

$$F(x) = 8 + e^{(-x)} \sin(x)$$

$$e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \frac{x^5}{5!}$$

$$e^{-x} = 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \frac{x^4}{4!} - \frac{x^5}{5!}$$

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!}$$

$$= 8 + \left(x - \frac{x^3}{3!} + \frac{x^5}{5!} \right) \left(1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \frac{x^4}{4!} - \frac{x^5}{5!} \right)$$

$$\cancel{8x} \cancel{-x^2} \cancel{+\frac{x^3}{2}} \cancel{-\frac{x^4}{6}} \cancel{+\frac{x^5}{24}} \cancel{-\frac{x^6}{120}} \cancel{+\frac{x^7}{720}} \cancel{-\frac{x^8}{40320}} \cancel{+\frac{x^9}{362880}} \cancel{-\frac{x^{10}}{3628800}}$$

$$= 8 - x^2 + \frac{x^3}{2} - \frac{x^4}{6} + \frac{x^5}{24} - \frac{x^6}{120}$$

$$\frac{x^3}{6} + \frac{x^4}{6} - \frac{x^5}{12} - \frac{x^6}{36}$$

$$\frac{x^5}{120} - \frac{x^6}{120}$$

$$= 8 - x^2 + \frac{x^3}{2} - \frac{x^4}{6} - \frac{x^4}{6} + \frac{x^5}{24} - \frac{x^5}{12} + \frac{x^5}{120}$$

$$\boxed{= 8 - x^2 + \frac{x^3}{3} - \frac{x^5}{30}}$$