```
Type "copyright", "credits" or "license" for more information.
IPython 7.31.1 -- An enhanced Interactive Python.
In [1]: import numpy as np
   ...: from scipy.stats import norm
   ...: from matplotlib import pyplot as plt
   ...: from astroML.resample import bootstrap
   ...: from astroML.stats import sigmaG
In [2]: p=1000
In [3]: q=10000
In [4]: np.random.seed(123)
   ...: data = norm(0, 1).rvs(p)
In [5]: mu1_bootstr = bootstrap(data, q, np.median, kwargs=dict(axis=1))
In [6]: x = np.linspace(-0.25, 0.15, 1000)
In [7]: sigma1 = np.sqrt(np.pi/(2*q))
   ...: print(sigma1)
0.012533141373155003
In [8]: gaussian mean=np.mean(mu1 bootstr)
   ...: gaussian std=np.std(mu1 bootstr)
   ...: pdf1=norm(gaussian mean,gaussian std).pdf(x)
In [9]: fig, ax = plt.subplots(figsize=(5, 5))
   ...: ax.hist(mu1_bootstr, bins=50, density=True, histtype='step',
                color='red', ls='dashed', label='Histogram of median')
   ...: ax.plot(x, pdf1, color='gray',label='Gaussian Distribution')
   ...: ax.set_xlabel(r'$\sigma$')
   ...: ax.set_ylabel(r'$p(\sigma|x,I)$')
   ...: ax.legend()
   ...: plt.show()
                       Histogram of median
   16
                           Gaussian Distribution
   14
   12
   10
   8
    6
    4
    2
     -0.25 -0.20 -0.15 -0.10 -0.05 0.00 0.05 0.10 0.15
```

In [10]:

Python 3.9.13 (main, Aug 25 2022, 23:51:50) [MSC v.1916 64 bit (AMD64)]

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```

IPython 7.31.1 -- An enhanced Interactive Python.

```
In [1]: import numpy as np
   ...: from scipy.stats import norm
   ...: from matplotlib import pyplot as plt
   ...: from astroML.resample import bootstrap
   ...: from astroML.stats import sigmaG
In [2]: q=[203,58,210,202,198,158,165,201,157,131,166,160,186,125,218,146]
   ...: q=np.array(q)
In [3]: t=[495,173,479,504,510,416,393,442,317,311,400,337,423,334,533,344]
   ...: t=np.array(t)
In [4]: sigmat=[21,15,27,14,30,16,14,25,52,16,34,31,42,26,16,22]
   ...: sigmat=np.array(sigmat)
In [5]: print(q)
   ...: print(t)
   ...: print(sigmat)
[203 58 210 202 198 158 165 201 157 131 166 160 186 125 218 146]
[495 173 479 504 510 416 393 442 317 311 400 337 423 334 533 344]
[21 15 27 14 30 16 14 25 52 16 34 31 42 26 16 22]
In [6]: from scipy.stats import linregress
   ...: slope, intercept, r_value, p_value, std_err = linregress(q, t)
   ...: sigma_m = std_err / np.sqrt(len(q))
   ...: plt.errorbar(q, t, yerr=sigmat, fmt='o', label='Data')
   ...: plt.plot(q, slope*np.array(q) + intercept, '-', label='Best-fit line')
   ...: plt.xlabel('q')
   ...: plt.ylabel('t')
   ...: plt.legend()
   ...: plt.show()
   ...: print("Standard uncertainty on the slope of the line:", sigma m)
  550
          Best-fit line
          Data
   500
   450
   400
± 350
  300
  250
   200
  150
                 100
                      120
                           140
                                160
                                     180
                                          200
                                               220
```

Standard uncertainty on the slope of the line: 0.04838899281730518

In [7]:

Python 3.9.13 (main, Aug 25 2022, 23:51:50) [MSC v.1916 64 bit (AMD64)] Type "copyright", "credits" or "license" for more information.

IPython 7.31.1 -- An enhanced Interactive Python.

```
In [1]: import numpy as np
   ...: from scipy import stats
   ...: from matplotlib import pyplot as plt
   ...: from astroML.plotting import setup_text_plots
   ...: setup_text_plots(fontsize=8, usetex=True)
   ...:
   ...: # Generate Dataset
   ...: np.random.seed(1)
   ...: N = 50
   ...: L0 = 10
   ...: dL = 0.2
   \dots: t = np.linspace(0, 1, N)
   ...: L obs = np.random.normal(L0, dL, N)
   ...: # Plot the results
   ...: fig = plt.figure(figsize=(5, 5))
   ...: fig.subplots_adjust(left=0.1, right=0.95, wspace=0.05,
   ...: bottom=0.1, top=0.95, hspace=0.05)
   ...: y_vals = [L_obs, L_obs, L_obs, L_obs + 0.5 - t ** 2]
   ...: y_{errs} = [dL, dL * 2, dL / 2, dL]
   ...: titles = ['correct errors',
        'overestimated errors',
         'underestimated errors',
   . . . :
   ...: 'incorrect model']
   ...:
   ...: chi2s=[]
   ...: chi2dofs=[]
   ...: for i in range(4):
            ax = fig.add_subplot(2, 2, 1 + i, xticks=[])
   ...:
            mu = np.mean(y_vals[i])
   ...:
   ...:
            z = (y_vals[i] - mu) / y_errs[i]
            chi2 = np.sum(z ** 2)
   ...:
   ...:
            chi2s.append(chi2)
            chi2dof = chi2 / (N - 1)
   . . . :
            chi2dofs.append(chi2dof)
   . . . :
   ...:
            sigma = np.sqrt(2. / (N - 1))
   ...:
            nsig = (chi2dof - 1) / sigma
   . . . :
   . . . :
   ...:
            ax.errorbar(t, y_vals[i], y_errs[i], fmt='.k', ecolor='gray', lw=1)
   ...:
            ax.plot([-0.1, 1.3], [L0, L0], ':k', lw=1)
   ...:
            ax.text(0.95, 0.95, titles[i], ha='right', va='top',
   . . . :
             transform=ax.transAxes,
   . . . :
             bbox=dict(boxstyle='round', fc='w', ec='k'))
   ...:
            ax.text(0.02, 0.02, r'$\hat{\mu} = %.2f$' % mu, ha='left', va='bottom',
   ...:
   ...:
            transform=ax.transAxes)
            ax.text(0.98, 0.02,
   . . . :
            r'$\chi^2_{\rm dof} = %.2f\, (%.2g\,\sigma)$' % (chi2dof, nsig),
             ha='right', va='bottom', transform=ax.transAxes)
   ...:
   ...: ax.set xlim(-0.05,1.05)
   ...: ax.set_xlim(8.6,11.4)
   ...: ax.yaxis.set_major_locator(plt.MultipleLocator(1))
   ...:
```

```
...: if i>1:
            ax.set xlabel('observations')
   . . . :
   ...: if i%2==0:
            ax.set_label('Luminosity')
   . . . :
   ...: else:
            ax.yaxis.set_major_formatter(plt.NullFormatter())
   ...:
   . . . :
   ...: plt.show()
   ...: print('Chi squares DOF values \n',chi2dofs)
   ...: print('p values are \n', np.array(1)-stats.chi2(chi2dofs).cdf(chi2s))
C:\Users\et22m\anaconda3\lib\site-packages\astroML\linear_model\linear_regression_errors.py:10:
{\tt UserWarning: LinearRegressionwithErrors\ requires\ PyMC3\ to\ be\ installed}
  warnings.warn('LinearRegressionwithErrors requires PyMC3 to be installed')
Traceback (most recent call last):
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\texmanager.py", line 233, in
run checked subprocess
    report = subprocess.check output(
  File "C:\Users\et22m\anaconda3\lib\subprocess.py", line 424, in check_output
    return run(*popenargs, stdout=PIPE, timeout=timeout, check=True,
  File "C:\Users\et22m\anaconda3\lib\subprocess.py", line 505, in run
    with Popen(*popenargs, **kwargs) as process:
  File "C:\Users\et22m\anaconda3\lib\site-packages\spyder kernels\customize\spydercustomize.py", line
108, in init
    super(SubprocessPopen, self). init (*args, **kwargs)
  File "C:\Users\et22m\anaconda3\lib\subprocess.py", line 951, in init
    self. execute child(args, executable, preexec fn, close fds,
  File "C:\Users\et22m\anaconda3\lib\subprocess.py", line 1420, in _execute_child
    hp, ht, pid, tid = _winapi.CreateProcess(executable, args,
FileNotFoundError: [WinError 2] The system cannot find the file specified
The above exception was the direct cause of the following exception:
Traceback (most recent call last):
  File "C:\Users\et22m\anaconda3\lib\site-packages\IPython\core\formatters.py", line 341, in call
    return printer(obj)
  File "C:\Users\et22m\anaconda3\lib\site-packages\IPython\core\pylabtools.py", line 151, in
print figure
    fig.canvas.print figure(bytes io, **kw)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\backend bases.py", line 2295, in
print figure
    self.figure.draw(renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\artist.py", line 73, in draw_wrapper
    result = draw(artist, renderer, *args, **kwargs)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\artist.py", line 50, in draw wrapper
    return draw(artist, renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\figure.py", line 2837, in draw
    mimage._draw_list_compositing_images(
```

```
File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\image.py", line 132, in
draw list compositing images
    a.draw(renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\artist.py", line 50, in draw_wrapper
    return draw(artist, renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\axes\_base.py", line 3091, in draw
    mimage. draw list compositing images(
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\image.py", line 132, in
draw list compositing images
    a.draw(renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\artist.py", line 50, in draw wrapper
    return draw(artist, renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\axis.py", line 1159, in draw
    ticklabelBoxes, ticklabelBoxes2 = self._get_tick_bboxes(ticks_to_draw,
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\axis.py", line 1085, in
get tick bboxes
    return ([tick.label1.get window extent(renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\axis.py", line 1085, in listcomp>
    return ([tick.label1.get window extent(renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\text.py", line 910, in
get window extent
    bbox, info, descent = self._get_layout(self._renderer)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\text.py", line 309, in _get_layout
    _, lp_h, lp_d = renderer.get_text_width_height_descent(
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\backends\backend_agg.py", line 259, in
get text width height descent
    w, h, d = texmanager.get text width height descent(
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\texmanager.py", line 335, in
get_text_width height descent
    dvifile = self.make_dvi(tex, fontsize)
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\texmanager.py", line 271, in make_dvi
    self. run checked subprocess(
  File "C:\Users\et22m\anaconda3\lib\site-packages\matplotlib\texmanager.py", line 237, in
run checked subprocess
    raise RuntimeError(
RuntimeError: Failed to process string with tex because latex could not be found
<Figure size 360x360 with 4 Axes>
Chi squares DOF values
 [0.9592891608441547, 0.23982229021103868, 3.837156643376619, 2.847675397709133]
p values are
 [6.36735109e-12 6.63208859e-05 0.00000000e+00 0.00000000e+00]
In [2]:
```