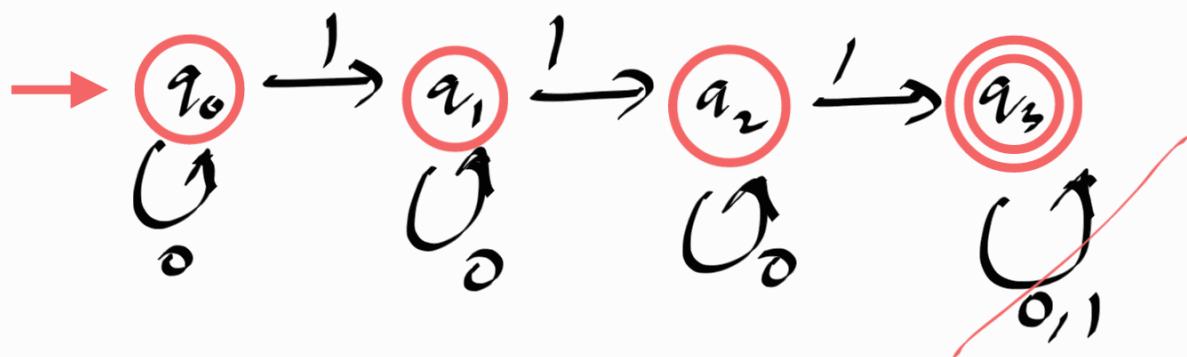


01/31/2025

clarifications.

Q1: A = $\{w \mid w \text{ contains at least } 3 \text{ is}\}$ $\Sigma = \{0, 1\}$



III
III) III x \leftarrow ^{not} accepted

What happens if
we do not have
this transition?

$$Q_2: \underline{A \circ B} = \{xy \mid x \in A, y \in B\}$$

How important is the order xy ?

$$\text{Let } \underline{A = \{0^*\}} \quad \underline{B = \{1^*\}}$$

$$\underline{0000} \underline{1111}, \underline{001111} \in A \circ B$$

$$\underline{111111} \in A \circ B \text{ why } 0^*$$

But what happens

$$\underline{1111} \underline{0000} \notin A \circ B$$

$$1111000 \in B \circ A$$

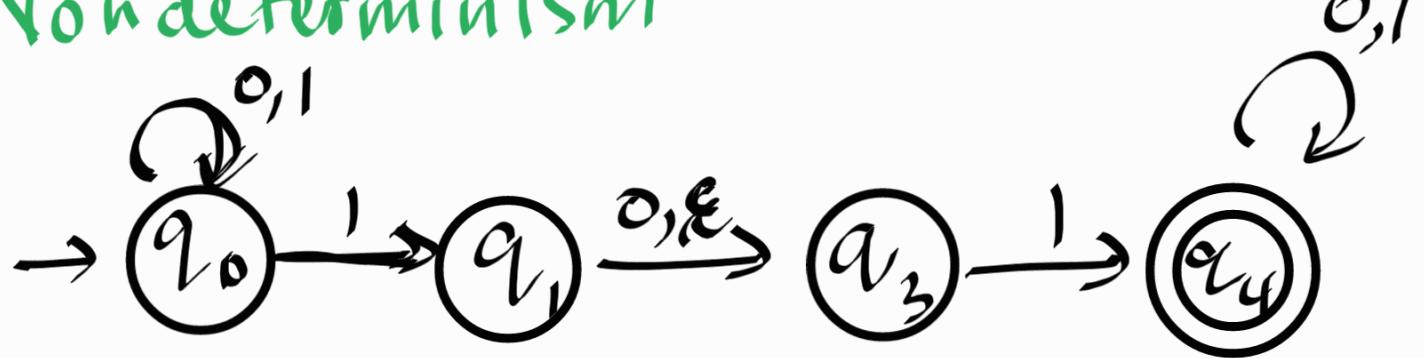
$$A \circ B \neq B \circ A \quad \text{when } A \neq B$$

Let's do some examples

Next week

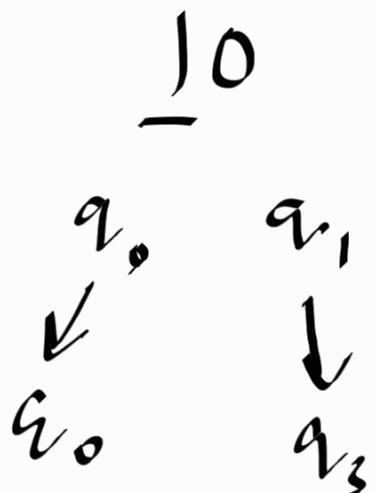
Deterministic - Given the current state and the input, we know exactly which state to reach to.

Non-determinism



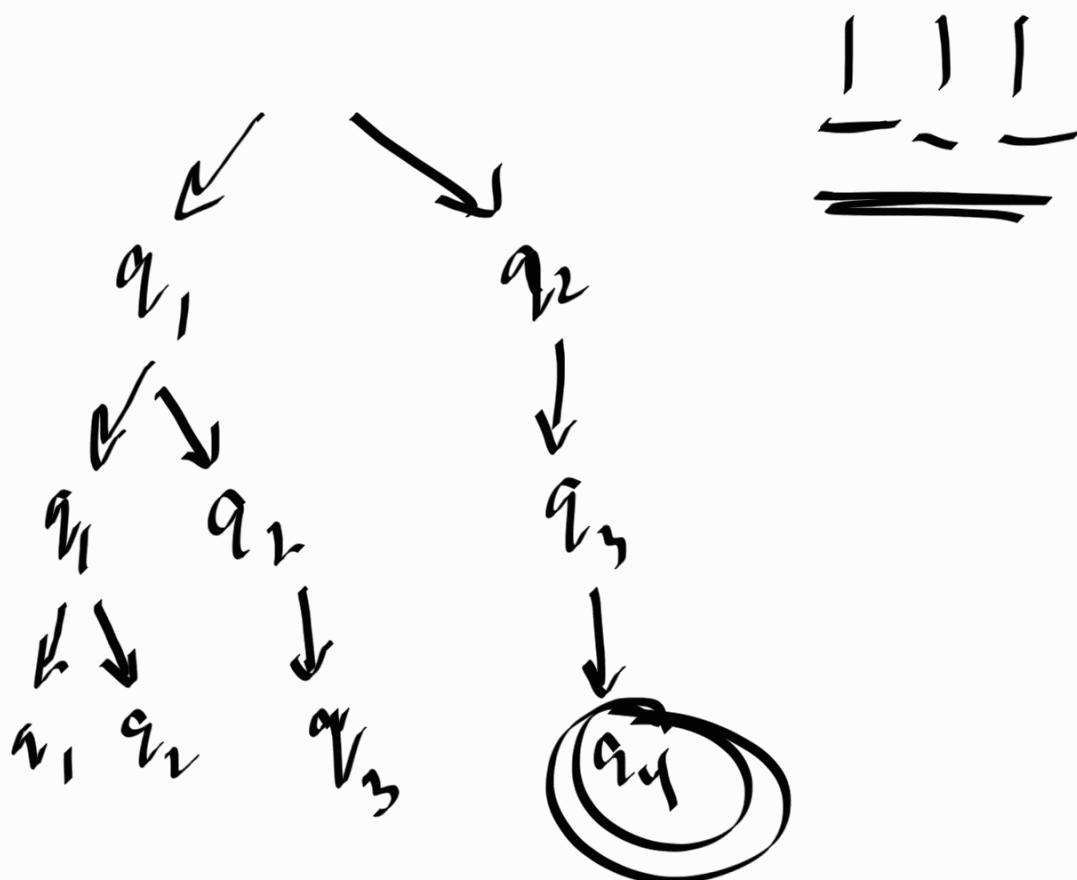
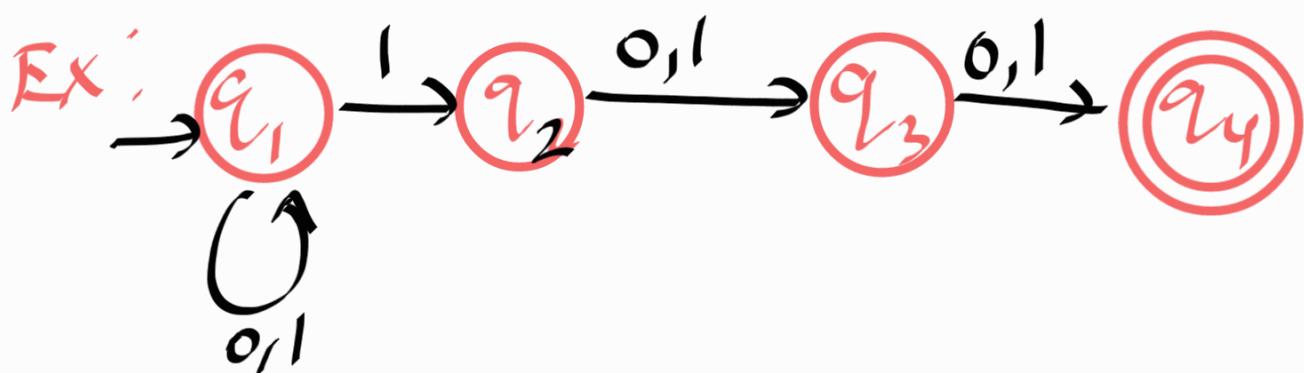
Language?

$$\begin{array}{c}
 \xrightarrow{\quad} (0|1)^* \mid (0|\epsilon) \mid (0|1)^* \\
 \hline
 \xleftarrow{\quad} \underline{(0|1)^*} \mid \underline{0} \mid \underline{(0|1)^*} \\
 \hline
 \xleftarrow{\quad} \underline{\underline{(0|1)^*}} \mid \underline{\underline{(0|1)^*}}
 \end{array}$$

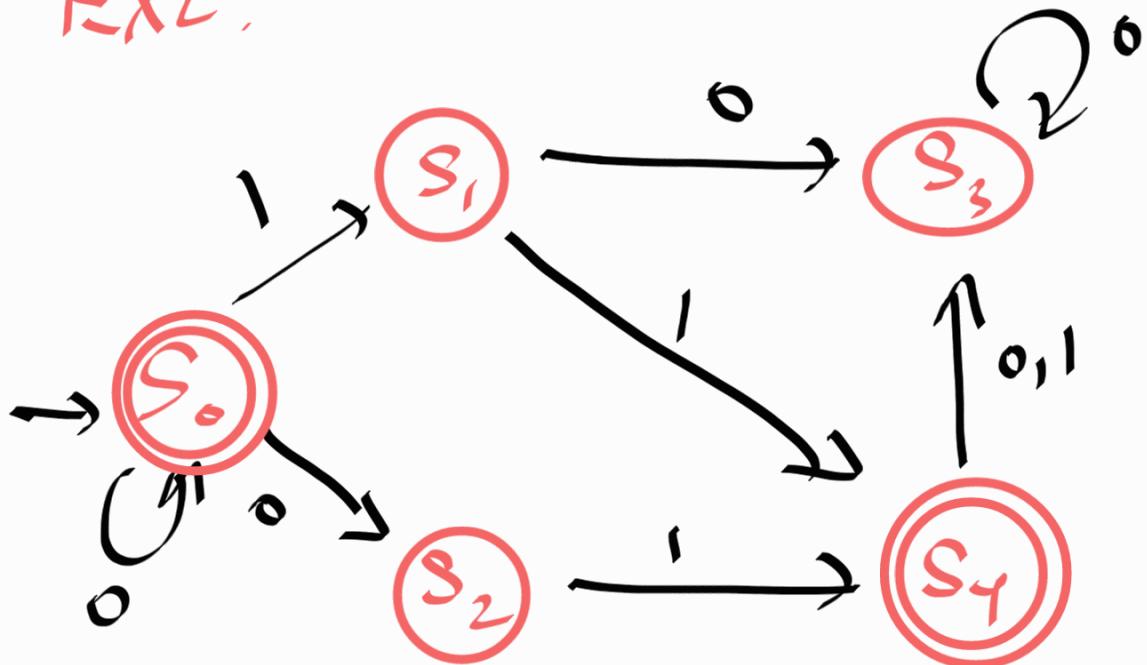


How does NFA compute?

- If any of the accept state can be reached by reading the input x in any way, we say NFA accepts x .



Ex 1:



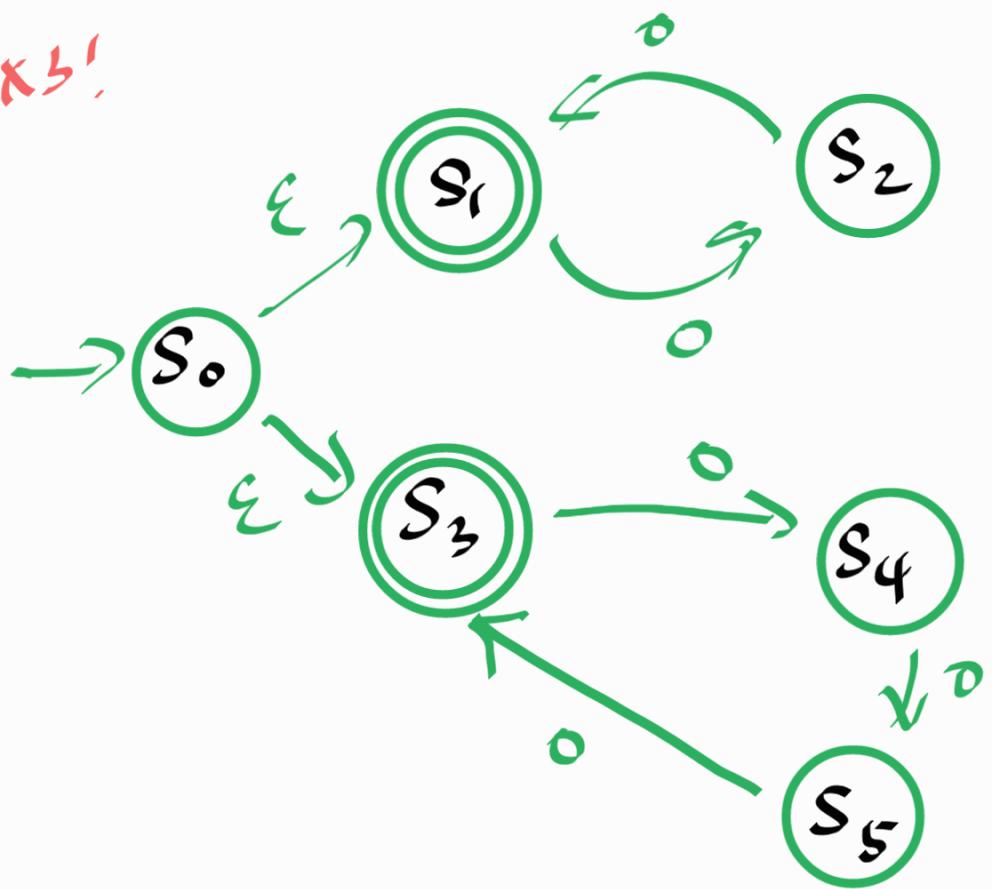
0 ✓
0* 1 0 X

0* 1 1 ✓

0* 1 1 (0|1) X

0* 0 1 ✓

$\widehat{Bx5!}$



Proper definition of NFA
is a 5-tuple

$$(Q, \Sigma, \delta, q_0, F), \text{ where}$$

01. Q is the set of states.

02. Σ is a finite alphabet.

03. $\delta: Q \times \Sigma \rightarrow P(Q)$

$$\sum_{\epsilon} = \sum \cup \{\epsilon\}$$

$P(Q)$ = power set of Q

04. $q_0 \in Q$ is the starting state.

05. $F \subseteq Q$ is the accepting state.

$$\text{Ex: } \delta(q_1, \epsilon) = \{q_1, q_3, q_4\}$$

$$\delta(q_2, 1) = \{q_4\}$$

Let $N = (\mathcal{Q}, \Sigma, \delta, q_0, F)$ be an NFA, and $w = \langle w_1, w_2, w_3, \dots, w_n \rangle$ $w_i \in \Sigma$

N accepts w if

$\exists r_0, r_1, r_2, \dots, r_n \in \mathcal{Q}$ s.t

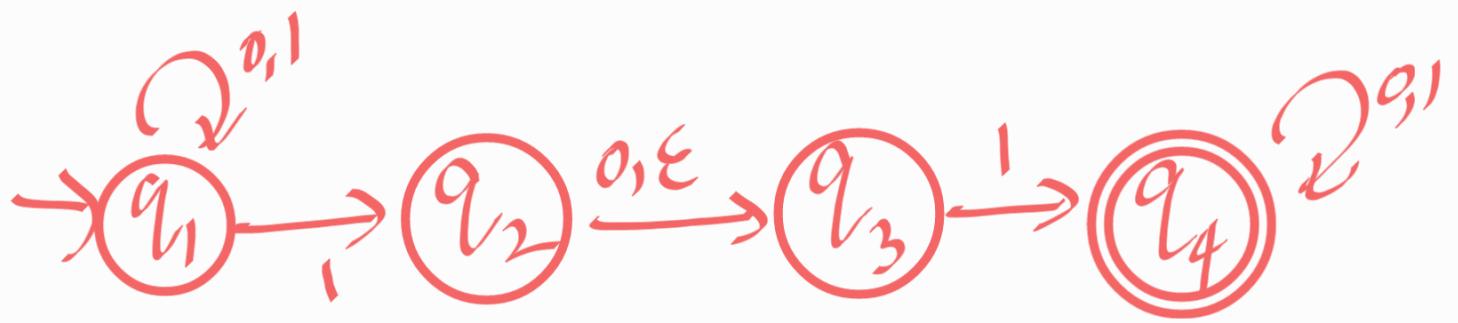
1. $r_0 = q_0$

2. $r_{i+1} \in \delta(r_i, w_{i+1})$, $\forall i \in [0, n-1]$

3. $r_n \in F$



TWO MACHINES ARE EQUIVALENT
if they accept the same language



1. $Q = \{q_1, q_2, q_3\}$

2. $\Sigma = \{0, 1\}$, $\Sigma_\epsilon = \{0, \epsilon\}$

3. δ is given as follows

$$\{\} = \emptyset$$

| | ϵ | 0 | 1 |
|-------|------------|---|---|
| q_1 | | | |
| q_2 | | | |
| q_3 | | | |
| q_4 | | | |

4. $q_1 \in Q$ is the start state.

5. $\{q_4\} \subseteq Q$ is the accepting state

