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Assignment 6

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Download all python codes from

https://github.com/adhvik24/AI1103-PROBABILITY-AND-RANDOM-VARIABLES/tree/main/ASSIGNMENT_6/ codes

and latex-tikz codes from

https://github.com/adhvik24/AI1103-PROBABILITY-AND-RANDOM-VARIABLES/blob/main/ASSIGNMENT_6/ AI1103_Assignment6.tex

1 CSIR UGC NET EXAM (Dec 2015), Q.3

The probability that a ticketless traveler is caught during a trip is 0.1. If the traveler makes 4 trips, the probability that he/she will be caught during at least one of the trips is:

(A)
$$1 - (0.9)^4$$

(B)
$$(1 - 0.9)^4$$

(C)
$$1 - (1 - 0.9)^4$$

(D)
$$(0.9)^4$$

2 Solution

Let $X_i \in \{0, 1\}$ represent the ith trip where 1 denotes a ticketless traveller is caught. Given,

$$Pr(X_i = 1) = p = 0.1$$
 (2.0.1)

Let,

$$X = \sum_{i=1}^{n} X_i \tag{2.0.2}$$

where n is the number of trips and X has a binomial distribution.

$$p_X(k) = \begin{cases} {}^{n}C_k p^K (1-p)^{n-k}, & 0 \le k \le n \\ 0, & otherwise \end{cases}$$
 (2.0.3)

As he/she makes 4 trips in total, Using (2.0.1) and (2.0.3),

$$Pr(X = 0) = p_X(0) \tag{2.0.4}$$

$$= {}^{4}C_{0} p^{0} (1-p)^{4}$$
 (2.0.5)

$$Pr(X = 0) = (0.9)^4 (2.0.6)$$

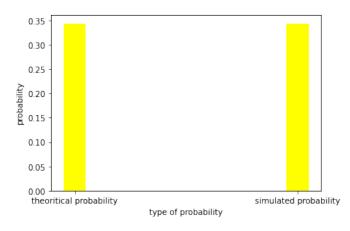


Fig. 1: probability that he/she will be caught during at least one of the trips

Then probability of being caught in atleast one trip is, (Using (2.0.6))

$$Pr(X \ge 1) = 1 - Pr(X < 1)$$
 (2.0.7)

$$= 1 - \Pr(X = 0) \tag{2.0.8}$$

$$= 1 - (0.9)^4 \tag{2.0.9}$$

Therefore the probability that he/she will be caught during at least one of the trips is $1 - (0.9)^4$. **ANSWER**: (A)