Find all valid combinations of k numbers that sum up to n such that the following conditions are true:

- Only numbers 1 through 9 are used.
- Each number is used at most once.

Return *a list of all possible valid combinations*. The list must not contain the same combination twice, and the combinations may be returned in any order.

### **Example 1:**

```
Input: k = 3, n = 7
Output: [[1,2,4]]
Explanation:
1 + 2 + 4 = 7
There are no other valid combinations.
```

### **Example 2:**

```
Input: k = 3, n = 9

Output: [[1,2,6],[1,3,5],[2,3,4]]

Explanation:
1 + 2 + 6 = 9
1 + 3 + 5 = 9
2 + 3 + 4 = 9

There are no other valid combinations.
```

### **Example 3:**

```
Input: k = 4, n = 1
Output: []
Explanation: There are no valid combinations. [1,2,1] is not valid because 1 is used twice.
```

### **Example 4:**

```
Input: k = 3, n = 2
```

```
Output: []
```

Explanation: There are no valid combinations.

# Example 5:

**Input:** 
$$k = 9$$
,  $n = 45$ 

## Explanation:

$$1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 = 45$$

There are no other valid combinations.

## **Constraints:**

- 2 <= k <= 9
- 1 <= n <= 60