

Supplementary Information for Characterization of a two-transmon processor with individual single-shot qubit readout

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S1. Sample preparation

The sample is fabricated on a silicon chip oxidized over 50 nm. A 150 nm thick niobium layer is first deposited by magnetron sputtering and then dry-etched in a SF_6 plasma to pattern the readout resonators, the current lines for frequency tuning, and their ports. Finally, the transmon qubit, the coupling capacitance and the Josephson junctions of the resonators are fabricated by double-angle evaporation of aluminum through a shadow mask patterned by e-beam lithography. The first layer of aluminum is oxidized in a $Ar - O_2$ mixture to form the oxide barrier of the junctions. The chip is glued with wax on a printed circuit board (PCB) and wire bonded to it. The PCB is then screwed in a copper box anchored to the cold plate of a dilution refrigerator.

S2. Sample parameters

The sample is first characterized by spectroscopy (see Fig. 1.b of main text). The incident power used is high enough to observe the resonator frequency ν_R , the qubit line ν_{01} , and the two-photon transition at frequency $\nu_{02}/2$ between the ground and second excited states of each transmon (data not shown). A fit of the transmon model to the data yields the sample parameters $E_J^I/h = 36.2$ GHz, $E_C^I/h = 0.98$ GHz, $d_I = 0.2$, $E_J^{II}/h = 43.1$ GHz, $E_C^{II}/h = 0.87$ GHz, $d_{II} = 0.35$, $\nu_R^I = 6.84$ GHz, and $\nu_R^{II} = 6.70$ GHz. The qubit-readout anticrossing at $\nu = \nu_R$ yields the qubit-readout couplings $g_0^I \simeq g_0^{II} \simeq 50$ MHz. Independent measurements of the resonator dynamics (data not shown) yield quality factors $Q_I = Q_{II} = 730$ and Kerr non linearities [13,[1]] $K_I/\nu_R^I \simeq K_{II}/\nu_R^{II} \simeq -2.3 \pm 0.5 \times 10^{-5}$.

S3. Experimental setup

- **Qubit microwave pulses:** The qubit drive pulses are generated by two phase-locked microwave generators whose continuous wave outputs are fed to a pair of I/Q-mixers. The two IF inputs of each of these mixers are provided by a 4-Channel 1 GS/s arbitrary waveform generator (AWG Tektronix AWG5014). Single-sideband mixing in the frequency range of 50-300 MHz is used to generate multi-tone drive pulses and to obtain a high ON/OFF ratio (> 50 dB) of the signal at the output of the mixers. Phase and amplitude errors of the mixers are corrected by measuring the signals at the output and applying sideband and carrier frequency dependent corrections in amplitude and offset to the IF input channels.
- **Flux Pulses:** The flux control pulses are generated by a second AWG and sent to the chip through a transmission line, equipped with 40 dB of attenuation distributed over different temperature stages and a pair of 1 GHz absorptive low-pass filters at 4 K. The input signal of each flux line is fed back to room temperature through an identical transmission line and measured to compensate the non-ideal frequency response of the line.
- **Readout Pulses:** The pulses for the Josephson bifurcation amplifier (JBA) readouts are generated by mixing the continuous signals of a pair of microwave generators with IF pulses provided by a 1 GS/s arbitrary function generator. Each readout pulse consists of a measurement part with a rise time of 30 ns and a hold time of 100 ns, followed by a $2 \mu s$ long latching part at 90 % of the pulse height.
- **Drive and Measurement Lines:** The drive and readout microwave signals of each qubit are combined and sent to the sample through a pair of transmission lines that are attenuated by 70 dB over different temperature stages and filtered at 4 K and 300 mK. A microwave circulator at 20 mK separates the input signals going to the chip from the reflected signals coming from the chip. The latter are amplified by 36 dB at 4 K by two cryogenic HEMT amplifiers (CIT Cryo 1) with noise temperature 5 K. The reflected readout pulses get further amplified at room temperature and demodulated with the continuous signals of the readout microwave sources. The IQ quadratures of the demodulated signals are sampled at 1 GS/s by a 4-channel Data Acquisition system (Acqiris DC282).

S4. Readout characterization

Errors in our readout scheme are discussed in detail in [13] for a single qubit. First, incorrect mapping $|0\rangle \rightarrow 1$ or $|1\rangle \rightarrow 0$ of the projected state of the qubit to the dynamical state of the resonator can occur, due to the stochastic nature of the switching between the two dynamical states. As shown in Fig. S4.1, the probability p to obtain the outcome 1 varies continuously from 0 to 1 over a certain range of drive power P_d applied to the readout. When the shift in power between the two $p_{|0\rangle,|1\rangle}(P_d)$ curves is not much larger than this range, the two curves overlap and errors are significant even at the optimal drive power where the difference in p is maximum. Second, even in the case of non overlapping $p_{|0\rangle,|1\rangle}(P_d)$ curves, the qubit initially projected in state $|1\rangle$ can relax down to $|0\rangle$ before the end of the measurement, yielding an outcome 0 instead of 1. The probability of these two types of errors vary in opposite directions as a function of the frequency detuning $\Delta = \nu_R - \nu > 0$ between the resonator and the qubit, so that a compromise has to be found for Δ . Besides, the contrast $c = \text{Max}(p_{|1\rangle} - p_{|0\rangle})$ can be increased [12] by shelving state $|1\rangle$ into state $|2\rangle$ with a microwave π pulse at frequency ν_{12} just before the readout resonator pulse. The smallest errors $e_0^{\text{I,II}}$ and $e_1^{\text{I,II}}$ when reading $|0\rangle$ and $|1\rangle$ are found for $\Delta_{\text{I}} = 440$ MHz and $\Delta_{\text{II}} = 575$ MHz and are shown by arrows in the top panels of Fig. S3.2: $e_0^{\text{I}} = 5\%$ and $e_1^{\text{I}} = 13\%$ (contrast $c_{\text{I}} = 1 - e_0^{\text{I}} - e_1^{\text{I}} = 82\%$), and $e_0^{\text{II}} = 5.5\%$ and $e_1^{\text{II}} = 12\%$ ($c_{\text{II}} = 82\%$). When using the $|1\rangle \rightarrow |2\rangle$ shelving before readout, $e_0^{\text{I}} = 2.5\%$ and $e_2^{\text{I}} = 9.5\%$ (contrast $c_{\text{I}} = 1 - e_0^{\text{I}} - e_2^{\text{I}} = 88\%$), and $e_0^{\text{II}} = 3\%$ and $e_2^{\text{II}} = 8\%$ ($c_{\text{II}} = 89\%$). These best results are very close to those obtained in [12], but are unfortunately not relevant to this work.

Indeed, when the two qubits are measured simultaneously, one has also to take into account a possible readout crosstalk, i.e. an influence of the projected state of each qubit on the outcome of the readout of the other qubit. We do observe such an effect and have to minimize it by increasing $\Delta_{\text{I,II}}$ up to ~ 1 GHz with respect to previous optimal values and by not using the shelving technique. An immediate consequence shown in Fig. 3.2 (b) is a reduction of the $c_{\text{I,II}}$ contrasts. The errors when reading $|0\rangle$ and $|1\rangle$ are now $e_0^{\text{I}} = 19\%$ and $e_1^{\text{I}} = 7\%$ (contrast $c_{\text{I}} = 74\%$) and $e_0^{\text{II}} = 19\%$ and $e_1^{\text{II}} = 12\%$ (contrast $c_{\text{II}} = 69\%$). Then to characterize the errors due to crosstalk, we measure the 4×4 readout matrix \mathcal{R} linking the probabilities p_{uv} of the four possible uv outcomes to the population of the four $|uv\rangle$ states. As shown in Fig. S3.2(c-d), we then rewrite $\mathcal{R} = \mathcal{C}_{\text{CT}} \cdot (\mathcal{C}_{\text{I}} \otimes \mathcal{C}_{\text{II}})$ as the product of a 4×4 pure crosstalk matrix \mathcal{C}_{CT} with the tensorial product of the two 2×2 single qubit readout matrices

$$\mathcal{C}_{\text{I,II}} = \begin{pmatrix} 1 - e_0^{\text{I,II}} & e_1^{\text{I,II}} \\ e_0^{\text{I,II}} & 1 - e_1^{\text{I,II}} \end{pmatrix}.$$

We also illustrate on the figure the impact of the readout errors on our swapping experiment by comparing the bare readout outcomes uv , the outcomes corrected from the independent readout errors only, and the $|uv\rangle$ population calculated with the full correction including crosstalk.

We now explain briefly the cause of the readout crosstalk in our processor. Unlike what was observed for other qubit readout schemes using switching detectors [5], the crosstalk we observe is not directly due to an electromagnetic perturbation induced by the switching of one detector that would help or prevent the switching of the other one. Indeed, when both qubits frequencies $\nu_{\text{I,II}}$ are moved far below $\nu_{\text{R}}^{\text{I,II}}$, the readout crosstalk disappears: the switching of a detector has no measurable effect on the switching of the other one. The crosstalk is actually due to the rather strong ac-Stark shift $\sim 2(n_{\text{H}} - n_{\text{L}})g_0^2/(R - \nu_{\text{R}}) \sim 500$ MHz of the qubit frequency when a readout resonator switches from its low to high amplitude dynamical state with $n_{\text{L}} \sim 10$ and $n_{\text{H}} \sim 10^2$ photons, respectively. The small residual effective coupling between the qubits at readout can then slightly shift the frequency of the other resonator, yielding a change of its switching probability by a few percent. Note that coupling the two qubits by a resonator rather than by a fixed capacitor would solve this problem.

S5. Removing errors on tomographic pulses before calculating the gate process map

Tomographic errors are removed from the process map of our $\sqrt{i\text{SWAP}}$ gate using the following method. The measured Pauli sets corresponding to the sixteen input states are first fitted by a model including errors both in the preparation of the state (index *prep*) and in the tomographic pulses (index *tomo*). The errors included are angular errors $\varepsilon_{\text{I,II}}^{\text{prep}}$ on the nominal π rotations around $X_{\text{I,II}}$, $\eta_{\text{I,II}}^{\text{prep,tomo}}$ and $\delta_{\text{I,II}}^{\text{prep,tomo}}$ on the nominal $\pi/2$ rotations around $X_{\text{I,II}}$ and $Y_{\text{I,II}}$, a possible departure $\xi_{\text{I,II}}$ from orthogonality of $(\vec{X}_{\text{I}}, \vec{Y}_{\text{I}})$ and $(\vec{X}_{\text{II}}, \vec{Y}_{\text{II}})$, and a possible rotation $\mu_{\text{I,II}}$ of the tomographic XY frame with respect to the preparation one. The rotation operators used for preparing the states and doing their tomography are thus given by

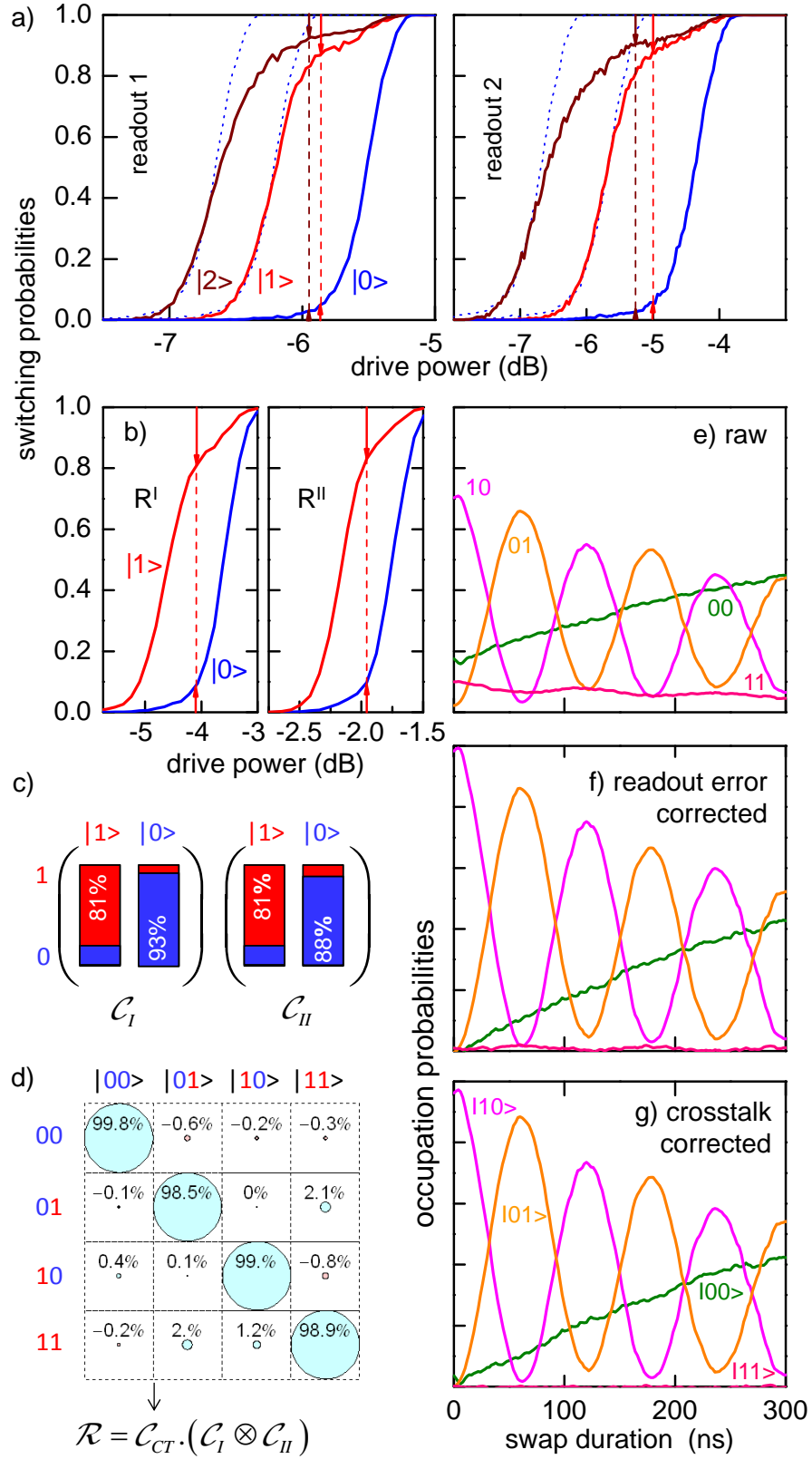


Figure 1: Readout imperfections and their correction. (a) Switching probabilities of the readouts as a function of their driving power, with the qubit prepared in state $|0\rangle$ (blue), $|1\rangle$ (red), or $|2\rangle$ (brown), at the optimal readout points. The arrows and dashed segments indicate the readout errors and contrast, at the power where the later is maximum. (b) Same as (a) but at readout points $R^{I,II}$ used in this work. (c-d) Single readout matrices $\mathcal{C}_{I,II}$ and pure readout crosstalk matrix \mathcal{C}_{CT} characterizing the simultaneous readout of the two qubits. (e-g) bare readout outcomes uv , outcomes corrected from the independent readout errors only, and $|uv\rangle$ population calculated with the full correction including crosstalk for the swapping experiment of Fig. 2.

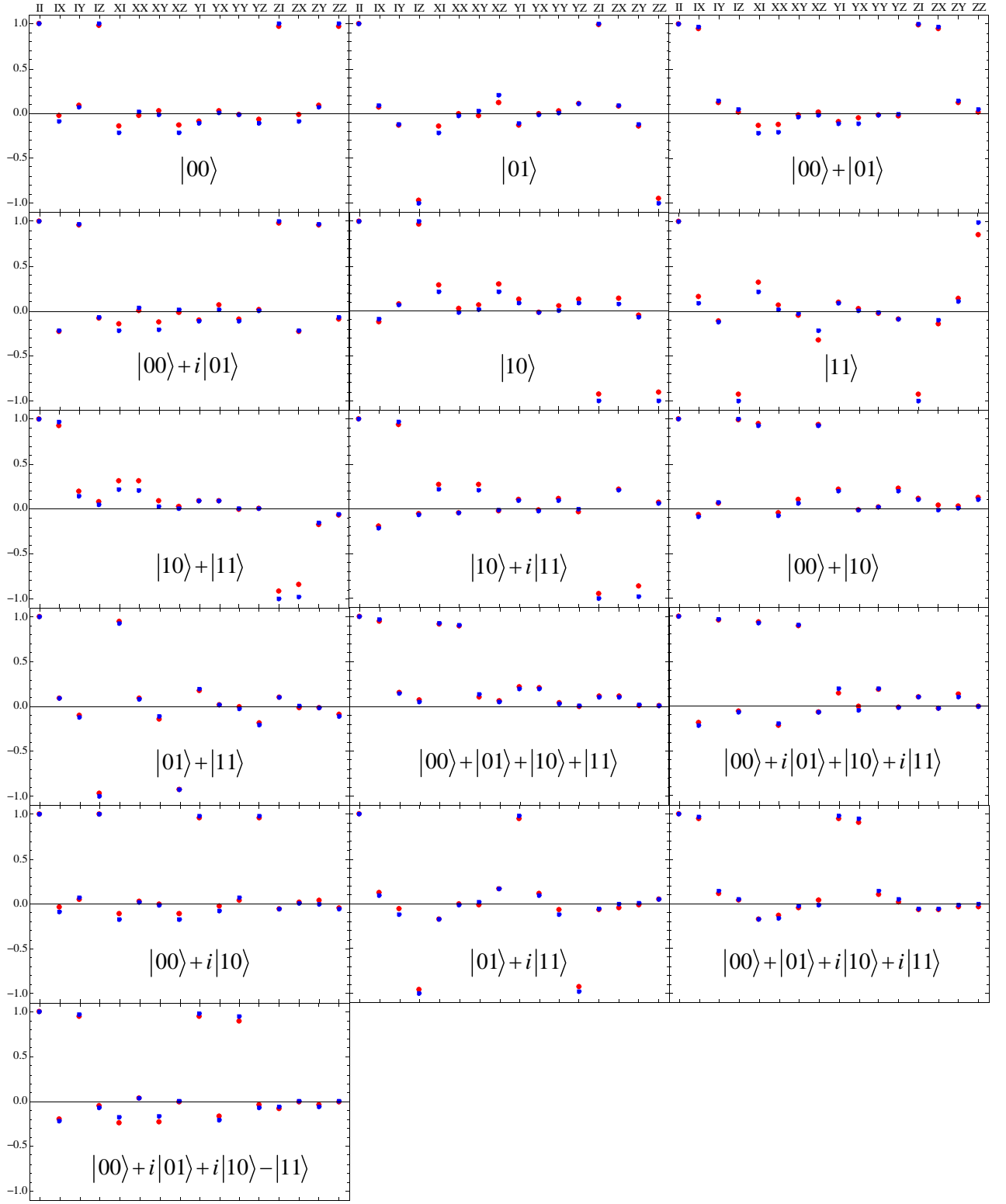


Figure 2: Fitting of the pulse errors at state preparation and tomography. Measured (red) and fitted (blue - see text) Pauli sets $\langle P_k^e \rangle$ for the sixteen targeted input states $\{|0\rangle, |1\rangle, |0\rangle + |1\rangle, |0\rangle + i|1\rangle\}^{\otimes 2}$. The $\{II, IX, IY, IZ, XI, \dots\}$ operators indicated in abscisse are the targeted operators and not those actually measured (due to tomographic errors).

$$\begin{aligned}
X_{I,\Pi}^{\text{prep}}(\pi) &= e^{-i(\pi+\varepsilon_{I,\Pi}^{\text{prep}})\sigma_x^{I,\Pi}/2}, \\
X_{I,\Pi}^{\text{prep}}(-\pi/2) &= e^{+i(\pi/2+\eta_{I,\Pi}^{\text{prep}})\sigma_x^{I,\Pi}/2}, \\
Y_{I,\Pi}^{\text{prep}}(\pi/2) &= e^{-i(\pi/2+\delta_{I,\Pi}^{\text{prep}})[\cos(\xi_{I,\Pi})\sigma_y^{I,\Pi}-\sin(\xi_{I,\Pi})\sigma_x^{I,\Pi}]/2}, \\
X_{I,\Pi}^{\text{tomo}}(\pi/2) &= e^{-i(\pi/2+\eta_{I,\Pi}^{\text{tomo}})[\sin(\mu_{I,\Pi})\sigma_x^{I,\Pi}+\cos(\mu_{I,\Pi})\sigma_y^{I,\Pi}]/2}, \\
Y_{I,\Pi}^{\text{tomo}}(-\pi/2) &= e^{+i(\pi/2+\delta_{I,\Pi}^{\text{tomo}})[\cos(\mu_{I,\Pi}+\xi_{I,\Pi})\sigma_y^{I,\Pi}-\sin(\mu_{I,\Pi}+\xi_{I,\Pi})\sigma_x^{I,\Pi}]/2}.
\end{aligned}$$

The sixteen input states are then $\{\rho_{\text{in}}^e = U|0\rangle\langle 0|U^\dagger\}$ with $\{U\} = \{I_I, X_I^{\text{prep}}(\pi), Y_I^{\text{prep}}(\pi/2), X_I^{\text{prep}}(-\pi/2)\} \otimes \{I_{II}, X_{II}^{\text{prep}}(\pi), Y_{II}^{\text{prep}}(\pi/2), X_{II}^{\text{prep}}(-\pi/2)\}$, and each input state yields a Pauli set $\{\langle P_k^e \rangle = \text{Tr}(\rho_{\text{in}}^e P_k^e)\}$ with $\{P_k^e\} = \{I_I, X_I^e, Y_I^e, Z_I\} \otimes \{I_{II}, X_{II}^e, Y_{II}^e, Z_{II}\}$, $X^e = Y^{\text{tomo}}(-\pi/2)^\dagger \sigma_z Y^{\text{tomo}}(-\pi/2)$, and $Y^e = X^{\text{tomo}}(\pi/2)^\dagger \sigma_z X^{\text{tomo}}(\pi/2)$. Figure S5.1 shows the best fit of the modelled $\{\langle P_k^e \rangle\}$ set to the measured input Pauli sets, yielding $\varepsilon_I^{\text{prep}} = -1^\circ$, $\varepsilon_{II}^{\text{prep}} = -3^\circ$, $\eta_I^{\text{prep}} = 3^\circ$, $\eta_{II}^{\text{prep}} = 4^\circ$, $\delta_I^{\text{prep}} = -6^\circ$, $\delta_{II}^{\text{prep}} = -3^\circ$, $\eta_I^{\text{tomo}} = -6^\circ$, $\eta_{II}^{\text{tomo}} = -4^\circ$, $\lambda_I^{\text{tomo}} = 12^\circ$, $\lambda_{II}^{\text{tomo}} = 5^\circ$, $\xi_I = 1^\circ$, $\xi_{II} = -2^\circ$, and $\mu_I = \mu_{II} = -11^\circ$.

Knowing the tomographic errors and thus $\{\langle P_k^e \rangle\}$, we then invert the linear relation $\{\langle P_k^e \rangle = \text{Tr}(\rho P_k^e)\}$ to find the 16×16 matrix B that links the vector $\overrightarrow{\langle P_k^e \rangle}$ to the columnized density matrix $\overrightarrow{\rho}$, i.e. $\overrightarrow{\rho} = B \cdot \overrightarrow{\langle P_k^e \rangle}$. The matrix B is finally applied to the measured sixteen input and sixteen output Pauli sets to find the sixteen $(\rho_{\text{in}}, \rho_{\text{out}})_k$ couples to be used for calculating the gate map.

[1] F. R. Ong *et al.*, Phys. Rev. Lett. 106, 167002 (2011).