

Assignment - 0

Part-A : Transfer function & Bode

Plots.

A.1

$$G_1(s) = \frac{10}{s+10}$$

1. Pole :

$$s + 10 = 0$$

$$s = -10$$

$$G_1(0) = \frac{10}{0+10} = 1$$

$$2. G_1(s) = \frac{10}{10(1 + s/10)} = \frac{1}{1 + s/10}$$

$$G_1(j\omega) = \frac{1}{1 + j\omega/10}$$

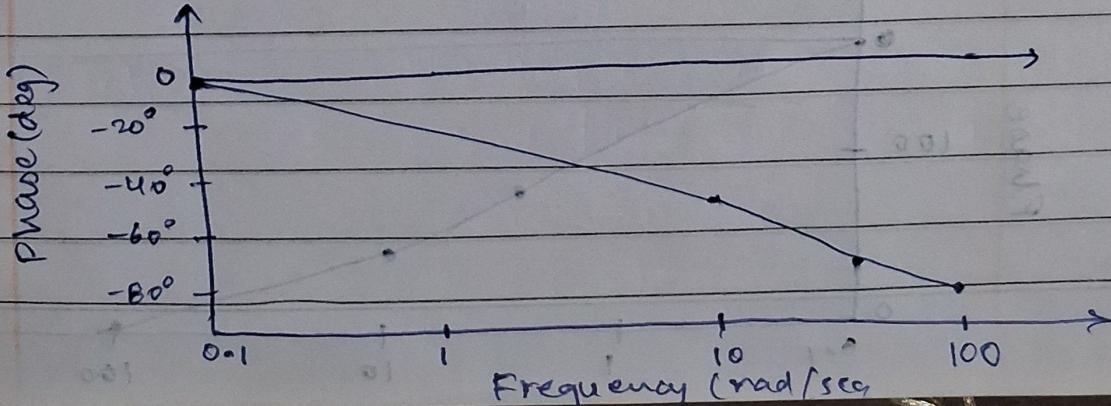
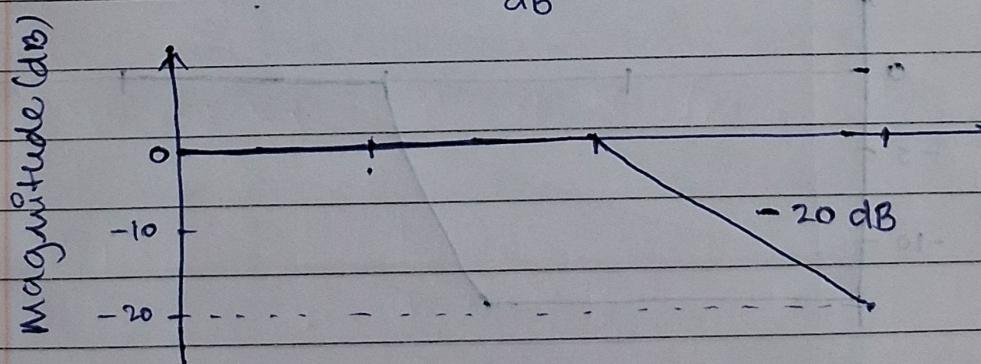
$$\omega < 10$$

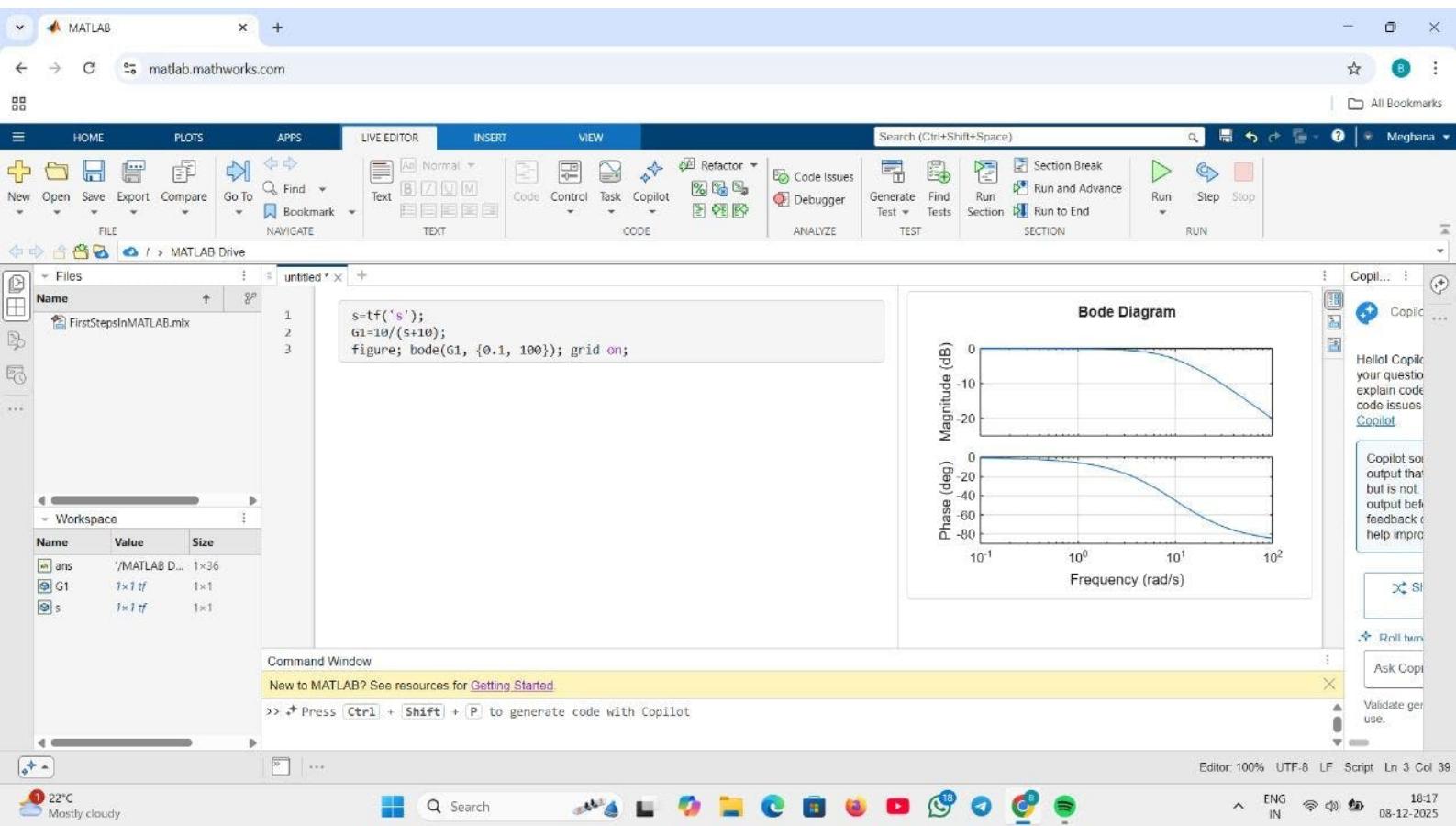
$$G_1 = \frac{1}{1} = 1 \Rightarrow G_{1, \text{dB}} = 20 \log 1 = 0$$

$$\omega > 10$$

$$G_1 = \frac{1}{j\omega/10} = \frac{10}{j\omega} = -\frac{10}{\omega} j$$

$$G_{1, \text{dB}} = 20 \log 10 - 20 \log \omega$$





$$\underline{A \cdot 2} \quad G_2(s) = \frac{s-2}{s+10}$$

1. ~~poles & zeros~~ : $s - 2 = 0$

$$s = 2$$

Pole: $s + 10 = 0$

$$s = -10$$

$$G_2(0) = \frac{0-2}{0+10} = -\frac{1}{5}$$

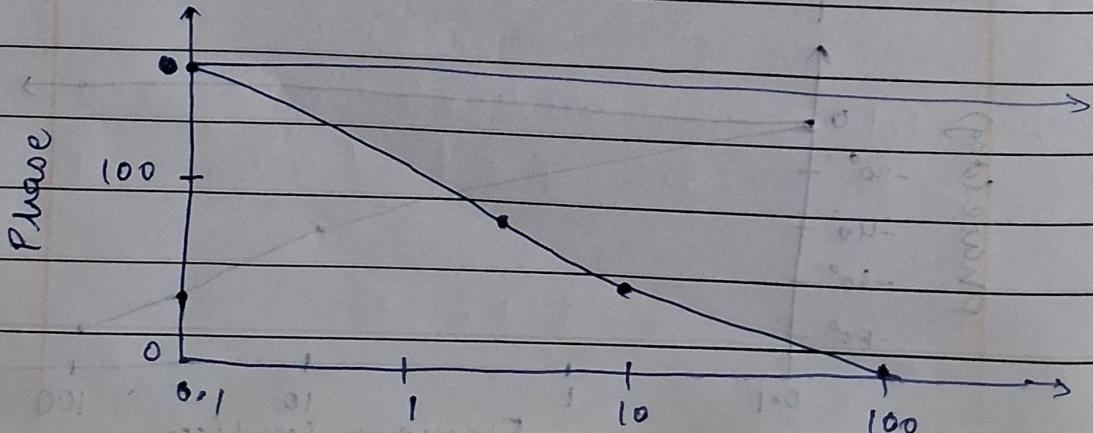
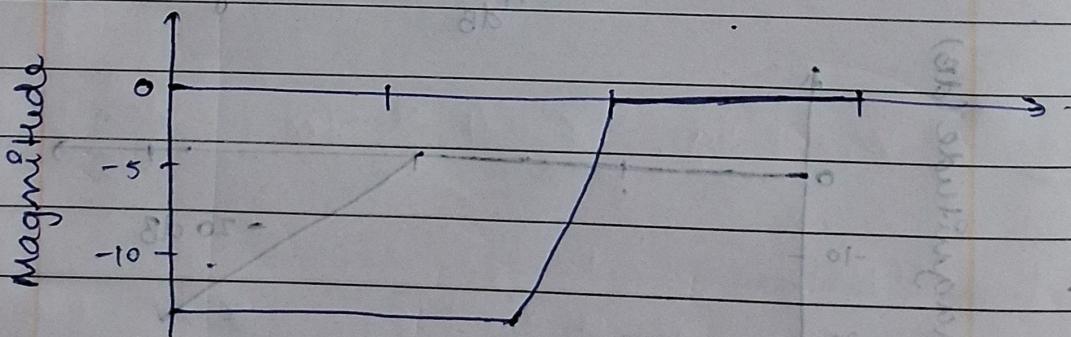
$$2. \quad G_2(j\omega) = \frac{-2(1-j\omega/2)}{10(1+j\omega/10)} = \frac{(1-j\omega/2)}{5(1+j\omega/10)}$$

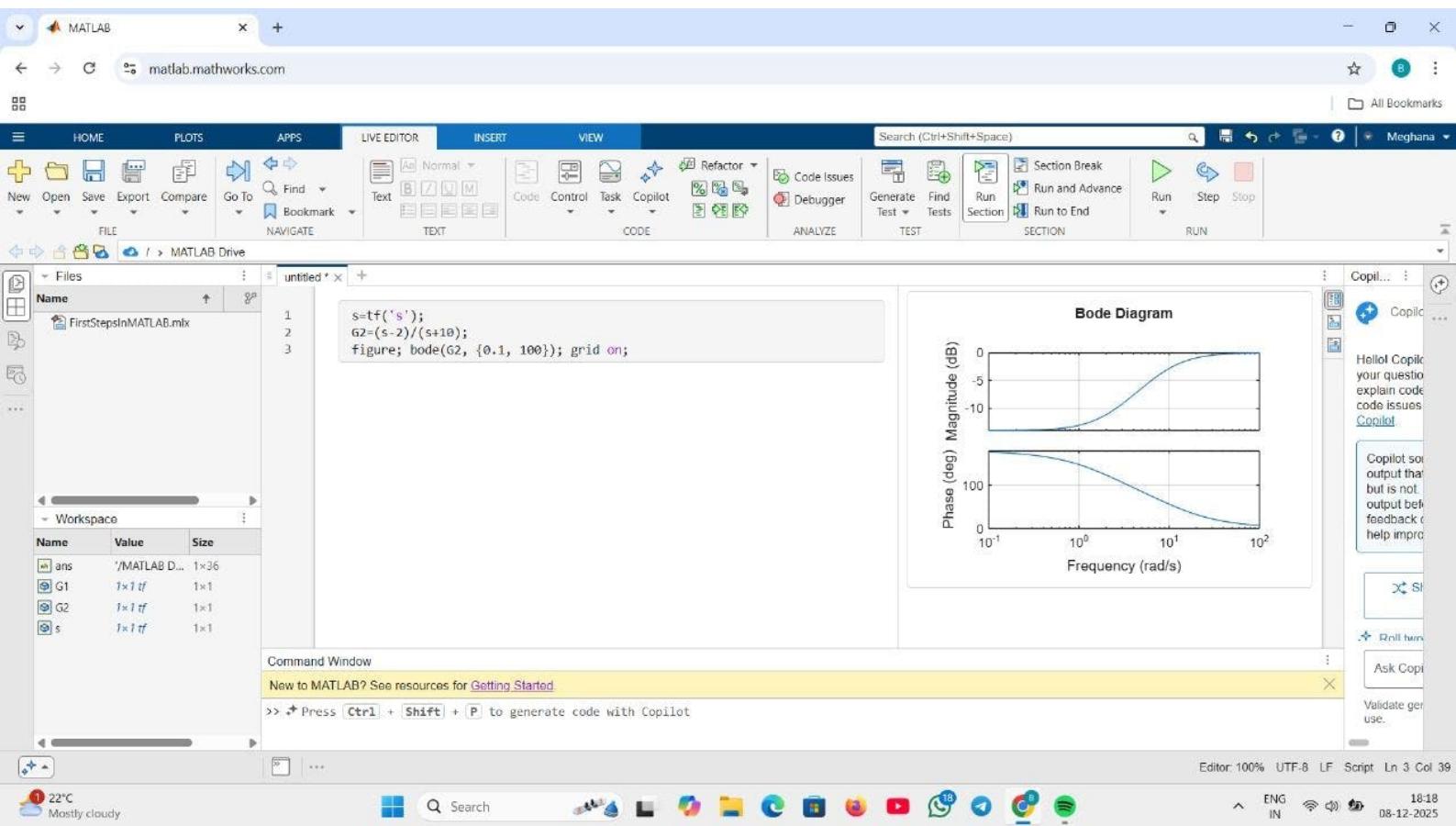
$$\omega < 2 \quad G_2 = \left(\omega - \frac{1}{5}\right)^0 \Rightarrow G_{2dB} = 20 \log(-\frac{1}{5})$$

$$2 < \omega < 10 \quad G_2 = \frac{j\omega/2}{5} = -\frac{j\omega}{10}$$

$$\Rightarrow G_{2dB} = 20 \log$$

$$\omega_B = \omega_A = 1 = 10$$





A.3

$$G_3(s) = \frac{100}{s^2 + 10s + 100}$$

1. Poles : $s^2 + 10s + 100 = 0$

$$s = -10 \pm \sqrt{100 - 400} = -10 \pm 10\sqrt{3}^{\circ}$$
$$= -5 \pm 5\sqrt{3}^{\circ}$$

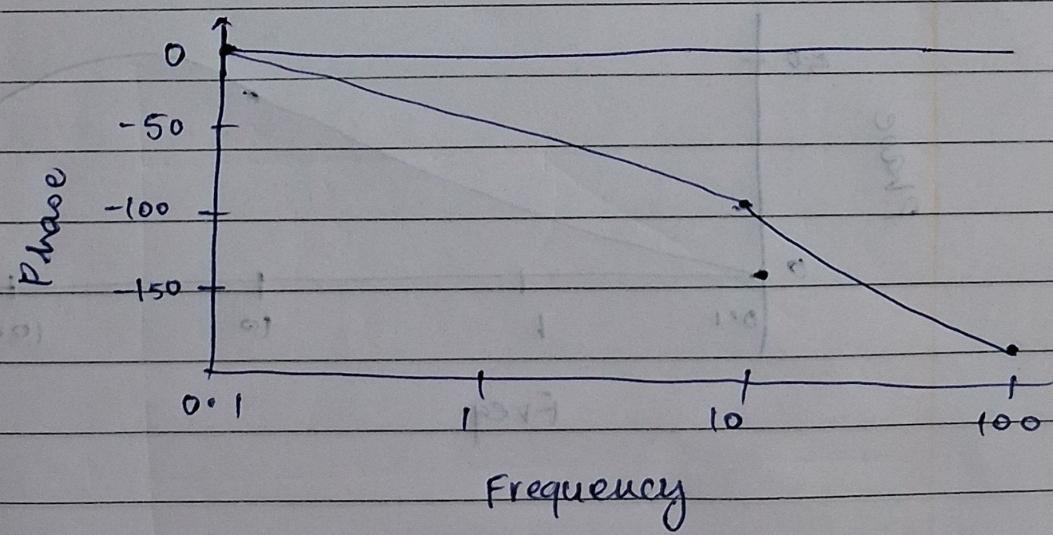
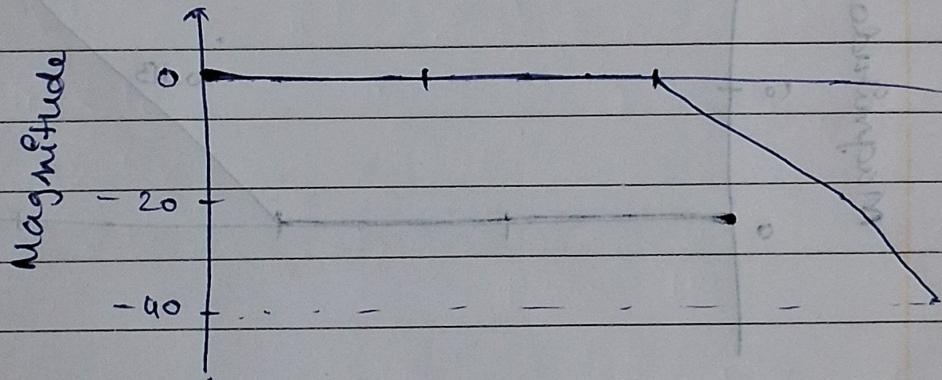
$$s_1 = -5 + 5\sqrt{3}^{\circ}, s_2 = -5 - 5\sqrt{3}^{\circ}$$

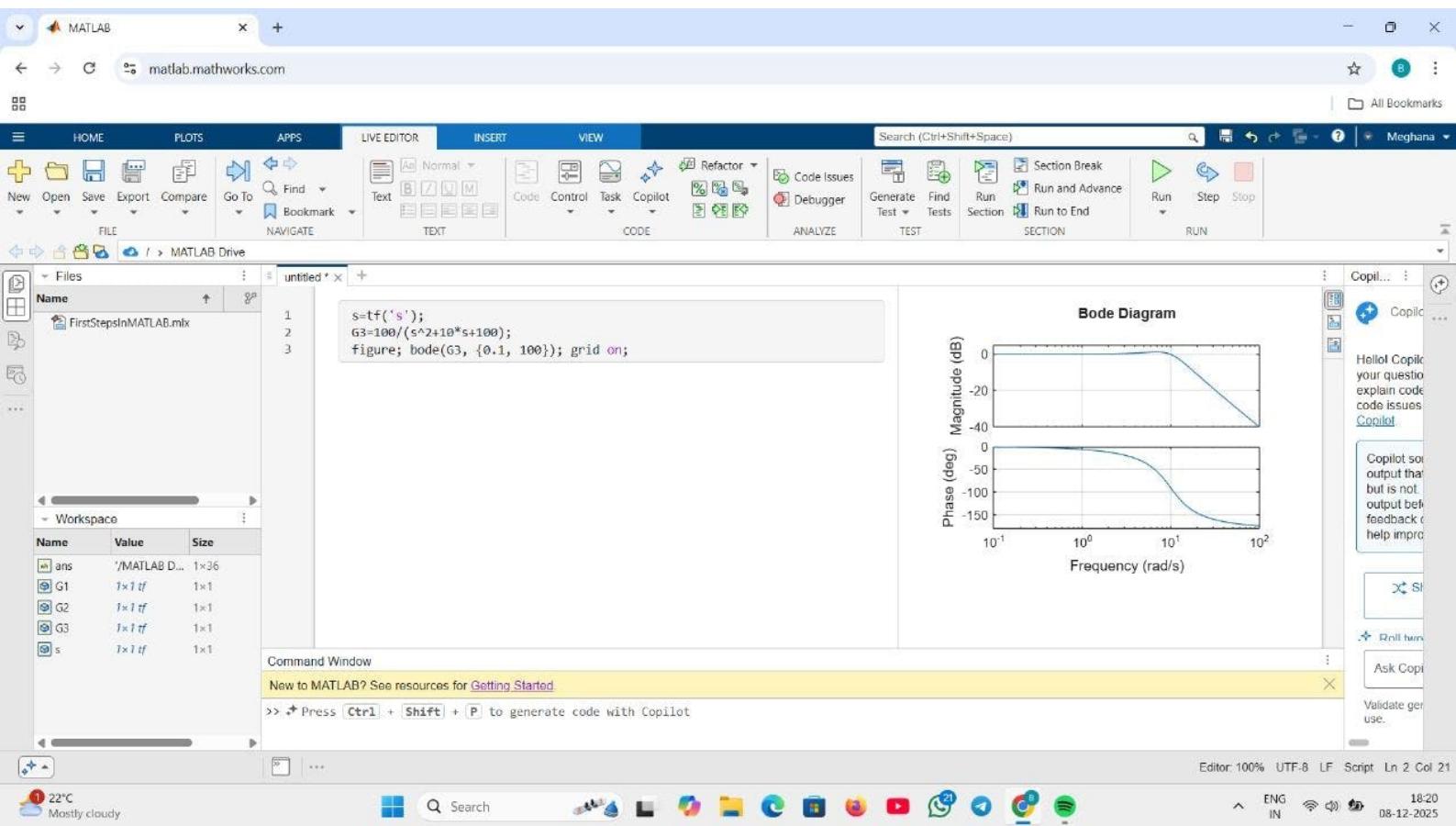
2. $\omega_n = \sqrt{100} = 10$

$$\zeta = \frac{10}{2\omega_n} = \frac{10}{20} = 0.5$$

$$G_3(\theta) = \frac{100}{100} = 1$$

2.





$$\underline{A.4} \quad G_{14}(s) = \frac{0.1s + 1}{0.01s + 1}$$

$$1. \text{ Zero: } 0.1s + 1 = 0$$

$$s = -10$$

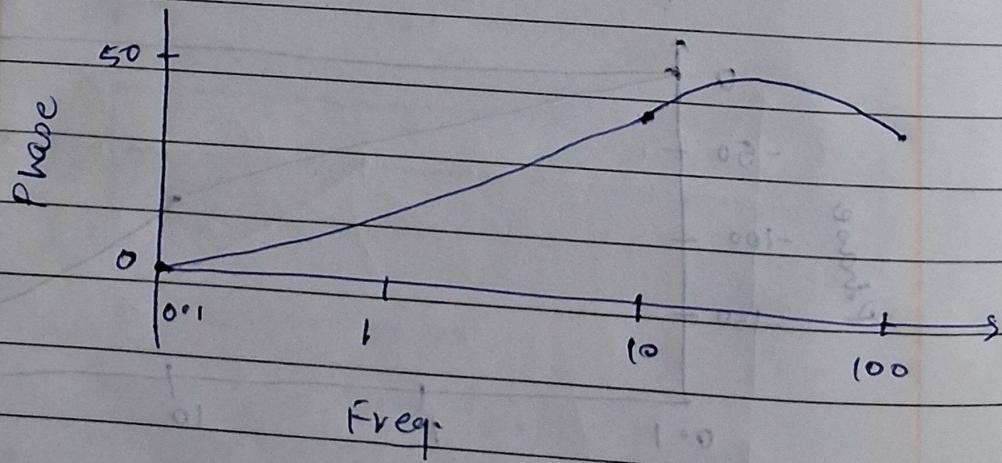
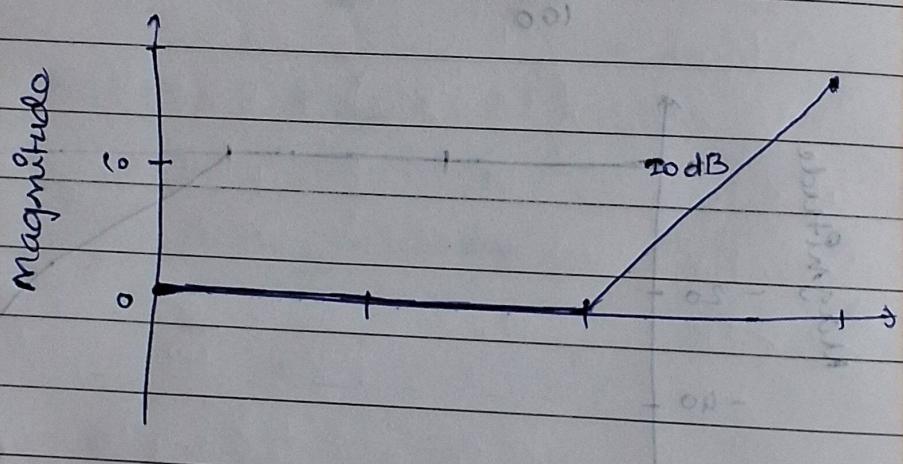
$$\text{Pole: } 0.01s + 1 = 0$$

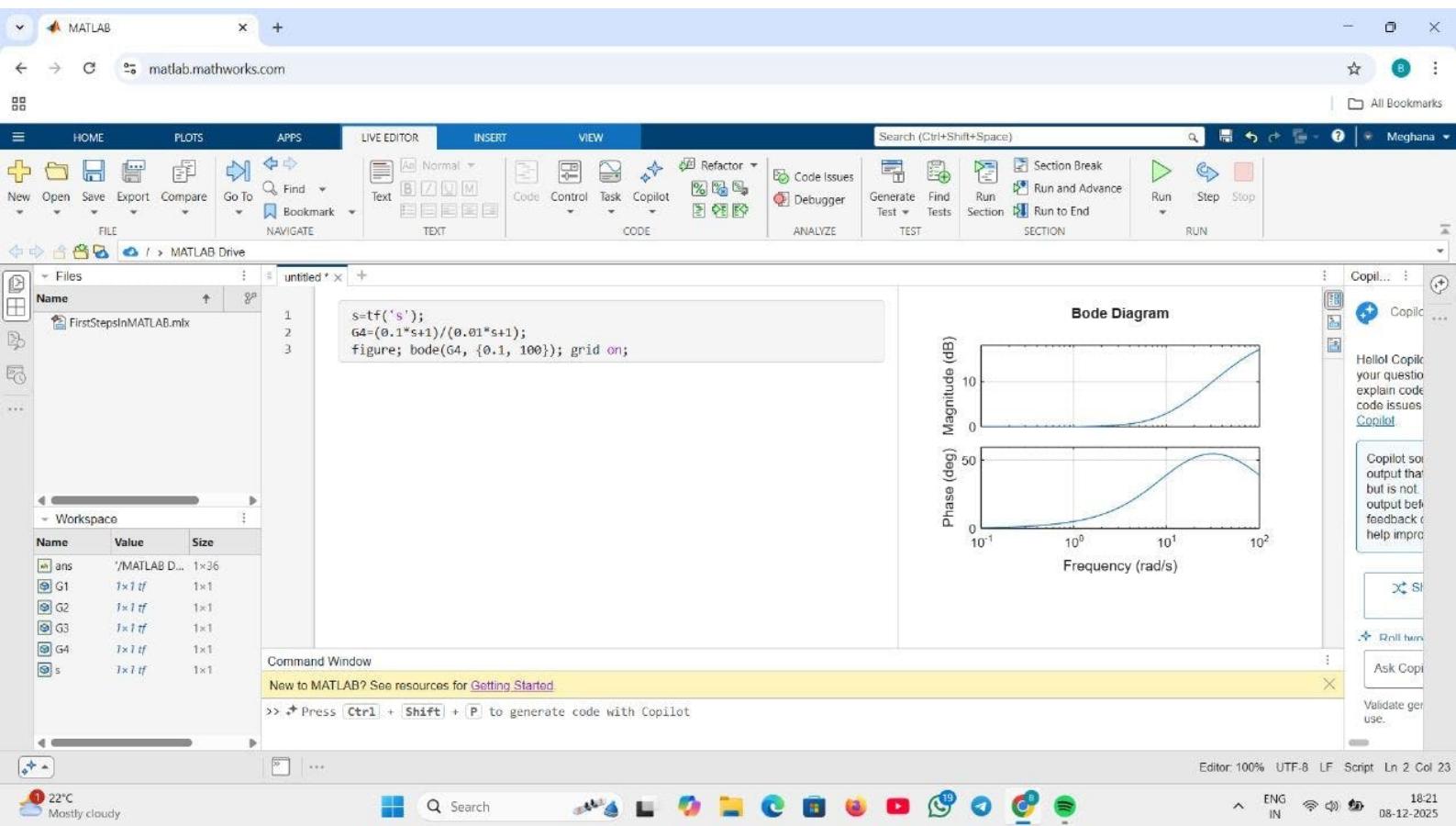
$$s = -100$$

$$G_{14}(0) = \frac{1}{1} = 1$$

2. ~~2~~

$$G_{14}(j\omega) = \frac{0.1(1 + \frac{s}{0.1})}{0.01(1 + \frac{s}{0.01})}$$

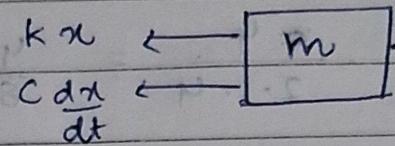




Part B - Mass-spring damper

B1.

1.



$$F - kx - c \frac{dx}{dt} = ma = m \frac{d^2x}{dt^2}$$

$$m \frac{d^2x}{dt^2} + c \frac{dx}{dt} + kx = F$$

2. Laplace transform, zero initial cond's

$$m s^2 X(s) + c s X(s) + k X(s) = F(s)$$

3. Transfer function $G(s) = \frac{X(s)}{F(s)}$

$$G(s) = \frac{1}{m s^2 + c s + k}$$

B2. $m = 1 \text{ kg}$, $c = 4 \text{ N}\cdot\text{s/m}$, $k = 16 \text{ N/m}$

$$1. G(s) = \frac{1}{1(s^2) + 4s + 16} = \frac{1}{s^2 + 4s + 16}$$

2. Poles :- $s^2 + 4s + 16 = 0$

$$s = \frac{-4 \pm \sqrt{16 - 4 \cdot 16}}{2} = \frac{-4 \pm 4\sqrt{3}i}{2}$$

$$s = -2 \pm i 2\sqrt{3}$$

$$S_1 = -2 + i2\sqrt{3}$$

$$S_2 = -2 - i2\sqrt{3}$$

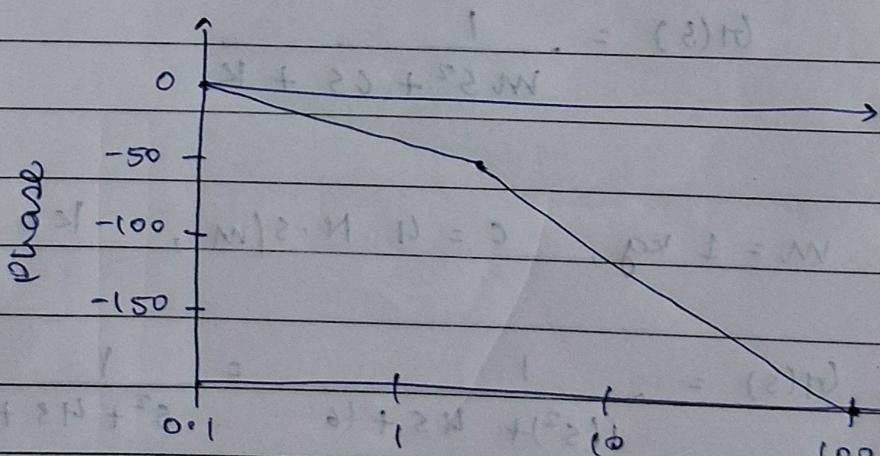
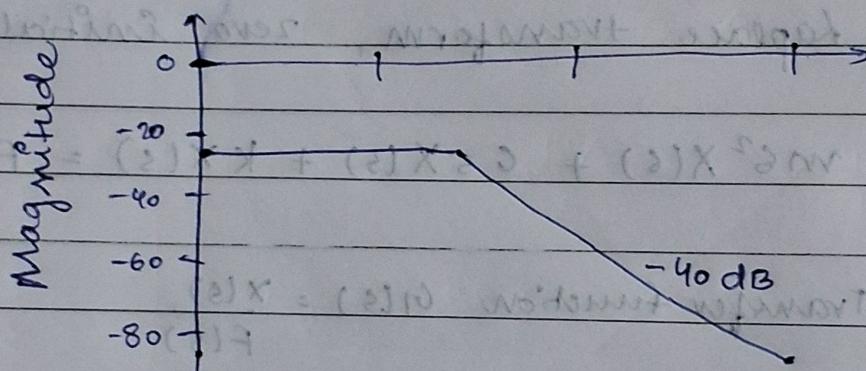
$$\omega_n = \sqrt{16} = 4$$

$$\xi = \frac{d}{2m\omega_n} = \frac{4}{2 \cdot 1 \cdot 4} = \frac{4}{8} = 0.5$$

$$G(0) = \frac{1}{16}$$

$$20 \log_{10} \left(\frac{1}{16} \right) \approx -24.08 \text{ dB}$$

3.



freq.

$$0 = \delta I + \delta P + \delta \Sigma$$

$$j\delta I + P - j\delta I - \delta I L + P = 0$$

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MATLAB

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1 s=tf('s');
2 G=1/(s^2+4*s+16);
3 figure; bode(G, {0.1, 100}); grid on;

Bode Diagram

Phase (deg) Magnitude (dB)

Frequency (rad/s)

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