

⊙ DAMA:

→ Seasonal DM observed (?) in NaI crystal.

⊙ Reactor anomaly:

→ Deficit of $\bar{\nu}_e$ close to reactor cores

→ Could be explain by a 4th sterile neutrino

CN3 THEORETICAL LANDSCAPE

→ Standard Model = Effective field theory (EFT)

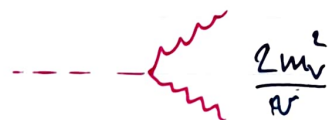
→ Scalar sector: least constraint, room for BSM physics

⊙ Scalar sector:

→ Higgs sector determined by only 1 free parameter: m_H

→ very predictive

→ coupling to vector boson exactly defined


$$\frac{2m_f^2}{v^2}$$


$$\frac{3m_h^2}{v^2}$$


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$$\frac{3m_h^2}{v^2}$$

→ After discovery (mass, spin), 1) coupling to bosons and fermions
2) self coupling

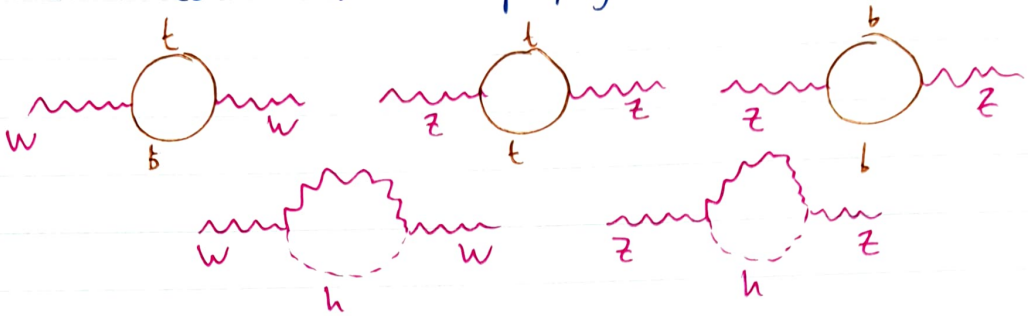
→ All these measurements are tests for BSM physics

ex of BSM: non-minimal Higgs scenarios

alternative to EWSB (ex: Higgs impostor)

⊙ Experimental constraints on m_h :

→ Radiative corrections on the propagators of bosons in the theory:



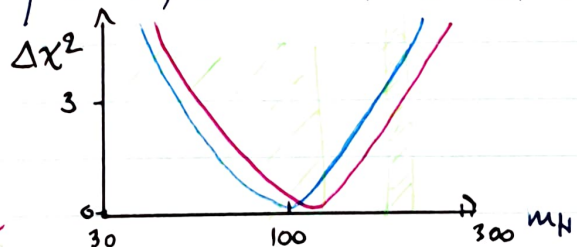
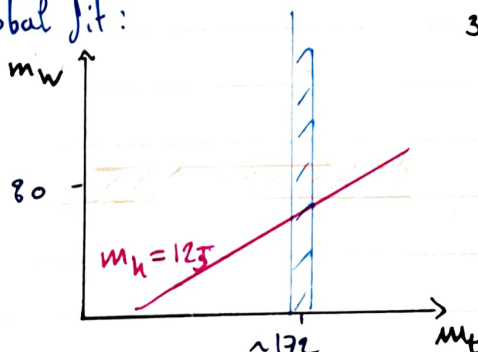
Since the Higgs contributes to loops → constraints on m_h

⊙ The E-W fit: free parameter:

- SM unifies e-m and weak interaction → only 2 coupling remain independent: 1) α
2) α_s
- Only the top quark has $m_t \sim m_Z$, all the other fermions have $m_f \ll m_Z$
- m_Z is precisely measured, but not m_W . Instead, we use G_F
- The Higgs mass m_h

↳ The free parameters are $\{\alpha_s(m_Z^2), \alpha(m_Z^2), m_Z, m_t, m_H, G_F\}$

→ Global fit:



3.1 Theoretical constraints on m_H

⊙ Perturbativity and unitarity:

→ Scattering of VB at high energies is divergent due to their longitudinal polarization. Consider $k_{VB}^\mu = (E_k, 0, 0, k)$ with $E_k^2 = k^2 - m_V^2$. The 3 polarizations vectors are

1) right handed: $\epsilon_+^\mu(k) = \frac{1}{\sqrt{2}} (0; 1, i, 0)$

2) left handed: $\epsilon_-^\mu(k) = \frac{1}{\sqrt{2}} (0; 1, -i, 0)$

3) Longitudinal: $\epsilon_L^\mu(k) = \frac{1}{m_V} (k; 0, 0, E_k)$

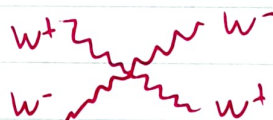
which satisfy for $a, b \in \{+, -, L\}$: $k_\mu \epsilon_a^\mu(k) = 0$

$$\epsilon_a^\mu(k) \epsilon_{b\mu}^*(k) = -\delta_{ab}$$

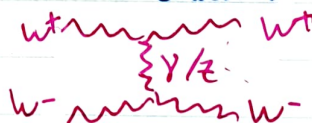
→ When $E_k \gg m_V$, $|\epsilon_L| \rightarrow \infty$: diagram with external VB have divergent cross sections.

Consider $W_L^+ W_L^- \rightarrow W_L^+ W_L^-$:

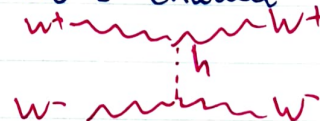
1) 4-pt interaction:



2) gauge exchange of γ/Z in the s-channel and t-channel



3) Higgs exchange in the s- and t-channel



→ The amplitude can be written as $\mathcal{A} = \mathcal{A}^{(2)} s^2 + \mathcal{A}^{(1)} s + \mathcal{A}^{(0)}$
When $s, t \gg m_V^2, m_H^2$, we have

$$\mathcal{A}^{(2)} \rightarrow 0$$

$$\mathcal{A}^{(1)} \rightarrow 0$$

$$\mathcal{A}^{(0)} \rightarrow -\frac{2m_H^2}{s^2} \simeq -4\lambda$$

any deviation in scalar sector may
spoil this $\rightarrow W_L W_L$ scattering strong
test of EWSB.

↳ If m_H too large \rightarrow change $WW \rightarrow WW$ interaction

\Rightarrow no looped situation at cern.

→ At loop level:

$$C \sim \frac{2\lambda^2}{16\pi^2}$$



If $\lambda \sim 32\pi^2$, the E-W theory should break down when $m_H > 6 \text{ TeV}$ (not perturbative anymore)

When more careful computation: upper bound $m_H < 710 \text{ GeV}$

⊙ The triviality bound:

→ Another bound of the theory is the triviality bound.

→ To ensure the theory remains consistent at all scale Q , couplings like $g_i = (0.41; 0.64; 1.2)$, $y_t = \sqrt{2} m_t / q$, $\lambda = m_h^2 / 2q^2$ must stay finite at all Q .

→ Renormalisation \Rightarrow running constants

$$\alpha: \frac{dg_1}{dt} = \frac{41}{10} \frac{1}{16\pi^2} (g_1)^3 \quad \frac{dg_2}{dt} = -\frac{19}{6} \frac{1}{16\pi^2} (g_2)^3$$

with $t = \ln(Q/Q_0)$

→ For large Higgs boson masses, $\frac{d\lambda}{dt} \approx \frac{24}{16\pi^2} \lambda^2$. After integration,

one obtains a Landau pole, the limit scale at which the theory stop being valid. Here, $Q_{LP} = m_h \exp\left\{\frac{4\pi^2 q^2}{3 m_h^2}\right\}$

PROP To have the theory valid at all scales requires vanishing couplings.

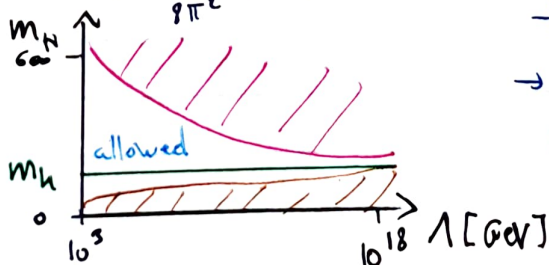
We call this the triviality condition.

⊙ Vacuum stability bound:

→ For low Higgs boson mass, $\frac{d\lambda}{dt} \approx -\frac{6}{16\pi^2} y_t^2$ so that for high Q , $\lambda < 0 \Rightarrow V < 0$.

Now, we know that $\lambda > 0 \Rightarrow$ vacuum stability bound

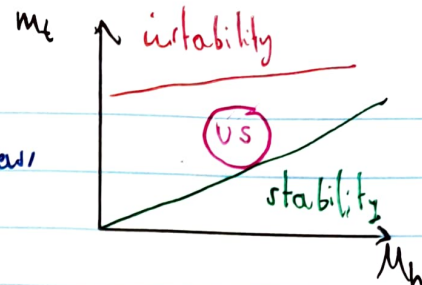
$$m_h^2 > \frac{q^2}{8\pi^2} (\dots) \ln(Q/Q_0)$$



→ if $m_h = 60 \text{ GeV} \Rightarrow$ unstable vacuum

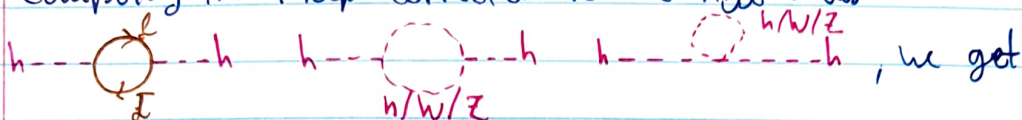
→ if $130 \text{ GeV} < m_h < 180 \text{ GeV}$, metastable situation

- Assuming only SM, one can compute the running of λ all the way to the Planck mass
- The (meta) stability depends on m_t, α_s, m_h mostly.



② Fine tuning constraints:

- Computing the 1-loop correction to the Higgs mass



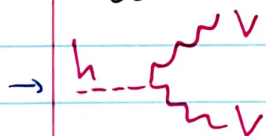
$$m_h^2 = (m_h^0)^2 + \frac{3\Lambda}{8\pi^2} (m_h^2 + 2m_W^2 + m_Z^2 - 4m_t^2)$$

The cancellation between the bare mass m_h^0 and the other terms need to cancel up to 32 digit for a theory valid till $\Lambda \sim 10^{16}$ GeV, the GUT scale.

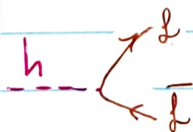
- Specific to scalars
- Fine-tuning makes the SM unnatural, even below \sim TeV.

3.2 Higgs properties

② Higgs boson couplings:



$$\mathcal{L}_{hVV} = \sqrt{12} G_F m_V^2 h V^\mu V_\mu \quad \text{quadratic}$$



$$\mathcal{L}_{hff} \propto \frac{m_f}{v} = \sqrt{12} G_F m_f h \quad \text{linear}$$

$$\text{with } G_F = \frac{g^2}{16\pi^2 m_W^2}$$

- Coupling proportional to the mass of the particles involved
 ↳ decay into the heaviest one allowed by phase-space.

① Higgs decay into fermions:

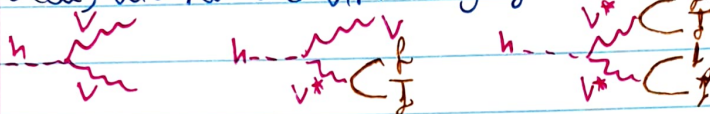
→ Born approximation:

$$\Gamma_{\text{born}}(h \rightarrow f\bar{f}) = \frac{G_F N_c}{4\sqrt{2}\pi} m_h m_f^2 \beta_f^3 \quad \beta_f = \left(1 - 4m_f^2/m_h^2\right)^{1/2}$$

with N_c a color factor.

② Higgs decays into W/Z bosons:

→ Decay into real and virtual gauge bosons:



→ When $m_h \gg m_v$, one has

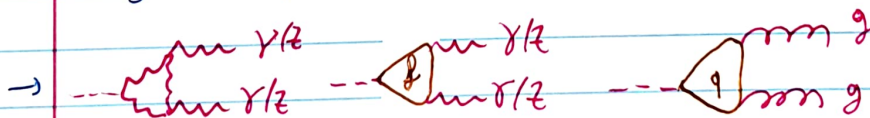
$$\Gamma(h \rightarrow WW) \simeq 2 \cdot \Gamma(h \rightarrow ZZ)$$

and $\Gamma(h \rightarrow WW + h \rightarrow ZZ) \propto m_h^3$. At large mass, the Higgs boson becomes a broad resonance, losing its particle-like nature.

← loose perturbativity

③ Higgs decays to massless particles:

→ Only at loop level



④ Summary:

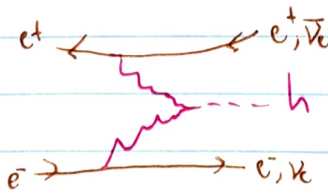
- Low mass: $b\bar{b}$ mostly
- Discovery: $\gamma\gamma$ -channel
- High mass: heavy boson dominates, + $t\bar{t}$.

① Higgs production:

→ At lepton colliders:

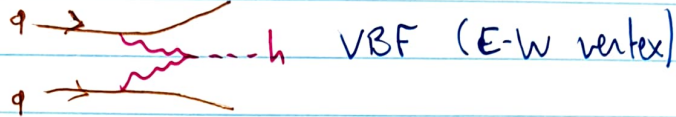
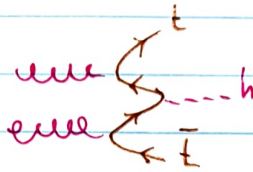
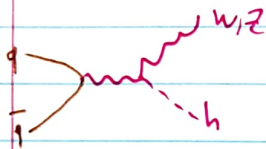


Higgsstrahlung



VBF

→ Hadron colliders:



VBF (E-W vertex)

② Searching for the Higgs at LHC:

→ $h \rightarrow WW/\tau\tau$; $h \rightarrow \gamma\gamma$; $h \rightarrow bb/\tau\tau$: need precise measurement of charged lepton, good calorimeter, determine of secondary vertex.

→ Some golden modes are mass dependent:

$$h \rightarrow \tau\tau \rightarrow 4\ell$$

$$h \rightarrow \gamma\gamma$$

$$h \rightarrow WW \rightarrow 2\ell 2\nu$$

but have low branching ratio.

→ Number of signal event $S \equiv N - B$, with statistical significance

$$\frac{S}{\sqrt{S+B}} \quad (\text{Poisson})$$

↳ Goal in search: maximize S/\sqrt{B}

→ Knowing the decay channels help accelerate the detection of the Higgs in 2012.