# Dissertation code Adhiraj

September 9, 2024

```
[]: dbutils.library.restartPython()
```

## 1 Model Training

```
[]: import numpy as np
    import pandas as pd
    import yfinance as yf
    import tensorflow as tf
    from tensorflow.keras.layers import LayerNormalization, Dropout, Dense, u
      →MultiHeadAttention, Input, GlobalAveragePooling1D, Reshape
    from tensorflow.keras.models import Model
    from tensorflow.keras.callbacks import ModelCheckpoint, EarlyStopping
    from sklearn.preprocessing import MinMaxScaler, StandardScaler
    from scipy.optimize import minimize
    import matplotlib.pyplot as plt
    import random
    import datetime
    # Get the current date
    current date = datetime.datetime.now().date()
     # Convert the date to a string
    date_string = current_date.strftime('\"\Y-\"m-\"\d') # Formats the date as_\_
      → "Year-Month-Day"
     # Full list of symbols in Russell 2000 - placeholder for actual list
    all_symbols = ['SMCI', 'MSTR', 'CVNA', 'DOC', 'PR', 'PSN', 'INSM', 'FIX', _
      'APG', 'ELF', 'AMKR', 'APPF', 'ONTO', 'PCVX', 'LNW', 'WFRD',
      'FLR', 'CERE', 'AIT', 'ATI', 'ENSG', 'FN', 'LNTH', 'ANF',

    'UFPI', 'MTDR',

                   'SSD', 'MLI', 'HLNE', 'SPSC', 'VKTX', 'RVMD', 'DRS', 'SSB',
```

```
'ALTR', 'BPMC', 'CHRD', 'SMMT', 'HALO', 'NSIT', 'MTSI', 'IBP', L

¬'TMHC', 'AAON', 'CRS',
               'EVLO', 'PRST', 'VAXX', 'TWOU', 'LPTV', 'AKTS', 'MAXN',
                'DZSI', 'CMAX', 'CARA', 'XAIR', 'VLD', 'WKHS', 'CUTR', 'BIG',
                'BTAI', 'FTCI', 'CUE', 'GORV', 'IMRX', 'EVA', 'BGFV', 'SPWR',
                'RBOT', 'ATRA', 'CARM', 'DFLI', 'BHIL', 'RENT', 'KZR', 'FGEN',
                'VATE', 'BGXX', 'VTNR', 'RPHM', 'PRTS', 'EYEN', 'XGN', 'AVTE',
                'RLYB', 'CMBM', 'VOXX', 'DNMR', 'EGRX', 'TSBX', 'MURA', 'OM',
                'GRTS', 'VOR', 'BRBS', 'FOSL'
]
start_date = '2021-07-01'
end date = '2024-07-01'
# Download data
try:
    data = yf.download(all_symbols, start=start_date, end=end_date)['Adju

close'].dropna(axis=1, how='all')

except Exception as e:
    print(f"Failed to download data: {e}")
    raise SystemExit("Exiting due to data download error.")
weekly_data = data.resample('W').last()
weekly_returns = weekly_data.pct_change().dropna()
scaler = StandardScaler()
mean_returns = np.mean(np.array(weekly_returns), axis=0)
mean returns = scaler.fit transform(mean returns.reshape(-1,1))
scores = mean_returns / scaler.fit_transform(np.std(np.array(weekly_returns),_
 \Rightarrowaxis=0).reshape(-1,1))
top_indices = np.argsort(scores.flatten())[-len(all_symbols):] # Select top_i
 ⇔stocks
top_stocks = [all_symbols[i] for i in top_indices]
# Filter data to include only top stocks
data = data[top stocks]
#weekly_data = data.resample('W').last()
#weekly_returns = weekly_data.pct_change().dropna()
weekly_data = data.resample('W').last()
weekly_returns = weekly_data.pct_change().dropna()
# Scale features
scaler = MinMaxScaler()
scaled_features = scaler.fit_transform(weekly_returns)
forecast_horizon = 8
# Prepare sequences for training
def create_sequences(data, seq_length=10, forecast_horizon=4):
```

```
X, Y = [], []
    for i in range(len(data) - seq_length - forecast_horizon + 1):
        X.append(data[i:i + seq_length])
        Y.append(data[i + seq_length:i + seq_length + forecast_horizon])
    return np.array(X), np.array(Y)
X, Y = create_sequences(scaled_features, 12, forecast_horizon =_
 ⇔forecast_horizon)
# Define the Transformer model
class TransformerBlock(tf.keras.layers.Layer):
    def __init__(self, embed_dim, num_heads, ff_dim, rate=0.1):
        super().__init__()
        self.att = MultiHeadAttention(num heads=num heads, key dim=embed dim)
        self.ffn = tf.keras.Sequential([Dense(ff_dim, activation="relu"),__
 →Dense(embed_dim)])
        self.layernorm1 = LayerNormalization(epsilon=1e-6)
        self.layernorm2 = LayerNormalization(epsilon=1e-6)
        self.dropout1 = Dropout(rate)
        self.dropout2 = Dropout(rate)
    def call(self, inputs, training=False):
        attn_output = self.att(inputs, inputs)
        attn_output = self.dropout1(attn_output, training=training)
        out1 = self.layernorm1(inputs + attn_output)
        ffn_output = self.ffn(out1)
        ffn output = self.dropout2(ffn output, training=training)
        return self.layernorm2(out1 + ffn_output)
def build_transformer_model(input_shape, num_features):
    inputs = Input(shape=input_shape)
    x = inputs
    for _ in range(4): # Number of Transformer blocks
        x = TransformerBlock(embed dim=input shape[-1], num heads=4,,,
 \hookrightarrowff_dim=256, rate=0.5)(x)
    x = GlobalAveragePooling1D()(x)
    x = Dense(128, activation='relu')(x)
    x = Dropout(0.5)(x)
    outputs = Dense(forecast_horizon * num_features, activation='linear')(x)
    outputs = Reshape((forecast horizon, num features))(outputs) # Ensure
 →output is reshaped to [forecast_horizon, num_features]
    model = Model(inputs=inputs, outputs=outputs)
    model.compile(optimizer=tf.keras.optimizers.SGD(learning rate=3e-5),
 ⇔loss="mse")
    return model
```

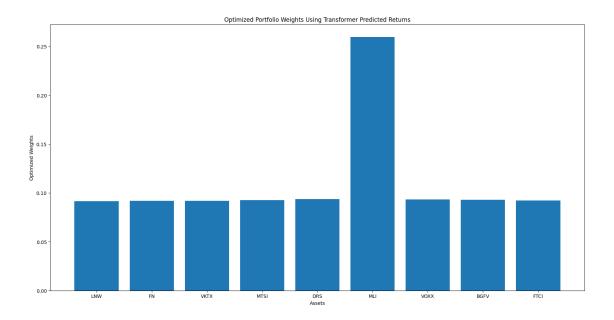
Model: "functional\_124"

Layer (type)	Output Shape	Param #
<pre>input_layer_120 (InputLayer)</pre>	(None, 12, 101)	0
<pre>transformer_block_96 (TransformerBlock)</pre>	(None, 12, 101)	217,002
<pre>transformer_block_97 (TransformerBlock)</pre>	(None, 12, 101)	217,002
<pre>transformer_block_98 (TransformerBlock)</pre>	(None, 12, 101)	217,002
<pre>transformer_block_99 (TransformerBlock)</pre>	(None, 12, 101)	217,002
<pre>global_average_pooling1d_24 (GlobalAveragePooling1D)</pre>	(None, 101)	0
dense_248 (Dense)	(None, 128)	13,056
dropout_324 (Dropout)	(None, 128)	0
dense_249 (Dense)	(None, 808)	104,232
reshape_24 (Reshape)	(None, 8, 101)	0

```
Total params: 985,296 (3.76 MB)
 Trainable params: 985,296 (3.76 MB)
Non-trainable params: 0 (0.00 B)
Epoch 1/200
                7s 7s/step - loss:
1/1
0.2963 - val_loss: 0.3003
Epoch 2/200
                1s 789ms/step - loss:
1/1
0.3008 - val_loss: 0.3003
Epoch 3/200
1/1
                1s 989ms/step - loss:
0.2960 - val_loss: 0.3003
Epoch 4/200
1/1
                1s 750ms/step - loss:
0.2961 - val_loss: 0.3002
Epoch 5/200
                1s 860ms/step - loss:
0.3038 - val_loss: 0.3002
Epoch 6/200
1/1
                1s 761ms/step - loss:
0.3058 - val_loss: 0.3002
                1s 660ms/step
1/1
```

## 2 Portfolio Optimisation after using transformer

```
# Combine historic and forecasted returns
all_returns = np.concatenate((weekly_returns.values, forecasted returns),_
 ⇔axis=0)
scaler = StandardScaler()
mean_returns = np.mean(all_returns, axis=0)
mean returns = scaler.fit transform(mean returns.reshape(-1,1))
volatility = scaler.fit_transform(np.std(all_returns, axis=0).reshape(-1,1))
factor = 0.2
def allocate_portfolio(risk_aversion, high_cap_weight_base,_
 →low_cap_weight_base):
   high cap weight = high cap weight base + factor * (risk aversion - 1.5) * |
 →(1 - high_cap_weight_base)
   low_cap_weight = low_cap_weight_base - factor * (risk_aversion - 1.5) *__
 →low_cap_weight_base
   return high_cap_weight, low_cap_weight
# Base weights assuming a balanced risk aversion (lambda = 1)
high_cap_weight_base = 0.55 # 55% to high cap at neutral risk aversion
low_cap_weight_base = 0.45 # 45% to low cap at neutral risk aversion
high cap weight, low cap weight = allocate portfolio(risk av,
 →high_cap_weight_base, low_cap_weight_base)
top_indices_high = np.argsort(mean_returns[:50].
 →flatten())[-int(high_cap_weight*10):] # Select top stocks
top indices low = np.argsort(-mean returns[50:].flatten())[:
 →int(low_cap_weight*10)] + 50
top indices = []
top_indices.extend(top_indices_high)
top indices.extend(top indices low)
top_stocks = [all_symbols[i] for i in top_indices]
top mean returns = mean returns[top indices]
cov_matrix = np.cov(top_mean_returns, rowvar=False)
optimized_weights = markowitz_optimization(top_mean_returns, cov_matrix,risk_av)
# Visualize the optimized portfolio weights
plt.figure(figsize=(20, 10))
plt.bar(top_stocks, optimized_weights)
plt.xlabel('Assets')
plt.ylabel('Optimized Weights')
plt.title('Optimized Portfolio Weights Using Transformer Predicted Returns')
plt.show()
```



```
[]: df = pd.DataFrame({
         'Stock': top_stocks,
         'Optimized Weight': optimized_weights
     })
     df.columns = ['Stock', 'Optimized_Weight']
     # Convert the DataFrame to a Spark DataFrame
     spark_df = spark.createDataFrame(df)
     # Create the database if it doesn't exist
     spark.sql("CREATE DATABASE IF NOT EXISTS adhi_db")
     # Write the DataFrame to the Spark SQL table, trying to overwrite the existing
      \hookrightarrow data
     if isinstance(risk_av, float):
         formatted_risk_av = str(risk_av).replace('.', '_')
     else:
         formatted_risk_av = str(risk_av)
     spark_df.write.option("overwriteSchema", "true").mode("overwrite").
      ⇔saveAsTable(f"adhi_db.trans_weights_{formatted_risk_av}")
```

```
[]: # Symbols for your stocks and weights from Markowitz Optimization
weights = optimized_weights

# Fetch historical data
data = yf.download(top_stocks, start=start_date, end=end_date)['Adj Close']
```

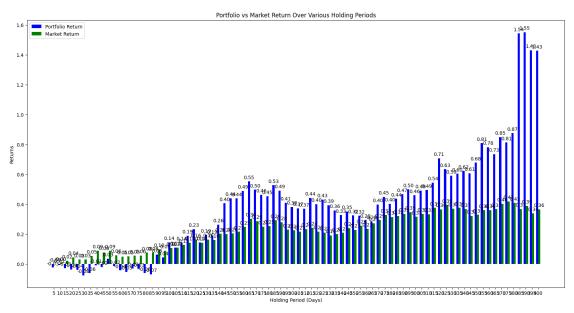
```
# Function to calculate returns for holding periods
def calculate_returns_for_periods(data, periods):
    if isinstance(data, pd.Series):
        # Handle Series input for single stock/index data
       returns = pd.DataFrame(index=data.index)
        for period in periods:
            returns[f'{period} day return'] = (data.pct_change(periods=period)*__
 ⇒weights).sum(axis=1)
    elif isinstance(data, pd.DataFrame):
        # Handle DataFrame input for multiple stocks
       returns = pd.DataFrame(index=data.index)
       for period in periods:
            returns[f'{period} day return'] = (data.pct_change(periods=period)*_
 ⇒weights).sum(axis=1)
   return returns
# Calculate returns for various holding periods
holding_periods = list(range(5,405,5)) # Example holding periods
portfolio_returns = calculate_returns_for_periods(data, holding_periods)
risks = portfolio_returns.std()
```

[\*\*\*\*\*\*\*\* 9 of 9 completed

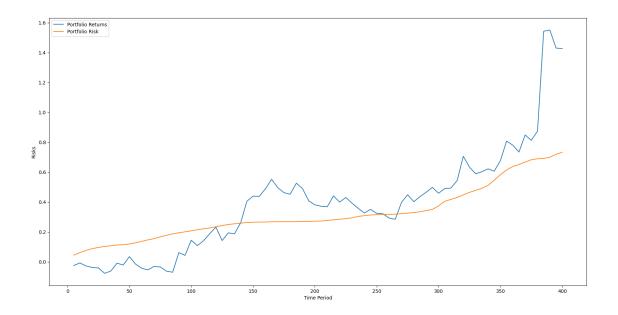
```
[]: # Fetch market index data
     market_data = yf.download('^GSPC', start=start_date, end=end_date)['Adj Close']__
     → # Russell 2000 as the market index
     def calculate_returns_for_periods_market(data, periods):
         if isinstance(data, pd.Series):
             # Handle Series input for single stock/index data
             returns = pd.DataFrame(index=data.index)
             for period in periods:
                 returns[f'{period} day return'] = data.pct_change(periods=period)
         elif isinstance(data, pd.DataFrame):
             # Handle DataFrame input for multiple stocks
             returns = pd.DataFrame(index=data.index)
             for period in periods:
                 returns[f'{period} day return'] = data.pct_change(periods=period)
         return returns
     # Calculate market returns for the same holding periods
     market_returns = calculate_returns_for_periods_market(market_data,__
      ⇔holding_periods)
     market_risks = market_returns.std()
```

[\*\*\*\*\*\*\*\* 100%\*\*\*\*\*\*\*\*\*\* 1 of 1 completed

```
[]: # Extract the last value for each period to represent the period return
     final_portfolio_returns = {period: portfolio_returns[f'{period} day return'].
      →iloc[-1] for period in holding_periods}
     final_market_returns = {period: market_returns[f'{period} day return'].iloc[-1]__
      →for period in holding_periods}
[]: comparison_df = pd.DataFrame({
         'Holding Period': holding_periods,
         'Portfolio Return': list(final_portfolio_returns.values()),
         'Market Return': list(final_market_returns.values()),
         'Portfolio Risk' : risks,
         'Market Risk' : market_risks
     })
[]: # Set the width for each bar
     bar width = 0.35
     # Set positions for the groups of bars
     index = np.arange(len(comparison_df['Holding Period']))
     plt.figure(figsize=(20,10))
     # Create a bar plot for the portfolio returns
     portfolio_bars = plt.bar(index - bar_width/2, comparison_df['Portfolio_u
      GReturn'], bar_width, label='Portfolio Return', color='blue')
     # Create a bar plot for the market returns, positioned next to the first
     market bars = plt.bar(index + bar width/2, comparison df['Market Return'],
      ⇒bar_width, label='Market Return', color='green')
     # Annotate each bar with its respective data value
     for bar in portfolio_bars:
         yval = bar.get_height()
         plt.annotate(f'{yval:.2f}',
                      (bar.get_x() + bar.get_width() / 2, yval),
                      ha='center', va='bottom', textcoords="offset points",
      \rightarrowxytext=(0,3))
     for bar in market_bars:
         yval = bar.get_height()
         plt.annotate(f'{yval:.2f}',
                      (bar.get_x() + bar.get_width() / 2, yval),
                      ha='center', va='bottom', textcoords="offset points",
      \rightarrowxytext=(0,3))
     # Add labels, title, and legend
     plt.xlabel('Holding Period (Days)')
```



[]: <matplotlib.legend.Legend at 0x7f71e8e54b20>

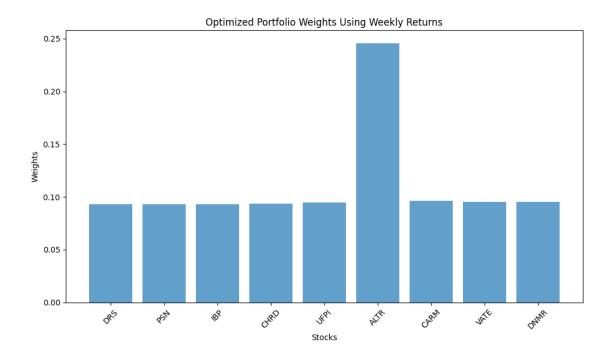


### 2.1 Markowitz w/o transformer

```
[]: import numpy as np
    import pandas as pd
    import yfinance as yf
    from sklearn.preprocessing import StandardScaler
    from scipy.optimize import minimize
    import matplotlib.pyplot as plt
    # Fetch historical stock data
    try:
        data = yf.download(all_symbols, start=start_date, end=end_date)['Adj_
     except Exception as e:
        print(f"Failed to download data: {e}")
        raise SystemExit("Exiting due to data download error.")
    # Calculate weekly returns
    weekly_data = data.resample('W').last()
    weekly_returns = weekly_data.pct_change().dropna()
    mean_daily_returns = weekly_returns.mean()
    # Scale the returns
    scaler = StandardScaler()
```

```
scaled_daily_returns = scaler.fit_transform(np.array(mean_daily_returns).
 \hookrightarrowreshape(-1,1))
top indices high = np.argsort(scaled daily returns[:50].
 →flatten())[-int(high_cap_weight*10):] # Select top stocks
top_indices_low = np.argsort(-scaled_daily_returns[50:].flatten())[:
 →int(low_cap_weight*10)] + 50
top_indices = []
top_indices.extend(top_indices_high)
top indices.extend(top indices low)
top_stocks1 = [all_symbols[i] for i in top_indices]
top mean returns = scaled daily returns[top indices]
cov_matrix = np.cov(top_mean_returns, rowvar=False)
#cov_matrix = np.cov(scaled_daily_returns, rowvar=False)
# Function for the Markowitz optimization
def markowitz_optimization(returns, cov_matrix, risk_aversion=4):
    n_assets = returns.shape[0]
    def objective(weights):
        return -(np.dot(weights, returns) - risk_aversion * np.dot(weights.T,_
 →np.dot(cov matrix, weights)))
    constraints = [{'type': 'eq', 'fun': lambda weights: np.sum(weights) - 1}]
    bounds = [(0, 1) for _ in range(n_assets)]
    result = minimize(objective, np.full(n_assets, 1/n_assets), method='SLSQP', __
 ⇒bounds=bounds, constraints=constraints)
    if not result.success:
        print("Optimization failed: ", result.message)
        return None
    return result.x
# Run Markowitz optimization
optimized_result = markowitz_optimization(top_mean_returns, cov_matrix,risk_av)
# Visualize the optimized portfolio weights
plt.figure(figsize=(10, 6))
plt.bar(top_stocks1, optimized_result, alpha=0.7)
plt.title('Optimized Portfolio Weights Using Weekly Returns')
plt.xlabel('Stocks')
plt.ylabel('Weights')
plt.xticks(rotation=45)
plt.tight_layout()
plt.show()
```

[\*\*\*\*\*\*\*\* 101 of 101 completed



```
[]: # Symbols for your stocks and weights from Markowitz Optimization
weights = optimized_result

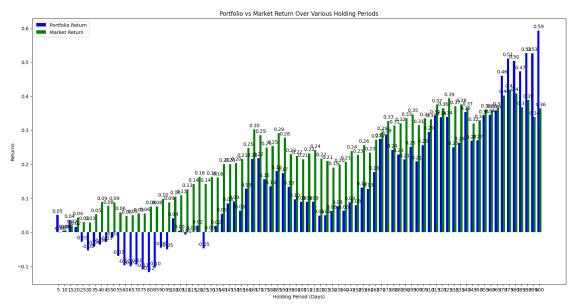
# Fetch historical data
data = yf.download(top_stocks1, start=start_date, end=end_date)['Adj Close']

# Function to calculate returns for holding periods
def calculate_returns_for_periods(data, periods):
    if isinstance(data, pd.Series):
        # Handle Series input for single stock/index data
        returns = pd.DataFrame(index=data.index)
```

```
returns[f'{period} day return'] = (data.pct_change(periods=period)*__
      ⇒weights).sum(axis=1)
         elif isinstance(data, pd.DataFrame):
             # Handle DataFrame input for multiple stocks
            returns = pd.DataFrame(index=data.index)
            for period in periods:
                returns[f'{period} day return'] = (data.pct_change(periods=period)*_
      ⇒weights).sum(axis=1)
        return returns
     # Calculate returns for various holding periods
     \#holding\_periods = list(range(5,205,5)) \# Example holding periods
    portfolio_returns1 = calculate_returns_for_periods(data, holding_periods)
    [******** 9 of 9 completed
[]: # Extract the last value for each period to represent the period return
    final_portfolio_returns1 = {period: portfolio_returns1[f'{period} day return'].
     →iloc[-1] for period in holding_periods}
    final market_returns1 = {period: market_returns[f'{period} day return'].
      →iloc[-1] for period in holding periods}
[]: comparison df1 = pd.DataFrame({
         'Holding Period': holding_periods,
         'Portfolio Return': list(final portfolio returns1.values()),
         'Market Return': list(final_market_returns1.values())
    })
[]: # Set the width for each bar
    bar_width = 0.35
    plt.figure(figsize=(20,10))
     # Set positions for the groups of bars
    index = np.arange(len(comparison_df1['Holding Period']))
    # Create a bar plot for the portfolio returns
    portfolio_bars = plt.bar(index - bar_width/2, comparison_df1['Portfolio_
      →Return'], bar_width, label='Portfolio Return', color='blue')
    # Create a bar plot for the market returns, positioned next to the first
    market_bars = plt.bar(index + bar_width/2, comparison_df1['Market_Return'],__
      ⇒bar_width, label='Market Return', color='green')
     # Annotate each bar with its respective data value
    for bar in portfolio_bars:
```

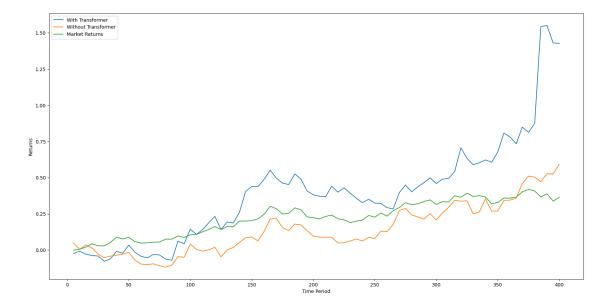
for period in periods:

```
yval = bar.get_height()
    plt.annotate(f'{yval:.2f}',
                  (bar.get_x() + bar.get_width() / 2, yval),
                 ha='center', va='bottom', textcoords="offset points", u
 \rightarrowxytext=(0,3))
for bar in market_bars:
    yval = bar.get_height()
    plt.annotate(f'{yval:.2f}',
                 (bar.get_x() + bar.get_width() / 2, yval),
                 ha='center', va='bottom', textcoords="offset points", u
 \rightarrowxytext=(0,3))
# Add labels, title, and legend
plt.xlabel('Holding Period (Days)')
plt.ylabel('Returns')
plt.title('Portfolio vs Market Return Over Various Holding Periods')
plt.xticks(index, comparison_df1['Holding Period']) # Set x-ticks to match the_
 ⇔holding periods
plt.legend()
# Show the plot
plt.show()
```



```
[]: plt.figure(figsize=(20,10))
```

#### []: <matplotlib.legend.Legend at 0x7f71e832bdc0>



```
[]: df = pd.DataFrame({
    'With Transformer': comparison_df['Portfolio Return'],
    'Without Transformer': list(final_portfolio_returns1.values()),
    'Market Returns': comparison_df['Market Return'],
    'Holding Periods': comparison_df['Holding Period'],
    'Portfolio Risk': comparison_df['Portfolio Risk'],
    'Market Risk': comparison_df['Market Risk']
})

spark_df = spark.createDataFrame(df)
spark.sql("CREATE DATABASE IF NOT EXISTS adhi_db")
if isinstance(risk_av, float):
    formatted_risk_av = str(risk_av).replace('.', '__')
```

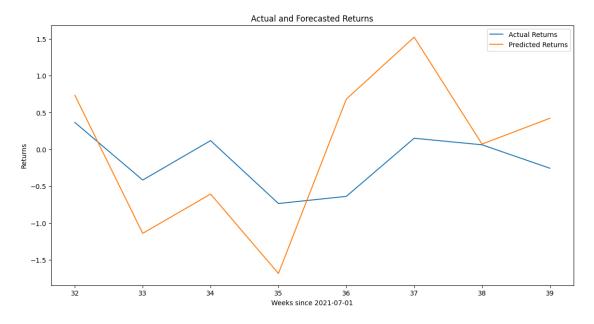
#### 3 Model Performance

```
[]: from datetime import datetime, timedelta
     forecasted_returns1 = np.mean(forecasted_returns,axis = 1)
     date = datetime.strptime(end_date, '%Y-%m-%d')
     # Calculate the date 8 weeks before
     end_date1 = date + timedelta(weeks=forecast_horizon)
     # Download and process data
     try:
         data1 = yf.download(all_symbols, start=start_date, end=end_date1)['Adju

close'].dropna(axis=1, how='all')

     except Exception as e:
         print(f"Failed to download data: {e}")
         raise SystemExit("Exiting due to data download error.")
     weekly data1 = data1.resample('W').last()
     weekly_returns1 = weekly_data1.pct_change().dropna()
     # Combine actual and predicted for plot
     all_actual_returns = np.mean(weekly_returns1,axis=1)
     scaler = StandardScaler()
     predicted_returns = scaler.fit_transform(forecasted_returns1.reshape(-1,1))
     all_actual_returns = scaler.fit_transform(np.array(all_actual_returns).
      \hookrightarrowreshape(-1,1))
     predicted_index = range(len(all_actual_returns) - forecast_horizon,_
      →len(all_actual_returns))
     # Plotting
     plt.figure(figsize=(14, 7))
     plt.plot(predicted_index,all_actual_returns[predicted_index], label='Actual_
      ⇔Returns')
     plt.plot(predicted_index, predicted_returns, label='Predicted Returns')
     #plt.plot(predicted index, forecasted returns, label='Predicted Returns')
     plt.title('Actual and Forecasted Returns')
     plt.xlabel('Weeks since ' + start_date)
     plt.ylabel('Returns')
     plt.legend()
     plt.show()
```

1/1 1s 551ms/step



#### 3.1 RMSE

[]: np.mean((all\_actual\_returns[predicted\_index] - predicted\_returns)\*\*2)\*\*0.5

[]: 0.8777246402749992