

Chi-Squared Test Pseudocode

This version of the document is dated 2019-02-06.

Introduction

This short article sets forth pseudocode for performing a [chi-squared test](#) using observed frequencies and probabilities.

In the pseudocode below—

- the [pseudocode conventions](#) apply,
- ALMOSTZERO is a number very close to 0 (for example, 10^{-100}), and
- EPSILON is a number setting an estimation tolerance for the p-value calculation (for example, 10^{-14}).

The following are the parameters for ChiSquaredTest below:

- probabilities is a list of probabilities for each event (ranging from 0, never, to 1, always).
- counts is a list with the same size as probabilities and gives, for each event, the number of times that event occurs. The sum of all items in counts should be at least 5.

ChiSquaredTest returns a list containing two items: the first item is the chi-squared statistic, and the second item is the *p-value* (the probability that a random sample's chi-squared statistic would be greater than or equal to that of the given sample). (Note that if probabilities has only one item, the p-value will be meaningless.)

Pseudocode

```
METHOD DoubleFactorial(x)
  if x<=1: return 1
  ret=1
  x=floor(x)
  smod = rem(x,2)
  k=0
  if smod==0: k=floor(x/2)
  if smod==1: k=floor((x-1)/2)+1
  i=0
  while i<k
    ret=ret*2*(i+1)-smod
    i=i+1
  end
  return ret
END METHOD
```

```
METHOD GammaOfHalfInteger(x)
  if x==0: return infinity
  if x<0: return error
  // Computes gamma(x/2) assuming `x` is an integer
  return DoubleFactorial(x-2)*sqrt(pi)/pow(2,(x-1)*0.5)
END METHOD
```

```
METHOD GammaRegQ(a,b)
  // Computes the Q version of the regularized gamma
  // function for `a` divisible by 1/2
```

```

if a==0: return infinity
if a<0: return error
mul=pow(b,a)*exp(-b)
// NOTE: All uses of this function assume `a` is divisible
// by 1/2. For general `a`, replace `GammaOfHalfInteger(a * 2)`
// with a call to the full-fledged gamma function like
// `gamma(a)`.
mul = mul / GammaOfHalfInteger(a * 2)
// NOTE: Continued fraction calculation technique
// described in Thompson and Barnett, "Coulomb and
// Bessel functions of complex arguments and order",
// June 1986.
ret=ALMOSTZERO // For example, 10^-100
dLast=0
cLast=ret
i=0
while i < 100
  // Get next convergent of continued fraction
  if i==0
    num=1.0
    den=1.0-a+b
    dencount=3.0
    numcount=1.0
  else
    num=numcount*(a-numcount)
    den=dencount-a+b
    dencount+=2.0
    numcount+=1.0
  end
  // Calculate more of continued fraction
  c=den+num/cLast
  d=den+num*dLast
  if d==0: d=ALMOSTZERO
  if c==0: c=ALMOSTZERO
  d=1.0/d
  delta=d*c
  ret*=delta
  // For example 10^-14
  if abs(delta-1.0)<EPSILON: break
  dLast=d
  cLast=c
  i=i+1
end
return mul*ret
END METHOD

METHOD ChiSquaredTest(probabilities, counts)
  if size(probabilities)!=size(counts): return error
  // Calculate number of samples
  numSamples=0
  i=0
  while i<size(counts)
    numSamples=numSamples+counts[i]
    i=i+1
  end
  // Calculate chi-squared statistic
  chisq=0
  i=0
  while i<size(probabilities)
    ex=probabilities[i]*numSamples*1.0
    chisq=chisq+pow(counts[i]-ex,2)/ex
    i=i+1
  end

```

```
end
// Calculate p-value
rga=(size(probabilities)-1)*0.5
pvalue=GammaRegQ(rga,chisq*0.5)
// Return statistic and p-value as a list
return [chisq, pvalue]
END METHOD
```