

# Laguerre functions

#Laguerre 陪多項式

$L(n, a, x) = \text{binomial}(a+n, n) * \text{hypergeometric\_M}(-n, a+1, x); L$

$$(n, a, x) \mapsto \binom{a+n}{n} M(-n, a+1, x)$$

#Laguerre 多項式

$L(n, x) = L(n, 0, x)$

#L0

$L(0, x).simplify\_hypergeometric();$

$$1$$

#L1

$L(1, x).simplify\_hypergeometric();$

$$-x + 1$$

#L2

$L(2, x).simplify\_hypergeometric();$

$$\frac{1}{2}x^2 - 2x + 1$$

```
p0 = plot(L(0,x),
(x,-2,10),rgbcolor=hue(0),ymin=-10,ymax=10,legend_label="L_0")
p1 = plot(L(1,x),
(x,-2,10),rgbcolor=hue(0.1),ymin=-10,ymax=10,legend_label="L_1")
p2 = plot(L(2,x),
(x,-2,10),rgbcolor=hue(0.2),ymin=-10,ymax=10,legend_label="L_2")
p3 = plot(L(3,x),
(x,-2,10),rgbcolor=hue(0.3),ymin=-10,ymax=10,legend_label="L_3")
p4 = plot(L(4,x),
(x,-2,10),rgbcolor=hue(0.4),ymin=-10,ymax=10,legend_label="L_4")
p5 = plot(L(5,x),
(x,-2,10),rgbcolor=hue(0.5),ymin=-10,ymax=10,legend_label="L_5")
p6 = plot(L(6,x),
(x,-2,10),rgbcolor=hue(0.6),ymin=-10,ymax=10,legend_label="L_6")
show(p0+p1+p2+p3+p4+p5+p6)
```

