

EE3900 Assignment - 2

Adhvik Mani Sai Murarisetty - AI20BTECH11015

Download latex-tikz codes from

<https://github.com/adhvik24/EE3900/blob/main/Assignment2/Assignment2.tex>

Download python codes from

<https://github.com/adhvik24/EE3900/blob/main/Assignment2/code.py>

1 MATRIX QN 2.70

Examine the consistency of the system of given equations:

$$x + 2y = 2$$

$$2x + 3y = 3$$

2 SOLUTION

If solution exists for the given system of equations then they said to be consistent, otherwise they are inconsistent. The above equations can be expressed as the matrix equation

$$\begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix} \mathbf{X} = \begin{pmatrix} 2 \\ 3 \end{pmatrix} \quad (2.0.1)$$

The augmented matrix for the above equation and row reducing as follows

$$\begin{pmatrix} 1 & 2 & 2 \\ 2 & 3 & 3 \end{pmatrix} \xrightarrow{R_2 \rightarrow R_2 - 2R_1} \begin{pmatrix} 1 & 2 & 2 \\ 0 & -1 & -1 \end{pmatrix} \quad (2.0.2)$$

$$\xrightarrow{R_1 \rightarrow R_1 + 2R_2} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & -1 \end{pmatrix} \quad (2.0.3)$$

$$\Rightarrow \text{Rank} \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix} = \text{Rank} \begin{pmatrix} 1 & 2 & 2 \\ 2 & 3 & 3 \end{pmatrix} = 2 \quad (2.0.4)$$

Here, $\text{Rank}(A) = \text{Rank}(A|B)$. Therefore, the system is consistent. Also, there exist a unique solution as $\text{Rank}(A) = n$ (number of unknown).

From equation (2.0.3), we get:

$$\mathbf{X} = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \quad (2.0.5)$$

Plotting the lines and the intersection point in Fig.1

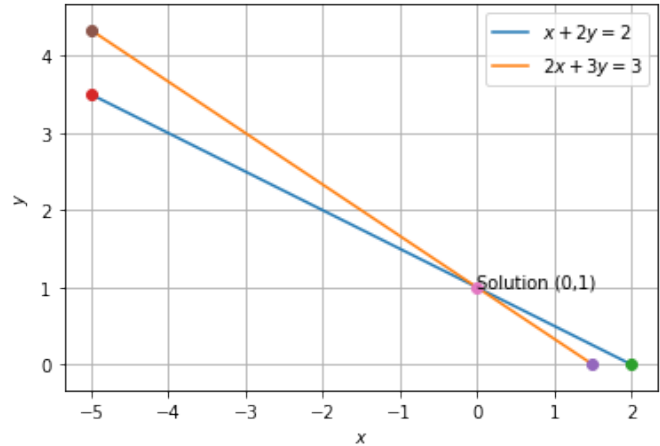


Fig. 1: Lines and their intersection denoting the solution

\therefore The given system of equation is consistent with unique solution of,

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$