

Tutorial 5Ques

BFS

- Breadth First Search
- BFS uses queue to find the shortest path
- BFS is better when target is closer to source
- As BFS considers all neighbours so it is not suitable for decision
- BFS is slower than DFS

DFS

- Depth First Search
- It uses stack to find the shortest path.
- DFS is better when target is far from source
- DFS is more suitable for decision tree. As with one decision we need to traverse further to argument for decision. If we search for conclusion.

Application of DFS

- Using DFS we can find path b/w two vertices.
- we can perform topological sorting which is used to scheduling jobs.
- we can use DFS to detect cycles.
- Using DFS, we can find strongly connected components of a graph.

Application of BFS:-

- BFS may also used to detect cycles.
- finding shortest path and minimal spanning tree in unweighted graphs.
- In networking finding a route for packet transmission.

- Finding a route through GPS navigation system.

Que 2.

BFS uses Queue data structure. In BFS you make any node in the graph as source node and start traversing from it. BFS traverses all the nodes in the graph and keeps dropping them as completed. BFS visits an adjacent unvisited node, marks it as done & inserts it into queue.

DFS uses stack data structure because DFS traverses a graph in a depthward motion and uses a stack to remember to get the next vertex to start a search, when a dead end occurs in any iteration.

Que 3 Sparse Graph:- A graph in which the number of edge is much less than the possible no. of edges.

Dense Graph:- A dense graph is a graph in which the no. of edges is close to the maximal no. of edges of edges.

→ If the graph is sparse, we should store it as list of edges.

Alternatively, if a graph is dense, we should store it as a adjacency matrix.

Q.4

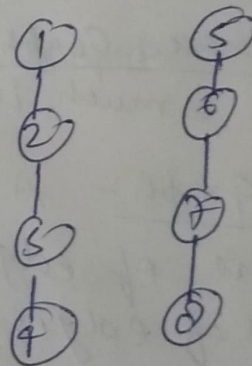
DFS can be used to detect cycle in a graph. DFS for a connected graph, produces a tree. There is a cycle in a graph only if there is a back edge present in the graph. A back edge is an edge that is formed from a node to itself or one of its ancestor in the tree produced by DFS.

BFS can also be used to detect cycles. Just perform BFS while keeping a list of previous nodes at each node visited or else constructing a tree from the starting node. If I visit a node that is already marked by BFS, I found a cycle.

Ques 5 Disjoint set data structures:-

- It allows to find out whether the two elements are in the same set or not efficiently.
- A disjoint set can be defined as the subsets when there is no common element b/w two sets.

e.g. $S_1 = \{1, 2, 3, 4\}$
 $S_2 = \{5, 6, 7, 8\}$



operations performed

(i) find:-

```

int find (int v)
{
    if (v == parent[v])
        return v;
    return parent[v] = find (parent[v]);
}
  
```

Union:-

```

void union (int a, int b)
{
    a = find(a)
    b = find(b)
  
```

if (a != b)

{ if (size[a] < size[b])

{ swap(a, b)

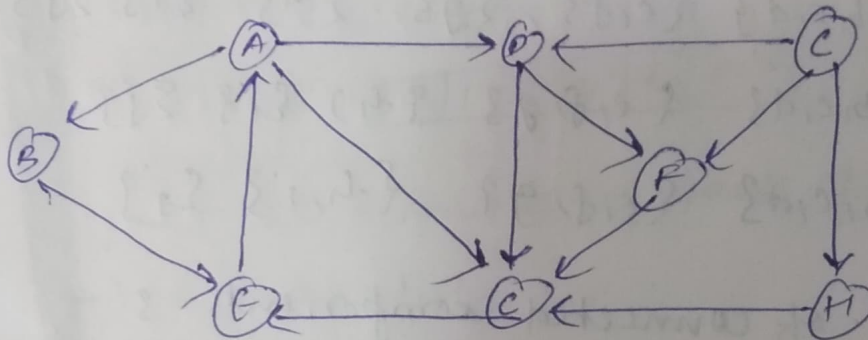
parent[b] = a;

size[a] += size[b];

}

}

Que 6



BFS:- Node :- B E C A D F

parent:- - B B E A D

path:- B → E → A → D → F

DPS:-

Node processed B B C E A D F

Stack B CE EE EE DE FE E

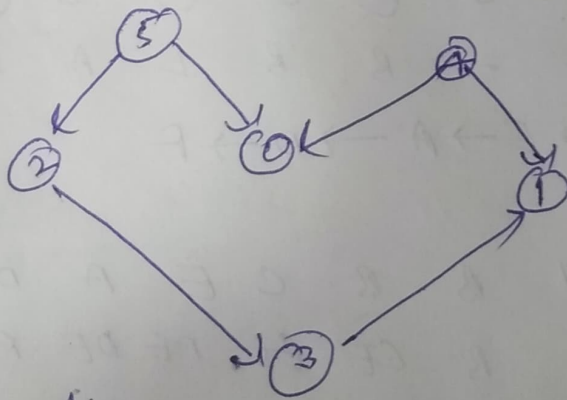
path:- B → C → E → A → D → F

Que 7

$V = \{a\} \cup \{b\} \cup \{c\} \cup \{d\} \cup \{e\} \cup \{f\} \cup \{g\} \cup \{h\} \cup \{i\} \cup \{j\}$
 $E = \{a,b\}, \{a,c\}, \{b,c\} \cup \{b,d\}, \{e,f\}, \{e,g\},$
 $\{h,i\} \cup \{j\}$

(a,b) $\{a,b\} \cup \{c\} \cup \{d\} \cup \{e\} \cup \{f\} \cup \{g\} \cup \{h\} \cup \{i\} \cup \{j\}$
 (a,c) $\{a,b,c\} \cup \{d\} \cup \{e\} \cup \{f\} \cup \{g\} \cup \{h\} \cup \{i\} \cup \{j\}$
 (b,c) $\{a,b,c\} \cup \{d\} \cup \{e\} \cup \{f\} \cup \{g\} \cup \{h\} \cup \{i\} \cup \{j\}$
 (b,d) $\{a,b,c,d\} \cup \{e\} \cup \{f\} \cup \{g\} \cup \{h\} \cup \{i\} \cup \{j\}$
 (e,f) $\{a,b,c,d\} \cup \{e,f\}, \{g\} \cup \{h\} \cup \{i\} \cup \{j\}$
 (e,g) $\{a,b,c,d\} \cup \{e,f,g\} \cup \{h\} \cup \{i\} \cup \{j\}$
 (h,i) $\{a,b,c,d\} \cup \{e,f,g\} \cup \{h,i\} \cup \{j\}$
 No. of connected components = 3

Ques



Adjacency list

0 →
 1 →
 2 → 3
 3 → 1
 4 → 0, 1
 5 → 2, 0

0	1	2	3	4	5
visited	visited	visited	visited	visited	visited
false	false	false	false	false	false

stack (empty)

Step 1:- Topological sort(0), visited[0] = true

Stack [0]

Step 2:- Topological sort(1), visited[1] = true.

Stack [0 | 1]

Step 3:- topological sort(2), visited[2] = true

Topological sort(3), visited[3] = true

Stack [0 | 1 | 3 | 2]

Step 4:- Stack [0 | 1 | 3 | 2 | 4]

Step 5:- Stack [0 | 1 | 3 | 2 | 4 | 5]

Step 6:- Print all elements of stack from top to bottom

→ 5, 4, 2, 3, 1, 0

Que 9 Algorithms that uses Priority Queue

(i) Dijkstra's shortest path algorithm using priority queue

When graph is sorted in the form of list or matrix, priority queue can be used to extract minimum efficiency when implementing Dijkstra's Algo.

(ii) Prim's Algorithm:- It is used to implement Prim's algorithm to store key of nodes to extract minimum key node at every step.

(iii) Data Compression:- It is used in Huffman's code which is used to compress data.

min heap

- In min-heap the key present at root node must be less than or equal to among the keys present at all its children

- uses the ascending priority

- The minimum key present at the root node

max heap

- In max-heap the key present at root node must be greater or equal to the key present at all its children.

- Uses descending priority

- The maximum key present at the root node