

## Answer of 1

Array	1	6	2	4	3	5
Index	0	1	2	3	4	5

Call #1:

quicksort(array, 0, 5)

Array	1	6	2	4	3	5
Index	0	1	2	3	4	5
	l, pivot					r

Pivot is picket the left-most one.

Now, do partition:

Swap, pivot with right position.  $i=0$  and  $j=4$ .

Array	5	6	2	4	3	1
Index	0	1	2	3	4	5
	L, i				j	Pivot, r

While  $\text{arr}[i] < \text{pivot}$ ,  $i++$ . We get below result as  $\text{arr}[0] > \text{pivot}$  i.e.  $5 > 1$ .

Array	5	6	2	4	3	1
Index	0	1	2	3	4	5
	L, i				j	Pivot, r

While  $\text{arr}[j] > \text{pivot}$ ,  $j--$ . We get  $j = -1$ .

Array	5	6	2	4	3	1
Index	0	1	2	3	4	5
	L, i					Pivot, r

Since,  $j$  crossed  $i$ . We stop and swap pivot with  $i$ . We get below results.

Array	1	6	2	4	3	5
Index	0	1	2	3	4	5
	L, i					r

Now we do self-calls:

quicksort(arr, 0, -1) -> This will stop as  $0 > -1$ .

quicksort(arr, 1, 5)

Self-call #1:

quicksort(arr, 1, 5)

Array	1	6	2	4	3	5
Index	0	1	2	3	4	5
		L, pivot				r

Partition:

Swap pivot element to right element. We have  $i=1$  and  $j = 4$ .

Array	1	5	2	4	3	6
Index	0	1	2	3	4	5
		L, i			j	r, pivot

While  $\text{arr}[i] < \text{pivot}$ ,  $i++$ . We'll get  $i = 5$  as everything is less than pivot.

Array	1	5	2	4	3	6
Index	0	1	2	3	4	5
		L			j	i, r, pivot

I crossed  $j$  so we don't loop over  $j$ . Now, swap pivot and  $i$  and return  $i=5$ .

Array	1	5	2	4	3	6
Index	0	1	2	3	4	5
		L				i, r

We got new pivot location  $i=5$  returned. Now, do self-calls on the left and right partitions.

quicksort(arr, 1, 4)

quicksort(arr, 6, 5) -> we don't do this as  $6 > 5$ .

Self-call #2:

quicksort(arr, 1, 4)

Pivot is always selected to be left.

Array	1	5	2	4	3	6
Index	0	1	2	3	4	5
		L, pivot			r	

Partition:

Swap pivot element to right element. We have i=1 and j = 3.

Array	1	3	2	4	5	6
Index	0	1	2	3	4	5
		L, i		j	R, pivot	

While arr[i] < pivot, i++. We'll get i= 5 as everything is less than pivot.

Array	1	3	2	4	5	6
Index	0	1	2	3	4	5
		L		j	i, R, pivot	

I crossed j so we don't loop over j. Now, swap pivot and i and return i=5.

Array	1	3	2	4	5	6
Index	0	1	2	3	4	5
		L			i, R	

We got new pivot location i=4 returned. Now, do self-calls on the left and right partitions.

quicksort(arr, 1, 3)

quicksort(arr, 5, 4) -> we don't do this as 5 > 4.

Self-call #3:

quicksort(arr, 1, 3)

Pivot is the left-most element.

Array	1	3	2	4	5	6
Index	0	1	2	3	4	5
		L, pivot		R		

Partition:

Swap pivot with right position.

Array	1	4	2	3	5	6
Index	0	1	2	3	4	5
		L, i	j	R, pivot		

While  $\text{arr}[i] < \text{pivot}$ ,  $i++$ . We'll get  $i = 1$  as  $4 > 3$ .

Array	1	4	2	3	5	6
Index	0	1	2	3	4	5
		L, i	j	R, pivot		

While  $\text{arr}[j] > \text{pivot}$ ,  $j--$ . We'll get  $j = 2$  as  $2 < 3$ .

Array	1	4	2	3	5	6
Index	0	1	2	3	4	5
		L, i	j	R, pivot		

As  $i$  and  $j$  are stuck, we swap the values and continue again.

Array	1	2	4	3	5	6
Index	0	1	2	3	4	5
		L, i	j	R, pivot		

While  $\text{arr}[i] < \text{pivot}$ ,  $i++$ . We'll get  $i = 2$ .

Array	1	2	4	3	5	6
Index	0	1	2	3	4	5
		L	J, i	R, pivot		

$i$  crossed  $j$  so we don't loop over  $j$ . Now, swap pivot and  $i$  and return  $i=2$ .

Array	1	2	3	4	5	6
Index	0	1	2	3	4	5
		L	i	R		

We got new pivot location  $i=2$  returned. Now, do self-calls on the left and right partitions.

quicksort(arr, 1, 1) we stop as low == high

quicksort(arr, 3, 3) we stop as low == high

We get final result.

Array	1	2	3	4	5	6
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## Answer of 2

Array: = [5, 1, 4, 3, 6, 2, 7, 1, 3]

Size,  $n = 9$

For simplification, see the sorted array only to see what L, E and R would be.

Since,  $n=9$ ,  $3n/4 = 3 * 9 / 4 \approx 6$ .

Array	5	1	4	3	6	2	7	1	3
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Sorted Array	1	1	2	3	3	4	5	6	7
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When pivot is 1.

$L = []$

$E = [1, 1]$

$R = [2, 3, 3, 4, 5, 6, 7]$

L is of size 0 and R is of size 7.

When pivot = 2

$L = [1, 1]$

$E = [2]$

$R = [3, 3, 4, 5, 6, 7]$

L is of size 2 and R is of size 6.

When pivot = 3

L = [1, 1, 2]

E = [3, 3]

R = [4,5,6,7]

L is of size 3 and R is of size 4.

When pivot = 4

L = [1, 1, 2, 3, 3]

E = [4 ]

R = [5,6,7]

L is of size 5 and R is of size 3.

When pivot = 5

L = [1, 1, 2, 3, 3, 4]

E = [5]

R = [6,7]

L is of size 6 and R is of size 2.

When pivot = 6

L = [1, 1, 2, 3, 3, 4, 5]

E = [6]

R = [7]

L is of size 7 and R is of size 1.

When pivot = 7

L = [1, 1, 2, 3, 3, 4, 5, 6]

E = [7]

R = []

L is of size 8 and R is of size 0.

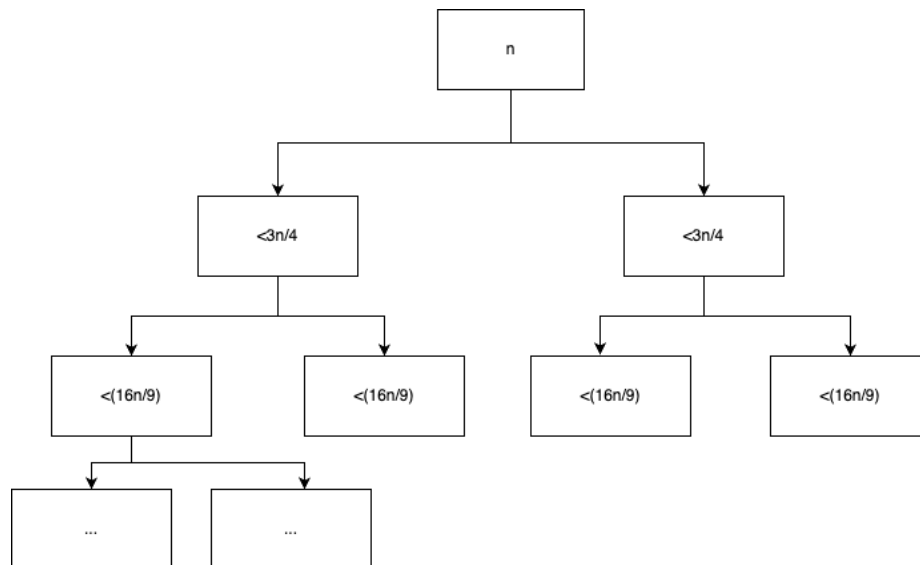
- a. From above, we can see that pivots [3,3, 4] are the only good pivots.

The pivots [1, 1, 2, 5, 6, 7] are bad pivots as either L or R is greater than 6.

- b. No, if the array have duplicates, then there's no guarantee that at least half of them would be good pivots.

## Answer of 3

The best case ideally would be to split the array in  $n/2$  for both Left and Right partition. However, pivot itself always makes sure that neither Left and Right can be  $n/2$ .



Running Time = no. of levels \* amount of work at each level

At each level, the array is divided into two partitions of  $< 3n/4$ . So, the height of the tree is the same as the number of levels.

$$n, \frac{3}{4}n, \left(\frac{3}{4}\right)^2 n, \left(\frac{3}{4}\right)^3 n, \dots, 1, 0$$

$$1 + \log_{4/3} n$$

Which will be  $O(\log n)$ .

At each level of the tree, the total processing time is  $O(n)$ .

Hence Total Running Time =  $O(n \log n)$

This is the best running time for quick sort  $O(n \log n)$ .

## Answer of 4

```
class Solution {
    public int findKthLargest(int[] nums, int k) {
        int position = nums.length - k;
        int start = 0;
        int end = nums.length - 1;

        while (start < end) {
            int cursor = quickSelect(nums, start, end);

            if (cursor == position) {
                break;
            } else if (position < cursor) {
                end = cursor - 1;
            } else {
                start = cursor + 1;
            }
        }

        return nums[position];
    }

    int quickSelect(int[] arr, int start, int end) {
        int pivot = arr[end];

        int position = start;

        for (int i = start; i < end; i++) {
            if (arr[i] < pivot) {
                if (position != i) {
                    swap(arr, i, position);
                }

                position++;
            }
        }

        arr[end] = arr[position];
        arr[position] = pivot;

        return position;
    }

    void swap(int[] arr, int index1, int index2) {
        int temp = arr[index1];
        arr[index1] = arr[index2];
        arr[index2] = temp;
    }
}
```



