




1.16 Strips

```
[18]: plt.style.use('classic')
      S = 5
      S = np.linspace(0, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Strip')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      Payoff = call_payoff(S, 5) + 2*put_payoff(S, 5)
      plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      S_t = 5
      r = 0.05
      t = 1
      Sigma = 0.3
      Cost = BS_call(S_t, 5, r, t, Sigma) + 2*BS_put(S_t, 5, r, t, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Strip payoff', 'Strip profit'], loc='best')
      #plt.savefig('Strip.png', bbox_inches="tight", dpi=600)
      plt.show()
```





1.17 Straps

```
[19]: plt.style.use('classic')

S = 5
S = np.linspace(0, S*2, 10000, endpoint=True)

fig, ax = plt.subplots()
fig.patch.set_facecolor('white')
plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
plt.title('Strap')
plt.ylabel('Payoff/Profit')
plt.xlabel('Stock price')

Payoff = 2*call_payoff(S, 5) + put_payoff(S, 5)
plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)

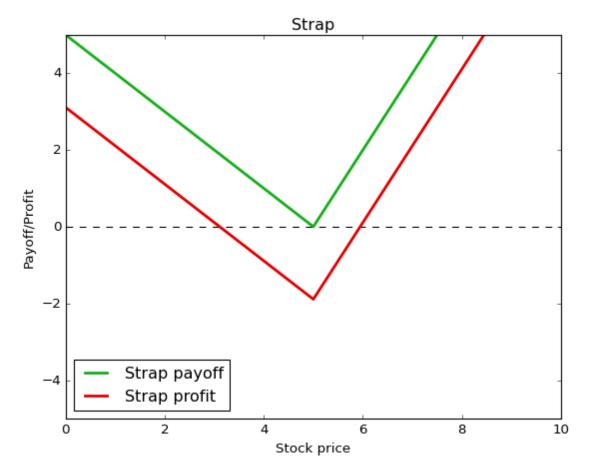
S_t = 5
```



```
r = 0.05
t = 1
Sigma = 0.3

Cost = 2*BS_call(S_t, 5, r, t, Sigma) + BS_put(S_t, 5, r, t, Sigma)
plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)

plt.xlim(0,10)
plt.ylim(-5,5)
plt.legend(['Strap payoff', 'Strap profit'], loc='best')
#plt.savefig('Strip.png', bbox_inches="tight", dpi=600)
plt.show()
```

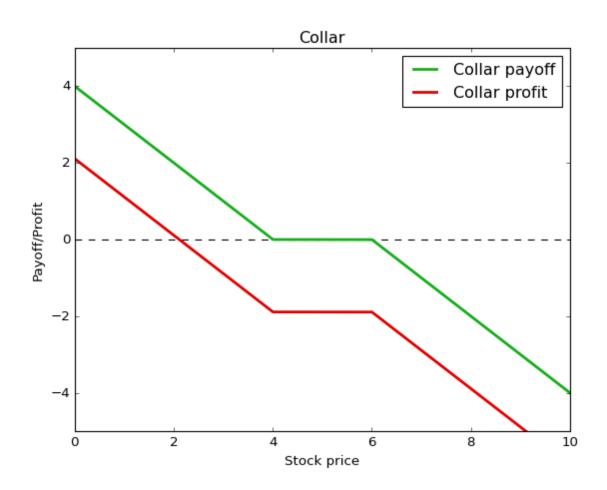




1.18 Collars

```
[20]: plt.style.use('classic')
      S = 5
      S = np.linspace(0, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Collar')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      Payoff = -call_payoff(S, 6) + put_payoff(S, 4)
      plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      S_t = 5
      r = 0.05
      t = 1
      Sigma = 0.3
      Cost = 2*BS_call(S_t, 5, r, t, Sigma) + BS_put(S_t, 5, r, t, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Collar payoff', 'Collar profit'], loc='best')
      #plt.savefig('Collar.png', bbox_inches="tight", dpi=600)
      plt.show()
```





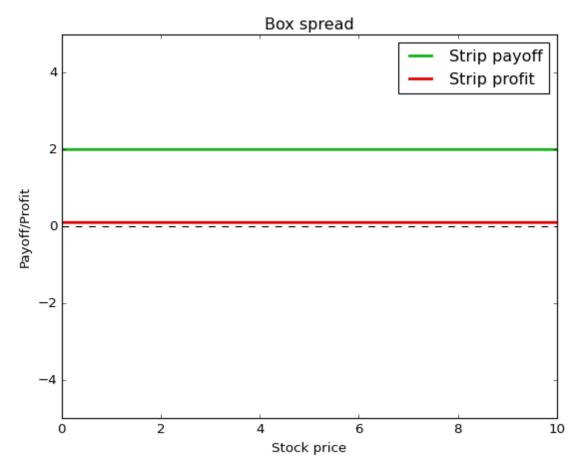
1.19 Box spread



```
S_t = 5
r = 0.05
t = 1
Sigma = 0.3

Cost = BS_call(S_t, 4, r, t, Sigma) - BS_put(S_t, 4, r, t, Sigma) + BS_put(S_t, 0, r, t, Sigma) - BS_call(S_t, 6, r, t, Sigma)
plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)

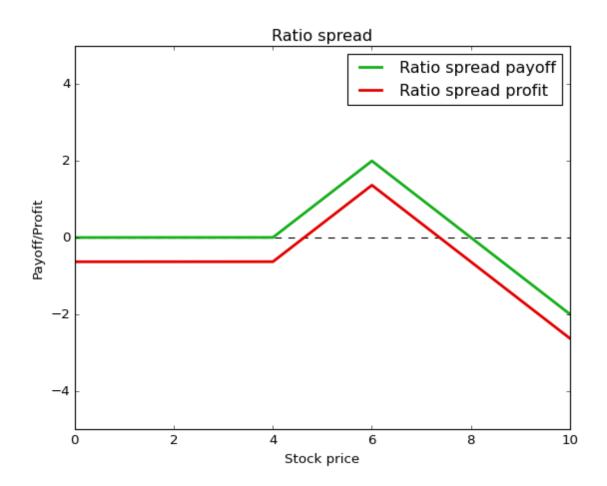
plt.xlim(0,10)
plt.ylim(-5,5)
plt.legend(['Strip payoff', 'Strip profit'], loc='best')
#plt.savefig('Strip.png', bbox_inches="tight", dpi=600)
plt.show()
```



1.20 Ratio spreads

```
[22]: plt.style.use('classic')
      S = 5
      S = np.linspace(0, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Ratio spread')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      Payoff = call_payoff(S, 4) - 2*call_payoff(S, 6)
      plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      S_t = 5
      r = 0.05
      t = 1
      Sigma = 0.3
      Cost = BS_{call}(S_t, 4, r, t, Sigma) - 2*BS_{call}(S_t, 6, r, t, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Ratio spread payoff', 'Ratio spread profit'], loc='best')
      #plt.savefig('Ratio_spread.png', bbox_inches="tight", dpi=600)
      plt.show()
```





1.21 Condors

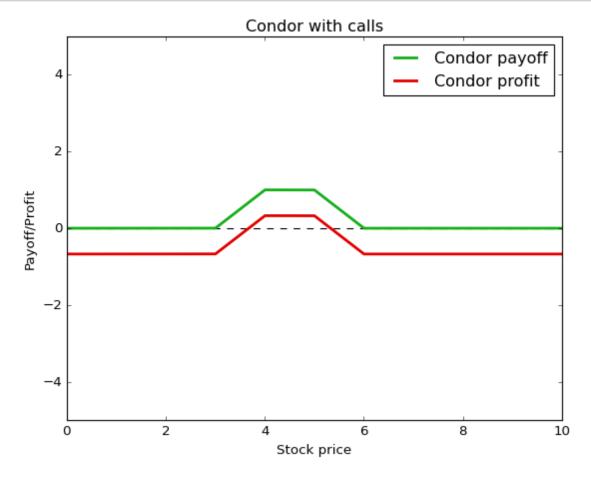


```
r = 0.05
t = 0.5
Sigma = 0.2

Cost = BS_call(S_t, 3, r, t, Sigma) - BS_call(S_t, 4, r, t, Sigma) -__

BS_call(S_t, 5, r, t, Sigma) + BS_call(S_t, 6, r, t, Sigma)
plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)

plt.xlim(0,10)
plt.ylim(-5,5)
plt.legend(['Condor payoff', 'Condor profit'], loc='best')
#plt.savefig('Condor_call.png', bbox_inches="tight", dpi=600)
plt.show()
```



1.22 Calendar spreads

```
[24]: plt.style.use('classic')
      S = 5
      S = np.linspace(0.0001, S*2, 10000, endpoint=True)
      fig, ax = plt.subplots()
      fig.patch.set_facecolor('white')
      plt.axhline(y=0, linestyle='--', color='black', label='_nolegend_')
      plt.title('Calendar spread')
      plt.ylabel('Payoff/Profit')
      plt.xlabel('Stock price')
      S_t = 5
      r = 0.05
      t_1 = 0.0001
      t_2 = 5
      Sigma = 0.3
      \#Payoff = BS\_call(S, 5, r, t_1, Sigma) - BS\_call(S, 5, r, t_2, Sigma)
      #plt.plot(S, Payoff, color='xkcd:green', linewidth=2.5)
      Payoff = BS_call(S, 5, r, t_2, Sigma) - BS_call(S, 5, r, t_1, Sigma)
      Cost = BS_{call}(S_t, 5, r, 4, Sigma) - BS_{call}(S_t, 5, r, 2, Sigma)
      plt.plot(S, Payoff - Cost, color='xkcd:red', linewidth=2.5)
      Payoff = BS_call(S, 5, r, t_2, Sigma) - BS_call(S_t, 5, r, 4, Sigma)
      plt.plot(S, Payoff, '--', color='xkcd:blue', linewidth=2.5)
      Payoff = -BS_call(S, 5, r, t_1, Sigma) + BS_call(S_t, 5, r, 2, Sigma)
      plt.plot(S, Payoff, '--', color='xkcd:orange', linewidth=2.5)
      plt.xlim(0,10)
      plt.ylim(-5,5)
      plt.legend(['Calendar spread profit', 'Long $T_2$ Call', 'Short $T_1$ Call'],
       →loc='best')
      #plt.savefig('Calendar_spread.png', bbox_inches="tight", dpi=600)
      plt.show()
```



