

```
In[256]:= A - BB > 0
          CC - CBAC ≥ 0
          ABC - CACA > 0
```

```
Out[256]= A - BB > 0
```

```
Out[257]= -CBAC + CC ≥ 0
```

```
Out[258]= ABC - CACA > 0
```

```
In[259]:= Clear[a11, a12, a21, a22,
               b11, b12, b21, b22,
               c11, c12, c21, c22];
          FA := {{a11, a12}, {a21, a22}};
          FB := {{b11, b12}, {b21, b22}};
          FC := {{c11, c12}, {c21, c22}};
          Ch1 := FA - FB.FB;
          Ch2 := FC.FC - FC.FB.FA.FC;
```

```
In[265]:= Ch1
```

```
Out[265]= {{a11 - b112 - b12 b21, a12 - b11 b12 - b12 b22}, {a21 - b11 b21 - b21 b22, a22 - b12 b21 - b222}}
```

```
In[266]:= FindInstance[a11 - b112 - b12 b21 > 0 && a12 - b11 b12 - b12 b22 ≥ 0 && a21 - b11 b21 - b21 b22 ≥ 0 &&
                      a22 - b12 b21 - b222 ≥ 0 && a11 > 0 && a12 ≥ 0 && a21 ≥ 0 && a22 ≥ 0 && b11 > 0 &&
                      b12 ≥ 0 && b21 ≥ 0 && b22 ≥ 0, {a11, a12, a21, a22, b11, b12, b21, b22}, Integers]
```

```
Out[266]= {{a11 → 5, a12 → 0, a21 → 0, a22 → 0, b11 → 2, b12 → 0, b21 → 0, b22 → 0}}
```

```
In[267]:= Begin["Ctx0`"];
          a11 = 5;
          a12 = a21 = a22 = 0;
          b11 = 2;
          b12 = b21 = b22 = 0;
          Ch2
```

```
Out[272]= {{-9 c112 + c12 c21, -9 c11 c12 + c12 c22}, {-9 c11 c21 + c21 c22, -9 c12 c21 + c222}}
```

```
In[273]:= FindInstance[-9 c112 + c12 c21 > 0 && -9 c11 c12 + c12 c22 ≥ 0 && -9 c11 c21 + c21 c22 ≥ 0 &&
                      -9 c12 c21 + c222 ≥ 0 && c11 > 0 && c12 ≥ 0 && c21 ≥ 0 && c22 ≥ 0, {c11, c12, c21, c22}, Integers]
```

```
Out[273]= {{c11 → 1, c12 → 68, c21 → 72, c22 → 286}}
```

```
In[274]:= Begin["Ctx1`"];
```

```
In[284]:= c11 = 1;
          c12 = 68;
          c21 = 72;
          c22 = 286;
          fuel = {2, 1}
```

```
Out[288]= {2, 1}
```

```
In[289]:= Ch1  
          Ch1.fuel
```

```
Out[289]= {{1, 0}, {0, 0}}
```

```
Out[290]= {2, 0}
```

```
In[291]:= Ch2  
          Ch2.fuel
```

```
Out[291]= {{4887, 18 836}, {19 944, 37 732}}
```

```
Out[292]= {28 610, 77 620}
```

```
In[293]:= Ch3 = FA.FB.FC - FC.FA.FC.FA
```

```
Out[293]= {{-15, 680}, {-1800, 0}}
```

```
In[294]:= Ch3.fuel
```

```
Out[294]= {650, -3600}
```

```
In[283]:= End[]
```

```
Out[283]= Ctx1`
```