



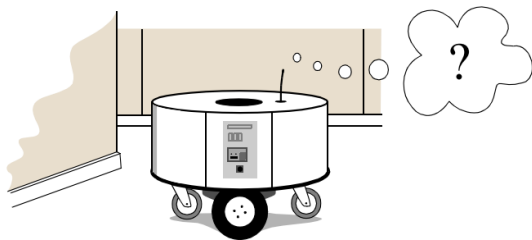
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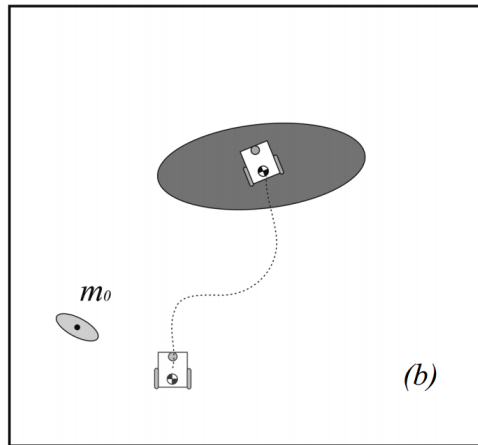
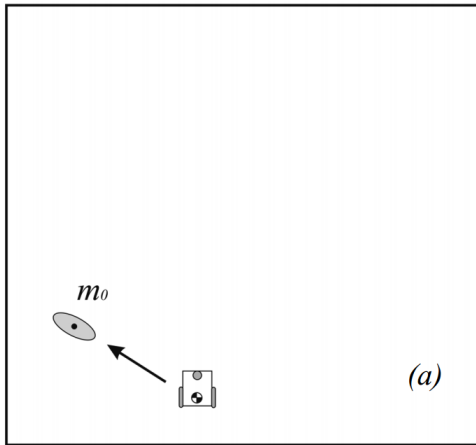
# A ROS implementation of a 6-DoF EKF for indoor drone Visual SLAM

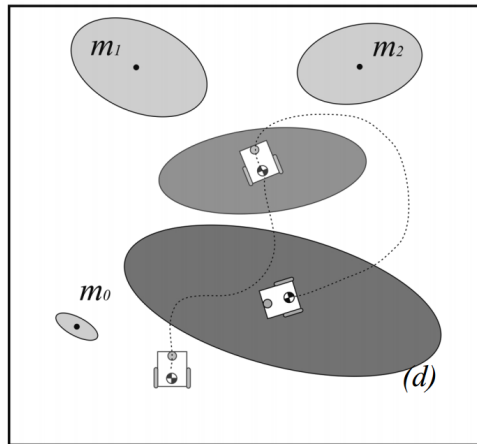
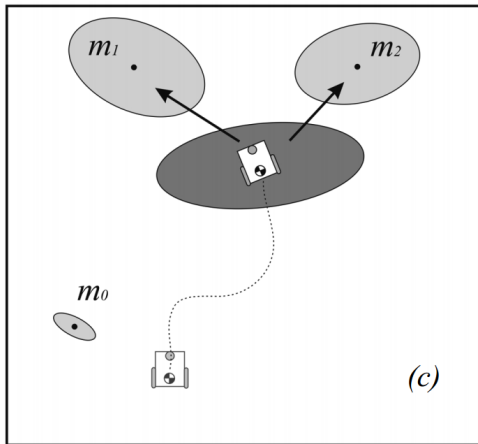
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15 Dec. 2020

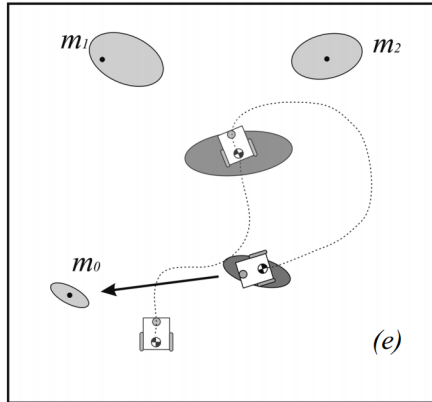
- Indoor environment
- Fully autonomous drone
- No GNSS nor Laser devices
- Inertial devices, range sensors, cameras and speed sensors are allowed
- Obstacles have at most 3mts height with passages of at least 1mt
- Landmarks: colored poles and QR markers
- 2-phase competition: inspection and path-follow

- Localization: where the robot is
- Mapping: build a map of the environment
- SLAM: localize itself while building a map









- Motion and observation processes are usually not linear
- Motion model:  $g(u_t, \mu_{t-1})$
- Observation model:  $h(\hat{\mu}_t)$
- EKF uses Taylor expansion to linearize the processes
- Builds feature-based maps
- The full-state (map) is
$$\mu = [q_r \quad m_0 \quad \dots \quad m_{n-1}]^T$$
- As in Kalman Filter, the process comprises 2 steps:  
prediction and correction

## Characteristics

- PixHawk 4 Flight Controller
- 8 range finder
- 4 monocular cameras
- 2 stereo cameras: 1 pointing down, 1 pointing forward
- 1 optical-flow device
- Accelerometer + gyroscope
- Magnetometer
- Barometer





- MAVROS node interfaces with the flight controller, and provides the control signal
- Control signal is composed by linear and angular velocities

$$u = \begin{bmatrix} v_x^b & v_y^b & v_z^b & \omega_x^b & \omega_y^b & \omega_z^b & \phi^b & \theta^b & \psi^b \end{bmatrix}^T$$

$$v^w = \mathbf{T} * \begin{bmatrix} v_x^b \\ v_y^b \\ v_z^b \end{bmatrix}$$

- Given the linear velocities transformation  $v^w$ , the motion model can be summarized as follow

$$g(\mu_{t-1}, u_t) = \begin{cases} \begin{bmatrix} \mu_{t-1,x^w} \\ \mu_{t-1,y^w} \\ \mu_{t-1,z^w} \end{bmatrix} + \Delta t * v^w \\ \mu_{t-1,\psi} + \Delta t * \omega_z^b \end{cases}$$

- Noise in the motion process is assumed to be  $\mathcal{N}(0, R_t)$

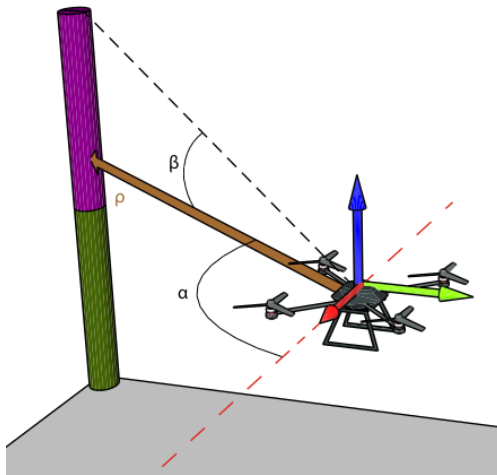
- 2 types of landmarks: Poles & Markers
  - ▶ Poles' observations is Range and Bearing
  - ▶ Markers' observations is the pose with respect to the camera reference frame
- Additionally, height correction is done using range sensor and 3D obstacle map
- Observation for landmark  $i$  is  $z_i = h_i(x_t) + \mathcal{N}(0, Q_t)$

■ Range and bearing information

- ▶  $\rho$ : distance
- ▶  $\beta$ : altitude
- ▶  $\alpha$ : azimuth

Observation model:

$$\begin{aligned} \begin{bmatrix} p_{i,x}^b \\ p_{i,y}^b \\ p_{i,z}^b \end{bmatrix} &= T_r^{-1} \begin{bmatrix} p_{i,x}^w \\ p_{i,y}^w \\ p_{i,z}^w \end{bmatrix} \\ h_i(\hat{\mu}_t) &= \begin{bmatrix} p_{i,\rho} \\ p_{i,\alpha} \\ p_{i,\beta} \end{bmatrix} = \begin{bmatrix} \sqrt{p_{i,x}^b{}^2 + p_{i,y}^b{}^2} \\ \text{atan2} \left( p_{i,y}^b, p_{i,x}^b \right) \\ \text{atan2} \left( p_{i,z}^b, p_{i,\rho} \right) \end{bmatrix} \end{aligned}$$

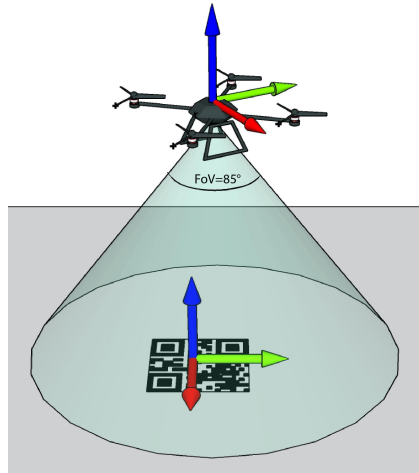


## Markers

- Markers are unknown first, and added to the map once the drone sees them
- Observations is composed by its position with respect to the camera reference frame
- To add new markers to the state  $h^{-1}(\hat{\mu}_t)$  should project the observation from the camera reference frame to the world reference frame

Observation model:

$$h_i(\hat{\mu}_t) = \begin{bmatrix} m_{i,x}^c \\ m_{i,y}^c \\ m_{i,z}^c \\ m_{i,\phi}^c \\ m_{i,\theta}^c \\ m_{i,\psi}^c \end{bmatrix} = (T_r * T_c)^{-1} * T_m$$



- The observations to correct the height are composed by the range sensor + Octomap measurement
- The height observation is
$$z = voxel_z + range_{distance}$$
- Hence, the observation model is simply:

something

$$h(\hat{\mu}_t) = \hat{\mu}_z + bias$$



## Normalized Estimation Error Squared

- Defined as:

$$NEES = (\mathbf{x} - \hat{\mathbf{x}})^T \Sigma^{-1} (\mathbf{x} - \hat{\mathbf{x}}) \leq \chi_{d,1-\alpha}^2$$

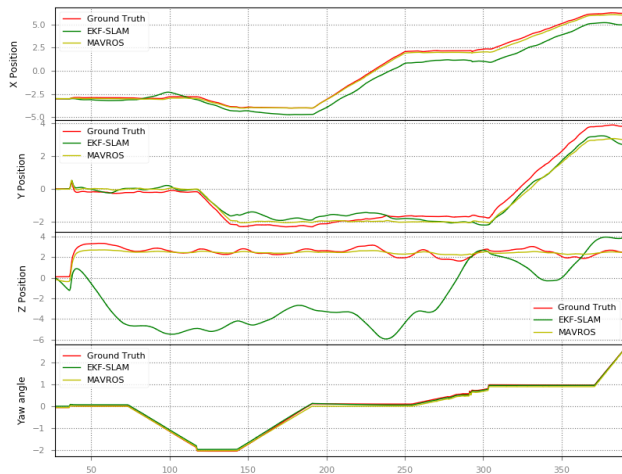
- Can be performed to check the consistency of the filter
- Consistency of the filter is maintained by using observations that satisfy the test

$$v^i = z_t^i - h^i(\hat{\mu}_t)$$

$$S = H_t^i \hat{\Sigma}_t H_t^{iT} + Q_t$$

$$D_i^2 = v^i S^{-1} v^i \leq \chi_{d,1-\alpha}^2$$

- the importance of known poles and known and unknown markers in the localization and mapping process
- the accuracy of markers' pose estimation
- the importance of the NEES test to evaluate measurements and the filter's consistency

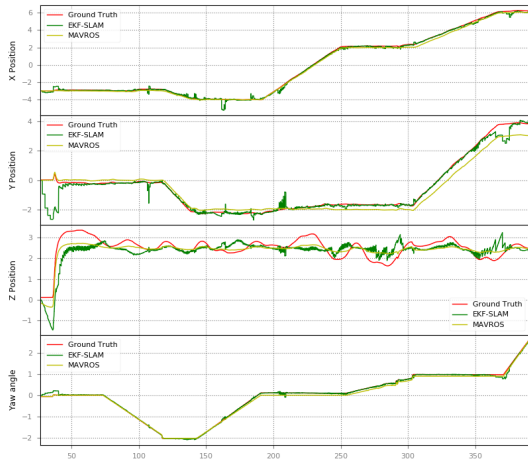


# Experiments & Results - Experiments A

## Real observation of poles

18/24

Experiment using *real observations* taken from the ROS bag.

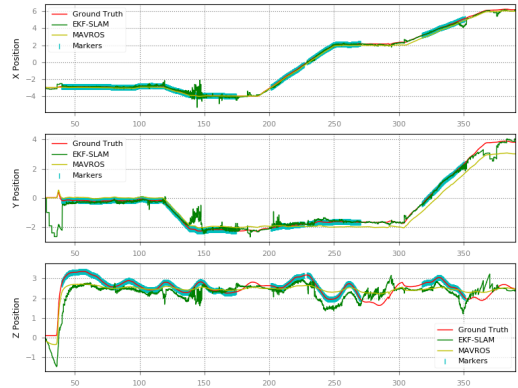


# Experiments & Results - Experiments B

## SLAM with poles and markers

19/24

This experiment uses markers and poles to localize. It had the objective of understanding the importance of both poles and markers in the SLAM situation.



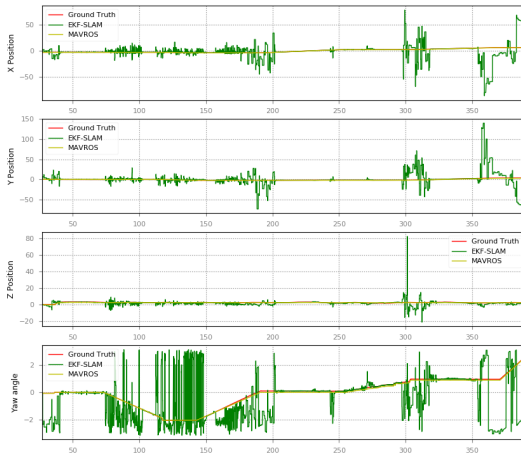
## Distance between real and estimated poses.

Measures the distance between the true position of markers and the one estimated by the algorithm in a context of *real observations*, both for markers and poles.

MARKER ID	EUCLIDEAN DISTANCE	$\psi$
0	0.076	0.034
1	0.186	0.052
4	0.119	0.055
5	0.155	0.013
Max.	0.186	0.055
Min.	0.076	0.013
Avg.	0.134	0.039

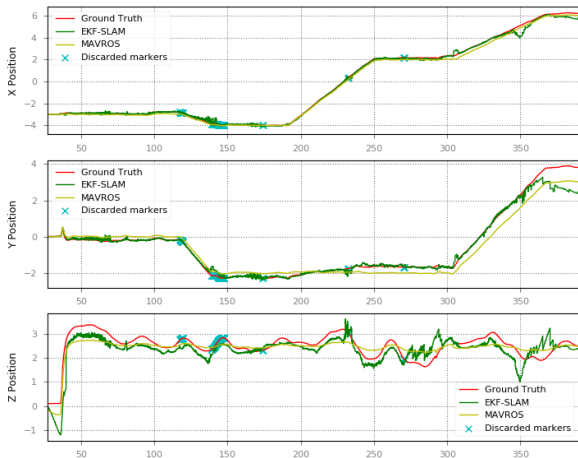
## NEES test influence

What happen when no  
NEES test is used?



What about the  $\chi^2_\alpha$  threshold?

- So far, was used a threshold that corresponds to 95% of valid measurements. This means that we assume that the 95% of the observations are valid.
- This corresponds to  $\alpha = 0.05$ , but this value is the standard one.
- What happen with other confidence levels? for instance  $\alpha = 0.9$



- The first 2 experiments showed the importance of poles and markers in the localization process.
- The markers' pose estimation in an SLAM situation is good enough for the competition context.
- NEES is fundamental for the consistency of the filter.
- Lower confidence of valid measurements implies discarding truly bad measurements, but on the other hand it can discard measurements that can be useful to correct the drone's pose.
- The value of  $\alpha$  becomes a parameter of the system.



- Deploy and test the proposed implementation in the real drone.
- Fine-tune the noise covariance matrices.
- Extensive experimentation with Octomap and range sensor for height update.
- Camera self calibration procedure to improve the Z position estimation using poles and markers
- Compare the current algorithm with other algorithms like Error-State EKF-SLAM, or UKF-SLAM, and evaluate their performance with the current implementation as baseline

# Thank you!



## Questions?