Decision Trees and Random Forests Data science Certificate

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May 2023

A Reminder on Supervised Learning

2 Decision Trees

Random Forests

May 2023

Outline

A Reminder on Supervised Learning

Decision Trees

Random Forests

A Reminder on Supervised Learning

- Observations: $(X_i)_{i=1,...n}$. Each X_i has d components.
- Outputs: $(Y_i)_{i=1,...n}$

3 Examples:

• Iris Dataset:

• MNIST:

House price prediction







Figure: Iris: setosa, versiocolor, virginica

One of the most widely used toy dataset in classification:

- 3 classes : ['setosa', 'versicolor', 'virginica']
- 50 points per class.
- 4 features: ['sepal length', 'sepal width', 'petal length', 'petal width']

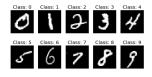


Figure:

Digit recognition from an image:

- 10 classes : $Y_i \in$
- 60k images, (50k train, 10k test), balanced
- 784 features.

House price Prediction

- ullet Output : house value $Y \in$
- 1500 examples
- 81 features: Construction year, Neighborhood, Surface, Floor, Balcony: both quantitative and qualitative, some ordinal variables.

Summary of those three datasets

Iris

MNIST

House price prediction

Number of examples n

Number of the features d

Type of the features

Space \mathcal{Y}

Task

Learning Pipeline

Training phase

Validation phase

Test phase

Deployment

Reminder on Linear and Logistic regression

Limits of Linear and logistic regression

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Decision Tree

Goals of Decision Trees

- Supervised Learning: solve the classification or regression task
- Provide some understanding: what on this example allows me to classify it? What are the important features?

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Goals of Decision Trees

- Supervised Learning: solve the classification or regression task
- Provide some understanding: what on this example allows me to classify it? What are the important features?

Two questions:

- How to train a decision tree? → training phase (learning algorithm)
- How to predict with a given decision tree? → inference phase

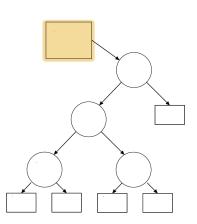
Inference Phase

• Root = observation = input

Nodes = tests

• Branches = possible outcomes

• Leaves = final decision = output



Training: how to build a tree.

Key question!

- What is a good tree?
- What do I need to choose?
- How to choose?

What do you think?

Building trees: CART



Building trees: CART



How to chose the best cut?

- e.g., Given a possible cut, measure the reduction of ńăimpurityăż:
 - lacktriangle in regression: mean-squared-error $\sum_{i\in C}(Y_i-ar{Y}_C)^2$
 - ▶ in classification: Gini's impurity.
- Find dimension and threshold with optimal impurity reduction.
- Iterate until stopping criterion is met.

Gini's impurity



Gini impurity measures how often a randomly chosen element from the set would be incorrectly labeled if it was randomly labeled according to the distribution of labels in the subset.

$$\mathsf{I}_G(p) = \sum_{i=1}^J p_i (1-p_i) = 1 - \sum_{i=1}^J {p_i}^2$$

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For two classes, related to the variance if classified as Bernoulli r.v..

Example: Iris Dataset







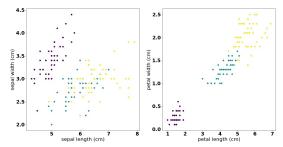
Figure: Iris: setosa, versiocolor, virginica

One of the most widely used toy dataset in classification:

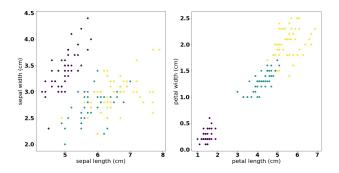
• 3 classes : ['setosa', 'versicolor', 'virginica']

50 points per class.

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Exercise: Guess Classification tree for Iris Dataset



In pratice: Scikit Learn

Universal Python library for Machine Learning:

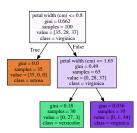
- Very easy to use
- Very well documented
- Open Source

https://scikit-learn.org/stable/modules/generated/sklearn.tree. DecisionTreeClassifier.html

Example: Iris Dataset

What do we need to specify?

Output:



```
from sklearn.datasets import load_iris
from sklearn.model selection import cross val score
from sklearn.tree import DecisionTreeClassifier, plot tree
from sklearn.model_selection import train_test_split
clf = DecisionTreeClassifier(max depth = 2,
                             random state=0)
iris = load_iris()
X_train, X_test, y_train, y_test = train_test_split(
    iris.data, iris.target, test size=0.33, random state=43)
cross val score(clf, iris,data, iris,target, cv=10)
clf.fit(X train.v train)
plot_tree(clf, feature_names = fn,
               class names=cn.
               filled = True)
plt.show()
```

Example:

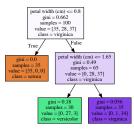
```
# Check
X_test[0,:], iris.target_names[y_test[0]]
Returns:
```

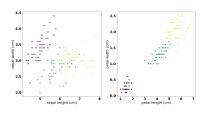
(array([4.8, 3.1, 1.6, 0.2]), 'setosa')

Code: https://colab.research.google.com/drive/ 1dXYIjacNAeASg154vIWyWjMQ1fgigSVA?usp=sharing#scrollTo= VeJHkJd7RsDw

Example: Iris Dataset

Output:





Example:

Check
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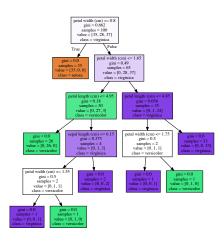
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What if I use a deeper tree? Or if I do not specify the depth in the model definition?

Deeper trees

Choose the Learning algorithm
clf = DecisionTreeClassifier(|random_state=0)



- When does the algorithm stop then ?
- What do you think about it ?

Stopping / Pruning

Trees that achieve perfect classification may suffer from over-fitting. (see example in the lab)

To avoid this problem, we can reduce the complexity of the trees:

- Stopping rules
 - ► Set a minimum number of samples inside each leaf.
 - Set a maximum depth.
- Pruning
 - ► Reduced error pruning.
 - Cost complexity pruning.

Pruning: example of Cost complexity pruning.

We create a sequence of Trees by changing one subtree at each step into a leaf, until we get only the root: the subtree is chosen to minimize the error made. 1 Then the test error is evaluated along the sequence, to choose the optimal pruning.



¹more details here

Cart: pros and cons

Pros:

- Simple to understand, interprete, visualize
- Implicitly perform features/variable selection
- can handle both categorical and numerical data
- little effort for data preparation
- Non linear relationships do not affect performance
- Can work with large number of observations.

Cons:

- Can create over-complex trees: overfitting
- Unstability: small variations of data can generate completely different trees
- Cannot guarantee global optimal tree
- Biased if some classes dominate

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Random Forests

To put it in simple words: ńărandom forests builds multiple decision trees and merges them together to get a more accurate and stable predictionsăż.

 \hookrightarrow key idea: create variable trees + aggregate them

How to create variability ?

Random Forests

To put it in simple words: ńărandom forests builds multiple decision trees and merges them together to get a more accurate and stable predictionsăż.

 \hookrightarrow key idea: create variable trees + aggregate them

How to create variability ?

- Instead of the most important features, search the best feature among a random subset (ntry).
- Work on subsets of data (bootstrap=True).
- More https://scikit-learn.org/stable/modules/generated/sklearn.ensemble.RandomForestRegressor.html

How to aggregate? How to interpret a Random Forest?

Aggregation

We using a voting or averaging process !

Feature importance

- how much tree nodes using a particular feature reduce impurity along the trees.
- suggests feature selection rule: drop out features with low importance to avoid overfitting.
- Attribute **feature_importance_** in RandomForestRegressor of Sklearn.

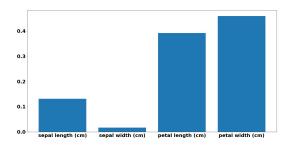


Figure: Feature importane output for a Random Forest Classifier in Python

Comparison with decision trees

Cons:

- Less interpretable
- Slower to run

Pros:

- Better in higher dimension
- More stable outputs
- Feature selection

Improving predictions - more arguments.

- n_estimators : number of trees in the forest
 - ► improves prediction / stability
 - ► slows down the algorithm
- max_features : maximum number of features considered to split a node
- min_sample_leaf: minimum number of samples that should remain in a leaf node.

RF pros and cons

RF Pros:

- works for classification and regression
- default hyperparameters often produce reasonable prediction -> easy to use.
- avoid overfitting if some good trees in the forest and easy feature selection -> high dimensional pb.
- 4 hard to beat in performance.
- Sonus : supports multiple outputs!

RF Cons:

- Fast to train but slow to provide new predictions -> ineffective for ńăreal-time predictionsăż.
- Good for prediction but bad for description.

What about Regression ?

Questions?

Boosting

Another import technique (very powerful!)

Main idea:

- Give more importance to difficult point iteratively
- Incrementally building an ensemble by training each new instance to emphasize the training instances previously mis-modeled.

Example: AdaBoost

See: https://scikit-learn.org/stable/modules/generated/sklearn.ensemble. AdaBoostClassifier.html

Bonus: Multiple Outputs

- Goal: predict several outputs simultaneously
- Solution:
 - ▶ each leaf contains a value for each output
 - ▶ to chose the splits, we use a (weighted) average of the impurity of each output.

Face completion with multi-output estimators



Bonus: complexity

Total complexity for one decision tree:

Worst case:

$$O(n^2d)$$

Balanced case:

O(nd)

Tips

- Decision trees tend to overfit: limit the depth or use min_samples_leaf (5 is a good initial pick)
- Visualize the tree with a small depth first
- Balance your dataset: trees tend to be biased towards dominating class.

Conclusion

- Trees are one of the simplest method (the most intuitive / human like)
- Random Forests give excellent results in many applications.

Lab:

- Example on a synthetic dataset of time series
- Application to inflation prediction in Brazil.