

# EE3900 Assignment - 4

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Download latex-tikz codes from

[https://github.com/adhvik24/EE3900/blob/main/Assignment\\_4/Assignment4.tex](https://github.com/adhvik24/EE3900/blob/main/Assignment_4/Assignment4.tex)

Download python codes from

[https://github.com/adhvik24/EE3900/blob/main/Assignment\\_4/Assignment4.py](https://github.com/adhvik24/EE3900/blob/main/Assignment_4/Assignment4.py)

## 1 LINEAR FORMS QN 2.17

A line perpendicular to the line segment joining the points  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$  and  $\begin{pmatrix} 2 \\ 3 \end{pmatrix}$  divides it in the ratio 1 : n. Find the equation of the line.

## 2 SOLUTION

Let  $\mathbf{M}$  be the midpoint of two points  $\mathbf{A} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$  and  $\mathbf{B} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ .

$$\mathbf{M} = \frac{n\mathbf{A} + \mathbf{B}}{n+1} = \frac{n\begin{pmatrix} 1 \\ 0 \end{pmatrix} + \begin{pmatrix} 2 \\ 3 \end{pmatrix}}{n+1} \quad (2.0.1)$$

$$\Rightarrow \mathbf{M} = \frac{1}{n+1} \begin{pmatrix} n+2 \\ 3 \end{pmatrix}$$

The direction vector of line AB is

$$\begin{pmatrix} 1 \\ 0 \end{pmatrix} - \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} -1 \\ -3 \end{pmatrix} \quad (2.0.2)$$

The direction vector of line AB is normal vector of perpendicular line. Then

$$\mathbf{n} = \begin{pmatrix} -1 \\ -3 \end{pmatrix} \quad (2.0.3)$$

The equation of line in terms of normal vector is then obtained as

$$\mathbf{n}^T(\mathbf{x} - \mathbf{M}) = 0 \quad (2.0.4)$$

$$\Rightarrow (-1 \ -3) \left( \mathbf{x} - \frac{1}{n+1} \begin{pmatrix} n+2 \\ 3 \end{pmatrix} \right) = 0 \quad (2.0.5)$$

$$\therefore (-1 \ -3) \mathbf{x} = \frac{-n-11}{n+1} \quad (2.0.6)$$

We got equation of the line perpendicular to line segment joining points  $\mathbf{A}$  and  $\mathbf{B}$  and dividing them in the ratio 1 : n.

For plotting let us take  $n = 2$ , Then the perpendicular line equation will be as,

$$(-1 \ -3) \mathbf{x} = \frac{-13}{3} \quad (2.0.7)$$

And the graph looks like,

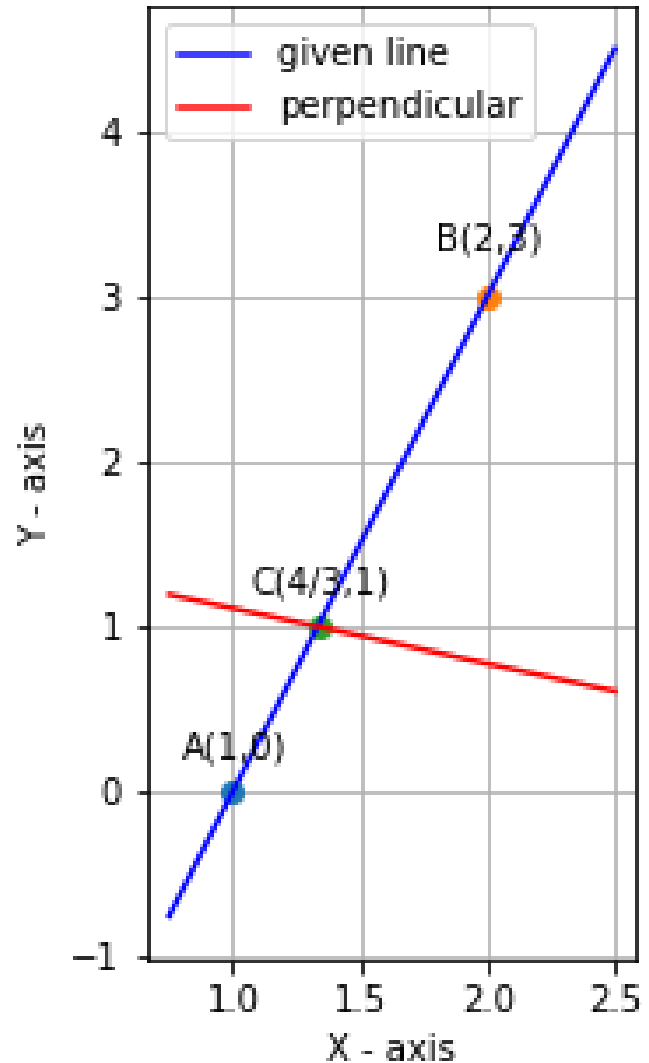


Fig. 1: graphical interpretation