

EE3900 Gate Assignment - 4

Adhvik Mani Sai Murarisetty - AI20BTECH11015

Download latex-tikz codes from

https://github.com/adhvik24/EE3900/blob/main/Gate_A4/main.tex

Download python codes from

https://github.com/adhvik24/EE3900/blob/main/Gate_A4/codes/plot.py

PROBLEM

(GATE EC-1997 Qn 5.2) If the fourier transform of the deterministic signal $x(t)$ is $X(f)$, then

1) The fourier transform of $x(t - 2)$ is

- a) $X(f)e^{-j4\pi f}$
- b) $X(2f)$
- c) $2X(2f)$
- d) $X(f - 2)$

2) The fourier transform of $x(\frac{t}{2})$ is

- a) $X(f)e^{-j4\pi f}$
- b) $X(2f)$
- c) $2X(2f)$
- d) $X(f - 2)$

SOLUTION

1) By the time shifting property of Fourier transform,

$$x(t - t_0) \xrightarrow{\mathcal{F}} e^{-j2\pi f t_0} X(f) \quad (0.0.1)$$

$$x(t - 2) \xrightarrow{\mathcal{F}} e^{-j4\pi f} X(f) \quad (0.0.2)$$

Let $x(t) = \text{rect}(t)$ and $\text{sinc}(t) = \frac{\sin(t)}{t}$

$$X(f) = \text{sinc}(f) \quad (0.0.3)$$

For $x(t) = \text{rect}(t - 2)$,

$$e^{-j4\pi f} X(f) = e^{-j4\pi f} \text{sinc}(f) \quad (0.0.4)$$

The correct option is (a).

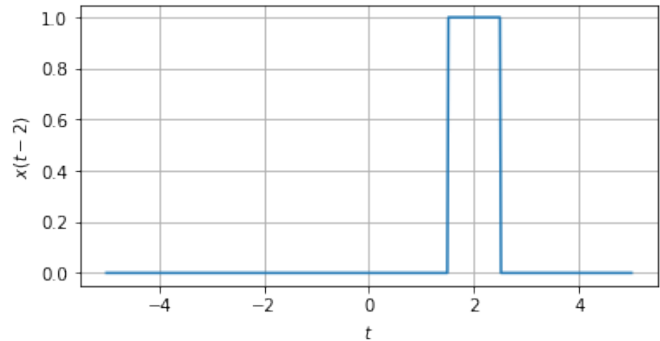


Fig. 1: Plot of $\text{rect}(t-2)$

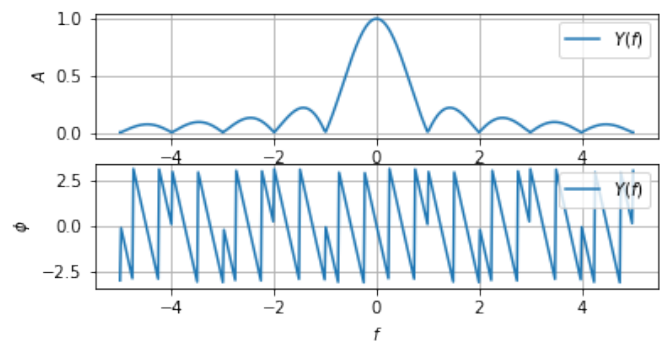


Fig. 2: Amplitude and phase v/s frequency plot

2) By the time scaling property of Fourier transform,

$$x(at) \xrightarrow{\mathcal{F}} \frac{1}{|a|} X\left(\frac{f}{|a|}\right) \quad (0.0.5)$$

$$x\left(\frac{t}{2}\right) \xrightarrow{\mathcal{F}} 2X(2f) \quad (0.0.6)$$

Let $x(t) = \text{rect}(t)$ and $\text{sinc}(t) = \frac{\sin(t)}{t}$

$$X(f) = \text{sinc}(f) \quad (0.0.7)$$

For $x(t) = \text{rect}\left(\frac{t}{2}\right)$,

$$2X(2f) = 2 \text{sinc}(2f) \quad (0.0.8)$$

The correct option is (c).

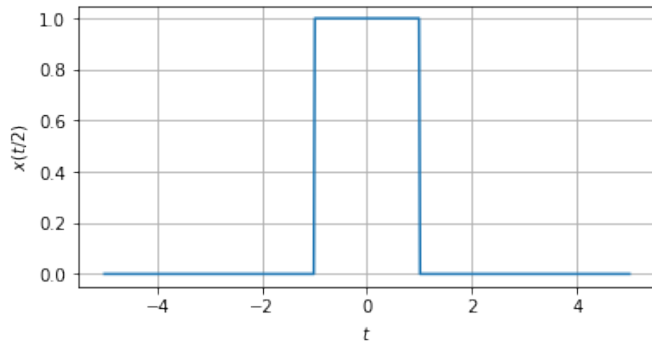


Fig. 3: Plot of $\text{rect}(\frac{t}{2})$

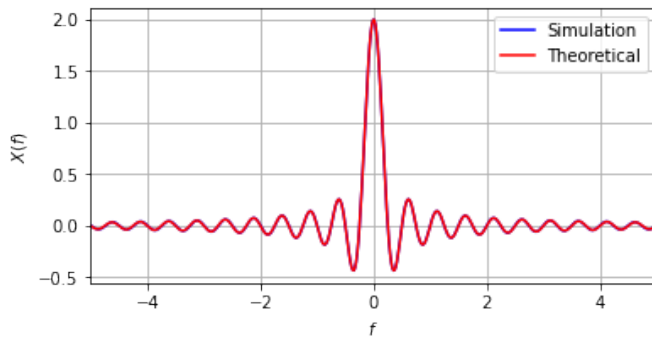


Fig. 4: Fourier transform Simulation v/s Theoretical