Advanced general relativity

ULB MA | 2023–2024 | Prof. Glenn BARNICH

Chapter 1: Auxiliary Fields

Handwritten notes (scanned)

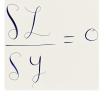
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Heads up: only Chapter 1 here. This DocHub upload contains **only the first chapter**. The full set of chapters, personal notes, exercise corrections, and a reference-book list are on my website.

- All chapters: see the course page
- Exercise corrections & personal work: see the main page.
- **Reference books:** see the book section.

Get the rest: scan or click here

https://adierckx.github.io/NotesAndSummaries/Master/MA1/PHYS-F-418













Disclaimer. The notes published here are based on my understanding of the courses and have not been independently reviewed or verified. I hope they are helpful, but there may be errors or inaccuracies. If you find any errors or have suggestions for improvement, please do not hesitate to contact me at ant.dierckx@gmail.com. Thank you!

ADVANCED GENERAL RELATIVITY

PHYS-F-418 ~ Glenn Barnich

- The major air of this course is to provide technical background material needed for standard competations in GR and its extension.

CHA AUXILIARY FIELDS

1.1 Generalized auxiliary Lields and Symmetries

-> Let the action S depends on 2 fields y', z":

S[y', 3 x] = Jdhx L[y', y'n, y'n, 3", 3 no, ...]

where do = 2nd

Lo Varying the action we get:

S5 = \int d^x \langle \frac{\int \L}{\int \gamma^i} + \int \L \cdot \gamma^\alpha \langle

> Renarder: for L=L(q,q,q), one gets: SL= dq 2qL+Sq 2L + Sq 2L 2q 2q

Furthermore, So = & So. Integrating by part, he get:

SL = Sq (DL - d DL + d2 DL) + (boundary terms)

Ly The Euler-Lagrange derivatives are given by:

\[
\frac{1}{5g!} = \frac{2L}{3g!} = \frac{

→ If we assure SL = 0 \(\(\) \(\

A field z " is an auxiliary field is SL = 0 (yi, yi, yin, yin,) algebaically. Let SIyi, 3x] such that SL Sy: This equivalent to SL =0 where

SL Sy:

[\$\frac{5\text{T}}{5\text{3}}\times =0 \quad \text{Lagrangian}

[\$\frac{5\text{T}}{5\text{3}}\times =0 \quad \text{Lagrangian} DEMO! We have to show that SL = SL . We consider: SS = SS[y, 3=Z] = Sanx Sr Sr + 3r | Sr + + 3r | (32 r Sr + 32 r Sr) + ... + 3L 3 25 29 + 25 Sg; + 35 Sg; + = Sd4x / SL Syi + SL SZX] = Sd4x SI 1 Symmetries: Let 5=[qi,...] = Sd4x L[q;qju,...]. There is a symetry when δοφί = Q[φ, φ, ,...] => So L = On ko and Sopin = In Sopi = In Oi Ju this case, we have:

SQL=0° 2L + 2n0° 2L + 2n2 2L + ... = 2n ko 0 (1)=3 (4-36 0) (30) (We found the Noether current for such that In jo = Q' SL

