Computer Security

Lecture 2

Classical Encryption Techniques 1

Dr. Mohamed Loey

Lecturer, Faculty of Computers and Information

Benha University

Egypt

Table of Contents

Symmetric Encryption

Substitution Techniques

Caesar Cipher

Monoalphabetic Cipher

Playfair Cipher

Hill Cipher

Table of Contents

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Substitution Techniques

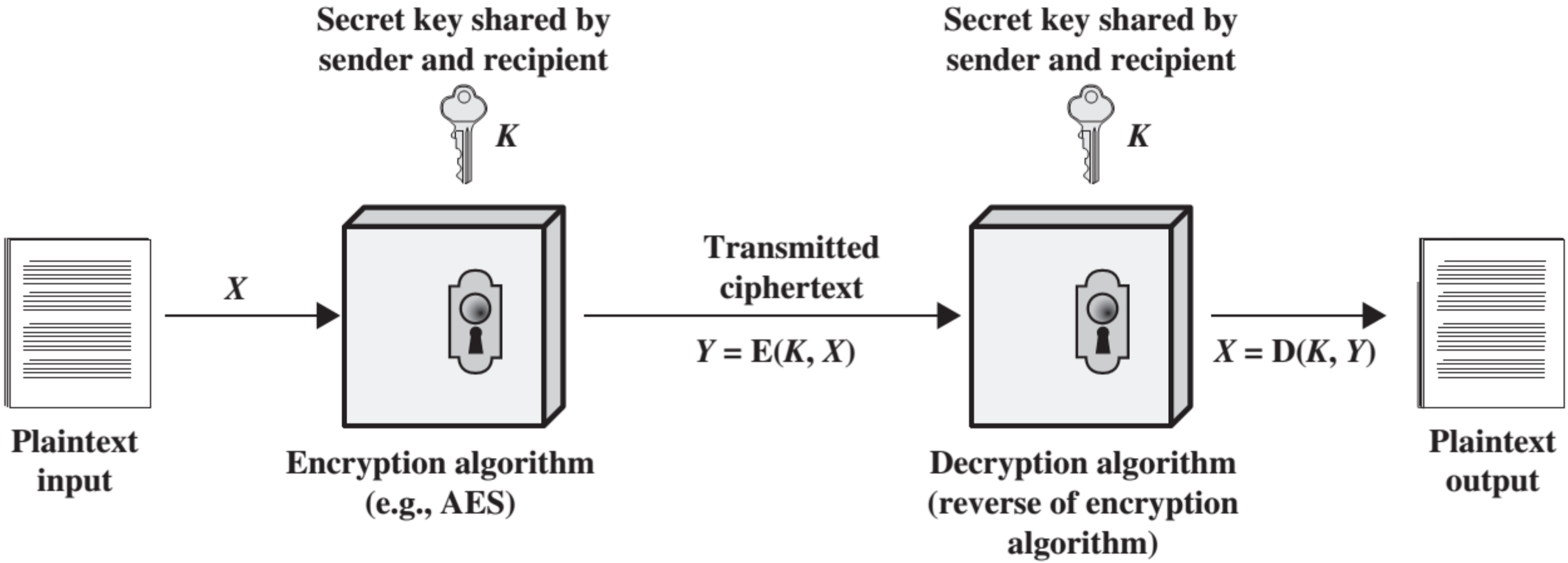
Caesar Cipher

Monoalphabetic Cipher

Playfair Cipher

Hill Cipher

Simplified Model of Symmetric Encryption



Simplified Model of Symmetric Encryption

- Encryption algorithm: The encryption algorithm performs various substitutions and transformations on the plaintext.

- Secret key: The secret key is also input to the encryption algorithm. The key is a value independent of the plaintext and of the algorithm. The algorithm will produce a different output depending on the specific key being used at the time.

Simplified Model of Symmetric Encryption

- Ciphertext: This is the scrambled message produced as output. It depends on the plaintext and the secret key.

- Decryption algorithm: This is essentially the encryption algorithm run in reverse. It takes the ciphertext and the secret key and produces the original plaintext.

Simplified Model of Symmetric Encryption

- Symmetric-key algorithms are algorithms for cryptography that use the same cryptographic keys for both encryption of plaintext and decryption of ciphertext.

Table of Contents

Symmetric Encryption

Substitution Techniques

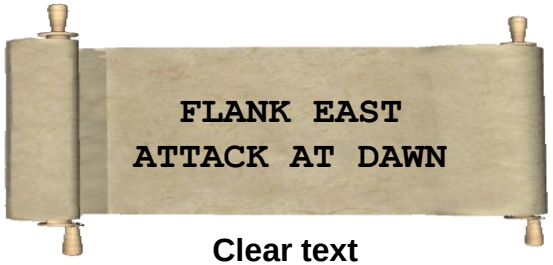
Caesar Cipher

Monoalphabetic Cipher

Playfair Cipher

Hill Cipher

1

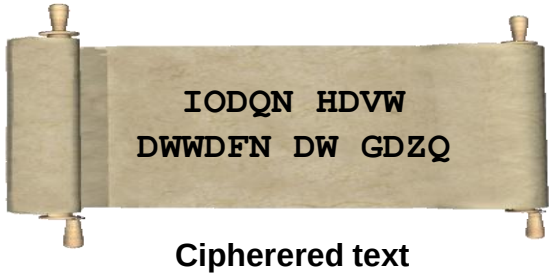


The clear text message would be encoded using a key of 3.

2

Shift the top scroll over by three characters (key of 3), an A becomes D, B becomes E, and so on.

3



The clear text message would be encrypted as follows using a key of 3.

Substitution Techniques

- Caesar Cipher
- Monoalphabetic Ciphers
- Playfair Cipher
- Hill Cipher
- Polyalphabetic Ciphers
- Vigenère Cipher
- Autokey Cipher
- Vernam Cipher

Table of Contents

Symmetric Encryption

Substitution Techniques

Caesar Cipher

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Hill Cipher

- **Caesar Cipher** is one of the simplest and most widely known encryption techniques.

```
plain:  a b c d e f g h i j k l m n o p q r s t u v w x y z
cipher: D E F G H I J K L M N O P Q R S T U V W X Y Z A B C
```

Caesar Cipher

```
plain:  meet me after the toga party
cipher: PHHW PH DIWHU WKH WRJD SDUWB
```

Caesar Cipher Algorithm

a	b	c	d	e	f	g	h	i	j	k	l	m
0	1	2	3	4	5	6	7	8	9	10	11	12

n	o	p	q	r	s	t	u	v	w	x	y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

Caesar Cipher Algorithm

$$C = \mathrm{E}(k, p) = (p + k) \bmod 26$$

$$p = \mathrm{D}(k, C) = (C - k) \bmod 26$$

Caesar Cipher Encrypt Example

- PlainText = dcodex
- K=3

1) P=d
2) P=3
3) C=P+K mod 26=3+3 mod 26=6 mod 26 =6
4) C=g

Caesar Cipher Encrypt Example

- PlainText = dcodex
- K=3

1) P=x
2) P=23
3) C=P+K mod 26=23+3 mod 26=26 mod 26= 0
4) C=a

Caesar Cipher Encrypt Example

- P= dcodex
- C= gfrgha
- K=3

Caesar Cipher Decrypt Example

- CipherText = gfrgha
- K=3

1) C=g
2) C=6
3) P=C-K mod 26=6-3 mod 26=3
4) P=d

Caesar Cipher Decrypt Example

- CipherText = gfrgha
- K=3

1) C=a
2) C=0
3) P=C-K mod 26=0-3 mod 26=-3 mod 26 =23
4) P=x

Caesar Cipher Decrypt Example

- C= gfrgha
- P= dcodex
- K=3

Bruteforce Cryptanalysis

- Three important characteristics of this problem enabled us to use a bruteforce cryptanalysis:
  - The encryption and decryption algorithms are known.
  - There are only 25 keys to try.
  - The language of the plaintext is known and easily recognizable.

Bruteforce Cryptanalysis

KEY	PHHW PH DIWHU WKH WRJD SDUWB
1	oggv og chvgt vjg vqic rctva
2	nffu nf bgufs uif uphb qbsuz
3	meet me after the toga party
4	ldds ld zesdq sgd snfz ozqsx
5	kccr kc ydrcp rfc rmey nyprw
6	jbbq jb xcqbo qeb qldx mxoqv
7	iaap ia wbpan pda pkcw lwnpu
8	hzzo hz vaozm ocz ojbv kvmot
9	gyyn gy uznyl nby niau julns
10	fxxm fx tymxk max mhzt itkmr
11	ewwl ew sxlwj lzw lgys hsjlq
12	dvvk dv rwkvi kyv kfxr grikp
13	cuuj cu qvjuh jxu jewq fqhjo
14	btti bt puitg iwt idvp epgin
15	assh as othsf hvs hcuo dofhm
16	zrrg zr nsgre gur gbtn cnegl
17	yqqf yq mrfqd ftq fasm bmdfk
18	xppe xp lqepc esp ezrl alcej
19	wood wo kpdob dro dyqk zkbdi
20	vnnc vn jocna cqn cxpj yjach
21	ummb um inbmz bpm bwoi xizbg
22	tlla tl hmaly aol avnh whyaf
23	skkz sk glzkx znk zumg vgxze
24	rjjy rj fkyjw ymj ytlf ufwyd
25	qiix qi ejxiv xli xske tevxc

- **How to implement Caesar Cipher technique on Arabic letters?**

Table of Contents

Symmetric Encryption

Substitution Techniques

Caesar Cipher

Monoalphabetic Cipher

Playfair Cipher

Hill Cipher

Monoalphabetic Cipher

- A **monoalphabetic cipher** uses fixed substitution over the entire message

- Random Key

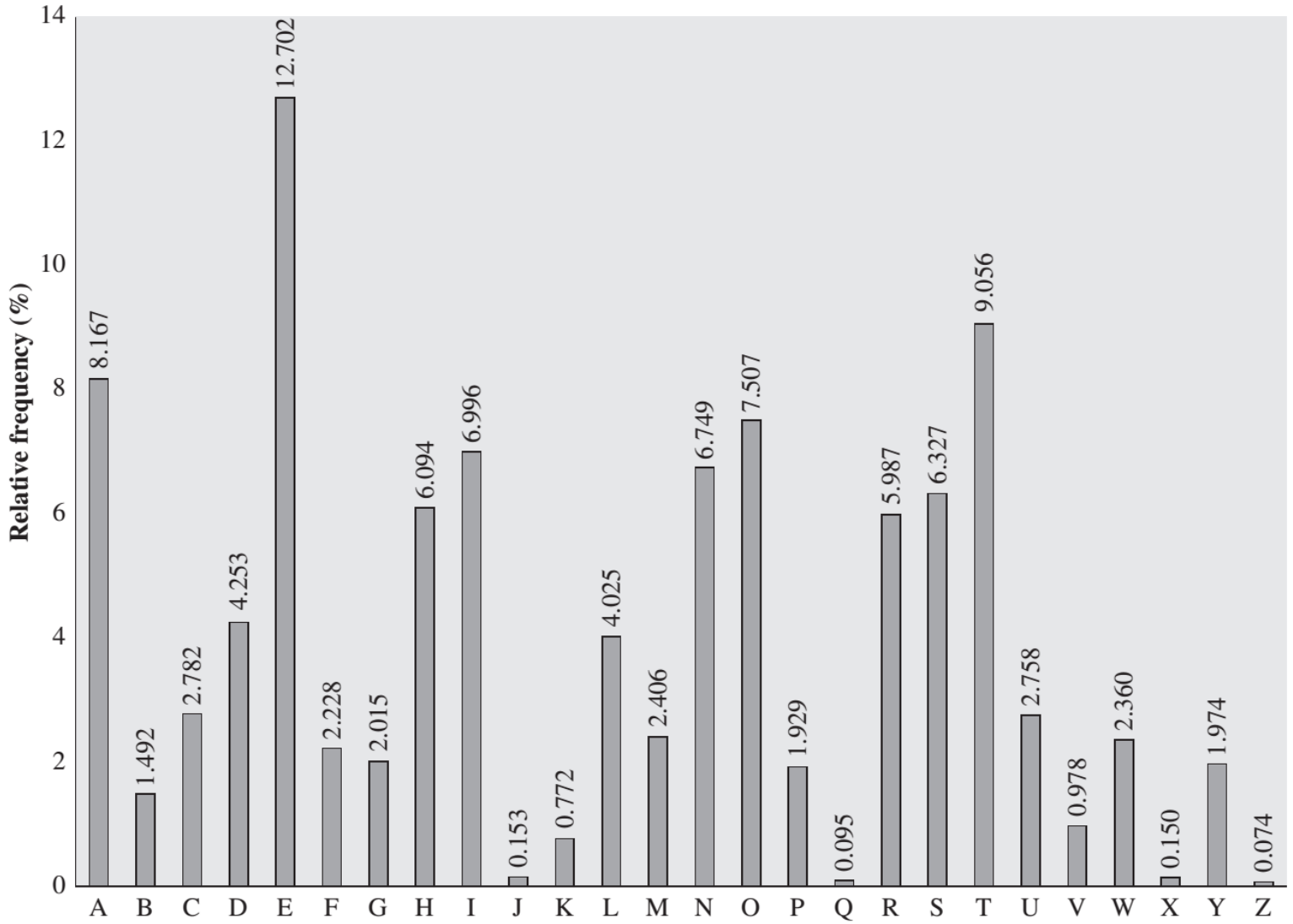
Monoalphabetic Cipher

- Example:
  - Plaintext alphabets: ABCDEFGHIJKLMNOPQRSTUVWXYZ
  - Ciphertext alphabet: ZEBRASCDFGHIJKLMNOPQTUVWXY

- P= ITEMS
- Encoding
- C= FQAIP
- Decoding
- P= ITEMS

Monoalphabetic Cipher Cryptanalysis

- Relative Frequency of Letters in English Text



Monoalphabetic Cipher Cryptanalysis

- C= UZQSOVUOHXMOPVGPOZPEVSGZWSZOPFPESXUDBMETSXAIZ
  VUEPHZHMDZSHZOWSFPAPPDTSVPQUZWYMXUZUHSX
  EPYEPOPDZSZUFPOMBZWPFUPZHMDJUDTMOHMQ

P 13.33	H 5.83	F 3.33	B 1.67	C 0.00
Z 11.67	D 5.00	W 3.33	G 1.67	K 0.00
S 8.33	E 5.00	Q 2.50	Y 1.67	L 0.00
U 8.33	V 4.17	T 2.50	I 0.83	N 0.00
O 7.50	X 4.17	A 1.67	J 0.83	R 0.00
M 6.67				

Monoalphabetic Cipher Cryptanalysis

- cipher letters P and Z are the equivalents of plain letters e and t

```
UZQSOVUOHXMOPVGPOZPEVSGZWSZOPFPESXUDBMETSXAIZ
 t a          e  e te  a that e e a        a
VUEPHZHMDZSHZOWSFPAPPDTSVPQUZWYMXUZUHSX
   e t   ta t ha e ee  a e  th    t  a
EPYEPOPDZSZUFPOMBZWPFUPZHMDJUDTMOHMQ
 e  e e tat  e   the   t
```

- Finally, The complete plaintext

```
it was disclosed yesterday that several informal but
direct contacts have been made with political
representatives of the viet cong in moscow
```

- **How to implement Monoalphabetic Cipher technique on Arabic letters?**

Table of Contents

Symmetric Encryption

Substitution Techniques

Caesar Cipher

Monoalphabetic Cipher

Playfair Cipher

Hill Cipher

Playfair Cipher

- The Playfair system was invented by Charles Wheatstone, who first described it in 1854.
- Used by many countries during wartime
- The Playfair algorithm is based on the use of a 5 x 5 matrix of letters constructed using a keyword.

- In this case, the keyword is **monarchy**.

M	O	N	A	R
C	H	Y	B	D
E	F	G	I/J	K
L	P	Q	S	T
U	V	W	X	Z

- 4 Rules:

1) If both letters are the same (or only one letter is left), add an "X" after the first letter.

2) If the letters appear on the same row of your table, replace them with the letters to their immediate right respectively

- 4 Rules:

3) If the letters appear on the same column of your table, replace them with the letters immediately below respectively

4) If the letters are not on the same row or column, replace them with the letters on the same row respectively but at the other pair of corners of the rectangle defined by the original pair.

Playfair Cipher

- P=Hide the gold in the tree stump (note the null "X" used to separate the repeated "E"s)
- P= HI DE TH EG OL DI NT HE TR EX ES TU MP
- K= playfair example

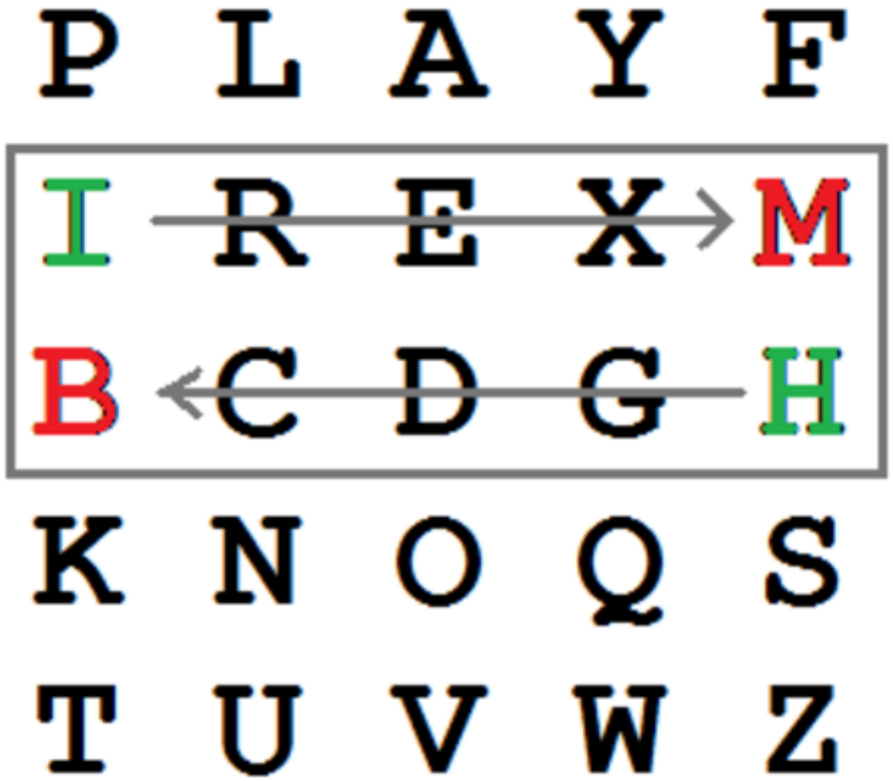
P	L	A	Y	F
I	R	E	X	M
B	C	D	G	H
K	N	O	Q	S
T	U	V	W	Z

- How to build 5x5 Matrix (assuming that I and J are interchangeable), the table becomes (omitted letters in red):

P L A Y F
I R E X M
B C D G H
K N O Q S
T U V W Z

- P= HI DE TH EG OL DI NT HE TR EX ES TU MP

1. The pair HI forms a rectangle, replace it with BM



HI

Shape: Rectangle
Rule: Pick Same Rows, Opposite Corners

BM

- P= HI DE TH EG OL DI NT HE TR EX ES TU MP

2. The pair DE is in a column, replace it with OD

P	L	A	Y	F
I	R	E	X	M
B	C	D	G	H
K	N	O	Q	S
T	U	V	W	Z

DE

Shape: Column
Rule: Pick Items Below Each Letter, Wrap to Top if Needed

OD

- P= HI DE TH EG OL DI NT HE TR EX ES TU MP

3. The pair TH forms a rectangle, replace it with ZB

P	L	A	Y	F
I	R	E	X	M
B	C	D	G	H
K	N	O	Q	S
T	U	V	W	Z

TH

Shape: Rectangle
Rule: Pick Same Rows, Opposite Corners

ZB

- P= HI DE TH EG OL DI NT HE TR EX ES TU MP

4. The pair EG forms a rectangle, replace it with XD

P	L	A	Y	F
I	R	E	X	M
B	C	D	G	H
K	N	O	Q	S
T	U	V	W	Z

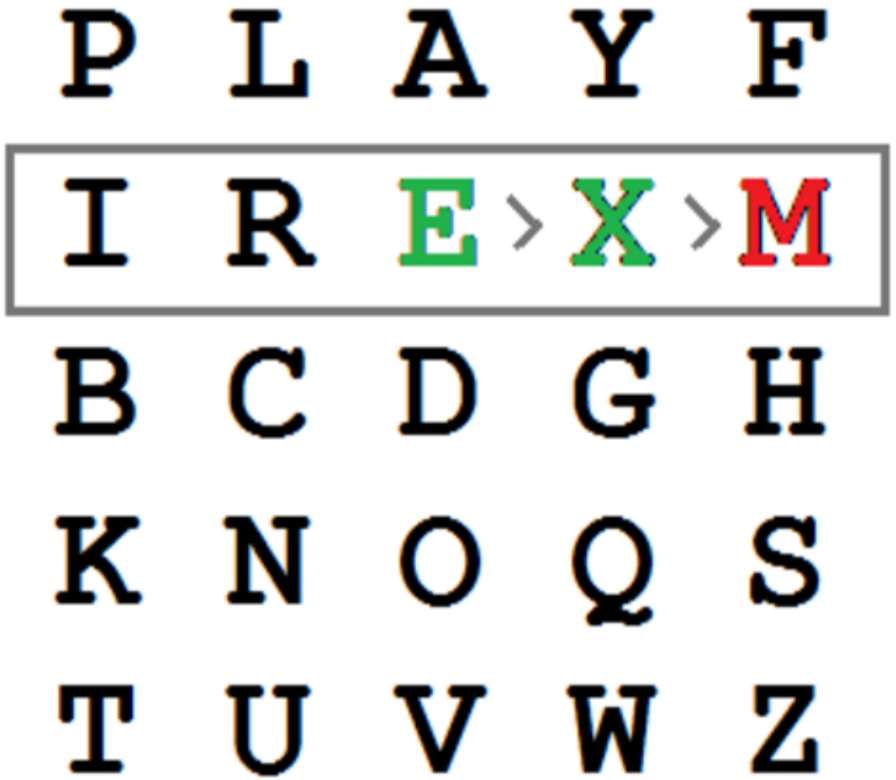
EG

Shape: Rectangle
Rule: Pick Same Rows, Opposite Corners

XD

- P= HI DE TH EG OL DI NT HE TR EX ES TU MP

10. The pair EX (X inserted to split EE) is in a row, replace it with XM



EX

Shape: Row
Rule: Pick Items to Right of Each Letter, Wrap to Left if Needed

XM

Playfair Cipher

- C= BM OD ZB XD NA BE KU DM UI XM MO UV IF

- the message "Hide the gold in the tree stump" becomes "BMODZ BXDNA BEKUD MUIXM MOUVI F"

- Using Playfair Cipher how to decrepit the following cipher text:

C= "BMODZ BXDNA BEKUD MUIXM MOUVI F"

K= playfair example

Table of Contents

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Hill Cipher

- The Hill Cipher was invented by Lester S. Hill in 1929
- The Hill Cipher based on linear algebra
- Encryption
  - 2 x 2 Matrix Encryption
  - 3 x 3 Matrix Encryption

Hill Cipher

- square matrix M by the equation $MM^{-1} = M^{-1}M = I$, where I is the identity matrix.

- C = P*K mod 26

Hill Cipher

a	b	c	d	e	f	g	h	i	j	k	l	m
0	1	2	3	4	5	6	7	8	9	10	11	12

n	o	p	q	r	s	t	u	v	w	x	y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

Hill Cipher Encryption

- Example of Key 2 x 2

- $K = \begin{pmatrix} H & I \\ L & L \end{pmatrix} = \begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix}$

- plaintext message "short example“

- P= short example

- $P = \begin{pmatrix} S \\ h \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 18 \\ 7 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$

Hill Cipher Encryption

- $P = \begin{pmatrix} S \\ h \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 18 \\ 7 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$
- $C = K * P \ mod \ 26$
- $\begin{bmatrix} k_0 & k_1 \\ k_2 & k_3 \end{bmatrix} * \begin{bmatrix} p_0 \\ p_1 \end{bmatrix} = \begin{bmatrix} k_0 * p_0 + k_1 * p_1 \\ k_2 * p_0 + k_3 * p_1 \end{bmatrix}$
- $\begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} * \begin{bmatrix} 18 \\ 7 \end{bmatrix} = \begin{bmatrix} 7 * 18 + 8 * 7 \\ 11 * 18 + 11 * 7 \end{bmatrix} = \begin{bmatrix} 182 \\ 275 \end{bmatrix}$
- $C = \begin{bmatrix} 182 \\ 275 \end{bmatrix} mod \ 26 = \begin{bmatrix} 0 \\ 15 \end{bmatrix} = \begin{bmatrix} a \\ p \end{bmatrix}$

- $P = \begin{pmatrix} S \\ h \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 18 \\ 7 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix}$$

$$7 \times 14 + 8 \times 17 = 234$$

$$11 \times 14 + 11 \times 17 = 341$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} = \begin{pmatrix} 234 \\ 341 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} = \begin{pmatrix} 234 \\ 341 \end{pmatrix} = \begin{pmatrix} 0 \\ 3 \end{pmatrix} \ mod\ 26$$

$$\begin{pmatrix} H & I \\ L & L \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} = \begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} = \begin{pmatrix} 234 \\ 341 \end{pmatrix} = \begin{pmatrix} 0 \\ 3 \end{pmatrix} \ mod\ 26 = \begin{pmatrix} A \\ D \end{pmatrix}$$

- $P = \begin{pmatrix} S \\ h \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 18 \\ 7 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix}$$

$$7 \times 19 + 8 \times 4 = 165$$

$$11 \times 19 + 11 \times 4 = 253$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} = \begin{pmatrix} 165 \\ 253 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} = \begin{pmatrix} 165 \\ 253 \end{pmatrix} = \begin{pmatrix} 9 \\ 19 \end{pmatrix} \ mod\ 26$$

$$\begin{pmatrix} H & I \\ L & L \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} = \begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} = \begin{pmatrix} 165 \\ 253 \end{pmatrix} = \begin{pmatrix} 9 \\ 19 \end{pmatrix} \ mod\ 26 = \begin{pmatrix} J \\ T \end{pmatrix}$$

- $P = \begin{pmatrix} S \\ h \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 18 \\ 7 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix}$$

$$7 \times 23 + 8 \times 0 = 161$$

$$11 \times 23 + 11 \times 0 = 253$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} = \begin{pmatrix} 161 \\ 253 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} = \begin{pmatrix} 161 \\ 253 \end{pmatrix} = \begin{pmatrix} 5 \\ 19 \end{pmatrix} \ mod\ 26$$

$$\begin{pmatrix} H & I \\ L & L \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} = \begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} = \begin{pmatrix} 161 \\ 253 \end{pmatrix} = \begin{pmatrix} 5 \\ 19 \end{pmatrix} \ mod\ 26 = \begin{pmatrix} F \\ T \end{pmatrix}$$

- $P = \begin{pmatrix} S \\ h \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 18 \\ 7 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix}$$

$$7 \times 12 + 8 \times 15 = 204$$

$$11 \times 12 + 11 \times 15 = 297$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} = \begin{pmatrix} 204 \\ 297 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} = \begin{pmatrix} 204 \\ 297 \end{pmatrix} = \begin{pmatrix} 22 \\ 11 \end{pmatrix} \ mod\ 26$$

$$\begin{pmatrix} H & I \\ L & L \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} = \begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} = \begin{pmatrix} 204 \\ 297 \end{pmatrix} = \begin{pmatrix} 22 \\ 11 \end{pmatrix} \ mod\ 26 = \begin{pmatrix} W \\ L \end{pmatrix}$$

- $P = \begin{pmatrix} S \\ h \end{pmatrix} \begin{pmatrix} o \\ r \end{pmatrix} \begin{pmatrix} t \\ e \end{pmatrix} \begin{pmatrix} x \\ a \end{pmatrix} \begin{pmatrix} m \\ p \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 18 \\ 7 \end{pmatrix} \begin{pmatrix} 14 \\ 17 \end{pmatrix} \begin{pmatrix} 19 \\ 4 \end{pmatrix} \begin{pmatrix} 23 \\ 0 \end{pmatrix} \begin{pmatrix} 12 \\ 15 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix}$$

$$7 \times 11 + 8 \times 4 = 109$$

$$11 \times 11 + 11 \times 4 = 165$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix} = \begin{pmatrix} 109 \\ 165 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix} = \begin{pmatrix} 109 \\ 165 \end{pmatrix} = \begin{pmatrix} 5 \\ 9 \end{pmatrix} \ mod\ 26$$

$$\begin{pmatrix} H & I \\ L & L \end{pmatrix} \begin{pmatrix} l \\ e \end{pmatrix} = \begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} \begin{pmatrix} 11 \\ 4 \end{pmatrix} = \begin{pmatrix} 109 \\ 165 \end{pmatrix} = \begin{pmatrix} 5 \\ 9 \end{pmatrix} \ mod\ 26 = \begin{pmatrix} F \\ J \end{pmatrix}$$

Hill Cipher Encryption

- $C = \binom{a}{p}\binom{a}{d}\binom{j}{t}\binom{f}{t}\binom{w}{l}\binom{f}{j}$
- This gives us a final ciphertext of "APADJ TFTWLFJ"

Hill Cipher Decryption

- $C = \binom{a}{p}\binom{a}{d}\binom{j}{t}\binom{f}{t}\binom{w}{l}\binom{f}{j}$
- This gives us a final ciphertext of "APADJ TFTWLFJ“
- $K = \begin{pmatrix} H & I \\ L & L \end{pmatrix} = \begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix}$
- We want to find K^{-1}

- $Step\ 1\ -\ Find\ the\ Multiplicative\ Inverse\ of\ the\ Determinant$
  - $D(K) = 7 * 11 - 8 * 11 = -11\ mod\ 26 = 15$
  - $DD^{-1} = 1\ mod\ 26 = 15 * D^{-1}$
  - $15 * D^{-1} mod\ 26 = 1$
  - Try and Test $1\ mod\ 26 = 105$
  - 105 mod 26 =1
  - $D^{-1} = 7$

- *Step 2 – Find the Adjugate Matrix of Key*

$$adj\begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} d & -b \\ -c & a \end{pmatrix}$$

$$adj\begin{pmatrix} 7 & 8 \\ 11 & 11 \end{pmatrix} = \begin{pmatrix} 11 & -8 \\ -11 & 7 \end{pmatrix} \bmod 26 = \begin{pmatrix} 11 & 18 \\ 15 & 7 \end{pmatrix}$$

- *Step 3 Multiply the Multiplicative Inverse of the Determinant by the Adjugate Matrix*

- $7 * \begin{pmatrix} 11 & 18 \\ 15 & 7 \end{pmatrix} = \begin{pmatrix} 77 & 126 \\ 105 & 49 \end{pmatrix} mod\ 26 = \begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} = K^{-1}$

- $C = \begin{pmatrix} a \\ p \end{pmatrix} \begin{pmatrix} a \\ d \end{pmatrix} \begin{pmatrix} j \\ t \end{pmatrix} \begin{pmatrix} f \\ t \end{pmatrix} \begin{pmatrix} w \\ l \end{pmatrix} \begin{pmatrix} f \\ j \end{pmatrix} = \begin{pmatrix} 0 \\ 15 \end{pmatrix} \begin{pmatrix} 0 \\ 3 \end{pmatrix} \begin{pmatrix} 9 \\ 19 \end{pmatrix} \begin{pmatrix} 5 \\ 19 \end{pmatrix} \begin{pmatrix} 22 \\ 11 \end{pmatrix} \begin{pmatrix} 5 \\ 9 \end{pmatrix}$

$$\begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} A \\ P \end{pmatrix} = \begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} 0 \\ 15 \end{pmatrix}$$

$$= \begin{pmatrix} 25 \times 0 + 22 \times 15 \\ 1 \times 0 + 23 \times 15 \end{pmatrix}$$

$$= \begin{pmatrix} 330 \\ 345 \end{pmatrix}$$

$$= \begin{pmatrix} 18 \\ 7 \end{pmatrix} \ mod\ 26$$

$$= \begin{pmatrix} S \\ h \end{pmatrix}$$

- $C = \begin{pmatrix} a \\ p \end{pmatrix} \begin{pmatrix} a \\ d \end{pmatrix} \begin{pmatrix} j \\ t \end{pmatrix} \begin{pmatrix} f \\ t \end{pmatrix} \begin{pmatrix} w \\ l \end{pmatrix} \begin{pmatrix} f \\ j \end{pmatrix} = \begin{pmatrix} 0 \\ 15 \end{pmatrix} \begin{pmatrix} 0 \\ 3 \end{pmatrix} \begin{pmatrix} 9 \\ 19 \end{pmatrix} \begin{pmatrix} 5 \\ 19 \end{pmatrix} \begin{pmatrix} 22 \\ 11 \end{pmatrix} \begin{pmatrix} 5 \\ 9 \end{pmatrix}$

$$\begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} A \\ D \end{pmatrix} = \begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} 0 \\ 3 \end{pmatrix}$$

$$= \begin{pmatrix} 25 \times 0 + 22 \times 3 \\ 1 \times 0 + 23 \times 3 \end{pmatrix}$$

$$= \begin{pmatrix} 66 \\ 69 \end{pmatrix}$$

$$= \begin{pmatrix} 14 \\ 17 \end{pmatrix} \ mod\ 26$$

$$= \begin{pmatrix} o \\ r \end{pmatrix}$$

- $C = \begin{pmatrix} a \\ p \end{pmatrix} \begin{pmatrix} a \\ d \end{pmatrix} \begin{pmatrix} j \\ t \end{pmatrix} \begin{pmatrix} f \\ t \end{pmatrix} \begin{pmatrix} w \\ l \end{pmatrix} \begin{pmatrix} f \\ j \end{pmatrix} = \begin{pmatrix} 0 \\ 15 \end{pmatrix} \begin{pmatrix} 0 \\ 3 \end{pmatrix} \begin{pmatrix} 9 \\ 19 \end{pmatrix} \begin{pmatrix} 5 \\ 19 \end{pmatrix} \begin{pmatrix} 22 \\ 11 \end{pmatrix} \begin{pmatrix} 5 \\ 9 \end{pmatrix}$

$$\begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} J \\ T \end{pmatrix} = \begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} 9 \\ 19 \end{pmatrix}$$

$$= \begin{pmatrix} 25 \times 9 + 22 \times 19 \\ 1 \times 9 + 23 \times 19 \end{pmatrix}$$

$$= \begin{pmatrix} 643 \\ 446 \end{pmatrix}$$

$$= \begin{pmatrix} 19 \\ 4 \end{pmatrix} \ mod\ 26$$

$$= \begin{pmatrix} t \\ e \end{pmatrix}$$

- $C = \begin{pmatrix} a \\ p \end{pmatrix} \begin{pmatrix} a \\ d \end{pmatrix} \begin{pmatrix} j \\ t \end{pmatrix} \begin{pmatrix} f \\ t \end{pmatrix} \begin{pmatrix} w \\ l \end{pmatrix} \begin{pmatrix} f \\ j \end{pmatrix} = \begin{pmatrix} 0 \\ 15 \end{pmatrix} \begin{pmatrix} 0 \\ 3 \end{pmatrix} \begin{pmatrix} 9 \\ 19 \end{pmatrix} \begin{pmatrix} 5 \\ 19 \end{pmatrix} \begin{pmatrix} 22 \\ 11 \end{pmatrix} \begin{pmatrix} 5 \\ 9 \end{pmatrix}$

$$\begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} F \\ T \end{pmatrix} = \begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} 5 \\ 19 \end{pmatrix}$$

$$= \begin{pmatrix} 25 \times 5 + 22 \times 19 \\ 1 \times 5 + 23 \times 19 \end{pmatrix}$$

$$= \begin{pmatrix} 543 \\ 442 \end{pmatrix}$$

$$= \begin{pmatrix} 23 \\ 0 \end{pmatrix} \ mod\ 26$$

$$= \begin{pmatrix} x \\ a \end{pmatrix}$$

- $C = \begin{pmatrix} a \\ p \end{pmatrix} \begin{pmatrix} a \\ d \end{pmatrix} \begin{pmatrix} j \\ t \end{pmatrix} \begin{pmatrix} f \\ t \end{pmatrix} \begin{pmatrix} w \\ l \end{pmatrix} \begin{pmatrix} f \\ j \end{pmatrix} = \begin{pmatrix} 0 \\ 15 \end{pmatrix} \begin{pmatrix} 0 \\ 3 \end{pmatrix} \begin{pmatrix} 9 \\ 19 \end{pmatrix} \begin{pmatrix} 5 \\ 19 \end{pmatrix} \begin{pmatrix} 22 \\ 11 \end{pmatrix} \begin{pmatrix} 5 \\ 9 \end{pmatrix}$

$$\begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} W \\ L \end{pmatrix} = \begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} 22 \\ 11 \end{pmatrix}$$

$$= \begin{pmatrix} 25 \times 22 + 22 \times 11 \\ 1 \times 22 + 23 \times 11 \end{pmatrix}$$

$$= \begin{pmatrix} 792 \\ 275 \end{pmatrix}$$

$$= \begin{pmatrix} 12 \\ 15 \end{pmatrix} \ mod\ 26$$

$$= \begin{pmatrix} m \\ p \end{pmatrix}$$

- $C = \begin{pmatrix} a \\ p \end{pmatrix} \begin{pmatrix} a \\ d \end{pmatrix} \begin{pmatrix} j \\ t \end{pmatrix} \begin{pmatrix} f \\ t \end{pmatrix} \begin{pmatrix} w \\ l \end{pmatrix} \begin{pmatrix} f \\ j \end{pmatrix} = \begin{pmatrix} 0 \\ 15 \end{pmatrix} \begin{pmatrix} 0 \\ 3 \end{pmatrix} \begin{pmatrix} 9 \\ 19 \end{pmatrix} \begin{pmatrix} 5 \\ 19 \end{pmatrix} \begin{pmatrix} 22 \\ 11 \end{pmatrix} \begin{pmatrix} 5 \\ 9 \end{pmatrix}$

$$\begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} F \\ J \end{pmatrix} = \begin{pmatrix} 25 & 22 \\ 1 & 23 \end{pmatrix} \begin{pmatrix} 5 \\ 9 \end{pmatrix}$$

$$= \begin{pmatrix} 25 \times 5 + 22 \times 9 \\ 1 \times 5 + 23 \times 9 \end{pmatrix}$$

$$= \begin{pmatrix} 323 \\ 212 \end{pmatrix}$$

$$= \begin{pmatrix} 11 \\ 4 \end{pmatrix} \ mod\ 26$$

$$= \begin{pmatrix} l \\ e \end{pmatrix}$$

- Using Hill Cipher how to implement 3x3 matrix encryption ? The key for a hill cipher is a matrix

e.g. $\boldsymbol{k} = \begin{matrix} 2 & 4 & 5 \\ 9 & 2 & 1 \\ 3 & 17 & 7 \end{matrix}$ and **message**= ATTACK AT DAWN

THANKS FOR YOUR TIME