

Simulating the combustion of gaseous fuels

6th OpenFoam Workshop Training Session

Dominik Christ

This presentation shows how to use OpenFoam to simulate gas phase combustion



Overview

Theory

Tutorial case

Solution strategies

Validation

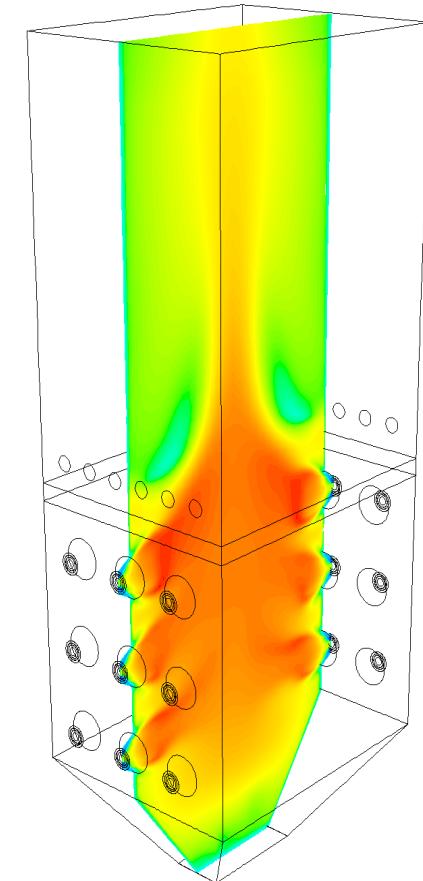
The focus of combustion simulation depends on the application



Burner design



Pollutant formation



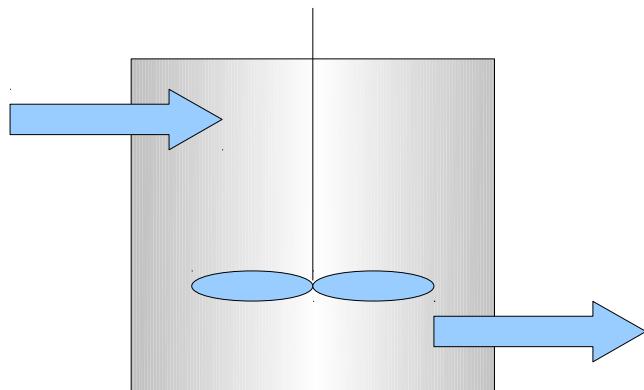
Furnace operation/retrofit

The focus of the present tutorial is simulating a model flame

- Model flames are a basis to test and evaluate combustion solvers
- Tutorial case is a turbulent methane/air flame (“Flame D” from Sandia/TNF workshop)
- Solver applications used are
 - rhoReactingFoam (PaSR model)
 - edcSimpleFoam (EDC model)
- Validation with experimental data to assess the solver/model accuracy



Photo: Sandia/TNF



Overview

Theory (combustion; radiation)

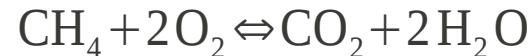
Tutorial case

Solution strategies

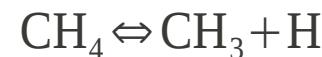
Validation

Combustion simulation is characterized by chemical reactions

Global reactions summarize the combustion process:



Detailed chemical mechanisms describe events on molecular level:



⋮

from GRI-Mech 3.0 (325 reactions, 53 species)

- *Chemical mechanisms need to be used within their specification limits, eg. GRI-Mech 3.0: methane/natural gas, T in 1000-2500 K, Φ in 0.1-5*
- *Detailed mechanism are more accurate (e.g. NO_x , ignition delay), but computationally much more expensive
→ level of detail needs to be chosen by the user*

Chemical reactions can be described with equilibrium or kinetic rates (incl. “infinite rate”)

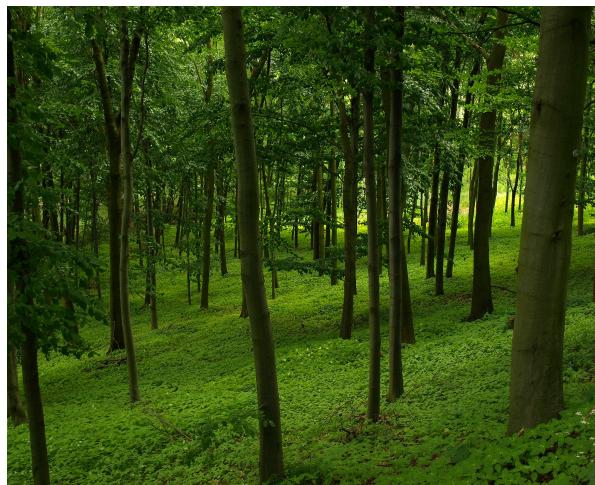
Equilibrium calculation depends only on thermodynamic data: h° , s° , cp°

But concerning combustion, many things are not in equilibrium!

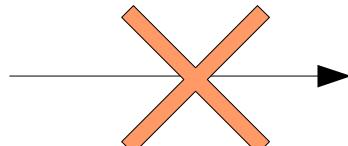
Chemical kinetics determine the reaction rate e.g. with an Arrhenius type formulation:

$$R = A T^b \exp\left(-\frac{E}{RT}\right) C_{CH_4} C_{O_2}^{0.5}$$

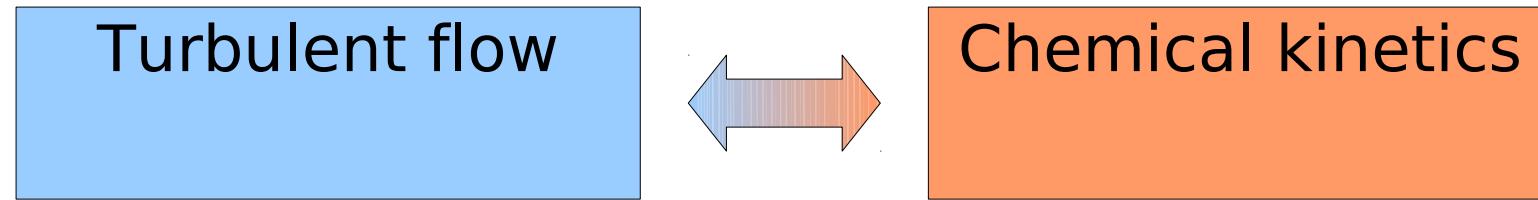
“Infinite rate” chemistry is a special case, where reaction rates are assumed to be infinitely fast



kinetically inhibited

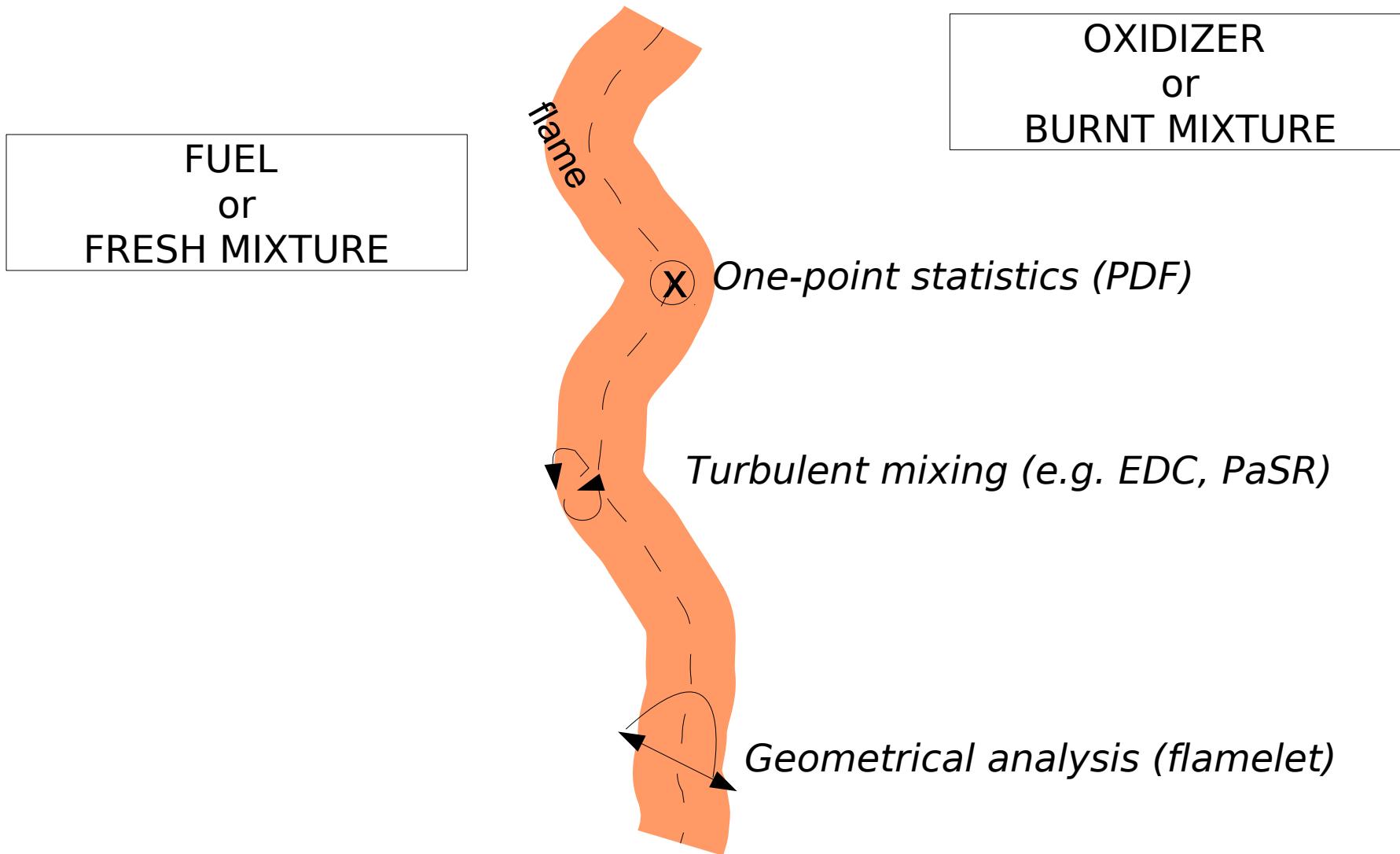


In turbulent flows, turbulence/chemistry interaction defines the reacting flow



- Turbulence enhances mixing of species such as fuel, oxidizer and products
- Strong turbulence can suppress combustion
→ local extinction
- In a laminar flow, combustion is controlled exclusively by chemical kinetics
- Combustion leads to flow acceleration
→ modification of flow field

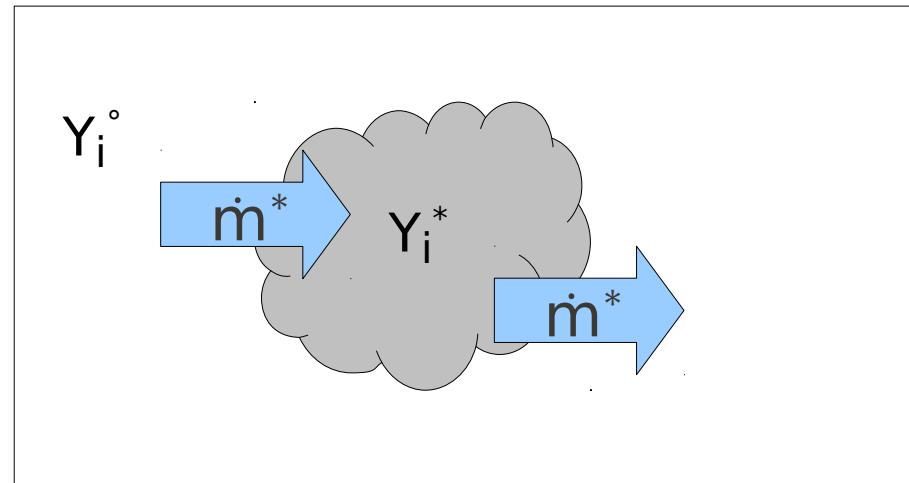
Different approaches exist to model the turbulence/chemistry interaction



cf. Poinsot, Veynante "Theoretical and Numerical Combustion"

The Eddy-Dissipation Concept (EDC) assumes reactions in *fine structures*

$$\overline{R}_i = \bar{\rho} \frac{\gamma^* \dot{m}^*}{(1 - \gamma^*)} (\overline{Y}_i - Y_i^*)$$



Fraction of the flow occupied
by *fine structures*:

$$\gamma^*$$

Relation of mean, *fine structure*
and *surrounding state*:

$$\overline{Y}_i = \gamma^* Y^* + (1 - \gamma^*) Y^o$$

EDC reaction rate depends on turbulent flow properties and chemical kinetics approach

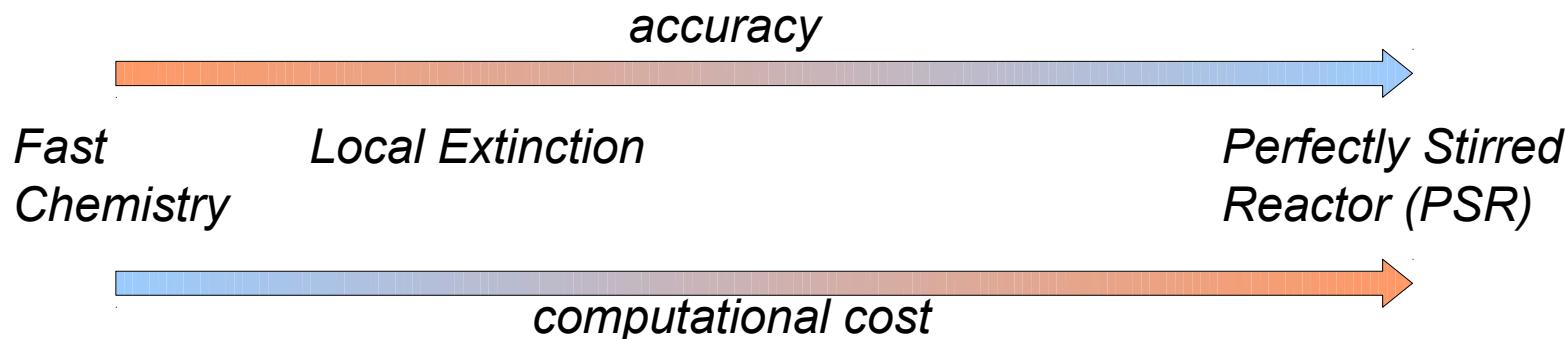
The fraction of the flow occupied by *fine structures*:

$$\gamma^* = 9.7 \left(\frac{v \cdot \epsilon}{k^2} \right)^{\frac{3}{4}}$$

Mass transfer rate between the *fine structures* and the *surroundings*:

$$\dot{m}^* = 2.45 \left(\frac{\epsilon}{v} \right)^{\frac{1}{2}}$$

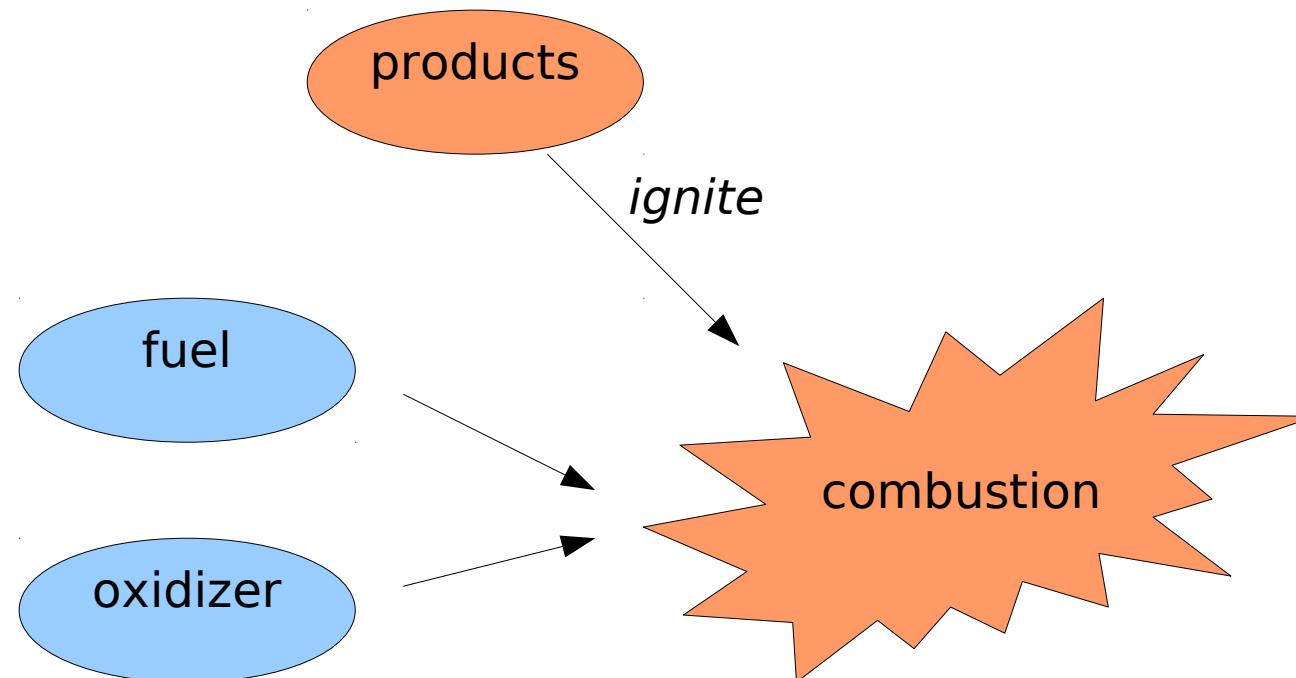
Chemical kinetics approaches for fine structure composition Y_i^* :



The Fast Chemistry approach assumes infinitely fast reactions

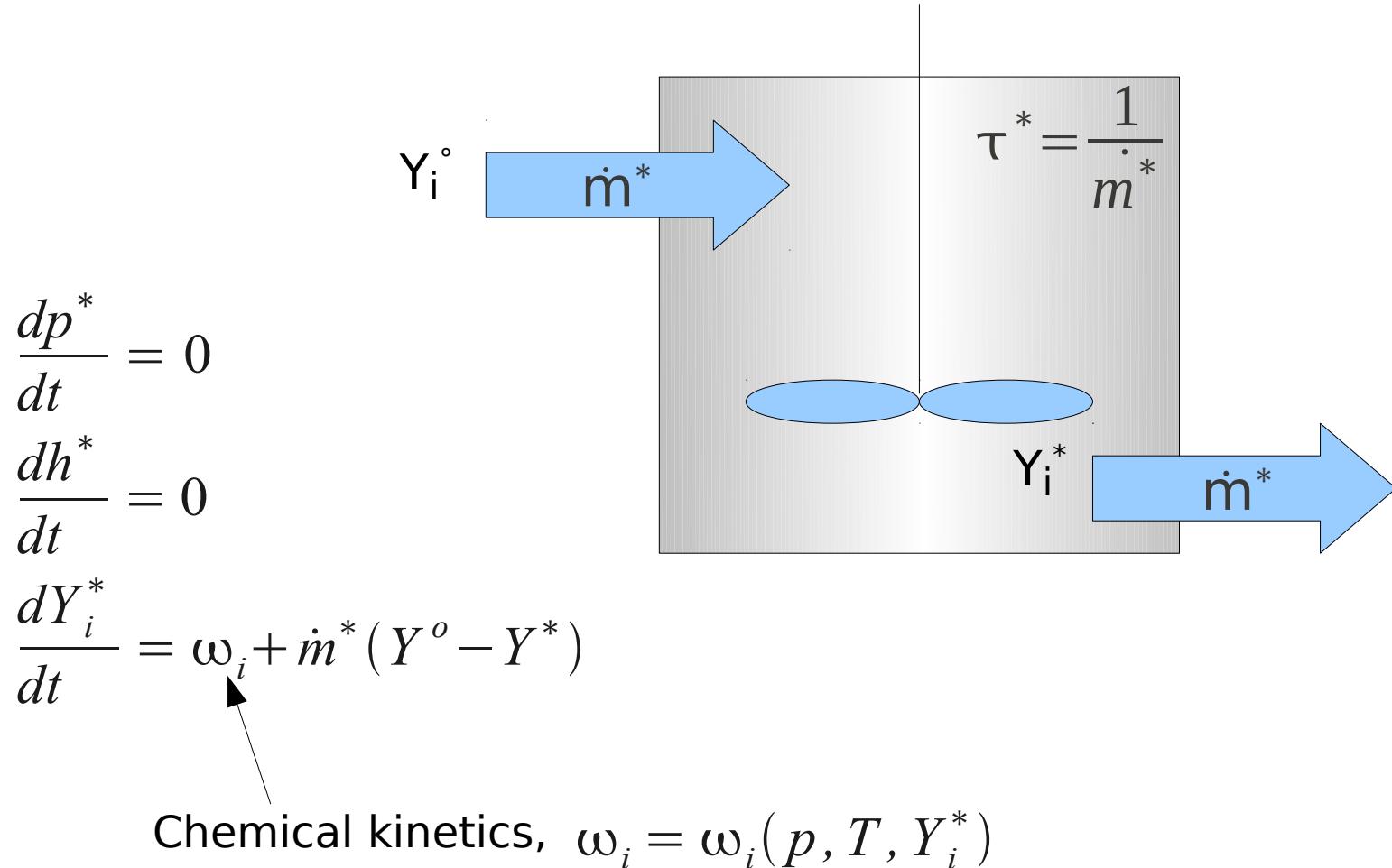
- Assumes sufficient time to achieve equilibrium inside fine structures
- Works only with irreversible global reactions

Combustion occurs if fuel, oxidizer and products meet simultaneously



→ *Product mass fractions must be initialized accordingly*

The PSR approach determines the steady-state of a perfectly stirred reactor



Local Extinction approach employs data from a priori PSR calculations

$$\tau^* < \tau_{ch} \Rightarrow R=0$$

τ_{ch} is the minimum residence time which sustains combustion in PSR.

Example 1:
Close to burner

high turbulence
($\tau^*=2.e-6$)

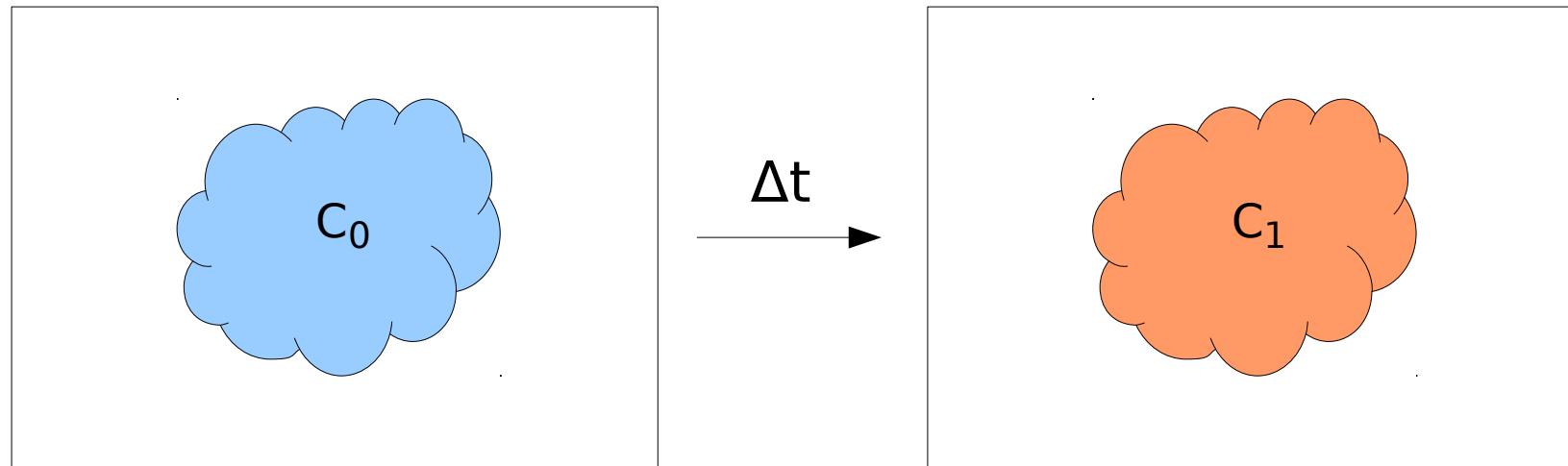
$T = 300\text{ K}$
($\tau_{ch}= 1.e-4$)

Example 2: Free
stream reaction zone

medium turbulence
($\tau^*=2.e-4$)

$T = 900\text{ K}$
($\tau_{ch}= 2.e-5$)

The PaSR combustion model derives the reaction rate in a transient manner



$$\bar{R}_i = \kappa \frac{C_{i,1} - C_{i,0}}{\Delta t}$$

Mixed fraction of cell that can react: κ

The parameter κ is based on two time scales

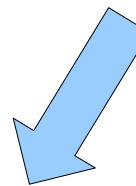
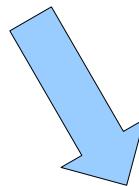
Turbulent mixing time scale:

$$\tau_m = \sqrt{\frac{k}{\epsilon} \left(\frac{\nu}{\epsilon} \right)^{\frac{1}{2}}}$$

Chemical time scale (infinite or finite rate):

$$\frac{1}{\tau_{ch}} = \max \left(-\frac{R_{fuel}}{\rho Y_{fuel}}, -\frac{R_{O_2}}{\rho Y_{O_2}} \right)$$

$$\frac{1}{\tau_{ch}} = -\frac{\partial R}{\rho \partial Y}$$



Mixed fraction that reacts:

$$\kappa = \frac{\tau_{ch}}{\tau_m + \tau_{ch}}$$

In OpenFOAM, mixing time scale is implemented slightly different

In rhoReactingFoam:

$$\tau_m = C_{mix} \sqrt{\frac{\mu_{eff}}{\rho \epsilon}}$$

In Chomiak (1996):

$$\tau_m = \sqrt{\frac{k}{\epsilon}} \left(\frac{v}{\epsilon} \right)^{\frac{1}{2}}$$

Both can be transformed into each other, using:

$$\frac{\mu_t}{\rho} = C_\mu \frac{k}{\epsilon}, \quad Sc_t = 1, \quad Re_t = \frac{k^2}{\epsilon v}$$

As result, we obtain:

$$C_{mix} = \sqrt{\frac{1}{1 + C_\mu Re_t}}$$

Chomiak (1996): *Flame Liftoff in Diesel Sprays* 25th
Symp. Int. on Comb. pp. 2557-2564

The value for C_{mix} needs to be estimated a priori

$$C_{mix} = \sqrt{\frac{1}{1 + C_\mu Re_t}}$$

Laminar flow
$Re_t = 0$
$C_{mix} = 1.0$

Typical turbulent flow
$Re_t \approx 1000$
$C_{mix} \approx 0.1$

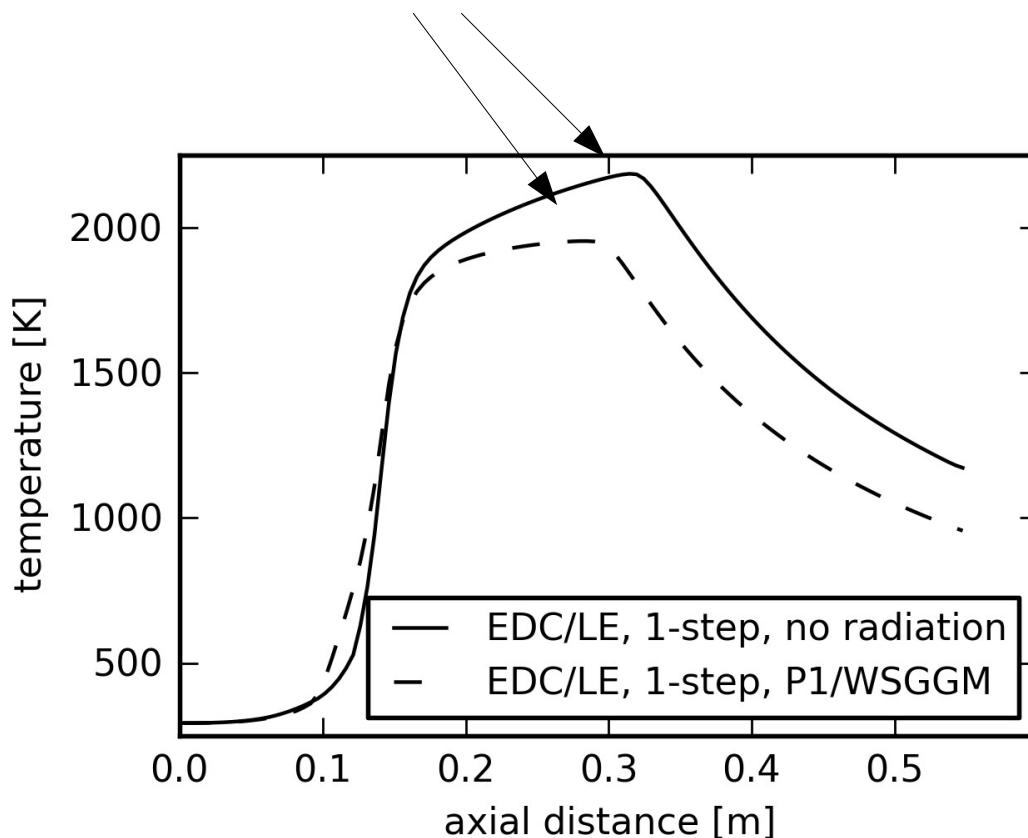
Extremely turbulent flow
$Re_t \rightarrow \infty$
$C_{mix} \rightarrow 0.0$

Typical values for C_{mix} : 0.001 – 0.3; cf. Nordin (2001)

Nordin (2001): *Complex Chemistry Modelling of Diesel Spray Combustion*, PhD-Thesis

Radiation heat transfer needs to be considered in combustion simulation

*Peak temperature ≈ 250 K higher
without radiation modelling*



Radiation Transport Equation:

P1 - Transport

Discrete Ordinates (DOM)

Gas-Absorption Modelling:

constant

RADCAL-Polynomials

WSGGM (custom)

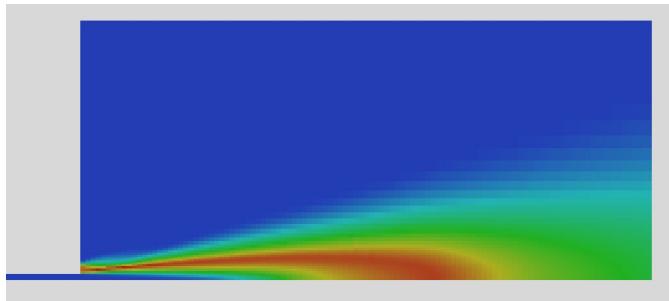
Overview

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Tutorial case

Solution strategies

Validation



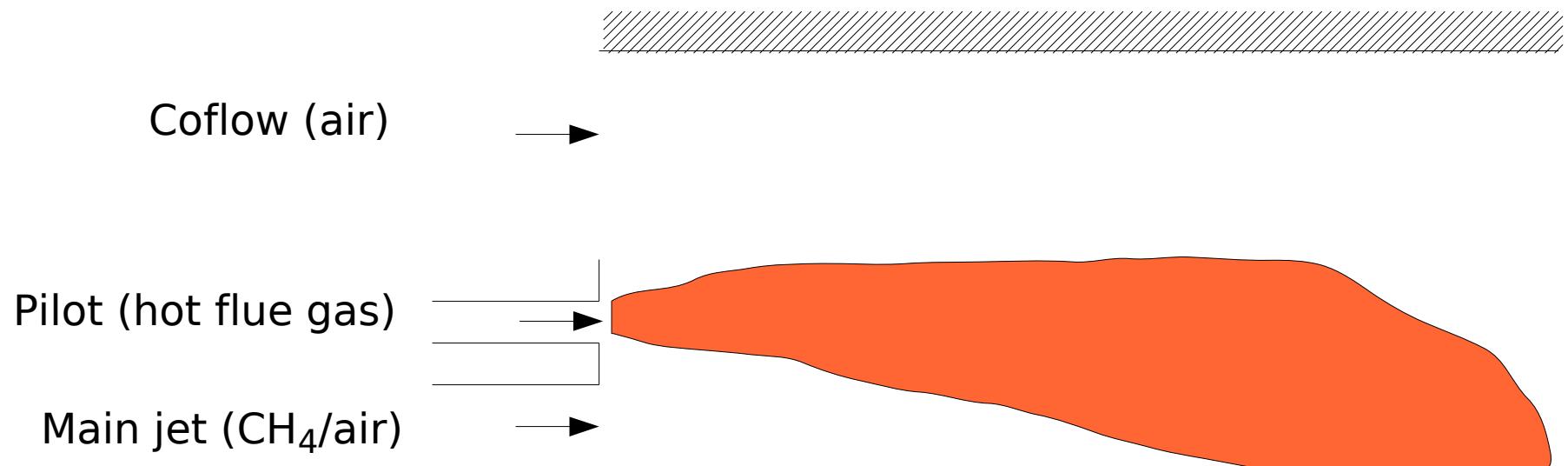
The tutorial case is a non-premixed piloted flame (“Flame D”)

Characteristics:

Steady-state, piloted, methane/air, diffusion flame, some local extinction

Geometry:

Axi-symmetric, 2D



The boundary conditions are identical for rhoReactingFoam and rhoSimpleFoam

	Ux [m/s]	p [Pa]	T [K]	Yi [-]	k [m ² /s ²]	epsilon [m ² /s ³]
Main jet	49.6	zeroGradient	294	fixedValue	$I_{turb}=0.0458$	$L_{turb}=5.04e-4$
Pilot	11.4	zeroGradient	1880	fixedValue	$I_{turb}=0.0628$	$L_{turb}=7.35e-4$
Coflow	0.9	zeroGradient	291	fixedValue	$I_{turb}=0.0471$	$L_{turb}=0.0197$
Outlet	zeroGradient	100000	zeroGradient	zeroGradient	zeroGradient	zeroGradient
Walls	0.0	zeroGradient	zeroGradient	zeroGradient	wall function	wall function

Front and backside of axi-symmetric domain are specified as 'wedge'.

edcSimpleFoam: Flow field initialized as required by chemical kinetics approach

- Fast Chemistry and Local Extinction: Set CO₂ and H₂O mass fraction to 0.01 everywhere.
- Perfectly Stirred Reactor: Initialize with Fast Chemistry or Local Extinction solution.
- Setup chemistryProperties:

```
edcFastChemCoeffs
{
    oxidiserName O2;
    mainFuelName CH4;
}
```

*no local extinction
above this
temperature*

```
edcLECoeffs
{
    oxidiserName O2;
    mainFuelName CH4;
    autoIgnitionTemperature
        868;
    curve1
    {
        temperature 300;
        tauChMin 7.00E-005;
    }
    ...
}
```

```
edcPSRCoeffs
{
    relativeTolerance 1.e-6;
    absoluteTolerance 1.e-14;
    maxIterations 1.e8;

    useBinaryTree off;
    binaryTreeTolerance 1e-4;
    binaryTreeSize 1.e7;
}
```

rhoReactingFoam: Choosing C_{mix} and ODE intergrator

- Estimate turbulent Reynolds number:

$$Re_t = 500 \rightarrow C_{\text{mix}} = 0.15$$

SIBS is stable enough for solving detailed chemistry

- Setup chemistryProperties:

```
odeCoeffs
{
    ODESolver      SIBS;
    eps            5.0e-4;
    scale          1.0;
}
```

Setting-up discretization schemes

- *Convective term:* Linear upwind discretization (2nd order accurate)

```
default      Gauss linearUpwind cellLimited Gauss linear 1;
```

For species Y_i (for rhoReactionFoam: Y_i and hs)

```
div(phi,Yi) Gauss multivariateSelection
{
    //hs      linearUpwind cellLimited Gauss linear 1;
    CH4      linearUpwind cellLimited Gauss linear 1;
    O2       linearUpwind cellLimited Gauss linear 1;
    ...
}
```

- *Time discretization:* (Pseudo) steady-state

edcSimpleFoam (steady-state solver)

```
default      steadyState;
```

rhoReactingFoam (transient solver)

```
default      SLTS phi rho 0.7;
```

```
default      CoEuler phi rho 0.4;
```

*global under-relaxation
factor*



max. CFL number

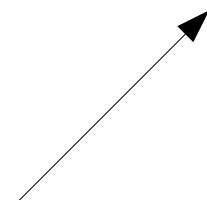


Setting-up fvSolution

Numerical solver precision depends on solver type:

Transient solver requires each time-step to be accurate
all variables: $\text{relTol} = 0. ;$

Steady state solver can reach solution through intermediate results
pressure: $\text{relTol } 0.001;$
other variables: $\text{relTol } 0.1;$

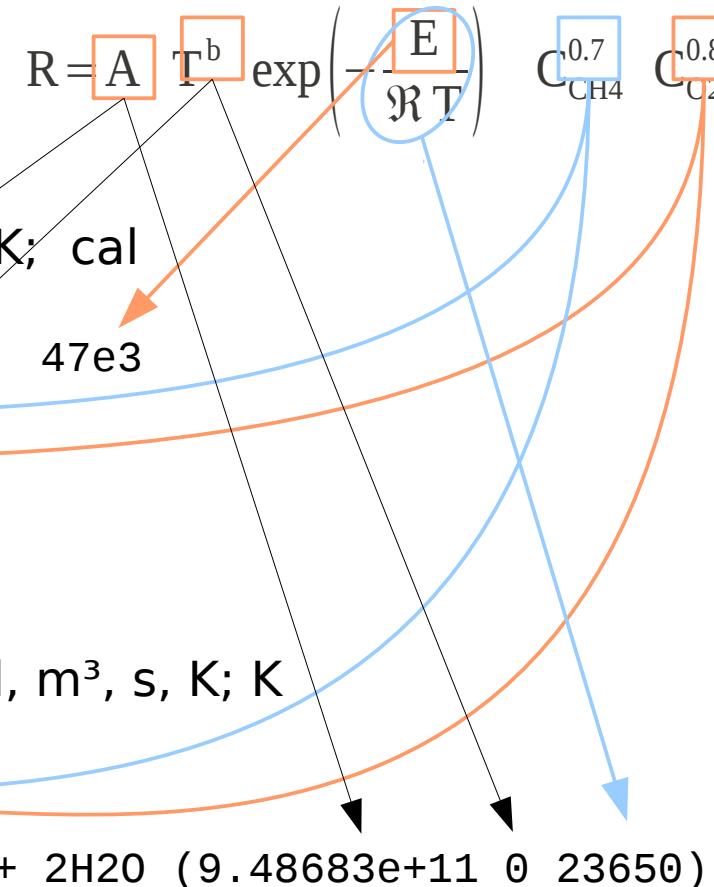
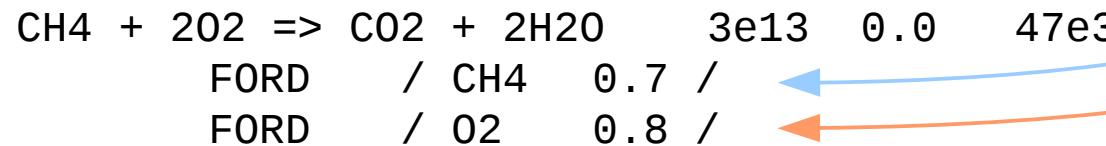


*intermediate results will not be
accurate*

Chemical mechanisms can be defined in Chemkin or OpenFOAM native format

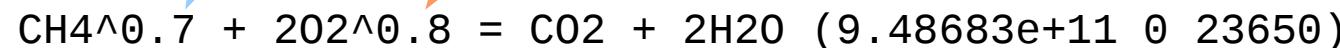
Example: Arrhenius type kinetics

Chemkin format uses units: mol, cm³, s, K; cal



OpenFoam native format uses units: kmol, m³, s, K; K

irreversibleArrheniusReaction



Use chemkinToFoam to convert chemkin files (or to check their consistency)

Overview

Theory



Tutorial case

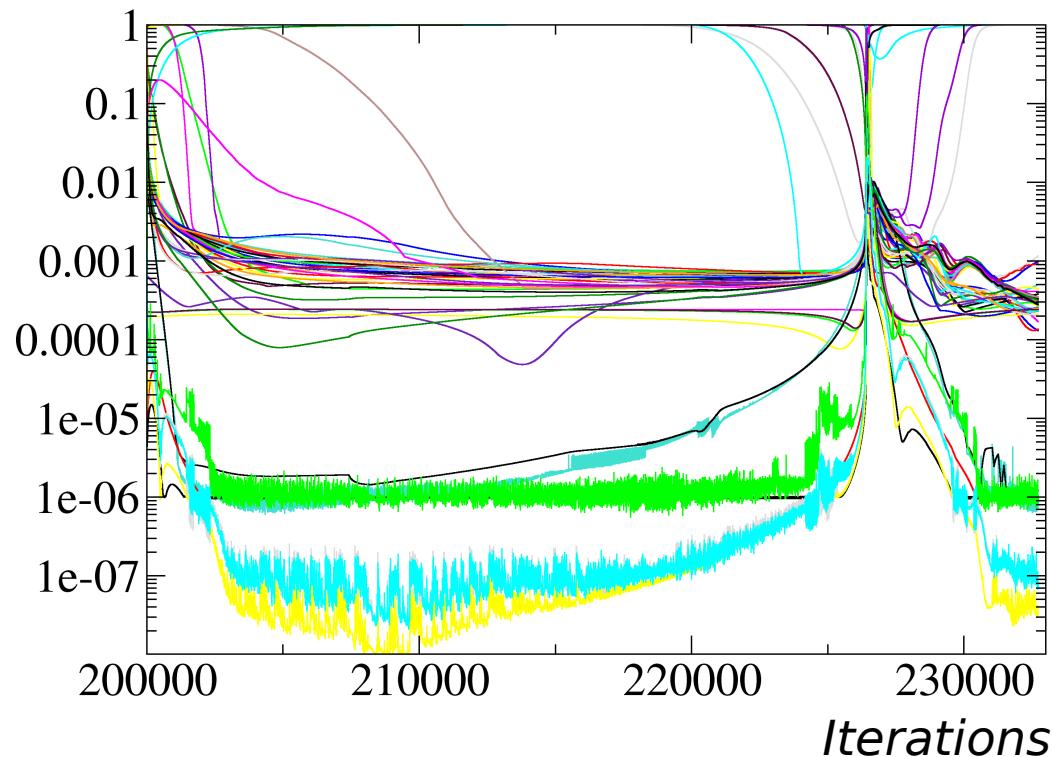


Solution strategies

Validation

Combustion simulation often faces stability issues

Residuals



Many error sources are possible because numerous models are applied simultaneously, for example:

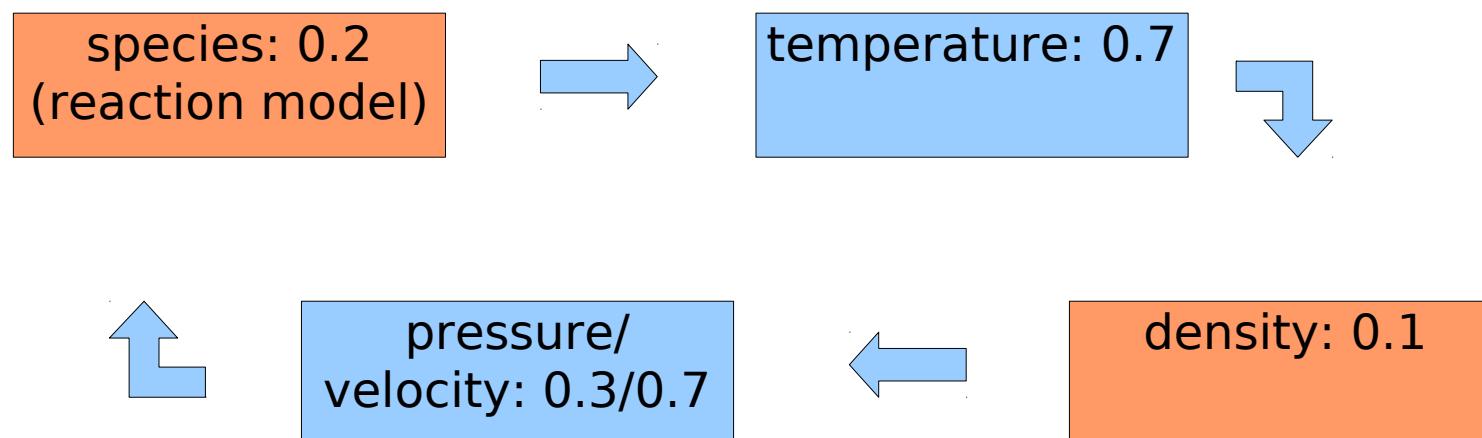
- Compressible flow
- Coupling of transport equations
- Numerically stiff reaction mechanisms

Solution strategies include good initialization and under-relaxation

Possible “well initialized” flow fields are:

- Cold flow
- Starting solution (steady-state; 1- or 2-Step)
- Products

Strong coupling between transport equations may be broken with different under-relaxation factors.



*Under-relaxation only applicable to steady-state cases.
Unsteady solver based on Transient-SIMPLER needed?*

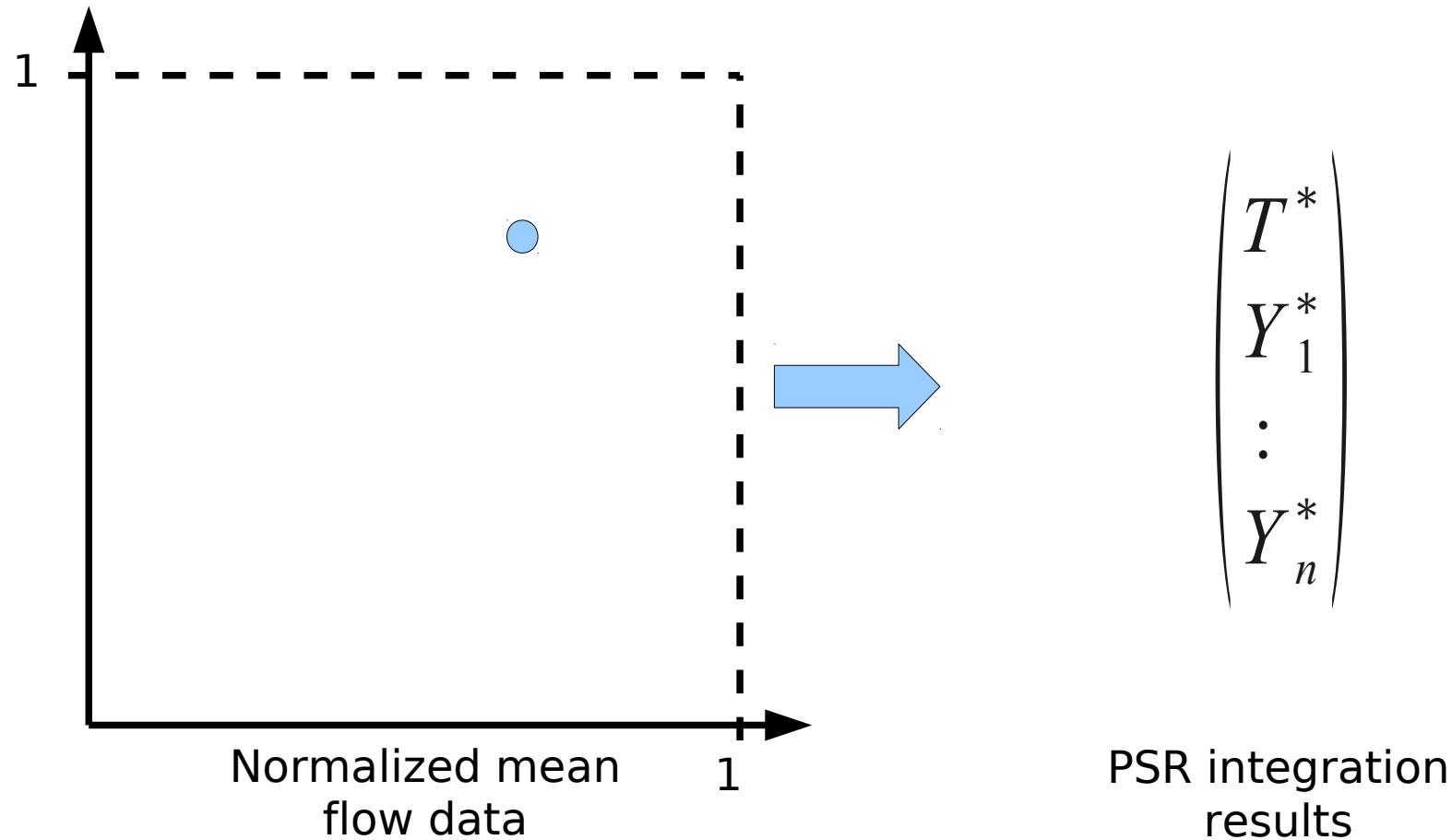
Tabulation of PSR reactor results can provide speed-up and additional stability

$$\begin{array}{c} \left(\begin{array}{c} \gamma^* \\ \dot{m}^* \\ Y_1 \\ \vdots \\ Y_n \end{array} \right) \longrightarrow \left(\begin{array}{c} T^* \\ Y_1^* \\ \vdots \\ Y_n^* \end{array} \right) \end{array}$$

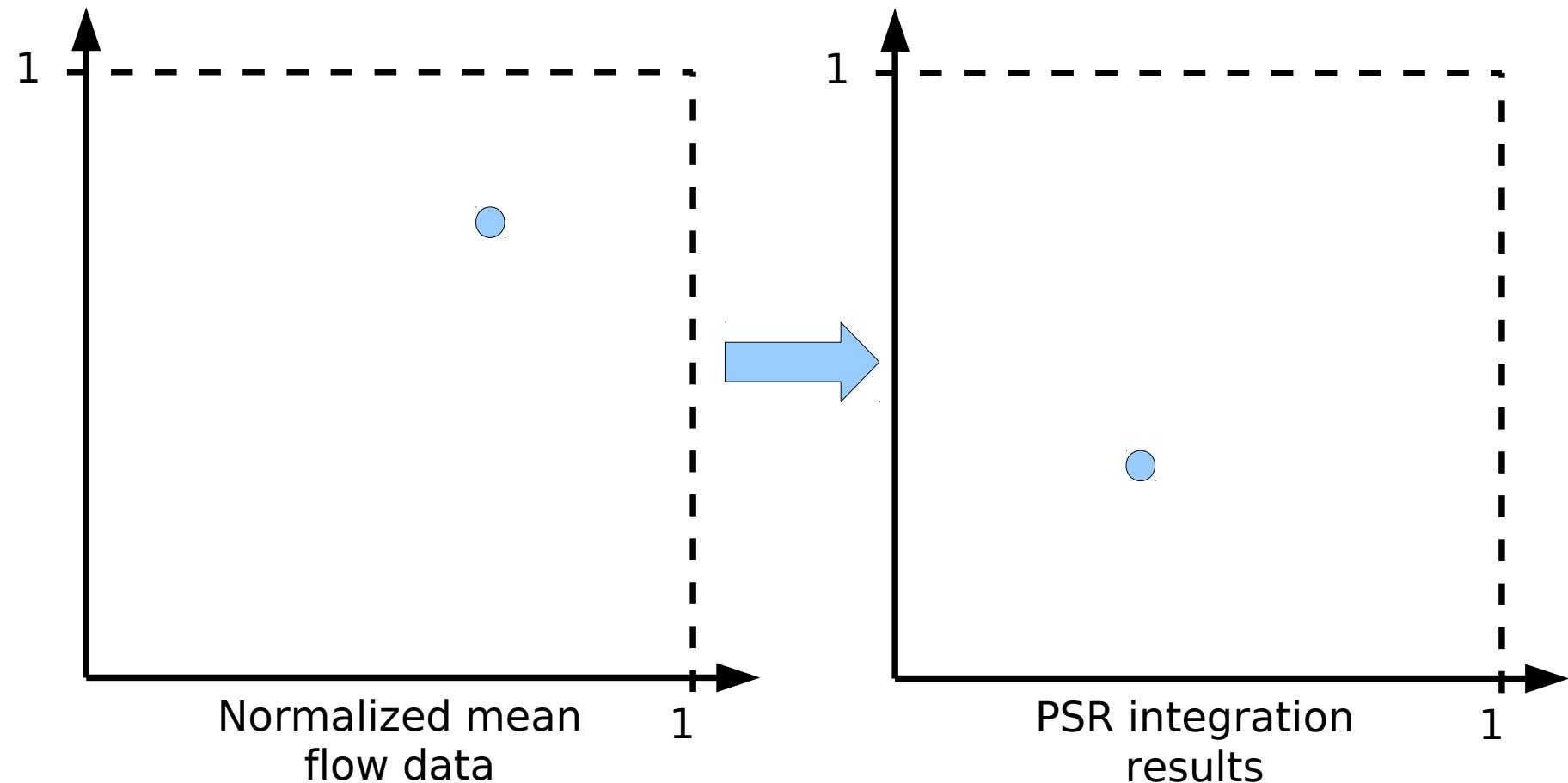
Mean flow data

PSR integration
results

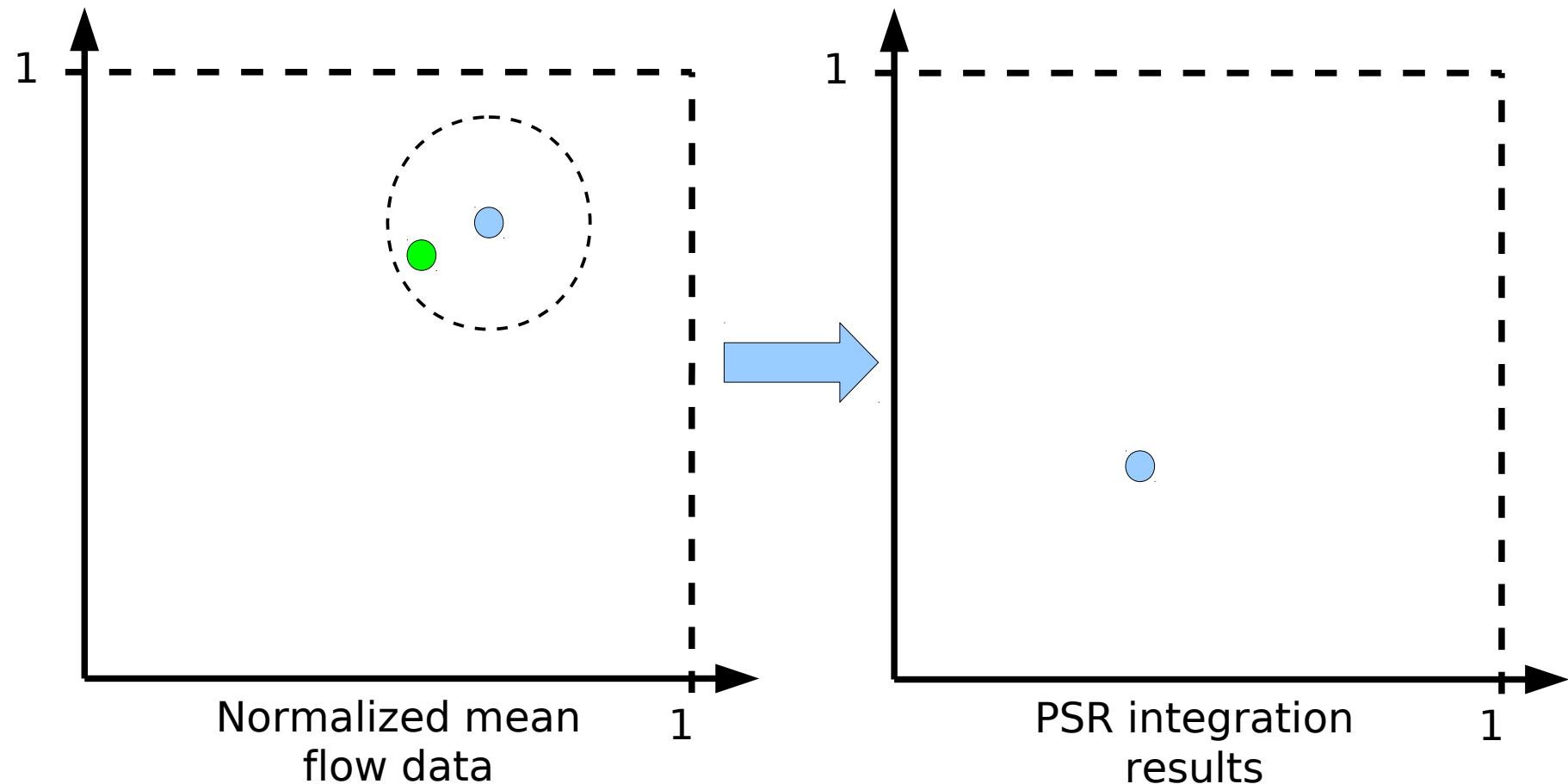
Tabulation of PSR reactor results can provide speed-up and additional stability



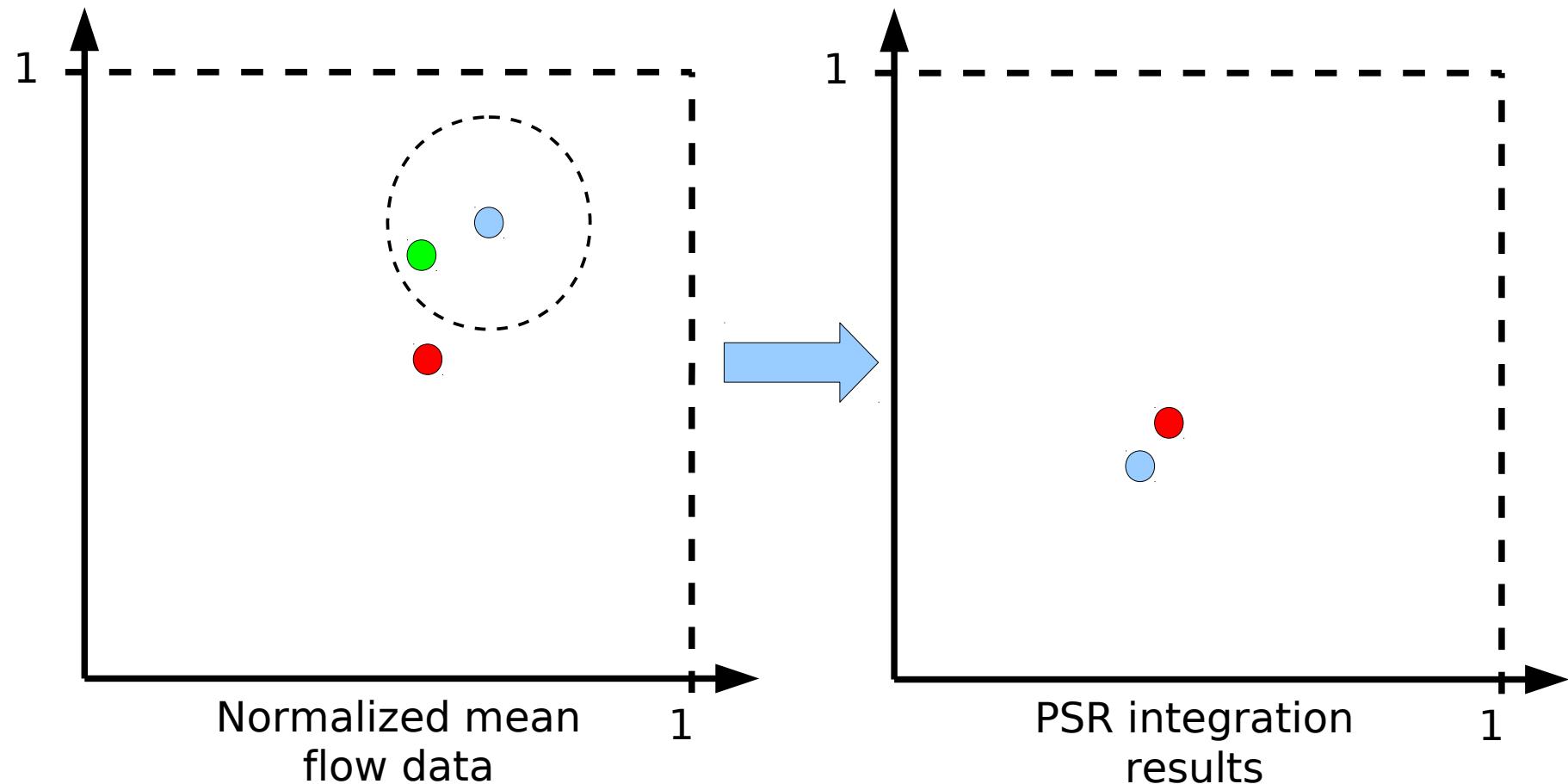
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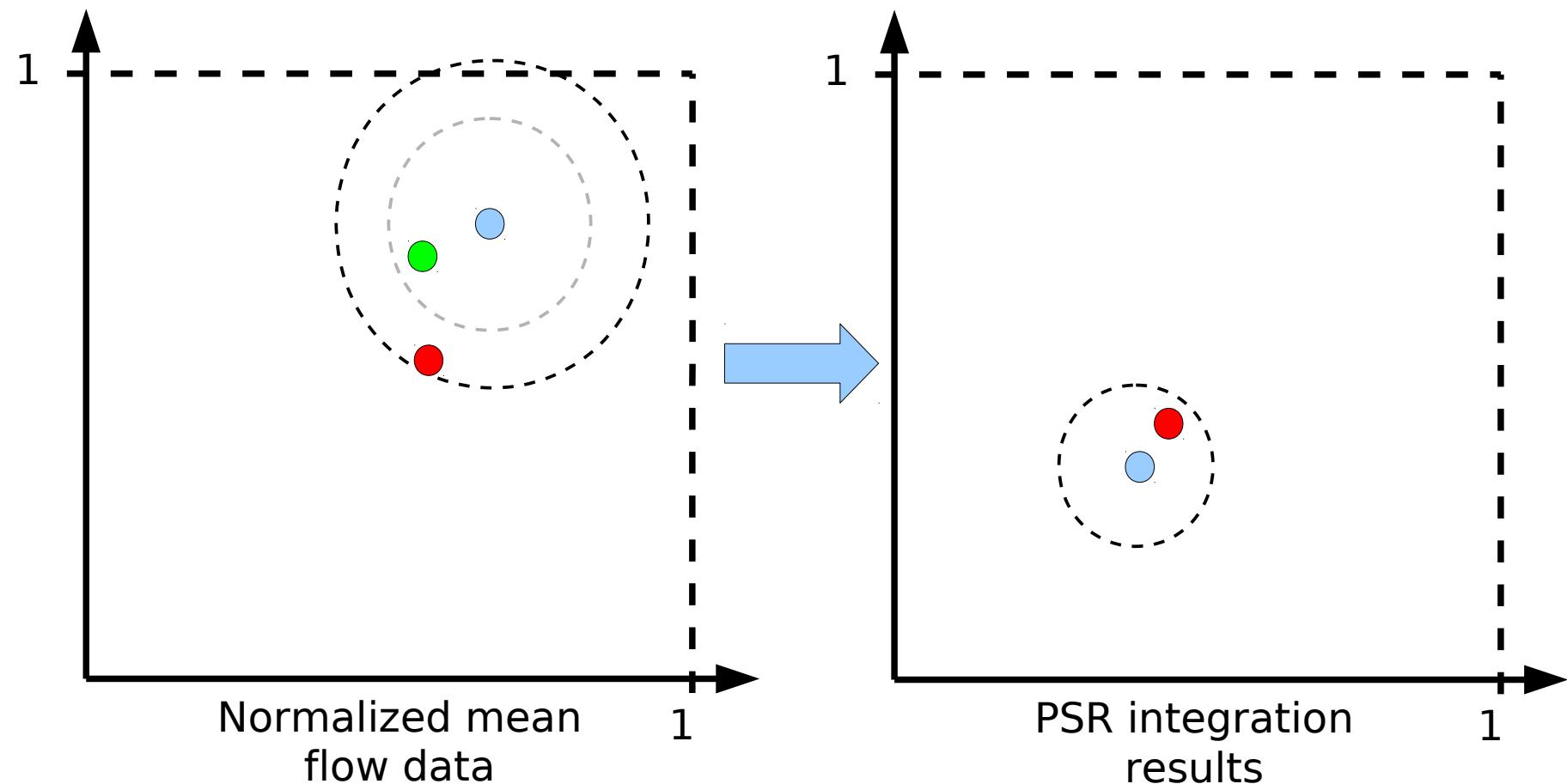
Tabulation of PSR reactor results can provide speed-up and additional stability



Tabulation of PSR reactor results can provide speed-up and additional stability



Tabulation of PSR reactor results can provide speed-up and additional stability



Limiting temperature is possible in steady-state cases

In a steady state case, intermediate “time steps” are not accurate.
→ Temperature may temporarily increase and needs to be limited

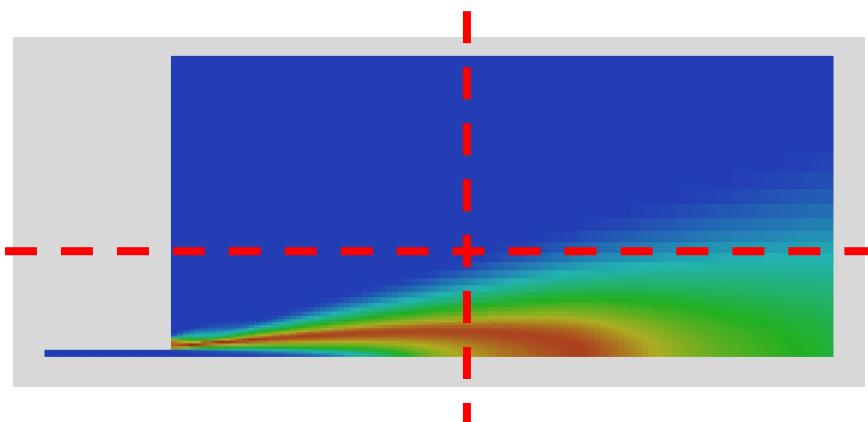
Solver level implementation in edcSimpleFoam:

- New enthalpy field calculated from species mass fractions and T_{\min}
- Another enthalpy field calculated for T_{\max}
- Both fields are used to limit enthalpy field
- T_{\max} and T_{\min} are specified in thermophysicalProperties

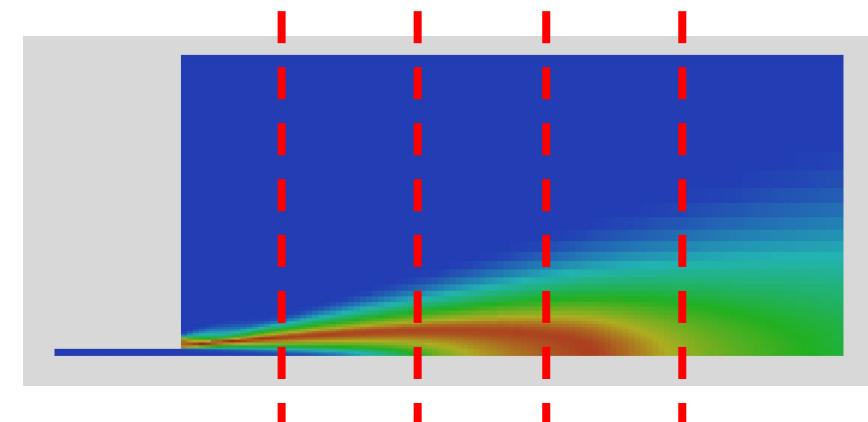
Request for integrated limitation filed in OpenCFD's bugtracker (Issue #57).

Optimal parallelization depends on the complexity of the chemical model

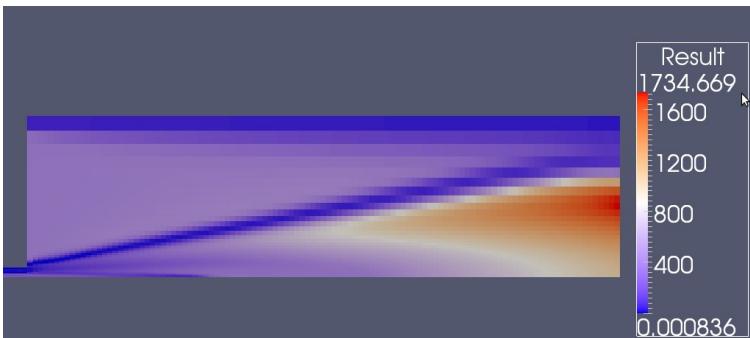
Integrating complex chemical mechanisms is computationally much more expensive than solving transport equations (even if there are many)!



optimized for network bandwidth



optimized for PSR-integration



Overview

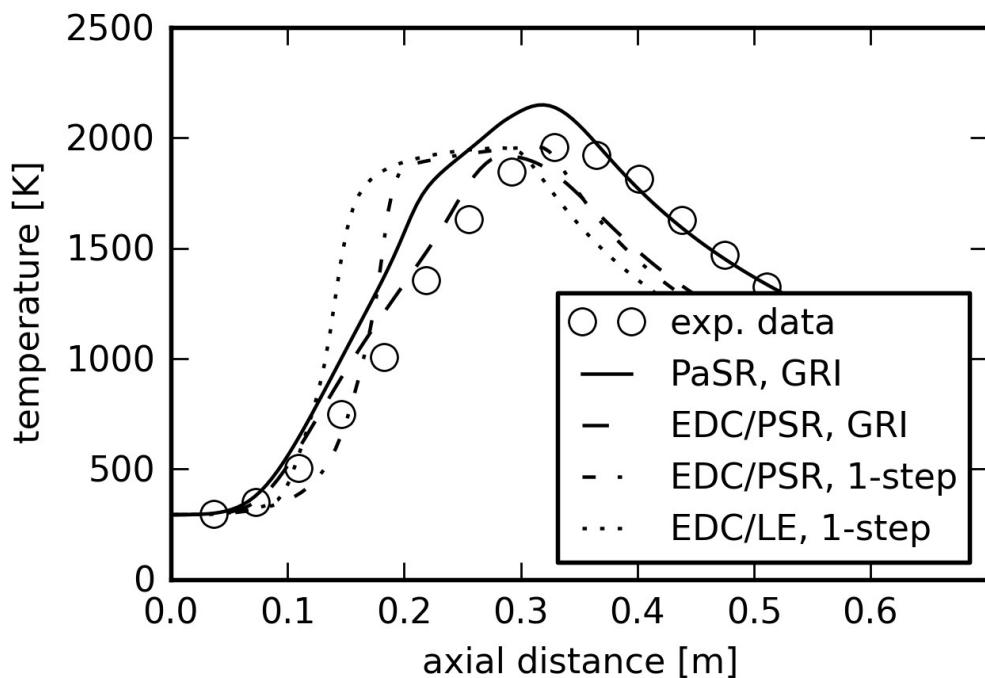
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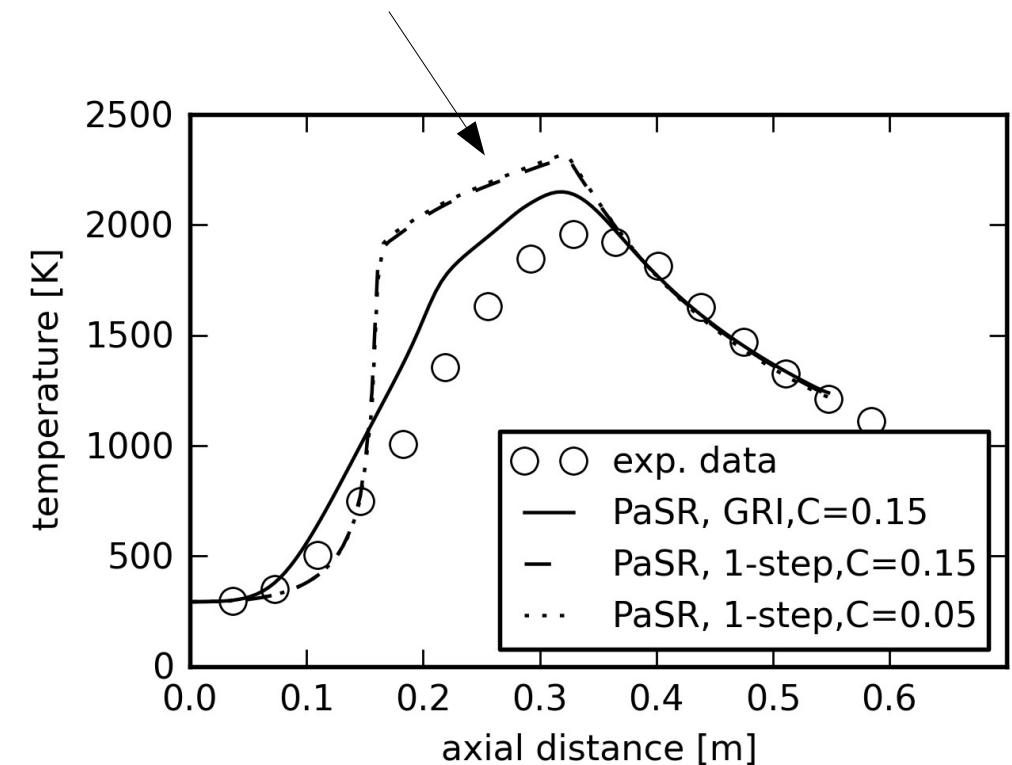
Solution strategies

Validation

Detailed reaction mechanism predicts temperature profile accurately



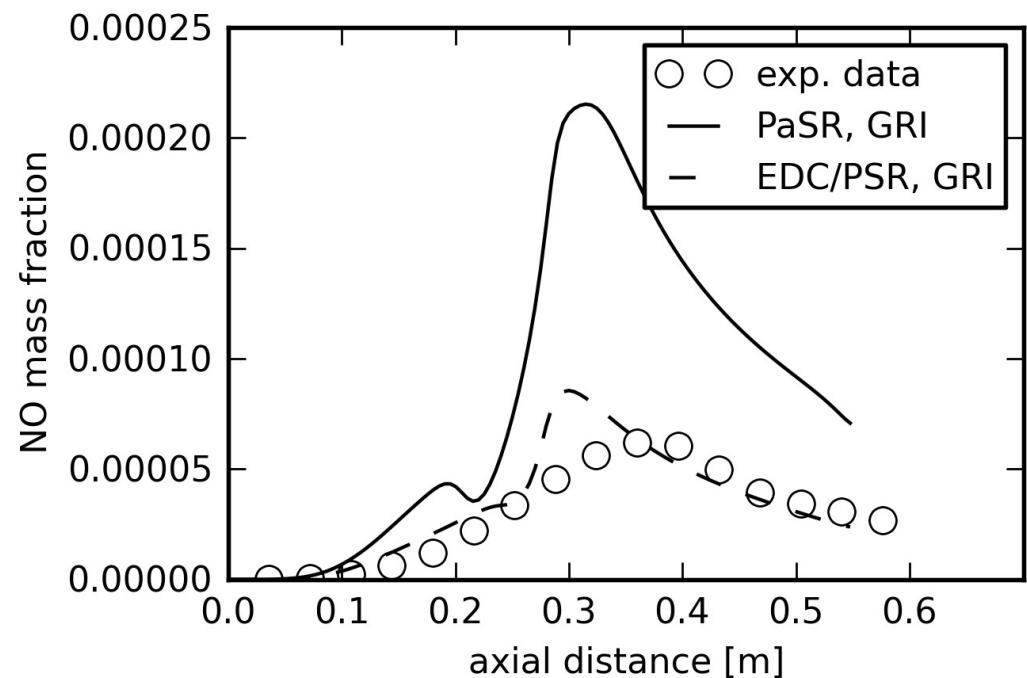
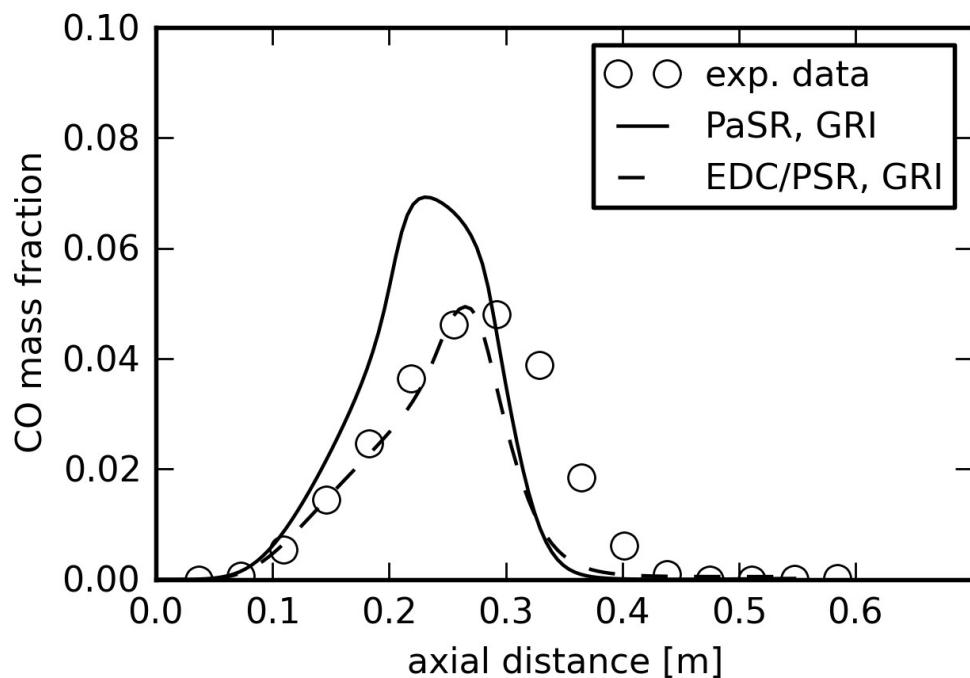
Influence of C_{mix} is minimal



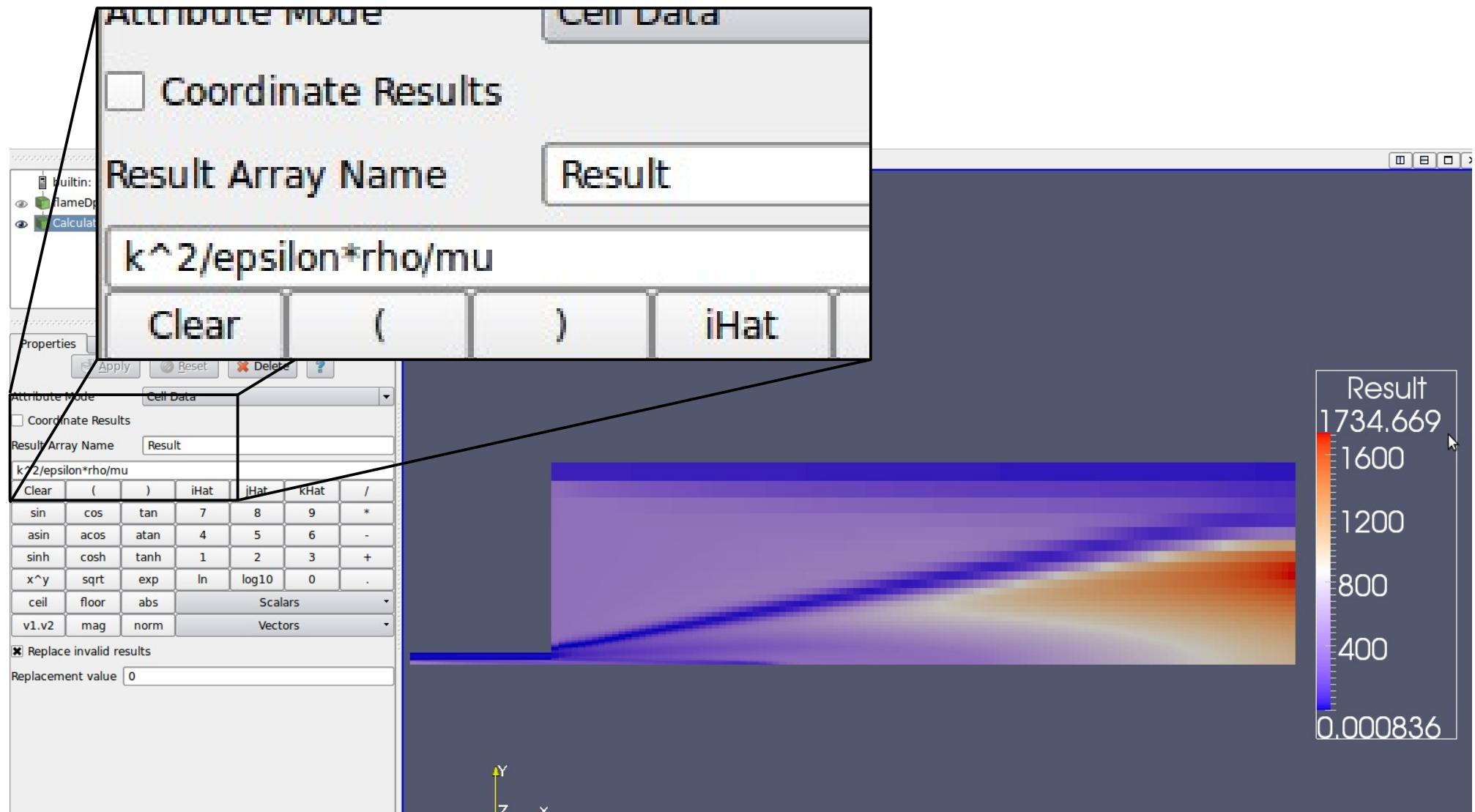
Radiation modeling used with EDC, not used with PaSR.

exp. data: Barlow, R. S. and Frank, J. H., Proc. Combust. Inst. 27:1087-1095 (1998)

Intermediate species and pollutants are more difficult to predict



ParaFoam's “calculator” can be used to check Re_t assumption



Comparison with measurements may require special post-processing

Common difficulties when comparing simulated mass fractions with measurements:

- Measured data are often mole fractions or concentrations
If not all (major) species are measured, correct conversion to mass fractions impossible

- Flue gas or emission monitoring can be measured in “dry gas”, i.e. after water vapor has been condensed out
Simulated data comprise a complete set, therefore they can be accurately converted

New utility massToMoleFraction handles conversion together with “-dryGas” option

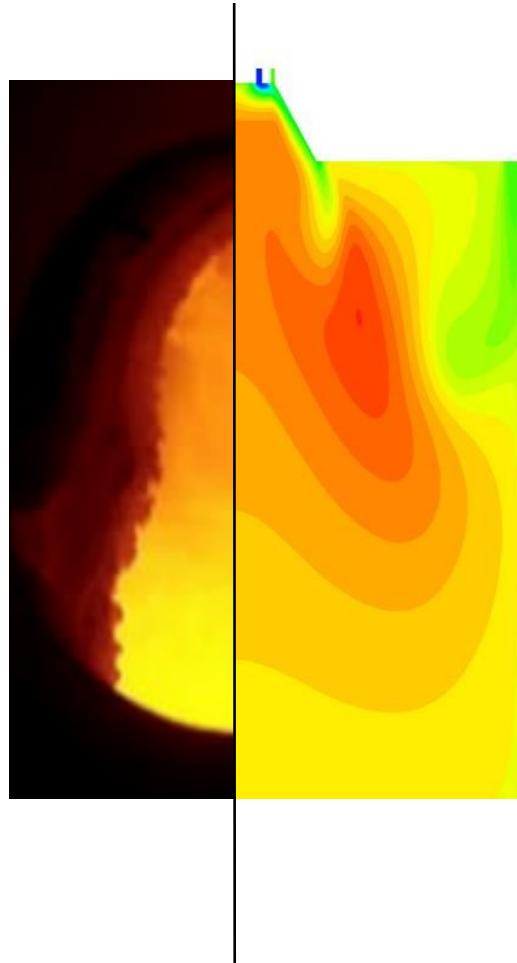
Final note: When using edcSimpleFoam or edcPisoFoam, please cite

for the EDC model:

B. Magnussen: *The Eddy Dissipation Concept: A Bridge between Science and Technology*, ECCOMAS Thematic Conference on Computational Combustion, Lisbon, Portugal, 2005

for the validation of the OpenFoam implementation:

B. Lilleberg, D. Christ, I.S. Ertesvåg, K.E. Rian, R. Kneer,
Numerical simulation with an extinction database for use with the Eddy Dissipation Concept for turbulent combustion
(submitted)



Thank you for your attention!