

IV Back-propagation Algorithm

Implement Back-propagation algorithm to experiment with the use of Neural Networks for a multi-class classification problem, and try and interpret the high-level or hidden representations learnt by it.

Back propagation Algorithm:

```
1. Load data set
2. Assign all network inputs and output
3. Initialize all weights with small random numbers, typically between -1 and 1
repeat
  for every pattern in the training set
    Present the pattern to the network
    // Propagated the input forward through the network:
    for each layer in the network
      for every node in the layer
        1. Calculate the weight sum of the inputs to the node
        2. Add the threshold to the sum
        3. Calculate the activation for the node
      end
    end
    // Propagate the errors backward through the network
    for every node in the output layer
      calculate the error signal
    end
    for all hidden layers
      for every node in the layer
        1. Calculate the node's signal error
        2. Update each node's weight in the network
      end
    end
    // Calculate Global Error
    Calculate the Error Function
  end
while ((maximum number of iterations < than specified) AND
(Error Function is > than specified))
```

Source Code:

```
import numpy as np
X = np.array([[2, 9], [1, 5], [3, 6]], dtype=float)
y = np.array([92, 86, 89], dtype=float)
X = X/np.amax(X,axis=0) # maximum of X array longitudinally y
= y/100

#Sigmoid Function
def sigmoid (x):
return (1/(1 + np.exp(-x)))

#Derivative of Sigmoid Function
```

```

def derivatives_sigmoid(x):
    return x * (1 - x)

#Variable initialization
epoch=7000 #Setting training iterations
lr=0.1 #Setting learning rate
inputlayer_neurons = 2 #number of features in data set
hiddenlayer_neurons = 3 #number of hidden layers neurons
output_neurons = 1 #number of neurons at output layer

#weight and bias initialization
wh=np.random.uniform(size=(inputlayer_neurons,hiddenlayer_neurons))
bh=np.random.uniform(size=(1,hiddenlayer_neurons))
wout=np.random.uniform(size=(hiddenlayer_neurons,output_neurons))
bout=np.random.uniform(size=(1,output_neurons))

# draws a random range of numbers uniformly of dim x*y
#Forward Propagation
for i in range(epoch):
    hinp1=np.dot(X,wh)
    hinp=hinp1 + bh
    hlayer_act = sigmoid(hinp)
    outinp1=np.dot(hlayer_act,wout)
    outinp= outinp1+ bout
    output = sigmoid(outinp)
    #Backpropagation
    EO = y-output
    outgrad = derivatives_sigmoid(output)
    d_output = EO* outgrad
    EH = d_output.dot(wout.T)
    hiddengrad = derivatives_sigmoid(hlayer_act)
    #how much hidden layer wts contributed to error
    d_hiddenlayer = EH * hiddengrad
    wout += hlayer_act.T.dot(d_output) *lr
    # dotproduct of nextlayererror and currentlayerop
    bout += np.sum(d_output, axis=0,keepdims=True) *lr
    wh += X.T.dot(d_hiddenlayer) *lr
    #bh += np.sum(d_hiddenlayer, axis=0,keepdims=True) *lr
    print("Input: \n" + str(X))
    print("Actual Output: \n" + str(y))
    print("Predicted Output: \n" ,output)

```

Output:

Input:

```

[[ 0.66666667 1. ]
 [ 0.33333333 0.55555556]
 [ 1. 0.66666667]]

```

Actual Output:

```
[[ 0.92]
```

```
[ 0.86]
```

```
[ 0.89]]
```

Predicted Output:

```
[[ 0.89559591]
```

```
[ 0.88142069]
```

```
[ 0.8928407 ]]
```