Introduction to Program Analysis

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Part 1

About These Slides

These slides constitute the lecture notes for CS618 Program Analysis course at IIT Bombay and have been made available as teaching material accompanying the book:

Intro to PA: About These Slides

Copyright

- Uday Khedker, Amitabha Sanyal, and Bageshri Karkare.
 Data Flow Analysis: Theory and Practice. CRC Press (Taylor and Francis Group). 2009.
- Apart from the above book, some slides are based on the material from the

(Indian edition published by Ane Books in 2013)

- A. V. Aho, M. Lam, R. Sethi, and J. D. Ullman. Compilers: Principles,
 - Techniques, and Tools. Addison-Wesley. 2006.
 M. S. Hecht. Flow Analysis of Computer Programs. Elsevier
- North-Holland Inc. 1977.

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Intro to PA: Outline

Motivating the Need of Program Analysis

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- Some representative examples
 - ► Classical optimizations performed by compilers
 - Optimizing heap memory usage
- Course details, schedule, assessment policies etc.
- Soundness and Precision
- Program Model

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Part 2

Classical Optimizations

Examples of Optimising Transformations (ALSU, 2006)

A C program and its optimizations

```
void quicksort(int m, int n)
{ int i, j, v, x;
   if (n \le m) return;
   i = m-1; j = n; v = a[n];
                                              /* v is the pivot */
   while(1)
                                        /* Move values smaller */
    { do i = i + 1; while (a[i] < v); /* than v to the left of */
       do i = i - 1; while (a[i] > v); /* the split point (sp) *
       if (i \ge i) break;
                                           /* and other values */
       x = a[i]; a[i] = a[i]; a[i] = x;
                                           /* to the right of sp */
                                           /* of the split point */
   x = a[i]; a[i] = a[n]; a[n] = x; /* Move the pivot to sp *
   quicksort(m,i); quicksort(i+1,n); /* sort the partitions to \star/
          /* the left of sp and to the right of sp independently \star/
```

Intermediate Code

13. if t5 > v goto 10

14. if i >= i goto 25

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For the boxed source code

1. i = m - 1

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- 2. j = n
- 3. t1 = 4 * n
- 4. t6 = a[t1]
- 5. v = t6
- 6. i = i + 1
- 7. t2 = 4 * i
- 8. t3 = a[t2]
- 9. if t3 < v goto 6
- 10. j = j 1

11. t4 = 4 * i

- 20. t5 = a[t4]
 - 21. a[t2] = t5

12. t5 = a[t4]

15. t2 = 4 * i

16. t3 = a[t2]

18. t2 = 4 * i

19. t4 = 4 * i

17. x = t3

22. t4 = 4 * i

24. goto 6 25. t2 = 4 * i

23. a[t4] = x

26. t3 = a[t2]

28. t2 = 4 * i

27. x = t3

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- 29. t1 = 4 * n30. t6 = a[t1]
- 31. a[t2] = t6
- 32. t1 = 4 * n
- 33. a[t1] = x

Intermediate Code: Observations

Multiple computations of expressions

- Simple control flow (conditional/unconditional goto) Yet undecipherable!
- Array address calculations

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Understanding Control Flow

- Identify maximal sequences of linear control flow
 - ⇒ Basic Blocks

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• No transfer into or out of basic blocks except the first and last statements Control transfer into the block: only at the first statement.

Control transfer out of the block : only at the last statement.

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Intermediate Code with Basic Blocks

1. 1 — 111 - 1	La de la companya de	23. a 14 - x
2. $j = n$	13. if $t5 > v goto 10$	24. goto 6
3. $t1 = 4 * n$	14. if $i >= j$ goto 25	25. t2 = 4 * i
4. t6 = a[t1] 5. v = t6	15. t2 = 4 * i	26. $t3 = a[t2]$
	16. $t3 = a[t2]$	27. $x = t3$
6. $i = i + 1$	17. $x = t3$	28. $t^2 = 4 * i$

12. t5 = a[t4]

9. if t3 < v goto 6 10. j = j - 111. t4 = 4 * j

7. t2 = 4 * i

8. t3 = a[t2]

20. t5 = a[t4]21. a[t2] = t5

18. t2 = 4 * i

19. t4 = 4 * i

22. t4 = 4 * i

29. t1 = 4 * n30. t6 = a[t1]

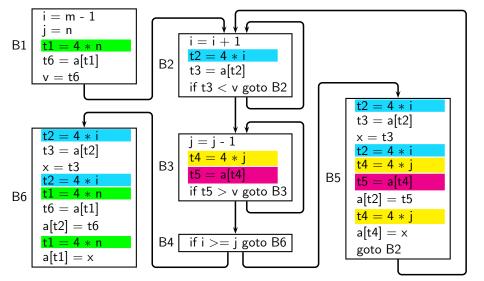
31. a[t2] = t632. t1 = 4 * n

33. a[t1] = x

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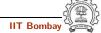
Program Flow Graph

Program Flow Graph



Program Flow Graph: Observations

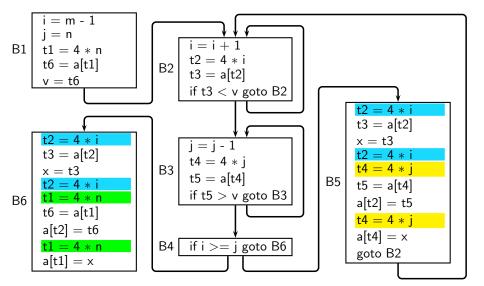
Nesting Level	Basic Blocks	No. of Statements
0	B1, B6	14
1	B4, B5	11
2	B2 B3	8



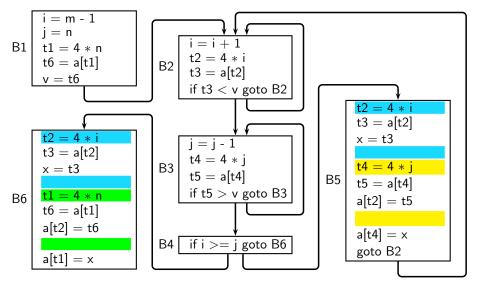
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Local Common Subexpression Elimination

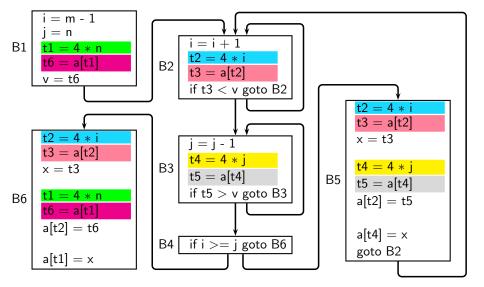


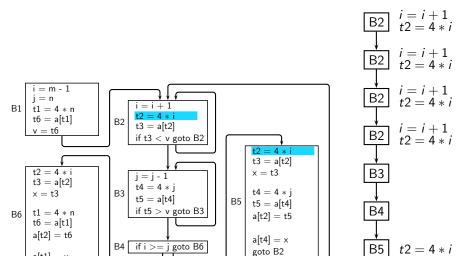
Local Common Subexpression Elimination



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Global Common Subexpression Elimination





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a[t1] = x

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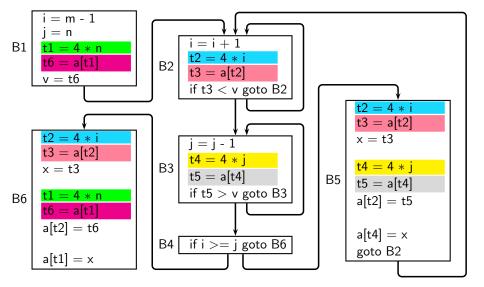
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B2 i = i + 1 t2 = 4 * iB2 i = i + 1 t2 = 4 * iB3 i = i + 1 t2 = 4 * i t2 = 4 * it3 = a[t2]

= m - 1i = i + 1t2 = 4 * iB1 t1 = 4 * nt6 = a[t1]i = i + 1 t2 = 4 * iv = t6B2 if $t3 < v \ goto \ B2$ t2 = 4 * it3 = a[t2]t2 = 4 * iB3 x = t3j = j - 1 t3 = a[t2]t4 = 4 * iВ3 t4 = 4 * ix = t3t5 = a[t4]B5 t5 = a[t4]B4 if t5 > v goto B3 t1 = 4 * nB6 a[t2] = t5t6 = a[t1]a[t2] = t6a[t4] = xB4 if i >= j goto B6 B₅ t2 = 4 * igoto B2 a[t1] = x

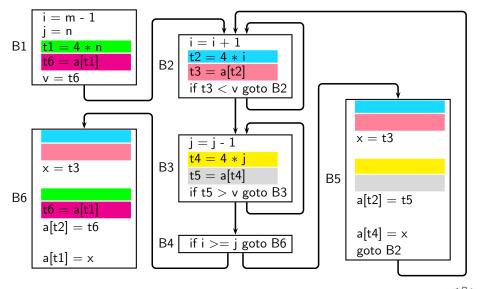
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Global Common Subexpression Elimination



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Global Common Subexpression Elimination



Other Classical Optimizations

Copy propagation

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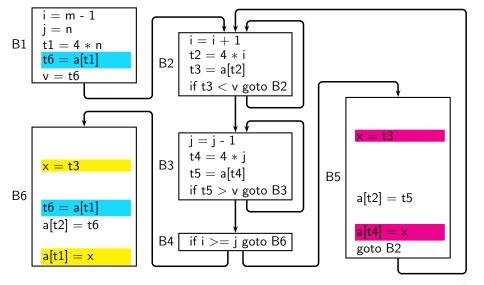
- Strength Reduction
- Elimination of Induction Variables
- Dead Code Elimination



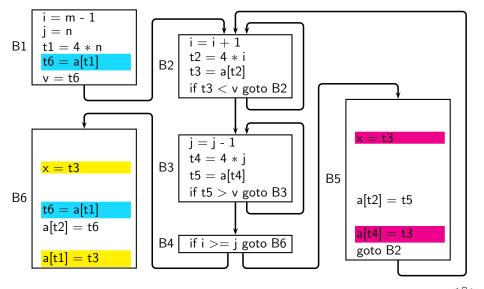
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Copy Propagation and Dead Code Elimination

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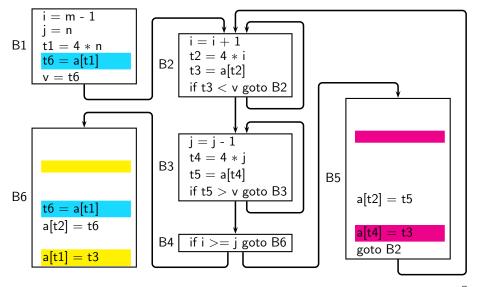


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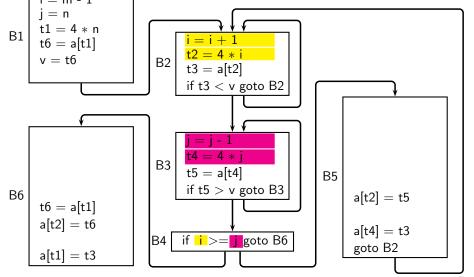
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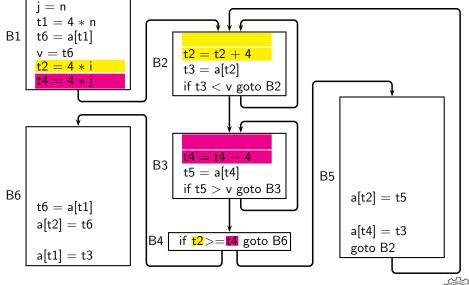


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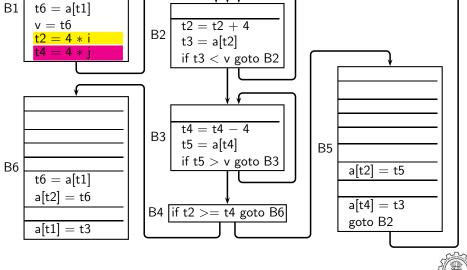
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Optimized Program Flow Graph

Nesting Level	No. of Statements	
	Original	Optimized
0	14	10
1	11	4
2	8	6

If we assume that a loop is executed 10 times, then the number of computations saved at run time

$$= (14-10) + (11-4) \times 10 + (8-6) \times 10^2 = 4 + 70 + 200 = 274$$

Observations

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- Optimizations are transformations based on some information.
- Systematic analysis required for deriving the information.

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We have looked at data flow optimizations.
 Many control flow optimizations can also be performed.

Categories of Optimizing Transformations and Analyses

Code Motion Redundancy Elimination Control flow Optimization	Machine Independent	Flow Analysis (Data + Control)
Loop Transformations	Machine Dependent	Dependence Analysis (Data + Control)
Instruction Scheduling Register Allocation Peephole Optimization	Machine Dependent	Several Independent Techniques
Vectorization Parallelization	Machine Dependent	Dependence Analysis (Data + Control)

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Discovering information about a given program

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What is Program Analysis?

Discovering information about a given program

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Representing the dynamic behaviour of the program

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What is Program Analysis?

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Discovering information about a given program

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- Representing the dynamic behaviour of the program
- Most often obtained without executing the program
 - ▶ Static analysis Vs. Dynamic Analysis
 - ► Example of loop tiling for parallelization



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Discovering information about a given program

- Representing the dynamic behaviour of the program
 - Most often obtained without executing the program
 - Static analysis Vs. Dynamic Analysis
 - Example of loop tiling for parallelization
- Must represent all execution instances of the program

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- Code optimization
 - ► Improving time, space, energy, or power efficiency Compilation for special architecture (eg. multicore)



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Why is it Useful?

- Code optimization
 - ▶ Improving time, space, energy, or power efficiency
 - Compilation for special architecture (eg. multicore)
- Verification and validation

Giving guarantees such as: The program will

- never divide a number by zero
- never dereference a NULL pointer
- close all opened files, all opened socket connections
- not allow buffer overflow security violation



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Why is it Useful?

- Code optimization
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- Software engineering
 - ► Maintenance, bug fixes, enhancements, migration
 - Example: Y2K problem

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Improving time, space, energy, or power efficiency
 Compilation for special architecture (eg. multicore)

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Why is it Useful?

Verification and validation

Code optimization

Giving guarantees such as: The program will

- never divide a number by zero
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- not allow buffer overflow security violation
- Software engineering
 - ▶ Maintenance, bug fixes, enhancements, migration
 - Example: Y2K problem
- Reverse engineering

To understand the program



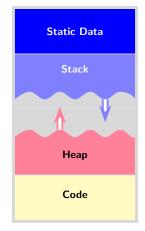
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Part 3

Optimizing Heap Memory Usage

Standard Memory Architecture of Programs



Heap allocation provides the flexibility of

• Variable Sizes. Data structures can grow or shrink as desired at runtime.

(Not bound to the declarations in program.)

• Variable Lifetimes. Data structures can be created and destroyed as desired at runtime.

(Not bound to the activations of procedures.)



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Decision 1: When to Allocate?

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- Explicit. Specified in the programs. (eg. Imperative/OO languages)
- Implicit. Decided by the language processors. (eg. Declarative Languages)

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Decision 1: When to Allocate?

- Explicit. Specified in the programs. (eg. Imperative/OO languages)
- Implicit. Decided by the language processors. (eg. Declarative Languages)

Decision 2: When to Deallocate?

- Explicit. Manual Memory Management (eg. C/C++)
- Implicit. Automatic Memory Management aka Garbage Collection (eg. Java/Declarative languages)

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State of Art in Manual Deallocation

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- Memory leaks
 10% to 20% of last development effort goes in plugging leaks
- Tool assisted manual plugging
 Purify, Electric Fence, RootCause, GlowCode, yakTest, Leak Tracer, BDW
 Garbage Collector, mtrace, memwatch, dmalloc etc.
- All leak detectors

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- ▶ are dynamic (and hence specific to execution instances)
- ▶ generate massive reports to be perused by programmers
- usually do not locate last use but only allocation escaping a call
 - ⇒ At which program point should a leak be "plugged"?

Garbage Collection ≡ Automatic Deallocation

• Retain active data structure.

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- Deallocate inactive data structure.
- What is an Active Data Structure?

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Garbage Collection ≡ Automatic Deallocation

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Retain active data structure.

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Deallocate inactive data structure.

• What is an Active Data Structure?

If an object does not have an access path, (i.e. it is unreachable) then its memory can be reclaimed.

Intro to PA: Optimizing Heap Memory Usage CS 618 Garbage Collection

■ Automatic Deallocation

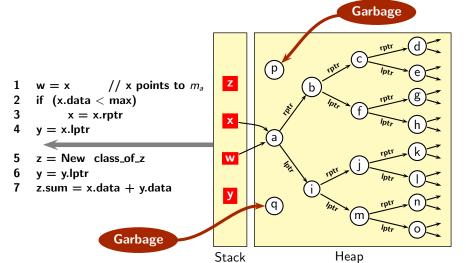
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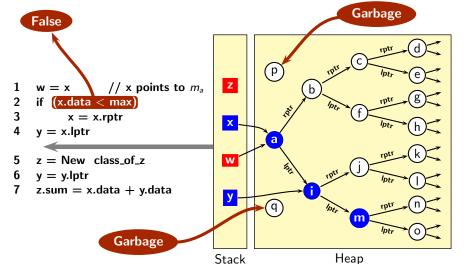
- Retain active data structure.
 - Deallocate inactive data structure.
- What is an Active Data Structure?

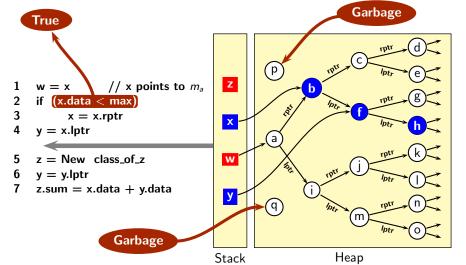
If an object does not have an access path, (i.e. it is unreachable) then its memory can be reclaimed.

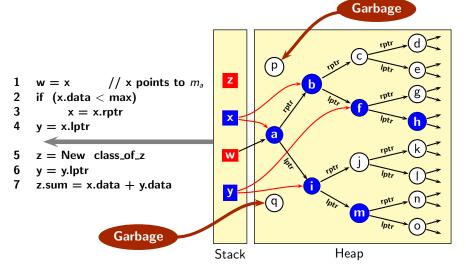
What if an object has an access path, but is not accessed after the given program point?

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All white nodes are unused and should be considered garbage

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Is Reachable Same as Live?

From www.memorymanagement.org/glossary

live (also known as alive, active): Memory(2) or an object is live if the program will read from it in future. The term is often used more broadly to mean reachable.

It is not possible, in general, for garbage collectors to determine exactly which objects are still live. Instead, they use some approximation to detect objects that are provably dead, *such as those that are not reachable*.

Similar terms: reachable. Opposites: dead. See also: undead.



Is Reachable Same as Live?

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Not really. Most of us know that.

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Even with the state of art of garbage collection, 24% to 76% unused memory remains unclaimed

• The state of art compilers, virtual machines, garbage collectors cannot distinguish between the two

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Comparison between different sets of objects:

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Live ? Reachable ? Allocated

Reachability and Liveness

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Comparison between different sets of objects:

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 $\mathsf{Live} \ \subseteq \ \mathsf{Reachable} \ \subseteq \ \mathsf{Allocated}$

Reachability and Liveness

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 $\mathsf{Live} \ \subseteq \ \mathsf{Reachable} \ \subseteq \ \mathsf{Allocated}$

The objects that are not live must be reclaimed.

Comparison between different sets of objects:

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Reachability and Liveness

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Comparison between different sets of objects:

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Live \subseteq Reachable \subseteq Allocated

The objects that are not live must be reclaimed.

¬ Live ? ¬ Reachable ? ¬ Allocated

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Reachability and Liveness

Comparison between different sets of objects:

Live \subseteq Reachable \subseteq Allocated

The objects that are not live must be reclaimed.

 \neg Live \supseteq \neg Reachable \supseteq \neg Allocated

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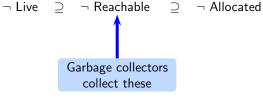
Reachability and Liveness

Comparison between different sets of objects:

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Live \subset Reachable \subset Allocated

The objects that are not live must be reclaimed.



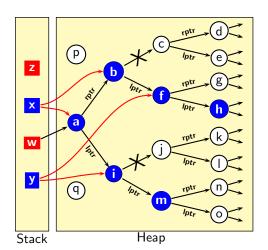
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Cedar Mesa Folk Wisdom

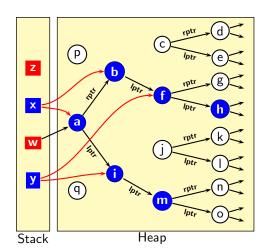
Make the unused memory unreachable by setting references to NULL. (GC FAQ: http://www.iecc.com/gclist/GC-harder.html)



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Cedar Mesa Folk Wisdom

Make the unused memory unreachable by setting references to NULL. (GC FAQ: http://www.iecc.com/gclist/GC-harder.html)



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• Most promising, simplest to understand, yet the hardest to implement.

Intro to PA: Optimizing Heap Memory Usage

- Which references should be set to NULL?
 - ► Most approaches rely on feedback from profiling.
 - No systematic and clean solution.

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Distinguishing Between Reachable and Live

The state of art

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- Eliminating objects reachable from root variables which are not live.
- Implemented in current Sun JVMs.
- Uses liveness data flow analysis of root variables (stack data).
- What about liveness of heap data?

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- // x points to ma
- 2 while (x.data < max) 3 x = x.rptr

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7

- 4 y = x.lptr
 - $z = New class_of_z$
- 5 6
 - y = y.lptr
 - z.sum = x.data + y.data



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Heap

Stack

if changed to while

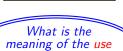
Liveness of Stack Data: An Informal Introduction

- // x points to ma 2 while (x.data < max)
- 3 x = x.rptr
- 4 y = x.lptr
 - 5 z = New class of z
- 6 y = y.lptr
- 7 z.sum = x.data + y.data



Stack

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of data?

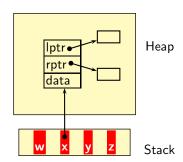
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Liveness of Stack Data: An Informal Introduction

- 1 w = x // x points to m_a
- 2 while (x.data < max)
- x = x.rptr
- 4 y = x.lptr
- 5 z = New class_of_z
- 6 y = y.lptr
- 7 z.sum = x.data + y.data



What is the meaning of the use of data?

Liveness of Stack Data: An Informal Introduction

and reading its contents

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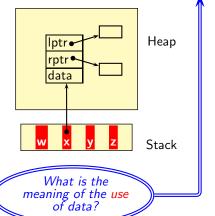
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2

4

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Liveness of Stack Data: An Informal Introduction

and reading its contents

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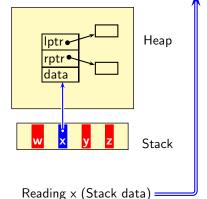
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4

5

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Liveness of Stack Data: An Informal Introduction

m_a

// x points to m_a

while (x.data < max)

x = x.rptry = x.lptr

. .

 $z = New class_of_z$

v.Intr

y = y.lptr

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2

4

5

6

7

z.sum = x.data + y.data

w x y z

lptr•

rptr **^** data

Reading x.data (Heap data) =

and reading its contents

Heap

Stack

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Liveness of Stack Data: An Informal Introduction

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- 2 while (x.data < max)
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Heap lptr• rptr • data Stack

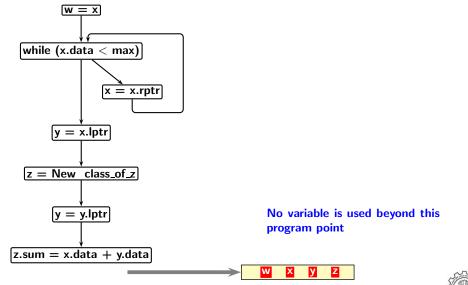
Reading x.rptr (Heap data) —

and reading its contents

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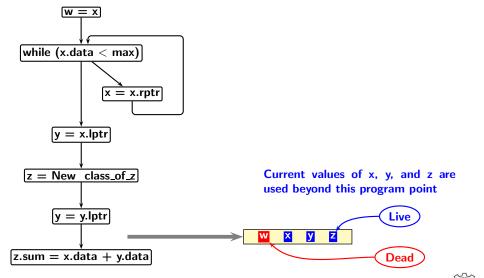
Liveness of Stack Data. All Illiothia introduction

Intro to PA: Optimizing Heap Memory Usage

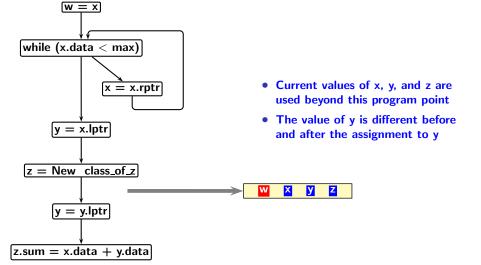


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Liveness of Stack Data: An Informal Introduction



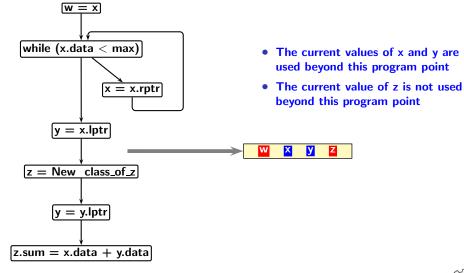
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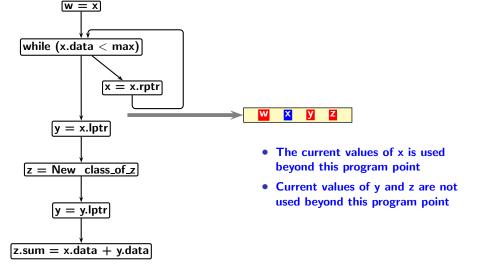
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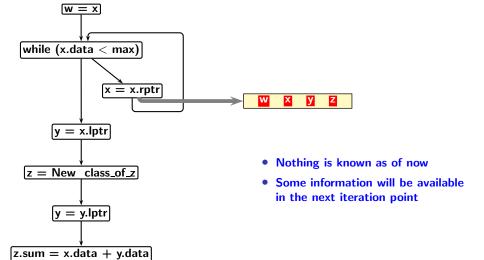
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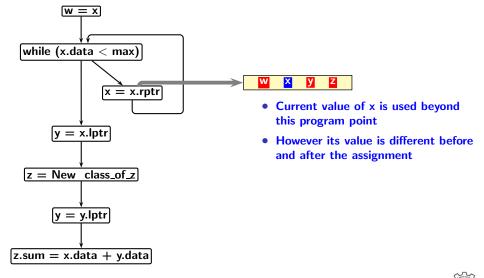
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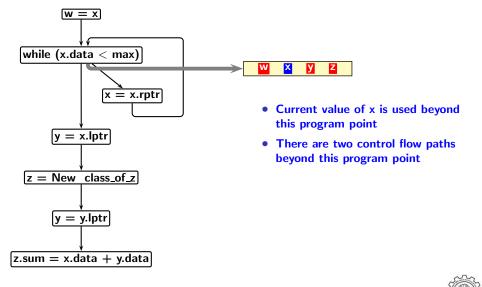
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Intro to PA: Optimizing Heap Memory Usage



Liveness of Stack Data: An Informal Introduction

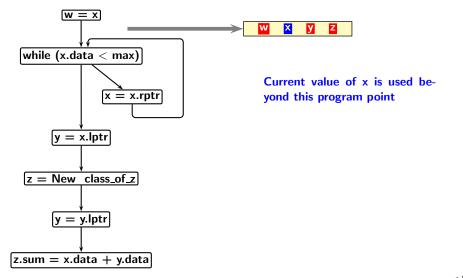


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Liveness of Stack Data: An Informal Introduction

Liveness of Stack Data: All informal introduction

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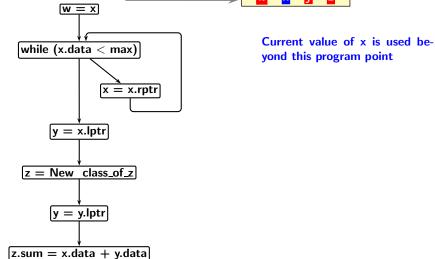


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Liveness of Stack Data: An Informal Introduction

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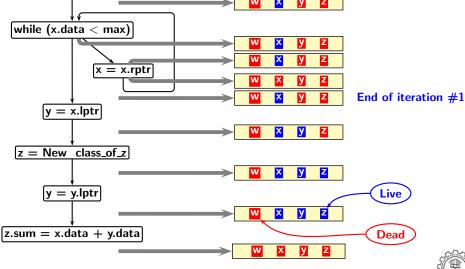


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Liveness of Stack Data: An Informal Introduction

W X Y Z

while (x.data < max)

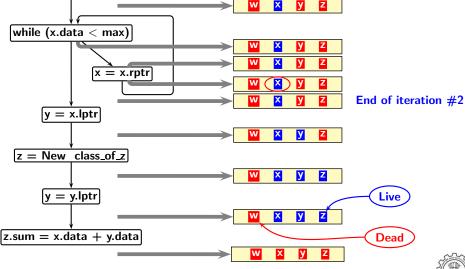


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Liveness of Stack Data: An Informal Introduction

W X Y Z

while (x.data < max)

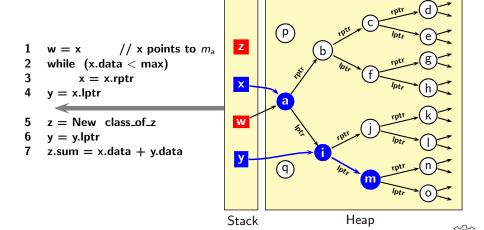


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Applying Cedar Mesa Folk Wisdom to Heap Data

Liveness Analysis of Heap Data

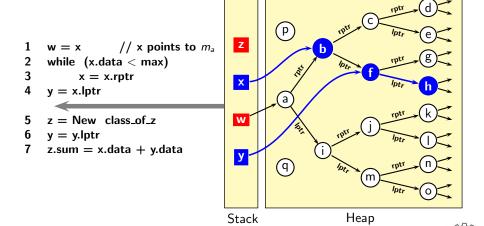
If the while loop is not executed even once.



Applying Cedar Mesa Folk Wisdom to Heap Data

Liveness Analysis of Heap Data

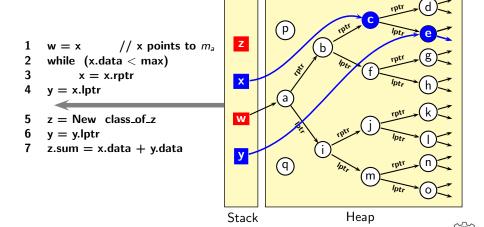
If the while loop is executed once.



Applying Cedar Mesa Folk Wisdom to Heap Data

Liveness Analysis of Heap Data

If the while loop is executed twice.



The Moral of the Story

Mappings between access expressions and I-values keep changing

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- This is a rule for heap data
 For stack and static data, it is an exception!
- Static analysis of programs has made significant progress for stack and static data.

What about heap data?

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- ► Given two access expressions at a program point, do they have the same l-value?
- ► Given the same access expression at two program points, does it have the same I-value?

Intro to PA: Optimizing Heap Memory Usage

w = null

x.lptr = null

y = z = null

```
w = x
```

while
$$(x.data < max)$$

$$x = x.rptr$$

$$x = x.rptr$$

$$y = x.lptr$$

y = y.lptr

$$y.\mathsf{lptr} = \mathsf{y.rptr} = \mathsf{null}$$

$$\mathsf{z.sum} = \mathsf{x.data} + \mathsf{y.data}$$

$$x = y = z = \text{null}$$

x.lptr.lptr.rptr = null

x.lptr = y.rptr = nully.lptr.lptr = y.lptr.rptr = null



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CS 618

3

y = z = null

 $1 \quad w = x$ w = null

2 while (x.data < max)

 $\{ \qquad \mathsf{x.lptr} = \mathsf{null}$

3 x = x.rptr }

x.rptr = x.lptr.rptr = null x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

4 y = x.lptr

x.lptr = y.rptr = null y.lptr.lptr = y.lptr.rptr = null

 $5 z = New class_of_z$

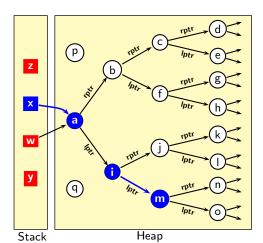
z.lptr = z.rptr = null

y = y.lptr

y.lptr = y.rptr = null z.sum = x.data + y.data

x = y = z = null

While loop is not executed even once



y = z = null

 $1 \quad w = x$

w = null

2 while (x.data < max)

 $\{ x.lptr = null \}$

 $\label{eq:continuous} \begin{array}{ll} 3 & \mathsf{x} = \mathsf{x.rptr} & \} \\ \mathsf{x.rptr} = \mathsf{x.lptr.rptr} = \mathsf{null} \end{array}$

x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

4 y = x.lptr

x.lptr = y.rptr = null y.lptr.lptr = y.lptr.rptr = null

 $z = New class_of_z$

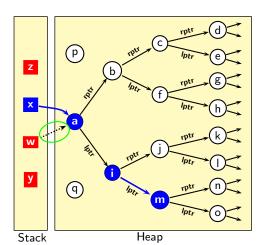
z.lptr = z.rptr = null

6 y = y.lptr y.lptr = y.rptr = null

z.sum = x.data + y.data

x = y = z = null

While loop is not executed even once



```
y = z = null
```

- $1 \quad w = x$ w = null
- 2 while (x.data < max)

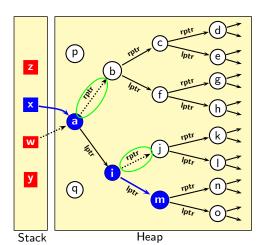
 $\{ x.lptr = null \}$

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x.rptr = x.lptr.rptr = null x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

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- z.sum = x.data + y.data
 - x = y = z = null

While loop is not executed even once



```
y = z = null
```

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- 2 while (x.data < max)

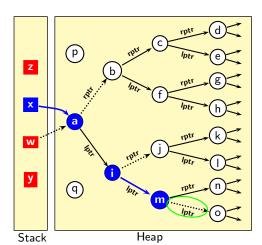
 $\{ \qquad \mathsf{x.lptr} = \mathsf{null}$

3 x = x.rptr } x.rptr = x.lptr.rptr = null

x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

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While loop is not executed even once



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- 2 while (x.data < max)

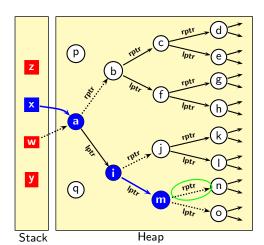
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- $4 \quad y = x.lptr$
 - x.lptr = y.rptr = null
- y.lptr.lptr = y.lptr.rptr = null 5 z = New class_of_z
 - z.lptr = z.rptr = null
- 6 y = y.lptr
- y.lptr = y.rptr = null z.sum = x.data + y.data
 - z.sum = x.data + y.dax = y = z = null

While loop is not executed even once



```
y = z = null
```

- $1 \quad w = x$ w = null
- 2 while (x.data < max)

 $\{ x.lptr = null \}$

3 x = x.rptr

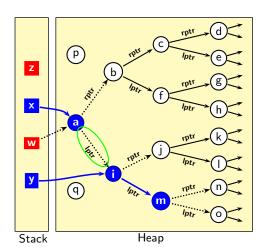
x.rptr = x.lptr.rptr = null x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

- 4 y = x.lptr
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- 5 z = New class_of_z
 - $\mathsf{z.lptr} = \mathsf{z.rptr} = \mathsf{null}$
- 6 y = y.lptr
 y.lptr = y.rptr = null

x = y = z = null

z.sum = x.data + y.data

While loop is not executed even once



```
y = z = null
```

- $1 \quad w = x$ w = null
- 2 while (x.data < max)

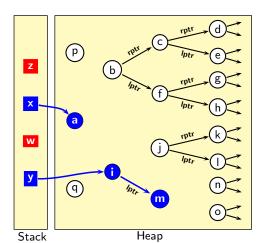
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 - x.lptr = y.rptr = null y.lptr.lptr = y.lptr.rptr = null
- $z = New class_of_z$
 - z.lptr = z.rptr = null
- 6 y = y.lptr
 y.lptr = y.rptr = null
- $7 ext{ z.sum} = x.data + y.data$
 - z.sum = x.data + y.datx = y = z = null

While loop is not executed even once



y = z = null

 $1 \quad w = x$ w = null

2 while (x.data < max)

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x.rptr = x.lptr.rptr = null x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

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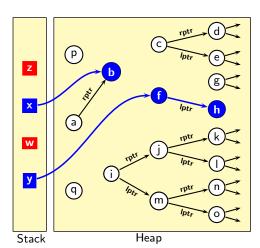
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z.lptr = z.rptr = null

 $6 \quad y = y.lptr$

y.lptr = y.rptr = null

7 z.sum = x.data + y.datax = y = z = null While loop is executed once



```
y = z = null
```

- $1 \quad w = x$ w = null
- 2 while (x.data < max)

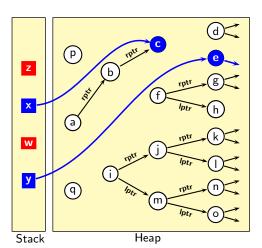
 $\{$ x.lptr = null

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x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

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- $z = New class_of_z$
 - z.lptr = z.rptr = null
- 6 y = y.lptr
- y.lptr = y.rptr = null
- 7 z.sum = x.data + y.data
 - x = y = z = null

While loop is executed twice



```
y = z = \text{null}
1 \quad w = x
w = \text{null}
```

2 while (x.data < max)

 $\{$ x.lptr = null

x = x.rptr

x.rptr = x.lptr.rptr = null x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

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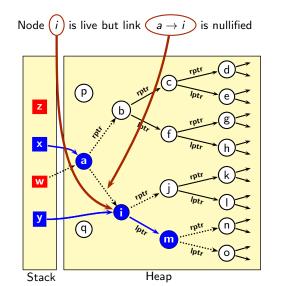
5 z = New class_of_z z.lptr = z.rptr = null

y = y.lptr

y.lptr = y.rptr = null

z.sum = x.data + y.data

x = y = z = null



y = z = null $1 \quad w = x$

w = xw = null

2 while (x.data < max)

 $\{$ x.lptr = null

x = x.rptr

x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

4 y = x.lptr

x.lptr = y.rptr = null y.lptr.lptr = y.lptr.rptr = null

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 $5 z = New class_of_z$

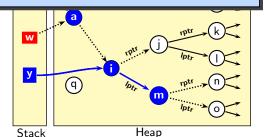
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6 y = y.lptr y.lptr = y.rptr = null

 $7 ext{ z.sum} = x.data + y.data$

x = y = z = null

 The memory address that x holds when the execution reaches a given program point is not an invariant of program execution



- y = z = null $1 \quad w = x$
- w = xw = null
- 2 while (x.data < max)
- $\{ x.lptr = null \}$
- 3 x = x.rptr } x.rptr = x.lptr.rptr = null
- x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null
- $4 \quad y = x.lptr$
- 4 y = x.ipti
 - x.lptr = y.rptr = null y.lptr.lptr = y.lptr.rptr = null
- 5 z = New class_of_z
- z.lptr = z.rptr = null
- 6 y = y.lptr y.lptr = y.rptr = null
- 7 z.sum = x.data + y.data x = y = z = null

- rptr out of x at a given program point is an invariant of program execution
- The memory address that x holds when the execution reaches a given program point is not an invariant of program execution
 Whether we dereference lptr out of x or

y q i ptr q i ptr n

Stack Heap

```
y = z = null

1 \quad w = x
```

w = null

2 while (x.data < max)

x = x.rptr }
x.rptr = x.lptr.rptr = null

x.lptr.lptr.lptr = null x.lptr.lptr.rptr = null

4 y = x.lptr

x.lptr = y.rptr = null y.lptr.lptr = y.lptr.rptr = null

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z.lptr = z.rptr = null

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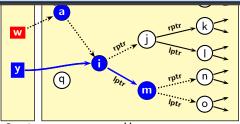
z.sum = x.data + y.data

x = y = z = null

 The memory address that x holds when the execution reaches a given program point is not an invariant of program execution

• Whether we dereference lptr out of x or

- rptr out of x at a given program point is an invariant of program execution
- A static analysis can discover only invariants



Stack Heap

y = z = nullw = x

w = null

while (x.data < max)

x.lptr = null3

x = x.rptrx.rptr = x.lptr.rptr = null

x.lptr.lptr.lptr = nullx.lptr.lptr.rptr = null

4 y = x.lptr

x.lptr = y.rptr = nully.lptr.lptr = y.lptr.rptr = null

 $5 z = New class_of_z$

z.lptr = z.rptr = null

y = y.lptry.lptr = y.rptr = null

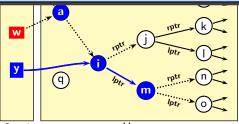
z.sum = x.data + y.data

x = y = z = null

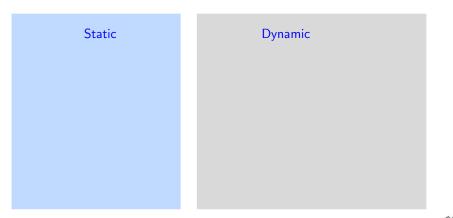
• The memory address that x holds when the execution reaches a given program point is not an invariant of program execution

• Whether we dereference lptr out of x or

- rptr out of x at a given program point is an invariant of program execution
- A static analysis can discover only some invariants



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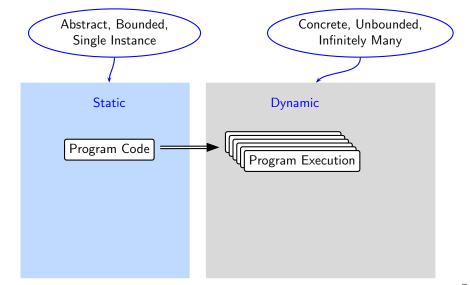


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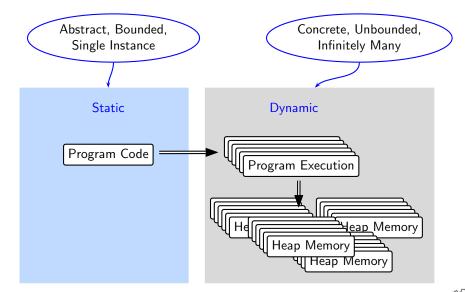
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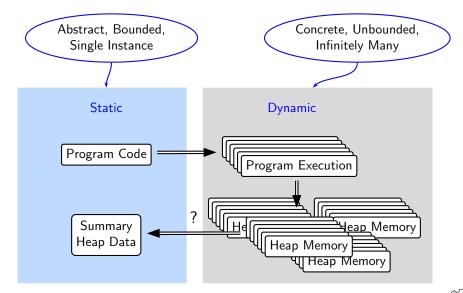
BIVV, What is Static Analysis of Heaps



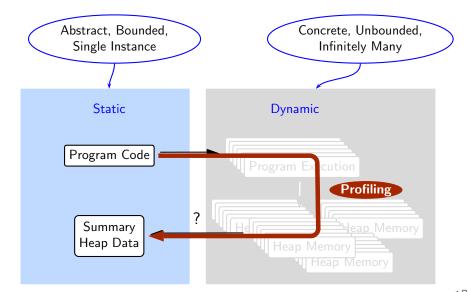
BTW, What is Static Analysis of Heap?

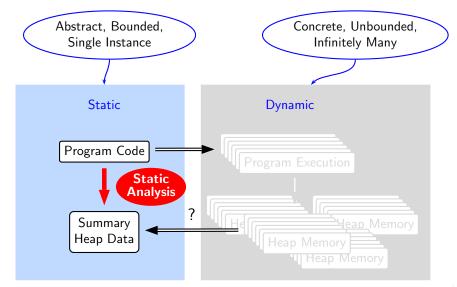


BTW, What is Static Analysis of Heap?



BTW, What is Static Analysis of Heap?





Part 4

Course Details

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sound & precise modelling of runtime behaviour of programs efficiently

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The Main Theme of the Course

Constructing suitable abstractions for sound & precise modelling of runtime behaviour of programs efficiently

Abstract, Bounded, Single Instance Concrete, Unbounded, Infinitely Many Static **Dynamic** Program Code Program Execution Static **Analysis** Memory Summary Information Memory Memor\

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Sequence of Generalizations in the Course Modules

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Bit Vector Frameworks

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Intro to PA: Course Details

Sequence of Generalizations in the Course Modules

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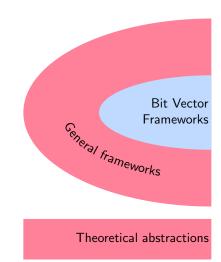
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Bit Vector Frameworks

Theoretical abstractions

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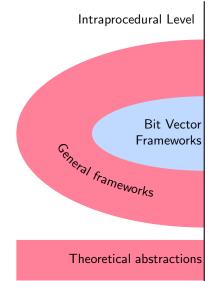
Sequence of Generalizations in the Course Modules



Sequence of Generalizations in the Course Modules

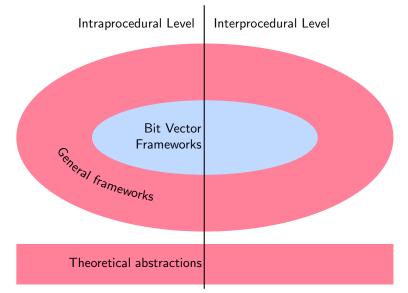
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Sequence of Generalizations in the Course Modules



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- Interleaved lectures and tutorials
- Plenty of problem solving

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- Practice problems will be provided,
 - Readymade solutions will not be provided
 - Your solutions will be checked
- Detailed course plan can be found at the course page: http://www.cse.iitb.ac.in/uday/courses/cs618-15/
- Moodle will be used extensively for announcements and discussions

Assessment Scheme

Tentative plan

Mid Semester Examination	30%
End Semester Examination	40%
Two Quizzes	10%
Programming Project	20%
Total	100%

• Can be fine tuned based on the class feedback



Assessment Scheme

Tentative plan

Mid Semester Examination	30%
End Semester Examination	40%
Two Quizzes	10%
Programming Project	20%
Total	100%

- Can be fine tuned based on the class feedback
- GCC based projets
 (Short introduction of GCC will be covered)



Course Strength and Selection Criteria

Course Carongan and Colocation Criticana

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- Unavailability of TAs forces restricting the strength to 30 (No offering in 2014)
- Selection based on a test covering the concepts in the first lecture
- May allow a reasonable many audits

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- Attending all lectures is sufficient
- ▶ No need to appear in examinations or do projects

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Questions ??

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Si Si

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See you on Friday 24 July . . .



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ster 🙂

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See you on Friday 24 July . . .

for your first enounter with a test in this semester

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Questions ??

Part 5

Soundness and Precision

Soundiness and Trecision of Static Analysis

```
int a;
int f(int b)
{ int c;
   c = a\%2;
   b = - abs(b);
   while (b < c)
      b = b+1;
   if (b > 0)
      b = 0;
   return b;
```

Example Program

Control Flow Graph

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Soundiess and Precision of Static Analysis

```
Absolute
int a;
int f(int b)
   int c;
   c = a\%2;
   b = - abs(b);
   while (b < c)
      b = b+1;
   if (b > 0)
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```

Example Program

Control Flow Graph

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Soundness and Precision of Static Analysis

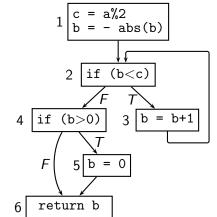
```
Example Program
           Absolute
int a;
int f(int b)
   int c;
   c = a\%2;
   b = - abs(b);
   while (b < c)
      b = b+1;
   if (b > 0)
      b = 0;
   return b;
```

```
Control Flow Graph
       = a\%2
        = - abs(b)
       if (b<c)
if (b>0)
             3 | b = b+1
 return b
```

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Execution Traces for Concrete Semantics

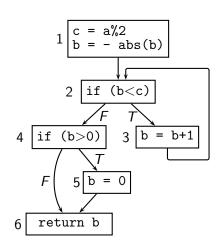
- A state: (Program Point, Variables \mapsto Values)
- A trace: a valid sequence of states starting with a given initial state



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Execution Traces for Concrete Semantics

- A state: (Program Point, Variables → Values)
- A trace: a valid sequence of states starting with a given initial state



Trace 1 a b c $Entry_1$, (5, 2, 7) $Entry_2$, (5, -2, 1) $Entry_3$, (5, -2, 1)

Entry₂, (5, -1, 1)Entry₃, (5, -1, 1)Entry₂, (5, 0, 1)Entry₃, (5, 0, 1)

Entry₂, (5, 1, 1)Entry₄, (5, 1, 1)Entry₅, (5, 1, 1)Entry₆, (5, 0, 1)

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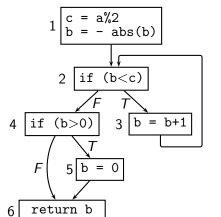
Execution Traces for Concrete Semantics

- A state: (Program Point, Variables → Values)
- A trace: a valid sequence of states starting with a given initial state

 $Entry_{2}, (5, 0, 1)$

Entry₃, (5, 0, 1)Entry₂, (5, 1, 1)Entry₄, (5, 1, 1)Entry₅, (5, 1, 1)

 $Entry_6$, (5, 0, 1)



Trace 1 Trace 1

 $\begin{array}{ll} \textit{Entry}_3, (5, -2, 1) & \textit{Entry}_3, (-5, -2, -1) \\ \textit{Entry}_2, (5, -1, 1) & \textit{Entry}_2, (-5, -1, -1) \\ \textit{Entry}_3, (5, -1, 1) & \textit{Entry}_4, (-5, -1, -1) \end{array}$

5

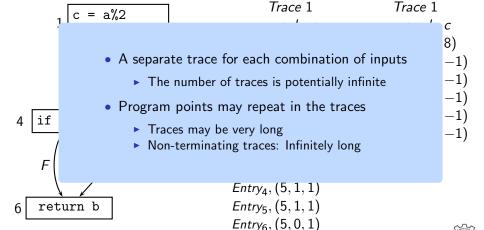
Entry₆, (-5, -1, -1)

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Execution Traces for Concrete Semantics

- A state: (Program Point, Variables → Values)
 A trace: a valid sequence of states starting with a given initial state
- 77 trace. a valid sequence of states starting with a given initial state

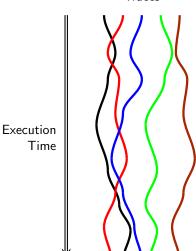


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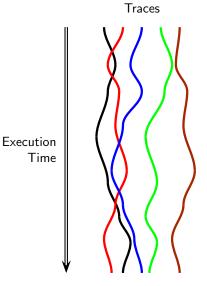
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Intro to PA: Soundness and Precision



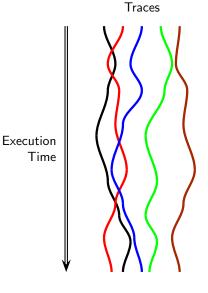
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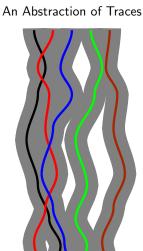




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(2)

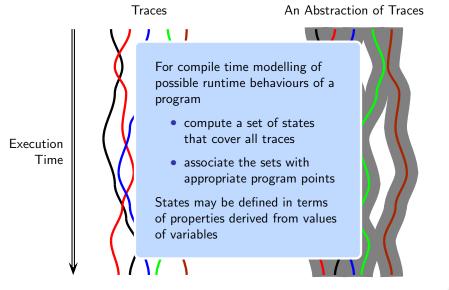


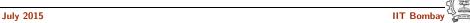


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Static Analysis Computes Abstractions of Traces (1)



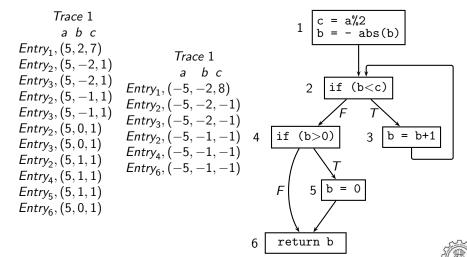


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Static Analysis Computes Abstractions of Traces (2)

A possible static abstraction using sets

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Static Analysis Computes Abstractions of Traces (2)

Trace 1

a b c

Entry₁, (5, 2, 7)

Entry₂, (5, -2, 1) Trace 1 Trace 1 Trace 1

Entry₂, (5, -2, 1) a b c Entry₃, (5, -2, 1) Entry₁, (-5, -2, 8) Entry₂, (-5, -2, -1)

 $Entry_{2}, (5, -1, 1) \\ Entry_{3}, (5, -1, 1) \\ Entry_{2}, (5, 0, 1) \\ Entry_{3}, (5, 0, 1) \\ Entry_{2}, (5, 1, 1) \\ Entry_{4}, (5, 1, 1) \\ Entry_{6}, (-5, -1, -1) \\ Entry_{6}, (-5, -1, -1)$

 $F = \begin{bmatrix} \text{if } (b>0) \\ 5 \\ \text{b} = 0 \end{bmatrix}$

return b

A possible static abstraction using sets

if (b < c)

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 $Entry_5$, (5, 1, 1) $Entry_6$, (5, 0, 1)

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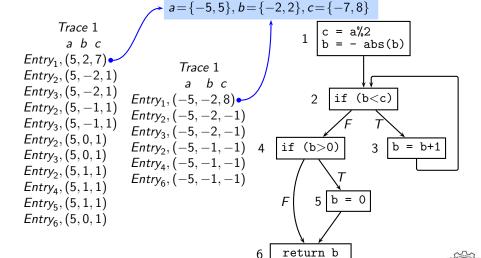
b = b+1

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Static Analysis Computes Abstractions of Traces (2)

A possible static abstraction using sets

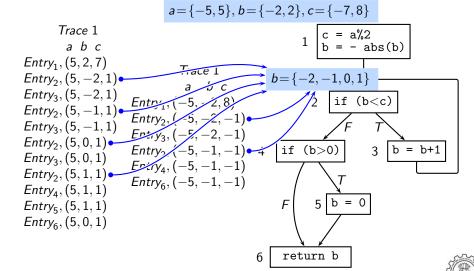


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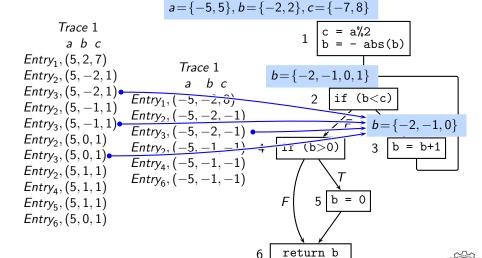
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sing sets

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Static Analysis Computes Abstractions of Traces (2)

A possible static abstraction using sets



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Static Analysis Computes Abstractions of Traces (2)

A possible static abstraction using sets $a = \{-5, 5\}, b = \{-2, 2\}, c = \{-7, 8\}$

```
Trace 1
                                                             1 \begin{vmatrix} c = a/2 \\ b = -abs(b) \end{vmatrix}
         abc
Entry_1, (5, 2, 7)
                                  Trace 1
                                                      b = \{-2, -1, 0, 1\}
Entry_2, (5, -2, 1)
Entry_3, (5, -2, 1)
                                                                   if (b<c)
                       Entry_1, (-5, -2, 8)
Entry_2, (5, -1, 1)
                       Entry_2, (-5, -2, -1)
                                                     b = \{-1, 1\} F
                                                                           b = \{-2, -1, 0\}
Entry_3, (5, -1, 1)
                       Entry<sub>3</sub>, (-5, -2, -1)
Entry_{2}, (5, 0, 1)
                                                       |if/(b>0)|
                       Entry<sub>2</sub>, (-5, -1, -1)
Entry_3, (5, 0, 1)
                       Entry (-5, -1, -1)
Entry_{2}, (5, 1, 1)
                       E_{riv_6}, (-5, -1, -1)
Entry_4, (5, 1, 1)
Entry_{5}, (5, 1, 1)
Entry_{6}, (5, 0, 1)
```

return b

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Static Analysis Computes Abstractions of Traces (2)

A possible static abstraction using sets

return b

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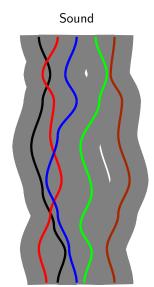
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Static Analysis Computes Abstractions of Traces (2)

A possible static abstraction using sets

Soundness of Abstractions (1)

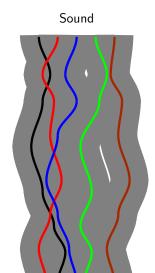


 An over-approximation of traces is sound

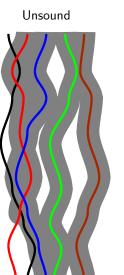


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Soundness of Abstractions (1)



- An over-approximation of traces is sound
- Missing any state in any trace causes unsoundness



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All variables can have arbitrary

b can have many more values

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$$a = \{-5, 5\}, b = \{-2, 2\}, c = \{-7, 8\}$$

$$1 \begin{bmatrix} c = a\%2 \\ b = -abs(b) \end{bmatrix}$$

$$b = \{-2, -1, 0, 1\}$$

$$2 \quad \text{if } (b < c) \end{bmatrix}$$

$$b = \{-1, 1\} \quad F \quad b = \{-2, -1, 0\}$$

$$4 \quad \text{if } (b > 0) \quad 3 \quad b = b + 1 \end{bmatrix}$$

 $b = \{1\}$

 $b = \{-1, 0\}$ return b

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at the entry of blocks 2 and 3 (e.g. -3,

-8, ...)

values at the start.

block 4 (e.g. 0)

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A sound abstraction using intervals An unsound abstraction

Intro to PA: Soundness and Precision

$$a = \{-5, 5\}, b = \{-2, 2\}, c = \{-7, 8\}$$

 $\begin{array}{c|c}
c = a\%2 \\
b = - abs(b)
\end{array}$

$$b = \{-2, -1, 0, 1\}$$

$$b = \{-1, 1\}$$
 F $b = \{-2, -1, 0\}$

$$b = b+1$$

 $b = \{1\}$

$$b = \{-1, 0\}$$

if (b>0)

return b

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- Overapproximated range of values denoted by
 - low_limit, high_limit Inclusive limits with
 - *low_limit* < *high_limit*
 - One continuous range per variable with no "holes"

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 $a=[-\infty,\infty], b=[-\infty,\infty], c=[-\infty,\infty]$

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 $a = \{-5, 5\}, b = \{-2, 2\}, c = \{-7, 8\}$

An unsound abstraction

 $1 \begin{vmatrix} c = a\%2 \\ b = -abs(b) \end{vmatrix}$

 $b = \{-2, -1, 0, 1\}$

if (b<c)

 $b = \{-1, 1\}$ F $b = \{-2, -1, 0\}$

3 | b = b+1

if (b>0) $b = \{1\}$

 $b = \{-1, 0\}$

return b

b = [-1, 1] / F $b = [-\infty, 0]$ if (b>0)

A sound abstraction using intervals

 $1 \begin{vmatrix} c = a/2 \\ b = -abs(b) \end{vmatrix}$

if (b<c)

 $b=[-\infty,1]$

b = [-1, 0]return b

3 b = b+1b = [1, 1]

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Intro to PA: Soundness and Precision

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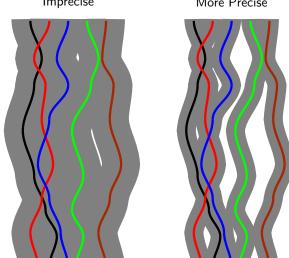
Imprecise

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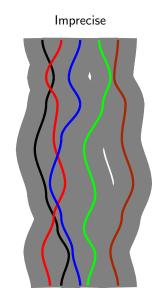
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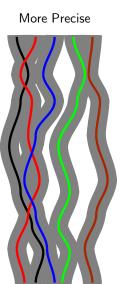
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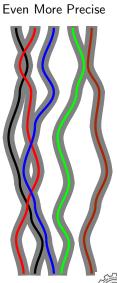
Imprecise More Precise



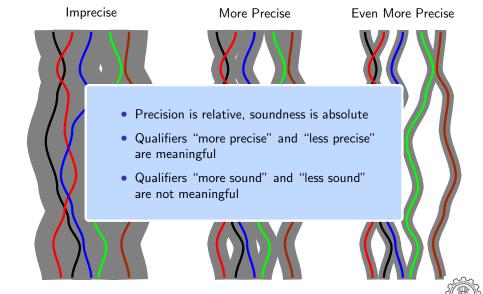








Precision of Sound Abstractions(1)



A precise abstraction using intervals An imprecise abstraction using intervals

 $a = [-\infty, \infty], b = [-\infty, \infty], c = [-\infty, \infty] \mid a = [-\infty, \infty], b = [-\infty, \infty], c = [-\infty, \infty]$ c = a%2 b = - abs(b) $b=[-\infty,1]$ if (b < c)b = [-1, 1] $b = [-\infty, 0]$ |b| = b+1if (b>0) b = [1, 1]b = [-1, 0]return b

c = a%2 b = - abs(b) $b = [-\infty, \infty]$ if (b<c) $b = [-\infty, \infty]$ F $b = [-\infty, \infty]$ if (b>0) |b| = b+1 $b = [-\infty, \infty]$

 $b = [-\infty, \infty]$

return b

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A precise abstraction using intervals An imprecise abstraction using intervals

 $a = [-\infty, \infty], b = [-\infty, \infty], c = [-\infty, \infty]$ $a = [-\infty, \infty], b = [-\infty, \infty], c = [-\infty, \infty]$ In general, computation of precise (or exact) static abstraction is undecidable b= We have to settle for some imprecision Goodness of static analysis lies in minimizing b = [-1, 1] $,\infty$ imprecision without compromising on soundness Additional expectations: Efficiency and scalability Some applications (e.g. debugging) may not need soundness b = [-1, 0] $b=[-\infty,\infty]$

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return b

Part 6

Program Model

CS 618 Intro to PA: Program Model

Program Representation

- Three address code statements
 - Result, operator, operand1, operand2
 - Assignments, expressions, conditional jumps
 - Intially only scalars
 Pointers, structures, arrays modelled later
- Control flow graph representation
 - ► Nodes represent maximal groups of statements devoid of any control transfer except fall through
 - ▶ Edges represent control transfers across basic blocks
 - ► A unique Start node and a unique End node Every node reachable from Start, and End reachable from every node
- Initially only intraprocedural programs
 Function calls brought in later

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```
{ int a, b, c, n;
                       1. a = 4
                       2. b = 2
                       3. c = 3
  a = 4;
                       4. n = c*2
  b = 2;
                       5. if (a \leq n)
  c = 3;
                              goto 8
  n = c*2;
                       6. a = a + 1
  while (a \le n)
                       7. goto 5
    a = a+1;
                       8. if (a < 12)
                              goto 11
                       9. t1 = a+b
  if (a < 12)
                      10. a = t1+c
    a = a+b+c;
                      11. return a
   return a;
```

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int main()

```
{ int a, b, c, n;
                       1. a = 4
                       2. b = 2
                       3. c = 3
  a = 4;
                       4. n = c*2
  b = 2;
                       5. if (a \leq n)
  c = 3;
                              goto 8
  n = c*2;
                       6. a = a + 1
  while (a \le n)
                       7. goto 5
    a = a+1;
                       8. if (a < 12)
                              goto 11
                       9. t1 = a+b
  if (a < 12)
                      10. a = t1+c
    a = a+b+c;
                      11. return a
   return a;
```

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int main()

Intro to PA: Program Model

```
{ int a, b, c, n;
                       1. a = 4
                       2. b = 2
                       3. c = 3
  a = 4;
                       4. n = c*2
  b = 2;
```

a = a + 1 | n3 if (a<12) n4 t1 = a+b

return a | n6

if $(a \le n) \mid_{n^2}$

n = c*2

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c = 3;

n = c*2;

while $(a \le n)$

a = a+1;

if (a < 12)

return a;

a = a+b+c;

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11. return a