Data Mining HW 3

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Question 1

```
a)
X = matrix(c(1,3,5,0,1, 2,4,4,2,3, 3,5,3,4,5), nrow=5)
x_t = t(X) %%
x_x_{tran} = X %*% t(X)
x_tran_x
##
       [,1] [,2] [,3]
## [1,]
         36
## [2,]
         37
             49
                  61
## [3,]
         38
             61
                  84
x_x_{tran}
##
       [,1] [,2] [,3] [,4] [,5]
## [1,]
         14
             26
                  22
                      16
                           22
## [2,]
         26
             50
                      28
                           40
                  46
## [3,]
         22
             46
                  50
                      20
                           32
## [4,]
        16
             28
                  20
                      20
                           26
         22
## [5,]
             40
                  32
                      26
                           35
 b)
ei_x_tran_x = eigen(x_tran_x)
ei_x_x_tran = eigen(x_x_tran)
ei_x_tran_x
## $values
## [1] 1.535670e+02 1.543300e+01 1.421085e-14
##
## $vectors
##
             [,1]
                       [,2]
                                 [,3]
## [1,] -0.4092828  0.8159785  0.4082483
## [2,] -0.5634593  0.1258846 -0.8164966
## [3,] -0.7176358 -0.5642094 0.4082483
ei_x_x_tran
## $values
## [1] 1.535670e+02 1.543300e+01 1.998401e-14 2.848207e-15 -4.440892e-16
##
## $vectors
##
            [,1]
                       [,2]
                                [,3]
                                           [,4]
                                                      [,5]
## [2,] -0.5705086 -0.0332003 0.7978581 -0.17481584 -0.07924371
## [3,] -0.5207430 -0.7358566 -0.4209721 -0.04034212 -0.09217818
## [4,] -0.3225785  0.5103921 -0.3207010 -0.18826321 -0.70508927
```

```
c)
A = ei_x_tran_x$vectors%*%diag(ei_x_tran_x$values)%*% t(ei_x_tran_x$vectors)
       [,1] [,2] [,3]
##
## [1,]
         36
             37
## [2,]
         37
             49
                  61
## [3,]
         38
             61
                  84
The output is the same as 2a.
 d)
svd_x = svd(X)
#Compare to b
svd_x$v
             [,1]
                       [,2]
                                 [,3]
## [1,] -0.4092828 -0.8159785 -0.4082483
## [2,] -0.5634593 -0.1258846 0.8164966
## [3,] -0.7176358  0.5642094 -0.4082483
ei_x_tran_x$vectors
##
             [,1]
                       [,2]
                                 [,3]
## [1,] -0.4092828  0.8159785  0.4082483
## [2,] -0.5634593  0.1258846 -0.8164966
## [3,] -0.7176358 -0.5642094 0.4082483
svd x$u
##
             [,1]
                       [,2]
                                  [,3]
## [1,] -0.2976957 0.1590639 0.90607622
## [2,] -0.5705086 -0.0332003 0.03827317
## [3,] -0.5207430 -0.7358566 -0.13315536
## [4,] -0.3225785 0.5103921 -0.18363343
## [5,] -0.4589849 0.4142600 -0.35511895
ei_x_x_tran$vectors
##
             [,1]
                       [,2]
                                 [,3]
                                            [,4]
## [2,] -0.5705086 -0.0332003 0.7978581 -0.17481584 -0.07924371
## [3,] -0.5207430 -0.7358566 -0.4209721 -0.04034212 -0.09217818
## [5,] -0.4589849  0.4142600 -0.2887141 -0.21515796  0.69862203
(svd x$d)^2
## [1] 1.53567e+02 1.54330e+01 3.28692e-31
(ei_x_tran_x$values)
## [1] 1.535670e+02 1.543300e+01 1.421085e-14
ei_x_x_tran$values
```

[1] 1.535670e+02 1.543300e+01 1.998401e-14 2.848207e-15 -4.440892e-16

We can see that V gives the eigenvectors of X'X and that the first two columns of U correspond to the first two eigenvectors of XX' since the rank of X is 2.

```
e)
ULV = svd_x$u %*% diag(svd_x$d) %*% t(svd_x$v)
ULV
                [,1] [,2] [,3]
##
## [1,] 1.000000e+00
                        2
## [2,] 3.00000e+00
                         4
                              5
## [3,] 5.000000e+00
                              3
## [4,] 4.870696e-16
                              4
                        2
## [5,] 1.000000e+00
Х
        [,1] [,2] [,3]
##
## [1,]
           1
                2
## [2,]
                4
                      5
           3
## [3,]
          5
                4
                      3
                2
## [4,]
           0
                      4
## [5,]
           1
                3
                      5
  f)
#set the third value to 0 since X has rank 2
svd_x_n = svd_x d[1:2]
#set the smallest eigenvalue to 0 to do the 1-d projection
svd_x_oned = svd_x$d
svd_x_oned[2:3] = 0
svd_u_one = svd_x$u
svd_u_one[,2:3] = 0
svd_v_one = svd_x$v
svd_v_one[,2:3] = 0
xhat = svd_u_one %*% diag(svd_x_oned) %*% t(svd_v_one)
xhat
##
            [,1]
                      [,2]
## [1,] 1.509889 2.078663 2.647437
## [2,] 2.893574 3.983581 5.073588
## [3,] 2.641167 3.636093 4.631018
## [4,] 1.636093 2.252407 2.868722
## [5,] 2.327935 3.204866 4.081797
xhat is very close to x, so the 1D estimate is a good approximation.
  g)
ssxhat = sum(xhat^2)
ssxhat
## [1] 153.567
sum(svd_x$d^2)
## [1] 169
The Frobenius norm of xhat is the same as the sum of squares of the singular values.
  h)
SSE = sum((X-xhat)^2)
SSE
```

```
## [1] 15.433
svd_x$d[2] ^ 2
## [1] 15.433
It is equal to the square of the k + 1 singular values, where k is the number of the top k singular value we
chose to compute the Xhat approximation.
energy = svd_x_oned^2/(sum(svd_x$d^2))
energy
## [1] 0.9086805 0.0000000 0.0000000
Question 2
library(data.table)
## Warning: package 'data.table' was built under R version 3.2.5
setwd("/Users/ethen/Desktop/northwestern/winter/MSIA 421 Data Mining/hw3")
theater <- fread('theater.csv')</pre>
theater \leftarrow theater[, -c(3, 5, 7, 10), with = FALSE]
# the theater subset data will be used in question e
theater_subset <- theater[ , .(dinner, play) ]</pre>
theater[ , c('dinner', 'play', 'age', 'educ', 'income', 'cnty') := NULL ]
alpha_theater1 <- psych::alpha(theater, check.keys = TRUE)</pre>
alpha theater1
##
## Reliability analysis
## Call: psych::alpha(x = theater, check.keys = TRUE)
##
##
     raw_alpha std.alpha G6(smc) average_r S/N
                                                    ase mean sd
##
         0.93
                    0.94
                            0.94
                                       0.59 15 0.0019 5.2 1.2
##
                           95% confidence boundaries
##
    lower alpha upper
## 0.93 0.93 0.94
##
##
    Reliability if an item is dropped:
##
                     raw_alpha std.alpha G6(smc) average_r S/N alpha se
## stimulate
                           0.92
                                     0.93
                                              0.93
                                                        0.58 12
                                                                    0.0022
## dislike-
                           0.94
                                     0.94
                                              0.94
                                                        0.64 16
                                                                    0.0017
## fun
                           0.92
                                     0.92
                                              0.92
                                                        0.57 12
                                                                    0.0023
                                                                    0.0021
                           0.93
                                     0.93
## irritate-
                                              0.93
                                                        0.59 13
## bad-
                           0.92
                                     0.93
                                              0.93
                                                        0.58 12
                                                                    0.0022
## timewellspent
                           0.93
                                     0.93
                                              0.93
                                                        0.59 13
                                                                    0.0021
```

0.93

0.94

0.93

0.58 12

0.64 16

0.58 12

0.0022

0.0018

0.0022

0.92

0.94

0.93

0.92

0.94

0.92

exciting

noteduc-

comfortable

```
0.93
## cannotappreciate-
                        0.93
                                   0.93
                                                    0.59 13
                                                               0.0021
##
##
  Item statistics
##
                       n raw.r std.r r.cor r.drop mean sd
## stimulate
                    2692 0.86 0.86 0.85
                                            0.82 5.3 1.7
## dislike-
                    2692 0.61 0.60 0.53
                                            0.51 4.8 1.7
## fun
                    2692 0.88 0.88 0.89
                                            0.85 5.3 1.6
                    2692 0.81 0.82 0.79
                                            0.76 5.2 1.5
## irritate-
## bad-
                    2692 0.86
                               0.86 0.85
                                            0.82 5.5 1.4
## timewellspent
                               0.80 0.78
                    2692 0.81
                                            0.75 5.1 1.6
## exciting
                    2692 0.87
                               0.87 0.86
                                            0.83 5.2 1.6
## noteduc-
                    2692
                          0.59
                               0.60 0.52
                                            0.50 4.9 1.5
## comfortable
                    2692 0.85 0.85 0.84
                                            0.81 5.2 1.5
## cannotappreciate- 2692 0.83 0.83 0.81
                                            0.78 5.6 1.5
## Non missing response frequency for each item
##
                           2
                                     4
                                         5
                      1
                                3
                                              6
## stimulate
                   0.05 0.03 0.03 0.18 0.16 0.26 0.28
## dislike
                   0.19 0.22 0.12 0.28 0.07 0.06 0.05
                                                        0
                   0.04 0.03 0.04 0.18 0.16 0.27 0.28
## fun
                                                        0
## irritate
                   0.23 0.27 0.16 0.24 0.04 0.03 0.03
                                                        0
## bad
                   0.30 0.27 0.15 0.23 0.02 0.02 0.02
                   0.03 0.04 0.06 0.26 0.12 0.23 0.25
## timewellspent
## exciting
                   0.04 0.03 0.04 0.23 0.18 0.25 0.24
                   0.20 0.21 0.14 0.32 0.06 0.04 0.03
## noteduc
                                                        0
## comfortable
                   0.03 0.03 0.04 0.26 0.16 0.26 0.23
                                                        0
## cannotappreciate 0.37 0.26 0.12 0.17 0.03 0.03 0.03
                                                        0
 b)
pca1 <- prcomp(theater)</pre>
pca1$sdev
## [1] 3.9578487 1.4705079 1.3525016 1.0562171 0.9577743 0.8441564 0.8021089
## [8] 0.7436424 0.6966951 0.6110656
```

4 eigenvalues are greater than 1.

pca1\$rotation

##		PC1	PC2	PC3	PC4
##	stimulate	-0.3646057	0.20482521	-0.13904938	0.018162565
##	dislike	0.2497032	0.75293543	0.56798229	-0.195442289
##	fun	-0.3605609	0.20875905	-0.14267364	0.009324962
##	irritate	0.3031613	0.14282089	-0.07515483	0.445852971
##	bad	0.3078863	0.05446465	-0.08228713	0.343278421
##	timewellspent	-0.3340471	0.24366524	-0.06300969	0.484920839
##	exciting	-0.3462710	0.24216527	-0.01878609	0.140614172
##	noteduc	0.2200925	0.40442360	-0.76210805	-0.400695571
##	comfortable	-0.3250952	0.17503867	-0.02451621	0.101350222
##	cannotappreciate	0.3199804	0.10943753	-0.19888022	0.467986279
##		PC	5 I	PC6 I	PC7 PC8
##	stimulate	-0.5503104	5 0.1772047	727 0.31438	183 -0.375692958
##	dislike	0.0274692	4 0.0689446	642 0.046520	065 -0.029891242
##	fun	-0.3088356	8 0.1168842	217 0.098867	729 0.097832828
##	irritate	-0.3939842	0 -0.6541049	546 -0.026702	264 0.168709029

```
-0.08155361 0.052273076 -0.13294364 -0.598406883
                     0.62190950 -0.157937601 0.39902480 -0.119786773
## timewellspent
## exciting
                    -0.09647051 -0.056899099 -0.22080368 0.534136067
## noteduc
                      0.17719861 -0.109979551 -0.01177851 0.002472106
## comfortable
                      0.10728004 - 0.006041583 - 0.81234758 - 0.266588965
## cannotappreciate -0.01278609  0.692303527 -0.05306349  0.301845196
                             PC9
                                           PC10
## stimulate
                    -0.12512459 0.4642889873
## dislike
                    -0.03303846 -0.0166694267
## fun
                    -0.02249555 -0.8228482968
## irritate
                    -0.26647682 0.0005698514
                     0.60339177 -0.1685185328
## bad
## timewellspent
                    -0.06795065 0.0043204783
## exciting
                      0.61957559 0.2661833089
## noteduc
                      0.02249027
                                  0.0498972820
## comfortable
                    -0.33064285
                                  0.0308739699
## cannotappreciate -0.22211035 0.0660648551
noteduc, dislike have smaller first loading vectors when it comes to magnitude.
  c)
# after removing noteduc and dislike,
# the drop of reliability remains the same for
# every single variable that we dropped
theater[ , c('dislike', 'noteduc') := NULL ]
##
         stimulate fun irritate bad timewellspent exciting comfortable
##
                 6
                      7
                               1
                                   1
                                                  6
                                                           6
                                                                        7
      1:
                 7
##
      2:
                                   4
                                                  4
                                                            4
                                                                        4
                      4
                               1
##
      3:
                 6
                      6
                               2
                                   2
                                                  6
                                                           6
                                                                        5
##
      4:
                 7
                      7
                               4
                                   1
                                                  5
                                                           5
                                                                        6
##
                 6
                      7
                                   1
                                                  7
                                                           7
                                                                        7
      5:
                               1
##
## 2688:
                 5
                      5
                               3
                                   3
                                                  4
                                                           5
                                                                        4
                 7
                                                  7
## 2689:
                      6
                               2
                                   1
                                                           6
                                                                        6
## 2690:
                 4
                      4
                               4
                                   4
                                                  4
                                                           4
                                                                        4
## 2691:
                 6
                                   1
                                                  5
                                                           5
                 7
                     7
                                                  7
                                                           6
                                                                        7
## 2692:
##
         cannotappreciate
##
      1:
##
      2:
                         1
##
                         2
      3:
##
      4:
                         3
##
      5:
                         1
##
## 2688:
                         3
## 2689:
                         1
## 2690:
                         4
## 2691:
                         1
## 2692:
alpha_theater2 <- psych::alpha(theater, check.keys = TRUE)</pre>
```

Warning in psych::alpha(theater, check.keys = TRUE): Some items were negatively correlated with tota
This is indicated by a negative sign for the variable name.

```
alpha_theater2
## Reliability analysis
## Call: psych::alpha(x = theater, check.keys = TRUE)
##
##
     raw_alpha std.alpha G6(smc) average_r S/N
                                                   ase mean sd
##
         0.95
                   0.95
                           0.95
                                      0.69 18 0.0015 5.3 1.3
##
                          95% confidence boundaries
##
   lower alpha upper
## 0.94 0.95 0.95
##
   Reliability if an item is dropped:
##
                     raw_alpha std.alpha G6(smc) average_r S/N alpha se
                                                       0.69 16
## stimulate
                          0.94
                                    0.94
                                             0.94
                                                                   0.0018
## fun
                          0.94
                                     0.94
                                             0.93
                                                       0.68 15
                                                                   0.0019
## irritate-
                          0.94
                                    0.94
                                             0.94
                                                       0.71 17
                                                                  0.0016
## bad-
                          0.94
                                    0.94
                                             0.94
                                                       0.69 16
                                                                  0.0017
## timewellspent
                          0.94
                                    0.94
                                             0.94
                                                       0.71 17
                                                                  0.0017
                                    0.94
                                                       0.68 15
## exciting
                          0.94
                                             0.94
                                                                  0.0018
## comfortable
                          0.94
                                    0.94
                                             0.94
                                                       0.69 16
                                                                   0.0018
                                                       0.71 17
## cannotappreciate-
                          0.94
                                    0.94
                                             0.94
                                                                   0.0017
##
##
   Item statistics
##
                        n raw.r std.r r.cor r.drop mean sd
## stimulate
                     2692 0.88 0.87
                                       0.86
                                               0.83 5.3 1.7
                                 0.90 0.90
## fun
                     2692
                          0.91
                                               0.87
                                                    5.3 1.6
## irritate-
                     2692
                           0.81
                                 0.81
                                       0.77
                                               0.75
                                                    5.2 1.5
## bad-
                     2692
                           0.86
                                 0.86
                                       0.84
                                               0.81
                                                     5.5 1.4
                           0.83
                                 0.82
                                       0.79
                                               0.77
## timewellspent
                     2692
                                                     5.1 1.6
                     2692
                           0.89
                                 0.89
                                       0.87
                                               0.85
                                                    5.2 1.6
## exciting
## comfortable
                     2692
                           0.87
                                 0.87
                                       0.84
                                               0.82
                                                    5.2 1.5
## cannotappreciate- 2692 0.82 0.82 0.79
                                               0.77
                                                    5.6 1.5
## Non missing response frequency for each item
                            2
                                 3
                                       4
                       1
                    0.05 0.03 0.03 0.18 0.16 0.26 0.28
## stimulate
## fun
                    0.04 0.03 0.04 0.18 0.16 0.27 0.28
                                                           0
## irritate
                    0.23 0.27 0.16 0.24 0.04 0.03 0.03
                    0.30 0.27 0.15 0.23 0.02 0.02 0.02
                                                           0
## timewellspent
                    0.03 0.04 0.06 0.26 0.12 0.23 0.25
                                                           0
## exciting
                    0.04 0.03 0.04 0.23 0.18 0.25 0.24
                                                           0
## comfortable
                    0.03 0.03 0.04 0.26 0.16 0.26 0.23
                                                           0
## cannotappreciate 0.37 0.26 0.12 0.17 0.03 0.03 0.03
                                                           0
# and the explained ratio of the first loading vector is larger
pca2 <- prcomp(theater)</pre>
summary(pca1)
## Importance of components:
                                      PC2
                                             PC3
##
                             PC1
                                                     PC4
                                                             PC5
                                                                     PC6
## Standard deviation
                          3.9578 1.47051 1.3525 1.05622 0.95777 0.84416
## Proportion of Variance 0.6405 0.08842 0.0748 0.04561 0.03751 0.02914
## Cumulative Proportion 0.6405 0.72891 0.8037 0.84932 0.88683 0.91597
##
                                      PC8
                                               PC9
                              PC7
                                                      PC10
```

```
## Standard deviation
                          0.80211 0.74364 0.69670 0.61107
## Proportion of Variance 0.02631 0.02261 0.01985 0.01527
## Cumulative Proportion 0.94227 0.96489 0.98473 1.00000
summary(pca2)
## Importance of components:
##
                             PC1
                                     PC2
                                              PC3
                                                      PC4
                                                              PC5
                                                                      PC6
                          3.7609 1.16042 0.96781 0.85433 0.80384 0.74448
## Standard deviation
## Proportion of Variance 0.7358 0.07005 0.04873 0.03797 0.03362 0.02883
## Cumulative Proportion 0.7358 0.80589 0.85462 0.89259 0.92621 0.95504
                              PC7
                                     PC8
## Standard deviation
                          0.69818 0.6138
## Proportion of Variance 0.02536 0.0196
## Cumulative Proportion 0.98040 1.0000
  d)
# reverse code the reversed coded columns
reverse_col <- c('irritate', 'bad', 'cannotappreciate')</pre>
max_score <- 7
theater[ , (reverse_col) := lapply(.SD, function(col) {
    (\max_{score} + 1) - col
}), .SDcols = reverse_col ]
# compute attitude variable
theater_subset[ , attitude := rowSums(theater) / ncol(theater) ]
theater_subset
##
         dinner play attitude
##
      1:
              2
                   4
                        6.625
##
                        5.125
      2:
              0
                   0
##
      3:
              2
                   0
                        5.875
##
              2
      4:
                   0
                        5.750
##
      5:
             2
                   0
                        6.875
##
     ---
## 2688:
             0
                   0
                        4.750
## 2689:
              0
                   0
                        6.500
## 2690:
              0
                   Ω
                        4.000
## 2691:
              0
                   1
                        5.625
## 2692:
              0
                        6.875
  e)
# there are NA values in theater subset, we tried dropping the
# NA values and setting the NA values to O and obtained similar result
theater_subset1 <- theater_subset[ complete.cases(theater_subset), ]</pre>
theater_subset1[ , new_feature := log(dinner + play + 1) ]
theater_subset[ is.na(dinner), dinner := 0 ]
theater_subset[ is.na(play), play := 0 ]
theater_subset[ , new_feature := log(dinner + play + 1) ]
with( theater_subset1, cor(new_feature, attitude, method = 'pearson') )
```

[1] 0.2729852

```
with( theater_subset, cor(new_feature, attitude, method = 'pearson') )
## [1] 0.274381
f)
```

The sum of dinner and play is not within the normal range of 1 to 7, by taking the log, we transform it to a narrower and more comparable range.

Question 3

V33 1278 0.80 0.79 0.77

```
music <- read.csv("music.csv")</pre>
retain_cols <- c('V28', 'V29', 'V30', 'V31', 'V32', 'V33',
                  'V34', 'V43', 'V46', 'V47', 'V50', 'V52')
music <- music[, retain_cols]</pre>
  a)
alpha_music <- psych::alpha(music)</pre>
alpha_music
##
## Reliability analysis
## Call: psych::alpha(x = music)
##
##
     raw_alpha std.alpha G6(smc) average_r S/N
                                                     ase mean sd
##
                    0.94
                                       0.58 16 0.0024
         0.94
                            0.94
                                                         2.8 1
##
##
    lower alpha upper
                           95% confidence boundaries
## 0.94 0.94 0.95
##
##
    Reliability if an item is dropped:
##
       raw_alpha std.alpha G6(smc) average_r S/N alpha se
## V28
            0.94
                       0.94
                               0.94
                                          0.57
                                                14
                                                      0.0027
## V29
            0.94
                       0.94
                               0.94
                                          0.57
                                                15
                                                      0.0026
## V30
            0.94
                       0.94
                               0.94
                                          0.57
                                                15
                                                      0.0026
## V31
            0.94
                       0.94
                               0.94
                                          0.60
                                                16
                                                      0.0024
## V32
            0.93
                       0.93
                               0.94
                                          0.56
                                                14
                                                      0.0027
## V33
            0.94
                       0.94
                               0.94
                                          0.57
                                                15
                                                      0.0026
## V34
            0.94
                       0.94
                               0.94
                                          0.58
                                                15
                                                      0.0026
## V43
            0.94
                       0.94
                                          0.57
                                                15
                                                      0.0026
                               0.94
## V46
            0.94
                       0.94
                               0.94
                                          0.57
                                                15
                                                      0.0026
                       0.94
## V47
            0.94
                               0.94
                                          0.58
                                                15
                                                      0.0025
            0.94
                       0.94
                               0.94
                                                      0.0025
## V50
                                          0.58
                                                15
## V52
            0.94
                       0.94
                               0.94
                                          0.58 15
                                                      0.0026
##
##
    Item statistics
##
          n raw.r std.r r.cor r.drop mean sd
## V28 1278  0.84  0.84  0.83
                                 0.80
                                        3.1 1.3
                                        3.0 1.2
## V29 1278 0.81 0.81
                          0.80
                                 0.77
## V30 1278
             0.80
                   0.80
                          0.78
                                 0.75
                                        2.8 1.3
## V31 1278
             0.64
                   0.65
                          0.60
                                 0.58
                                        3.0 1.2
## V32 1278
             0.85
                   0.85
                          0.84
                                 0.82 2.7 1.3
```

0.75 2.4 1.3

```
## V34 1278 0.78 0.77 0.75
                                0.73 2.4 1.4
## V43 1278 0.80 0.80
                         0.78
                                0.75 2.3 1.3
                  0.80
                         0.79
## V46 1278
            0.81
                                0.76
                                     2.5 1.4
## V47 1278
                  0.74
            0.74
                         0.71
                                0.68
                                      3.2 1.3
## V50 1278
             0.75
                   0.75
                         0.72
                                0.70
                                      2.9 1.3
## V52 1278
            0.78 0.79 0.76
                                0.74
                                      3.0 1.2
## Non missing response frequency for each item
##
          0
               1
                    2
                         3
                              4
                                   5 miss
## V28 0.02 0.12 0.12 0.33 0.27 0.13
                                        0
## V29 0.02 0.13 0.13 0.39 0.22 0.11
## V30 0.03 0.19 0.17 0.28 0.22 0.11
                                        0
## V31 0.02 0.11 0.15 0.35 0.27 0.10
                                        0
## V32 0.02 0.20 0.19 0.30 0.19 0.09
## V33 0.03 0.29 0.21 0.25 0.14 0.08
                                        0
## V34 0.03 0.33 0.18 0.19 0.18 0.09
## V43 0.03 0.33 0.23 0.23 0.11 0.06
                                        0
## V46 0.02 0.30 0.18 0.26 0.14 0.10
## V47 0.02 0.13 0.10 0.27 0.30 0.18
                                        0
## V50 0.02 0.15 0.14 0.34 0.25 0.10
                                        0
## V52 0.02 0.12 0.14 0.41 0.21 0.10
pca <- prcomp(music)</pre>
pca$sdev
```

```
## [1] 3.5079660 1.1715773 1.0560283 0.9252190 0.8715732 0.8055641 0.7721219 ## [8] 0.7408483 0.7128224 0.6874437 0.6526254 0.5724456
```

3 eigenvalues are greater than 1.

c)

A person's similarity of taste in music with friends or a person's willingless to share his/her personal taste in music.