

# Computational Analysis of Protein Coevolution and Interaction

Fábio Madeira, PhD student

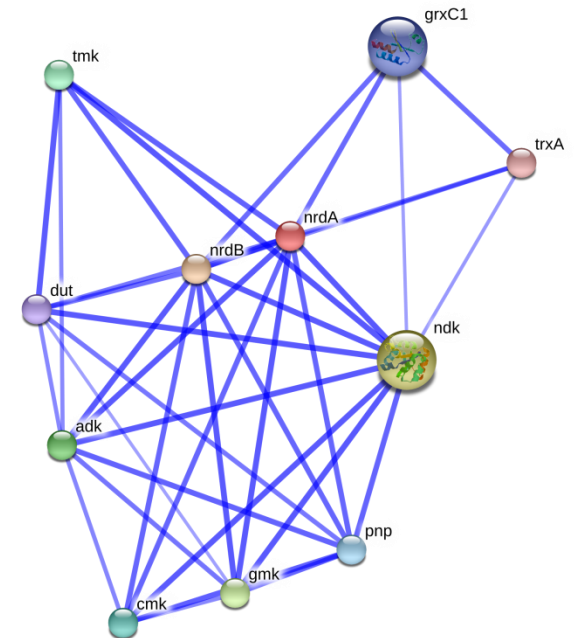
CENTRIA-DI, Faculdade de Ciências e Tecnologia



Universidade  
Nova de Lisboa

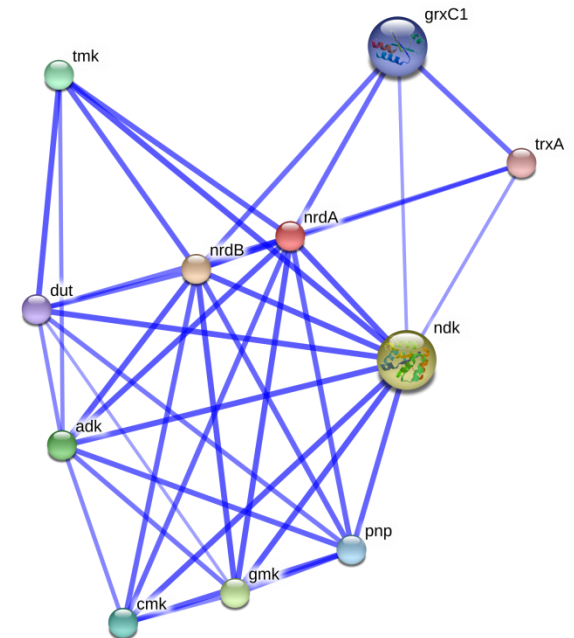
1. Introduction
2. Motivation
3. Objectives
4. Results
5. Summary

- Play a crucial role in biological systems



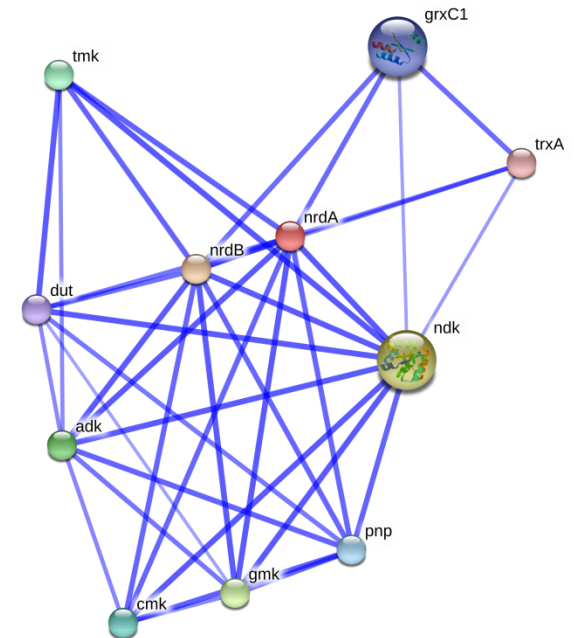
**Protein interactions of RNR (STRING)**

- Play a crucial role in biological systems
- Invaluable in expanding our understanding of diverse biological processes



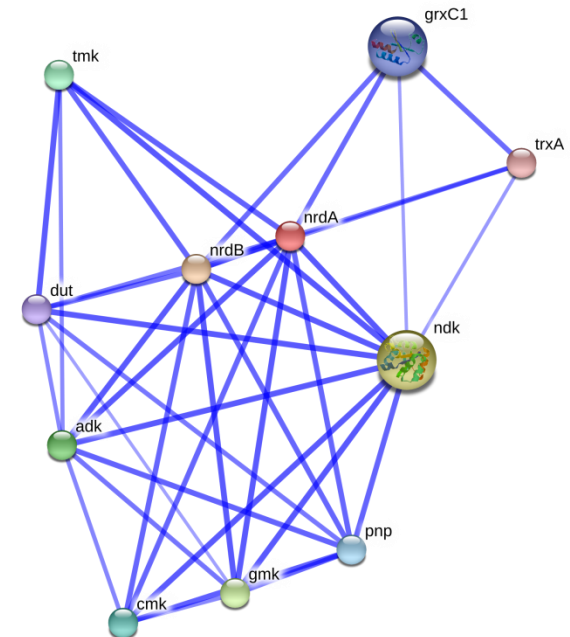
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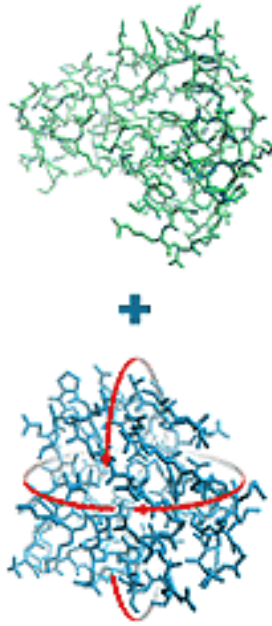


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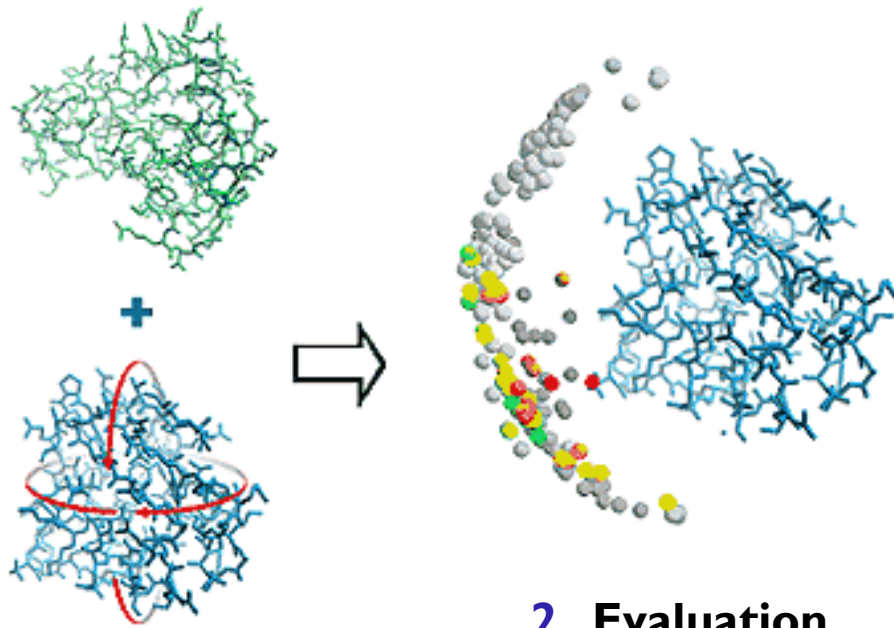
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- Hard to determine by experimental methods
- Hard to determine by computational methods



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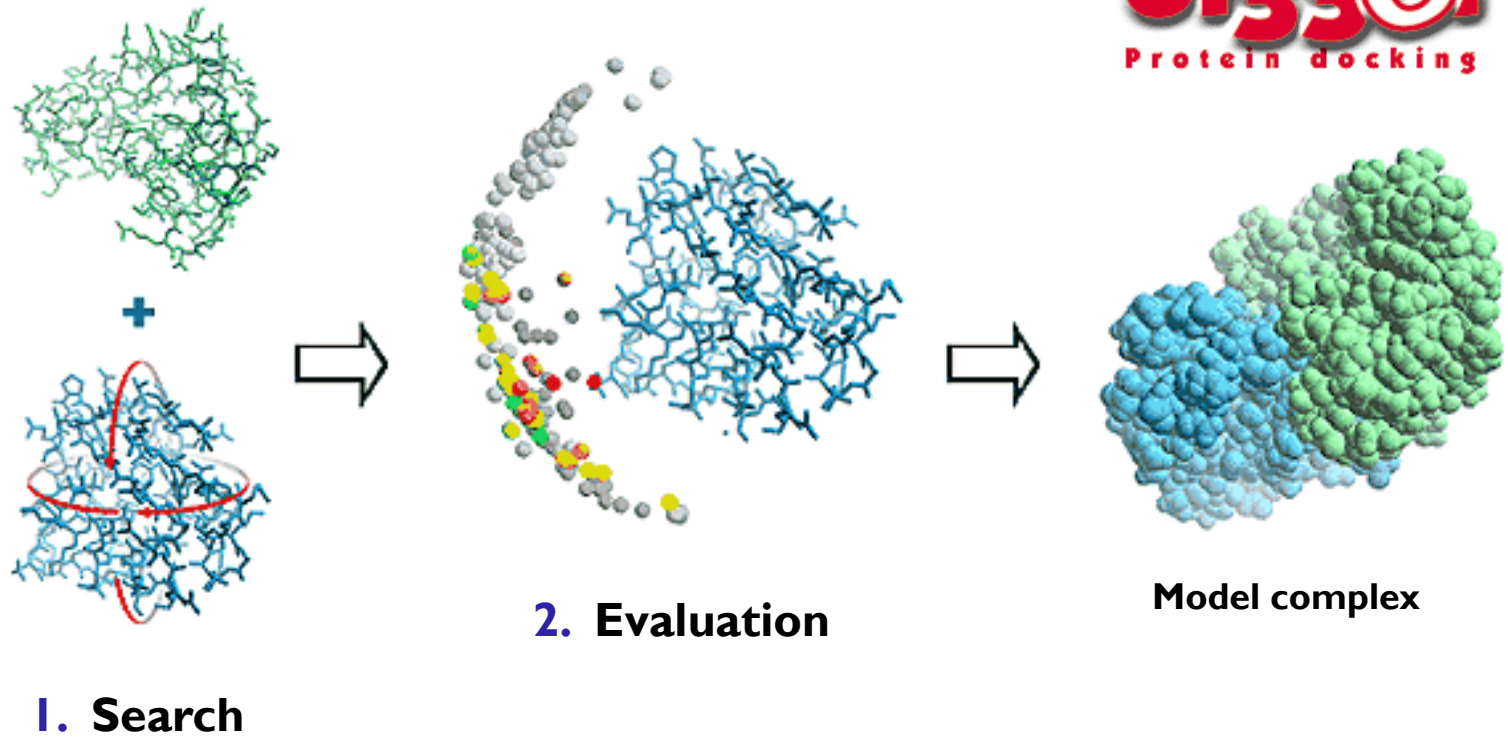


## I. Search



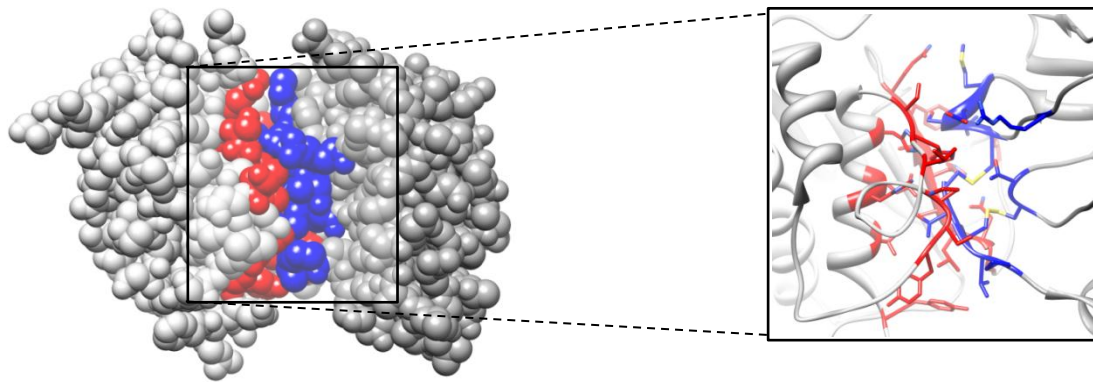
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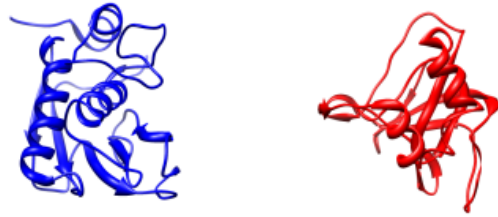




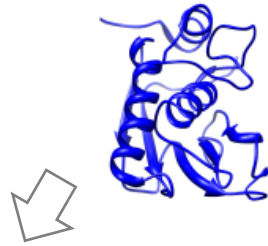
- Accumulation of sequence changes in one protein triggered by changes in other regions of the same protein or in another protein

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- Applied successfully for:
  - **Prediction of protein interactions**
  - **To guide protein docking**

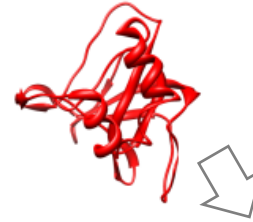




**I. Homologous sequences**

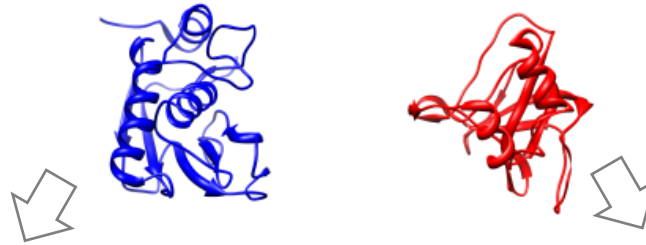


DPSLDRPFISEGTTLKDLIYDMTT



VEGMIKLALSTASGLAHLHMEI

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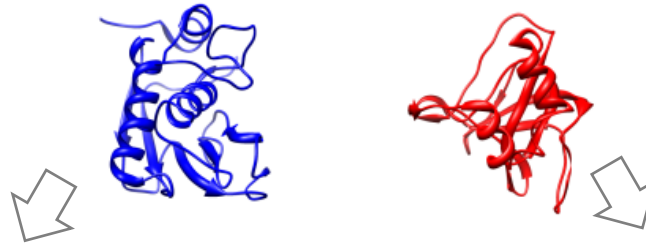


**DPSLDRPFISEGTTLKDLIYDMTT**  
 -----EPRPDGRDWSVELQEL--  
 -----KPGPDLGRDWSVELQEL--  
 -----EPESDGRDWSAELPEL--  
 -----EPEPGSGGDCSEELPEL--  
 -----DPEPGSGGDCSEELPEL--  
 PEPEQEPEPDSSGGDCSAELPEL--  
 RKQGLHSMNMMEAACSEPSLDL--

## 2. MSA computation

**VEGMIKLALSTASGLAHLHMEI**  
 WGSSLRMALSLAQGLAFLHEER  
 WGSSLRMALSLAQGLAFLHEER  
 WGSSLRMALSLAQGLAFLHEER  
 WGSSLSMALSLAEGLAFLHGRR  
 WGSSLSMALSLAEGLAFLHERR  
 --SSMSMALSLAQGLAFLHER--  
 --SSCRLAHSITRGLAYLHTRR

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 -----EPRPDSGRDWSVELQEL--  
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 -----EPESDSGRDWSAELPEL--  
 -----EPEPGSGGDCSEELPEL--  
 -----DPEPGSGGDCSEELPEL--  
 PEPEQEPEPDSGGDCSAELPEL--  
 RKQGLHSMNMMEAACSEPSLDL--

**x**

i

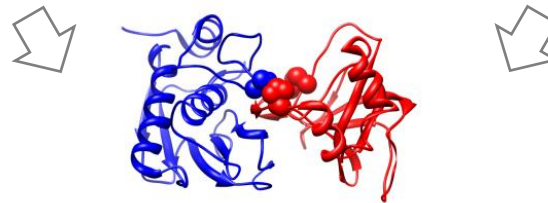
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 WGSSLRMALSLAQGLAFLHEER  
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 WGSSLSMALSLAEGLAFLHGRR  
 WGSSLSMALSLAEGLAFLHERR  
 --SSMSMALSLAQGLAFLHER--  
 --SSCRLAHSITRGLAYLHTRR

**y**

j

## 3. Coevolution analysis



- Matrix-based
  - Physicochemical propensities and contact preferences (CPVN, CLM, etc.)
- Correlation-based
  - Correlation coefficient (Pearson's, Spearman's, Quartets, OMES, etc.)
- Statistical-based
  - Perturbation of MSA (MI, SCA, ELSC, etc.)
- Phylogenetic-based
  - Similarity of phylogenetic trees (e.g. Mirrortree, etc.)



MSA =

```

QFGLFSPEEIRASSVALIR--YPETLENG--VPKESGLVCAGHFGHIELVK
QFGLFSPEEIKRMSVVHVE--YPETMDEQRQRPRTKGLECPGHFGHIELAT
ELGVLDPEIIKKISVCEIV--NVDIYKDG--FPREGGLYCPGHFGHIELAK
QFGVLSPDELKRMSVTEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGVLSPDELKRMSVTEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGILSPDEIRRMSVTEGGVQFAETME--GGRPKLGGLECPGHFGHIDLAK
QFGILGPTEEIKRMSVAH--VEFPEVYE--NGKPKLGGLDPCGHFGHLELAK
QFGILSPEEIRSMSVAK--IEFPETMDESGQRPRVGGLDCPGHFGHIELAK
QFGILSPDEIRQMSVIH----VEHSETTEK GKPKVGGLECPGHFGYLELAK
-----ECPGHFGHIELAK
-----ECPGHFGFIELAK
QFEIFKERQIKSYAVCLVEHAKSYANA----ADQSGEAECPGHFGYIELAE
QFEVFKEAQIKAYAKCIIIEHAKSYEHG----QPVRGGIECPGHFGYVELAE

```

MSA =

```

QFGLFSPEEIRASSVALIR--YPETLENG--VPKESGLVCAGHFGHIELVK
QFGLFSPEEIKRMSVVHVE--YPETMDEQRQRPRTKGLECPGHFGHIELAT
ELGVLDPEIIKKISVCEIV--NVDIYKDG--FPREGGLYCPGHFGHIELAK
QFGVLSPELKRMSVTEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGVLSPELKRMSVTEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGILSPDEIRMSVTEGGVQFAETME--GGRPKLGGLECPGHFGHIDLAK
QFGILGP EEIKRMSVAH--VEFPEVYE--NGKPKLGGLDPCGHFGHLELAK
QFGILSPEEIRSMVAK--IEFPETMDESGQRPRVGGLDCPGHFGHIELAK
QFGILSPDEIRQMSVIH----VEHSETTEKGKPKVGGLECPGHFGYLELAK
-----ECPGHFGHIELAK
-----ECPGHFGFIELAK
QFEIFKERQIKSYAVCLVEHAKSYANA----ADQSGEAECPGHFGYIELAE
QFEVFKEAQIKAYAKCIIIEHAKSYEHG----QPVRGGIECPGHFGYVELAE

```

- Insufficient evolutionary divergence
- Sample size effects
- Small taxa coverage
- False correlations as result of misalignments
- **Underlying assumption of independent mutations**

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- Coevolution data can help predict protein interaction and to guide docking

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- BiGGER can use contact information to constraint the search space and improve the quality of the models

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- BiGGER can use contact information to constraint the search space and improve the quality of the models
- Limitations of MSA, such as the assumption of independent mutations

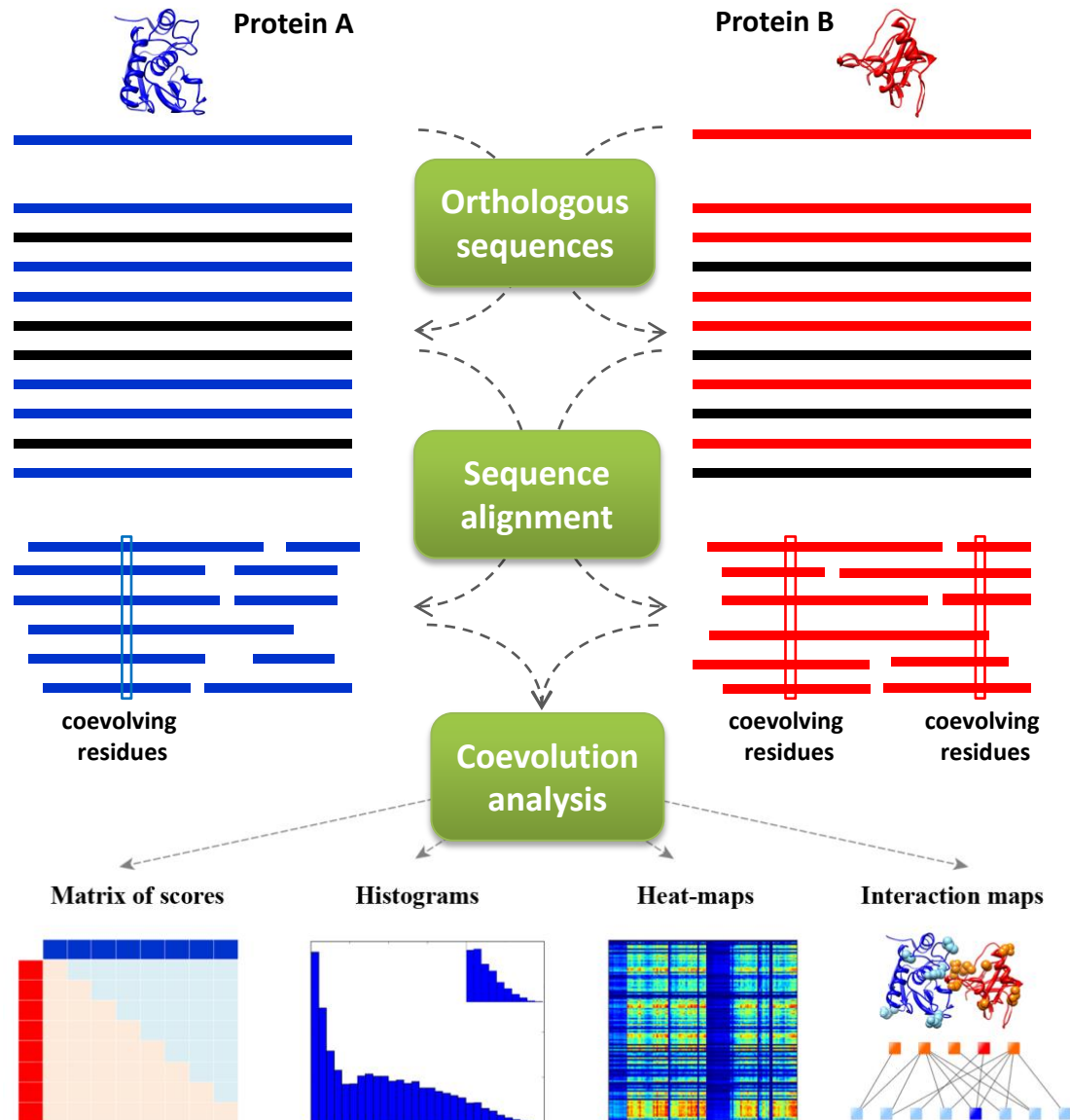
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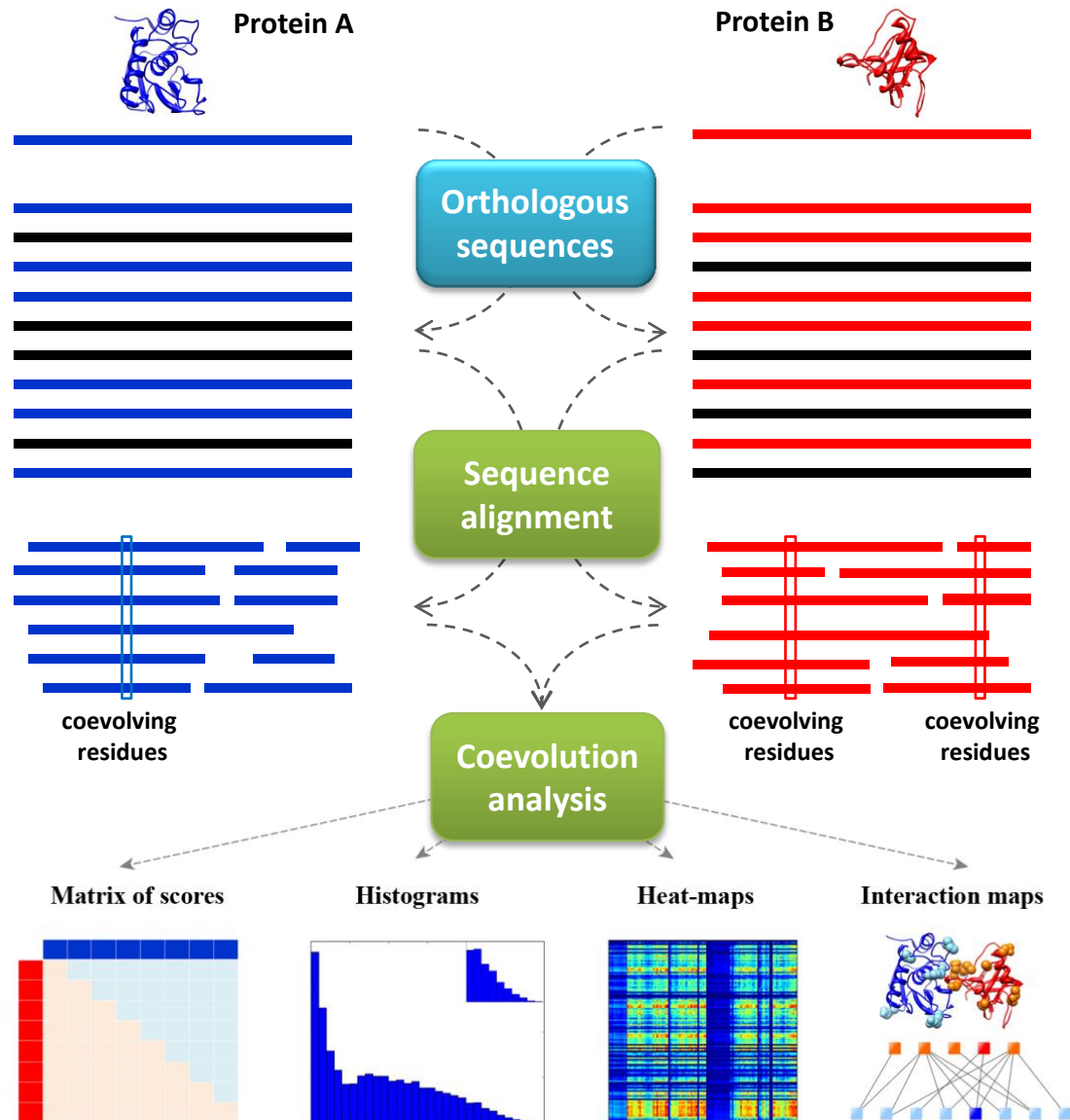
- The computational analysis of protein coevolution and interaction will focus on:

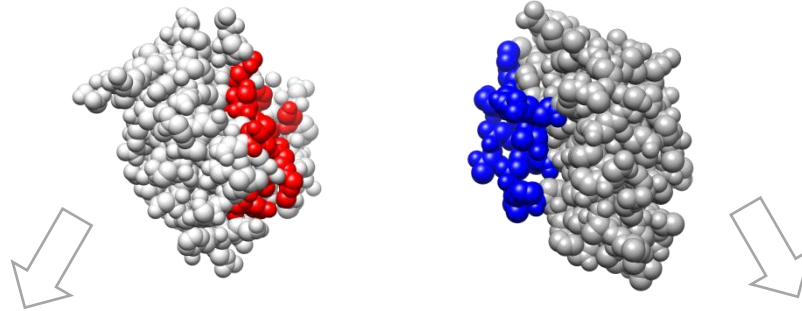


- The computational analysis of protein coevolution and interaction will focus on:
  - Refinement of Multiple Sequence Alignments
  - Integration of protein coevolution data in the protein docking workflow
  - Development and assessment of different coevolution measures
  - Development of new scoring methods to rank docking solutions

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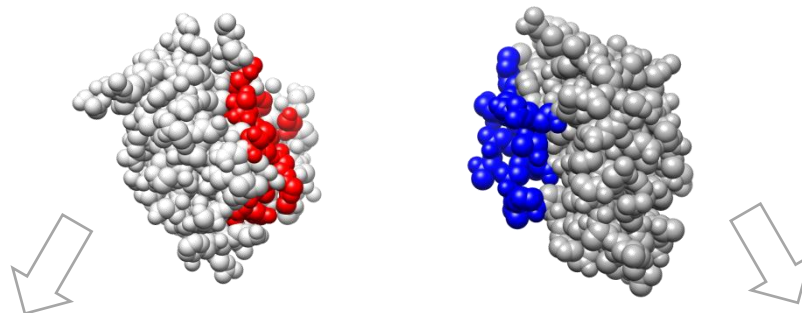






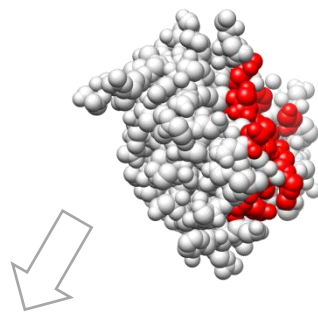
Organism1	DPSLDRPFISEGTTLKDLIYDMTT
Organism2	-----EPRPDSSGRDWSVELQEL--
Organism3	-----KPGPDLGRDWSVELQEL--
Organism4	-----EPESDSSGRDWSAELPEL--
Organism5	-----EPEPGSGGDCSEELPEL--
Organism6	-----DPEPGSGGDCSEELPEL--
Organism7	PEPEQEPEPDSSGGDCSAELPEL--
Organism8	RKQGLHSMNMMEAACSEPSLDL--

Organism3	VEGMIKLALSTASGLAHLHMEI
Organism1	WGSSLRMALSLAQGLAFLHEER
Organism9	WGSSLRMALSLAQGLAFLHEER
Organism8	WGSSLRMALSLAQGLAFLHEER
Organism5	WGSSLSMALSLAEGLAFLHGRR
Organism10	WGSSLSMALSLAEGLAFLHERR
Organism2	--SSMSMALSLAQGLAFLHER-
Organism11	--SSCRLAHSITRGLAYLHTRR

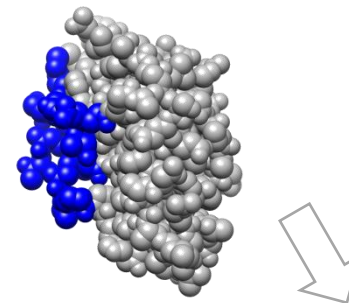


<b>Organism1</b>	DPSLDRPFISEGTTLKDLIYDMTT
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Organism7	PEPEQEPEPDSSGGDCSAELPEL--
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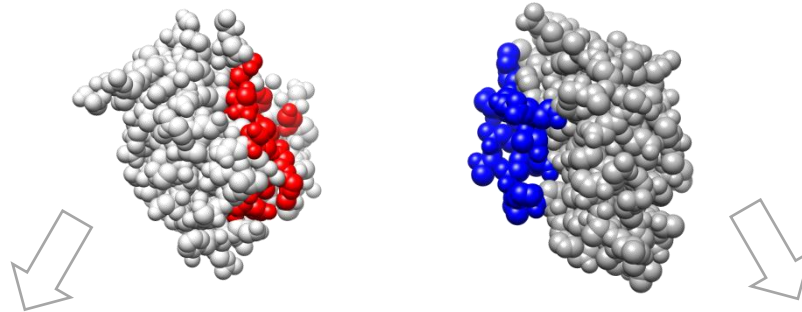
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<b>Organism8</b>	WGSSLRMALSLAQGLAFLHEER
<b>Organism5</b>	WGSSLSMALSLAEGLAFLHGRR
Organism10	WGSSLSMALSLAEGLAFLHERR
<b>Organism2</b>	--SSMSMALSLAQGLAFLHER-
Organism11	--SSCRLAHSITRGLAYLHTRR



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<b>Organism3</b>	-----KPGPDLGRDWSVELQEL--
<del>Organism4</del>	<del>-----EPESD SGRDWSAELPEL--</del>
<b>Organism5</b>	-----EPEPGSGGDCSEELPEL--
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<b>Organism2</b>	--SSMSMALSLAQGLAFLHER-
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- p-distance [Jukes and Cantor, 1969]

$$d = p = \frac{N_{dif}}{N_{total}}$$

- Jukes-Cantor [Jukes and Cantor, 1969]

$$d = -\frac{19}{20} \log(1 - p * \frac{20}{19})$$

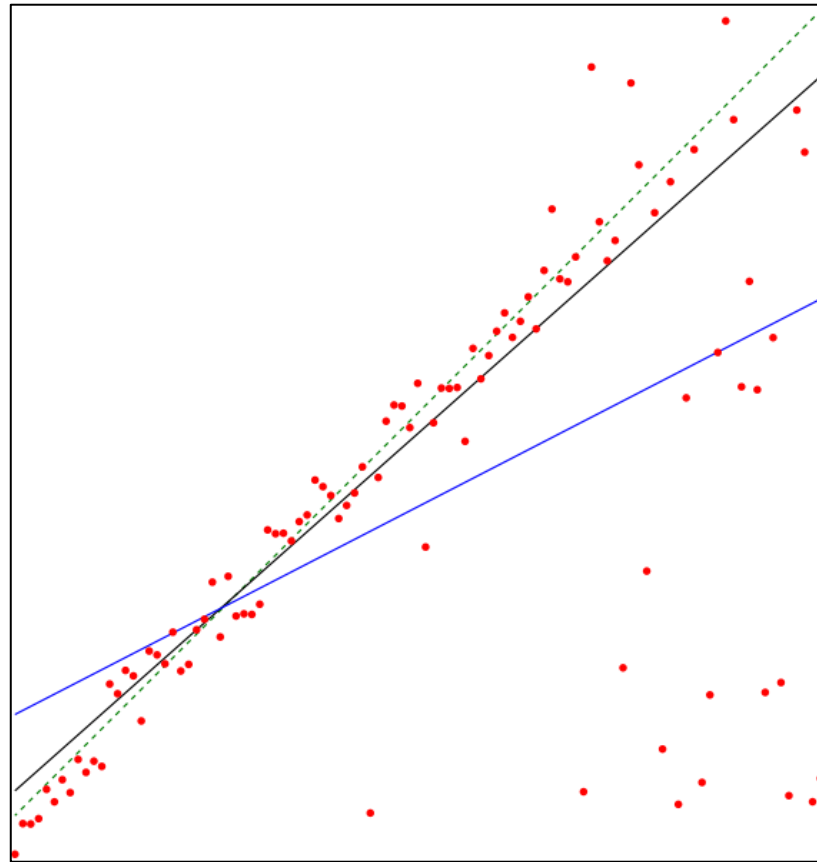
- Kimura distance [Kimura, 1983]

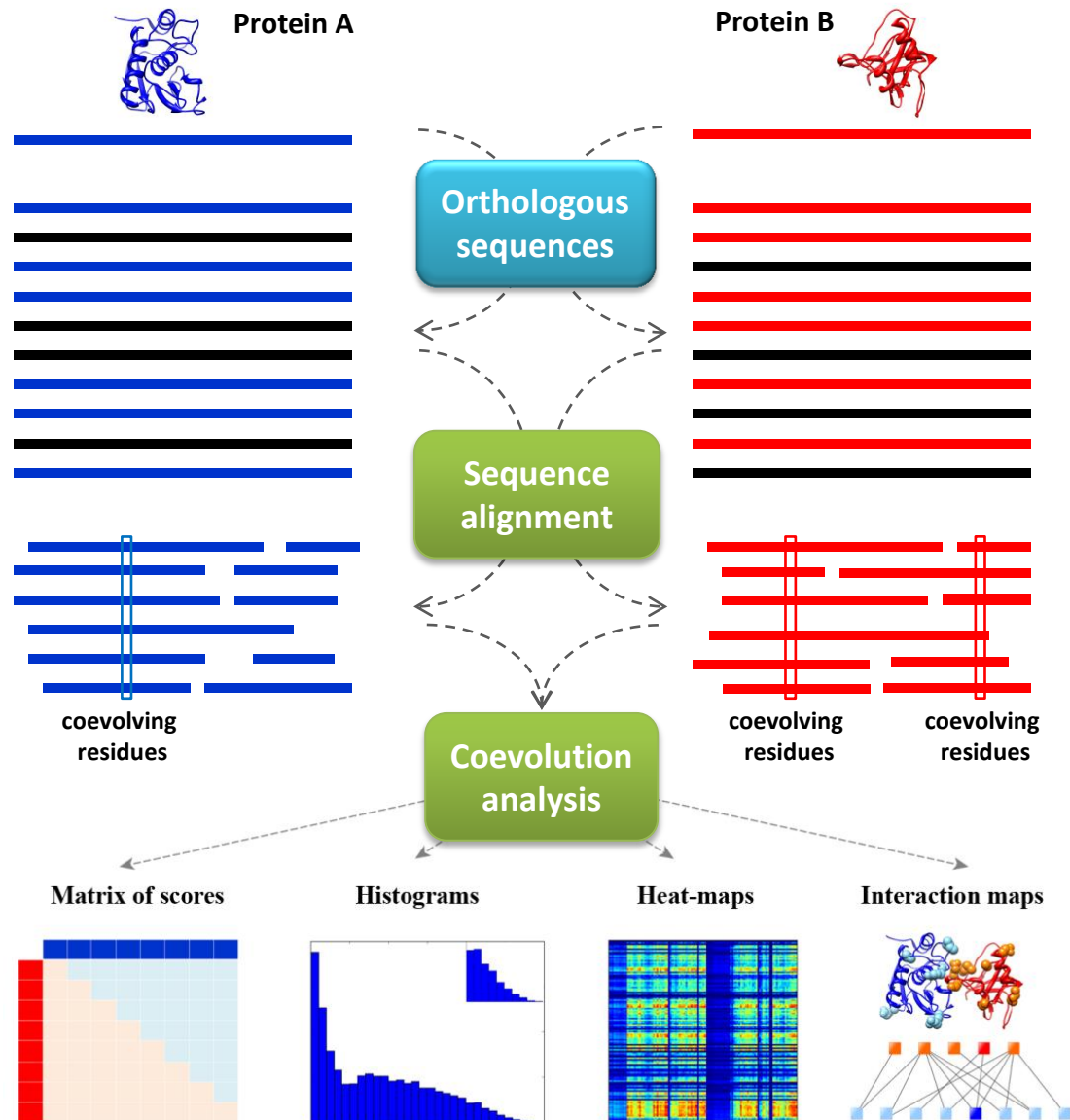
$$d = -\ln(1 - p - 0.2^2)$$

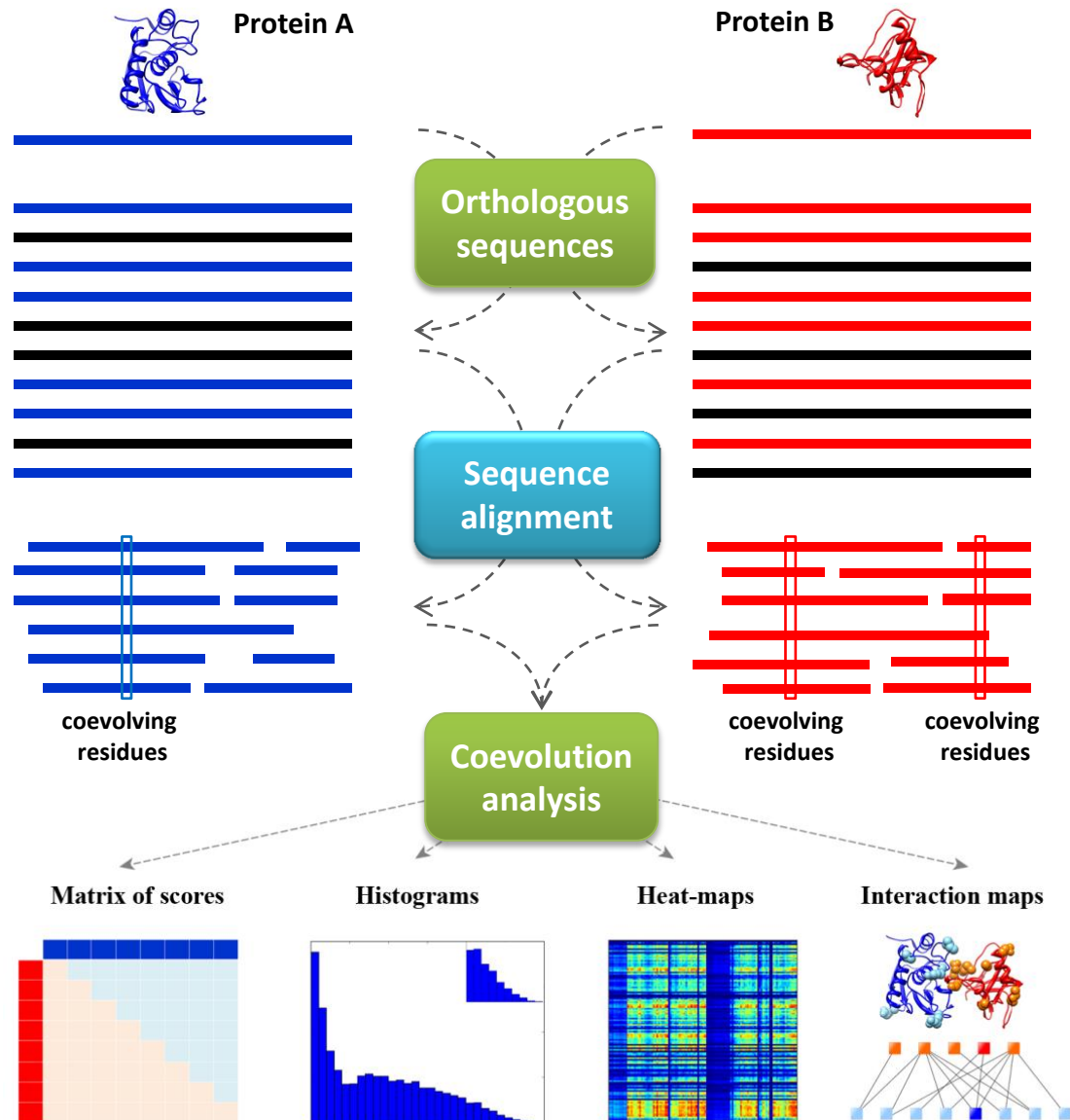
- Pairwise score using Dayhoff or PAM matrices [Gonnet, 2000]

$$d = \sum \frac{1 - S_{ij}}{S_{ii}} * \frac{1 - S_{ij}}{S_{jj}}$$

- Median  $m$  of the slopes  $(y_j - y_i)/(x_j - x_i)$  determined by all pairs of sample points  $\in (x, y)$ , which have distinct  $x$ -coordinates [Theil, 1950] and [Sen, 1968]







```

QFGLFSPEEIRASSVALIR--YPETLENG--VPKESGLVCAGHFGHIELVK
QFGLFSPEEIKRMSVVHVE--YPETMDEQRQRPRRTKGLECPGHFGHIELAT
ELGVLDPEI IKKISVCEIV--NVDIYKDG--FPREGGLYCPGHFGHIELAK
QFGVLSDELKRMSTVEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGVLSDELKRMSTVEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGILSPDEIRRMSTVEGGVQFAETME--GGRPKLGGLECPGHFGHIDLAK
QFGILGP E EIKRMSVAH--VEFPEVYE--NGKPKLGGLD CPGHFGHLELAK
QFGILSP E EIRSMSTVAK--IEFPETMDESGQRPRVGGLDCPGHFGHIELAK
QFGILSPDEIRQMSVIH----VEHSETTEKKGPKVGGLECPGHFGYLELAK
-----ECPGHFGHIELAK
-----ECPGHFGFIELAK
QFEIFKERQIKSYAVCLVEHA KSYANA----ADQSGEAECPGHFGYIELAE
QFEVFKEAQIKAYAKCIEHA KSYEHG----QPV RG GIECPGHFGYVELAE

```

misalignments



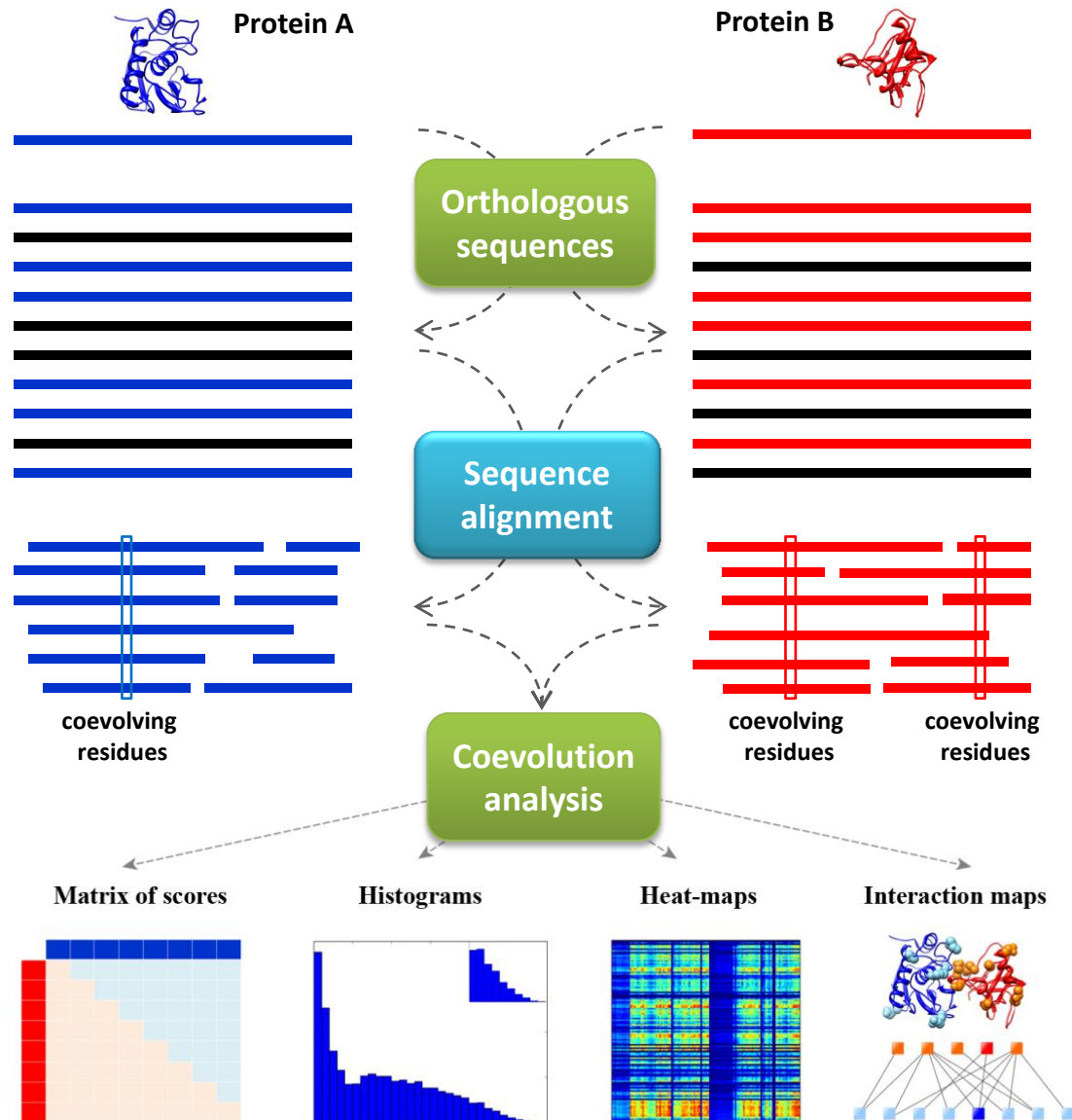
Accounts for correlated mutations

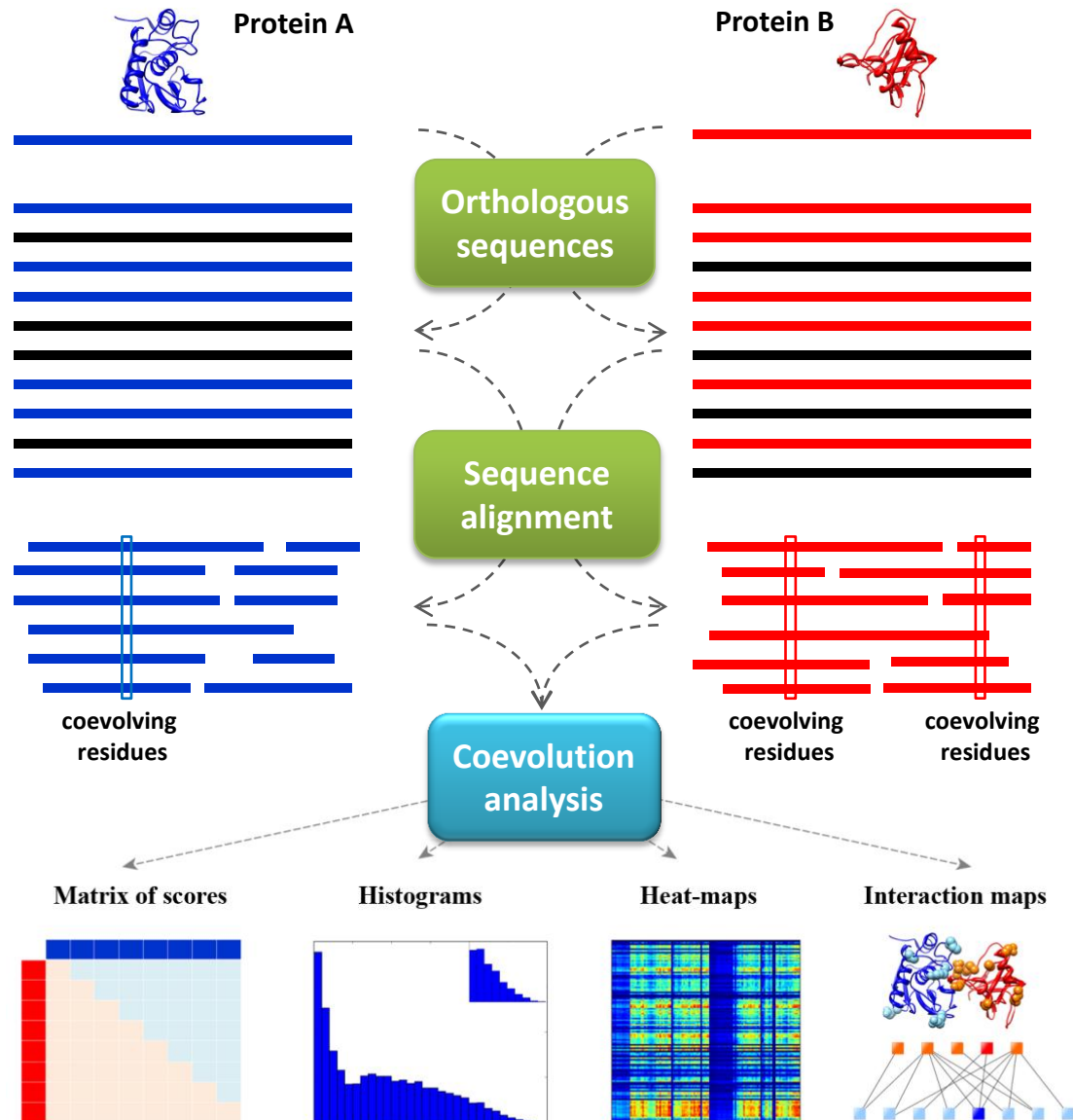
```

QFGLFSPEEIRASSVAL--IRYPETLE--NGVPKESGLVCAGHFGHIELVK
QFGLFSPEEIKRMSVVH--VEYPETMDEQRQRPRRTKGLECPGHFGHIELAT
QFGILSP E EIRSMSTVAK--IEFPETMDESGQRPRVGGLDCPGHFGHIELAK
ELGVLDPEI IKKISVCE--IVNVDIYK--DGFREGGLYCPGHFGHIELAK
QFGVLSDELKRMSTVEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGVLSDELKRMSTVEGGIKYPETTE--GGRPKLGGLECPGHFGHIELAK
QFGILSPDEIRRMSTVEGGVQFAETME--GGRPKLGGLECPGHFGHIDLAK
QFGILGP E EIKRMSVAH--VEFPEVYE--NGKPKLGGLD CPGHFGHLELAK
QFGILSPDEIRQMSVIH--VEHSETTE--KGKPKVGGLECPGHFGYLELAK
-----ECPGHFGHIELAK
-----ECPGHFGFIELAK
QFEIFKERQIKSYAVCL--VEHA KSYA--NAADQSGEAECPGHFGYIELAE
QFEVFKEAQIKAYAKCI--IEHA KSY--EHGQPV RG GIECPGHFGYVELAE

```

- Constraint Programming





- Contact Preferences, Volume Normalized (**CPVN**) [Glaser et al, 2001]
- Contact PDB-derived Likelihood Matrix (**CLM**) [Singer et al, 2002]
- Residue-residue Volume Normalized (**VOL**) [Esque et al, 2010]

$$CM_{x,y} = \sum_i^n \sum_j^n \frac{S_{ij}}{n}$$



- Pearson's correlation (**Pearson**) [Göbel et al, 1994]
- Spearman's rank correlation (**Spearman**) [Pazos et al, 1997]
- McLachlan Based Substitution Correlation (**McBASC**) [Fodor and Aldrich, 2004]
- **Quartets** [Galitsky, 2002]

$$CM_{x,y} = \frac{1}{N^2} \sum_i \sum_j \frac{W_{ij}(S_{xij} - \langle S_x \rangle)(S_{yij} - \langle S_y \rangle)}{\sigma_x \sigma_y}$$

- Observed Minus Expected Squared (**OMES**) [Kass and Horovitz, 2002]

$$CM_{x,y} = \sum_l \frac{(N_{obs} - \frac{C_{xi}C_{yj}}{N_{valid}})^2}{N_{valid}}$$

- Mutual Information (**MI**) [*Gloor et al, 2005*]
- MI by pair Entropy (**MI/E**) [*Martin et al, 2005*]
- Row and Column Weighed MI (**RCW MI**) [*Gouveia-Oliveira et al, 2007*]

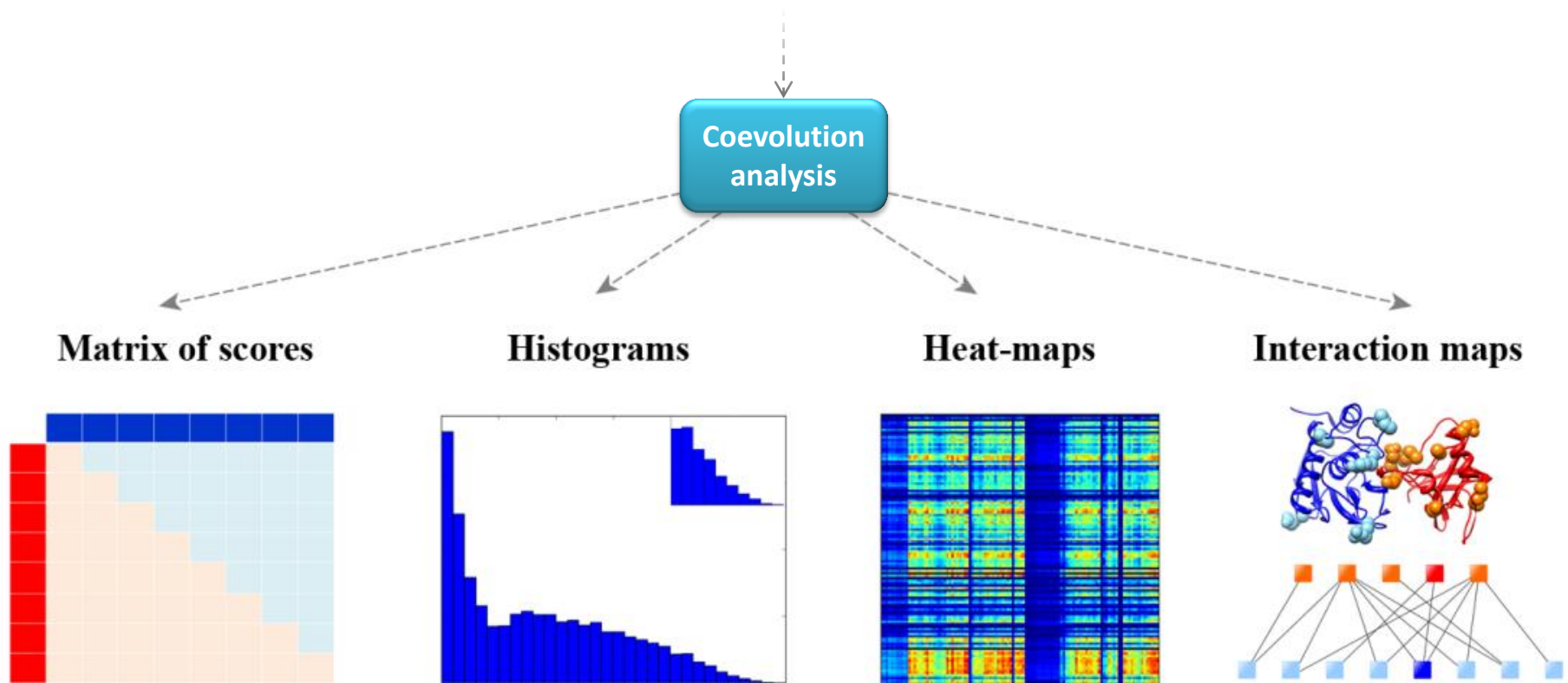
$$MI_{x,y} = \sum_i \sum_j P(x_i y_j) \log \frac{P(x_i y_j)}{P(x_i) P(y_j)}$$

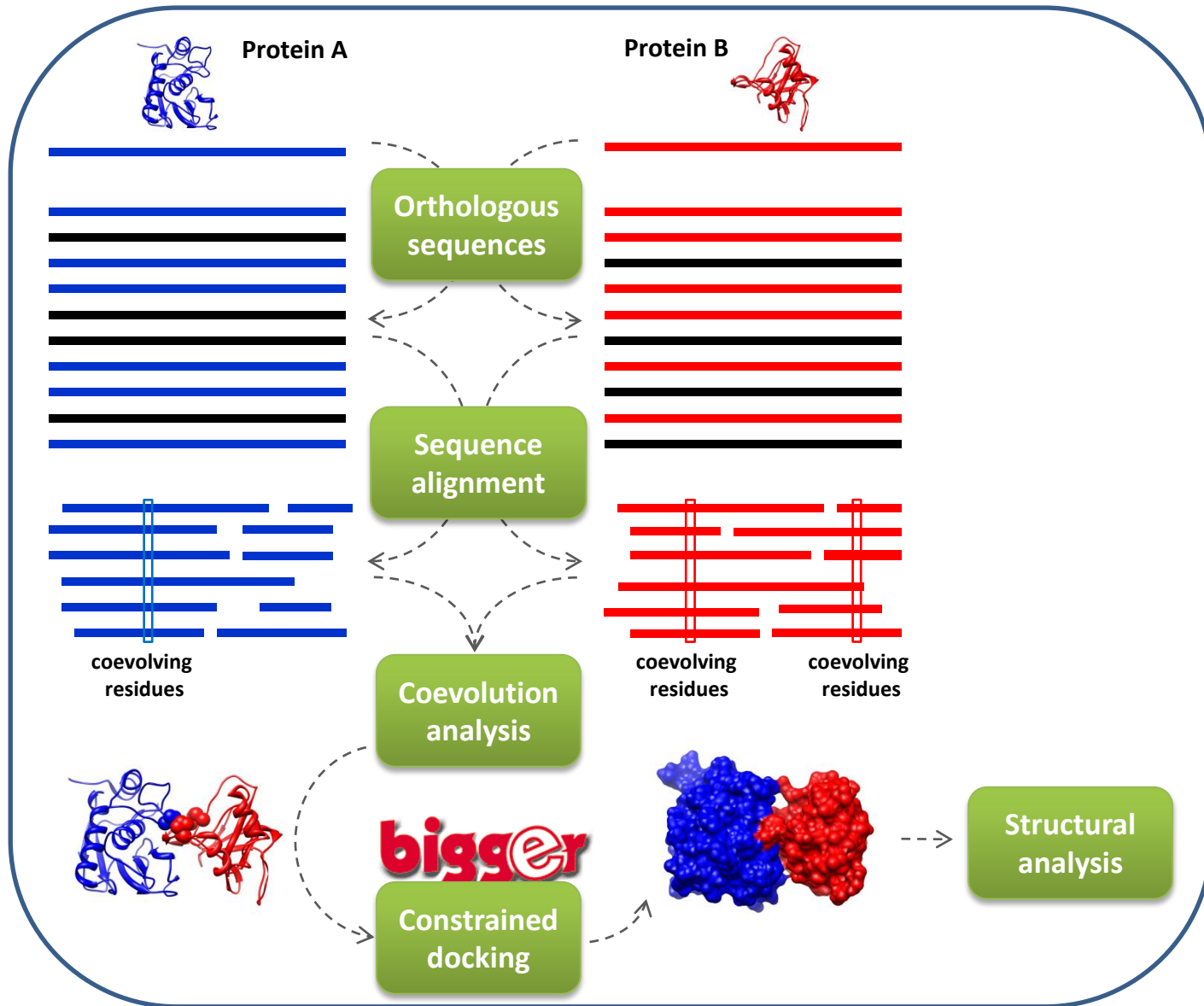
- Statistical Coupling Analysis (**SCA**) [*Lockless and Ranganathan, 1999*]

$$\Delta\Delta G_{x,y} = \sqrt{\sum_i (\ln P_{x|\delta y}^i - P_x^i)^2}$$

- Explicit Likelihood of Subset Covariation (**ELSC**) [*Dekker et al, 2004*]

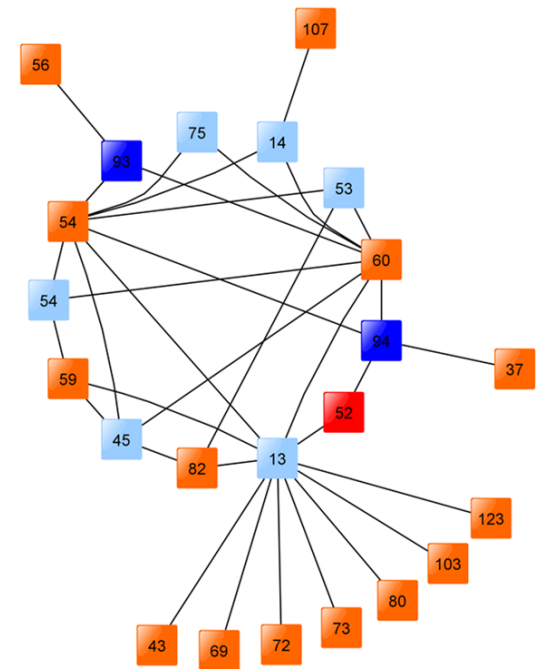
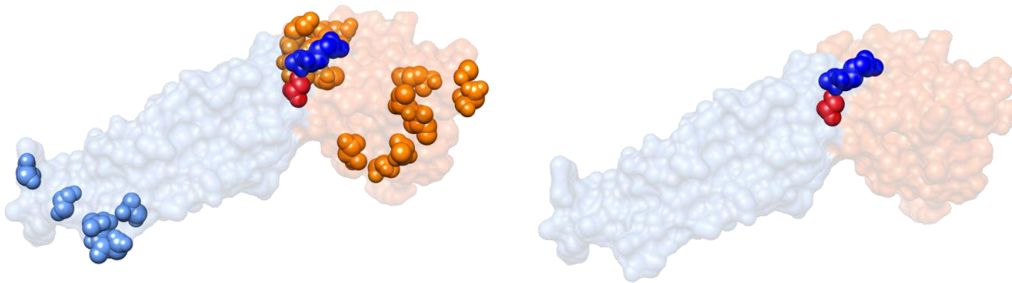
$$\Lambda_x^y = \prod_r \frac{\binom{N_{r,y}}{n_{r,y}}}{\binom{N_{r,y}}{m_{r,y}}}$$



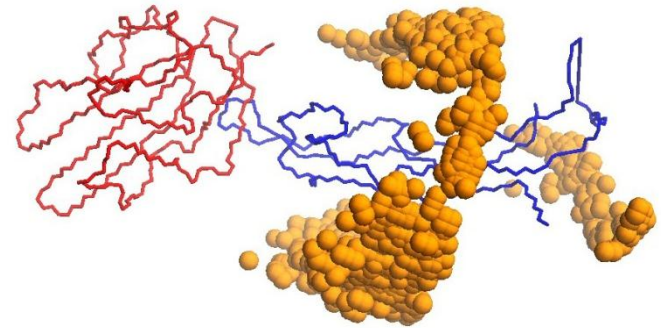


## Protein complex TGF- $\beta$ 3/TGF- $\beta$ receptor type II (Iktz)

- Most residues were at the surface level
- 3 out of 23 residues were at the interface
- 8 residues from TGF- $\beta$ 3
- 15 residues from TGB- $\beta$  receptor

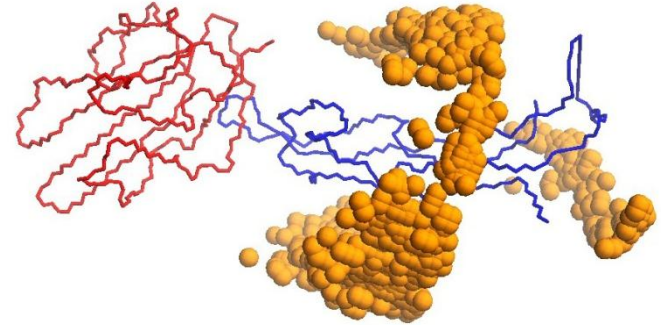


- Possible pairs of contacts = 11772
- Tested contacts = 120
- Reduced the search space to 0.01% of possible contact points



*Difficult complex to model*

- Possible pairs of contacts = 11772
- Tested contacts = 120
- Reduced the search space to 0.01% of possible contact points



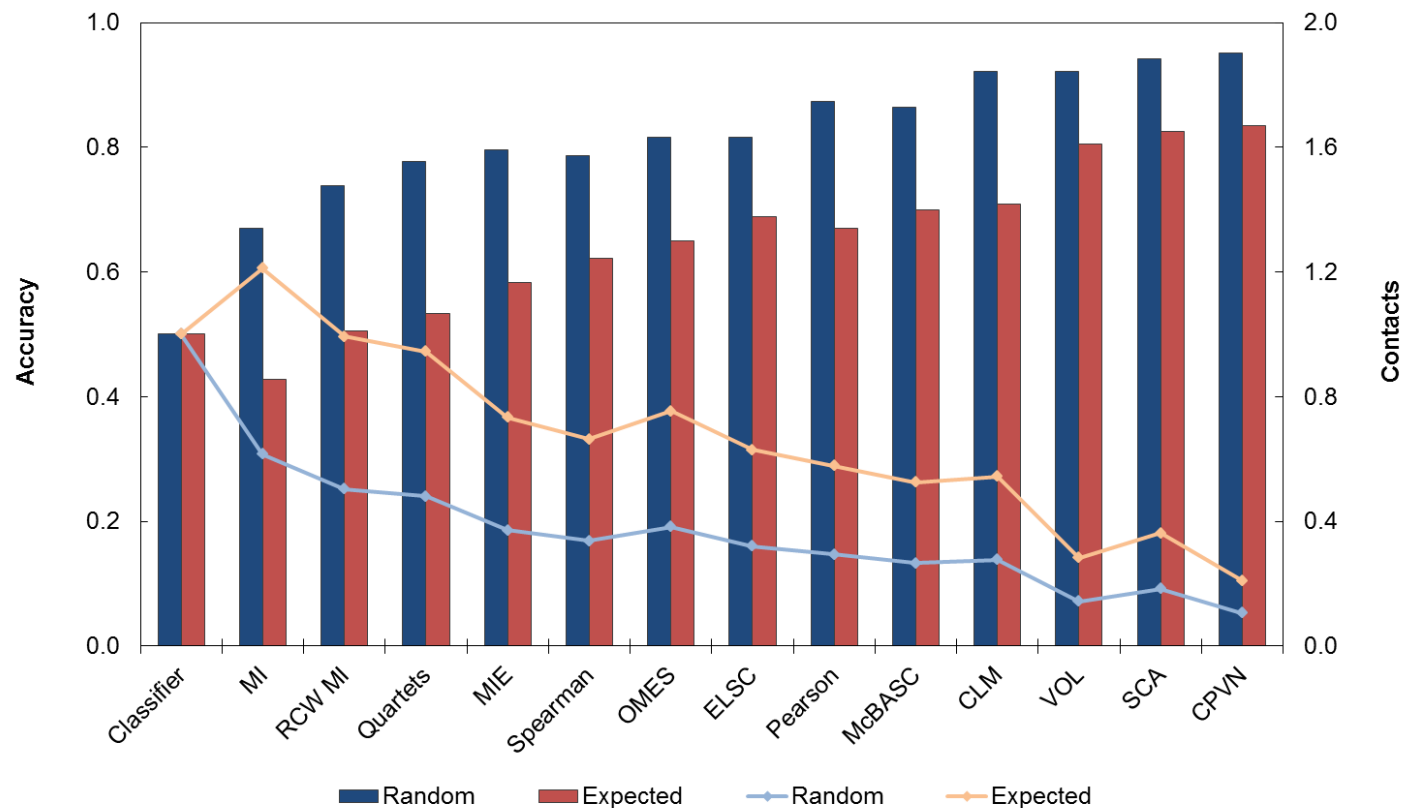
*Difficult complex to model*

- Given the complexity of protein-protein docking, finding even only one positive interface contact can help constraint the search space and improve the accuracy of constrained docking algorithms such as BiGGER [*Palma et al, 2000*]

- Survey which method is better suited for the identification of interface contact points using a large protein complex dataset (unpublished)



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1. Introduction
2. Motivation
3. Objectives
4. Results
5. Summary

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- Open source
- Source code at <https://github.com/fmadeira/pycoevol>

Thanks for your attention!

Computational Analysis of Protein Coevolution and Interaction

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