

Imperative to Functional Programming with Java 8

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Agenda

- Basic Vocabulary and Concepts
- Changing Your Thinking
- Going Deeper

Topics

- Immutability
- First-class functions
- Higher-order functions
- Currying
- Partial application
- Function pipelines
- Function composition
- Recursion
- Map, filter, and reduce
- Continuations
- Memoization
- Monads (computation expressions)

BASIC VOCABULARY & CONCEPTS

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Basic Vocabulary and Concepts

- Lambda calculus was introduced by mathematician **Alonzo Church** in the 1930s
- it makes functions first-class objects
- first-class functions were introduced in C# 3.0 in 2007 while in Java in 2014!

What is a λ-expression

- A λ (lambda) expression is an anonymous function that can be passed as argument or returned as the value of function calls.
- In the Java context they are similar to anonymous methods. Like a method it provides a list of formal parameters and a body—an expression or block—expressed in terms of those parameters
- They make it easier to distribute processing of collections over multiple threads
- Collection methods take a function and apply it to every element

λ -expressions

- $f(x) = y$, maps $x \rightarrow y$, e.g. $f(x) = 2*x$, maps $x \rightarrow 2*x$
- double dbl(double x) { return 2*x; }
 → $(\text{double } x) \rightarrow 2*x$

param type

body

```
FileFilter directoryFilter = new FileFilter() {  
    public boolean accept(File file) {  
        return file.isDirectory();  
    }  
};
```

```
FileFilter directoryFilter =  
    (File f) -> f.isDirectory();  
// f -> f.isDirectory();
```

Parameter
list

@FunctionalInterface

- Lambdas are lexically scoped, meaning that a lambda recognizes the immediate environment around its definition as the next outermost scope.

λ -expressions

Syntax:

(parameters) -> expression

or

(parameters) -> { statements; }

E.g.

(int x, int y) -> x + y

(x, y) -> x % y

() -> Math.pi

(String s) -> s.toUpperCase() or

String::toUpperCase

x -> 2 * x

c -> { int n = c.size(); c.clear(); return n; }

No return

← Method Reference

Functional interfaces

```
@FunctionalInterface
```

```
public interface MyInterface<T> {  
    MyInterface<T> apply();  
    default boolean isComplete() {  
        return false;  
    }  
    // ...  
}
```

A *functional interface* is an interface that has just one abstract method (and zero or more default or implemented methods), and thus represents a functional contract.

Functional interfaces

@FunctionalInterface

```
public interface UnaryOperator<T> {  
    T apply(T t);  
}
```

- describes the function: $f : T \rightarrow T$

java.util.function

- Consumer<T> $T \rightarrow void$
- Supplier<T> $() \rightarrow T$
- Predicate<T> $T \rightarrow boolean$
- Function<T, R> $T \rightarrow R$
- BiFunction<T, U, R> $(T, U) \rightarrow R$
- UnaryOperator<T> $T \rightarrow T$
- BinaryOperator<T> $(T, T) \rightarrow T$

java.util.function.Consumer<T>

```
interface Consumer<T> {  
    void accept(T t); // T -> void  
}
```

java.util.function.Supplier<T>

```
interface Supplier<T> {  
    T get(); // () -> T  
}
```

java.util.function.Predicat<T>

```
interface Predicate<T> {  
    boolean test(T t); // T -> boolean  
    default Predicate<T> and(Predicate<? super T> other);  
    default Predicate<T> or(Predicate<? super T> other);  
    default Predicate<T> negate();  
    static <T> Predicate<T> isEqual(Object other);  
}
```

java.util.function.Function<T, R>

```
interface Function<T, R> {  
    R apply(T t);           // T -> R  
    default <V> Function<V, R>  
        compose(Function<? super V, ?  
        extends T> before);  
    default <V> Function<T, V>  
        andThen(Function<? super R, ?  
        extends V> after);  
    static <T> Function<T, T>  
        identity();  
}
```

First-class
function

First-class functions

- Can be used wherever we use values, e.g.

```
Function<Person, String> byName  
= person -> person.getName();  
  
List<Person> people;  
  
people.stream().map(byName)  
.collect(toList());
```

First-class functions

- Can be used wherever we use values, BUT

```
List<Function<Integer,  
Integer>> functionList = new  
ArrayList<>() {  
(Integer x) -> doubl(x),  
(Integer x) -> square(x) };
```

Function closures

Function closure

- Functions that use variables defined outside of them, e.g.

```
public static Predicate<String>
startsWith(final String letter)
{
    return name ->
        name.startsWith(letter);
}
```

letter is defined in the method that contains the startsWith() function

and **letter** needs to be
“effectively final”

Higher-order Functions

- Functions that take or return other functions
 - pass functions to functions
 - create functions within functions
 - return functions from functions

Higher-order
function

```
public static int sum  
(Function<Integer, Integer> function,  
int a, int b) {  
    if (a > b) return 0;  
    else return function.apply(a) +  
sum(function, a + 1, b);  
}
```

Return functions

- Higher-order functions can also return functions:

```
Function<Integer, Integer>
```

```
evenOrOdd(int n) {
```



Return
function

```
    return (n % 2 == 0) ?
```

```
        x -> 2*x : x -> 3*x;
```

```
}
```

Method References

- When a λ -expression simply calls a single method e.g.

```
s -> s.toUpperCase()
```

the following syntax is preferred:

```
String::toUpperCase
```

- This syntax is called method reference

Method References

Category	Syntax	λ -expression	Example
Static	ClassName:: staticMethod	(args) -> ClassName. staticMethod(args)	String::valueOf
Bound Instance	ObjectName:: instMethod	(args) -> ObjectName.instMethod (args)	str::replace
Unbound Instance	ClassName:: instMethod	(arg0, rest) -> arg0.instMethod (rest)	String::concat
Constructor	ClassName::new	(args) -> new ClassName(args)	File:::new

Bound Method References

```
Map<String, String> map = new  
TreeMap<>();  
  
map.put("alpha", "A");  
map.put("bravo", "B");  
map.put("charlie", "C");  
  
String s = "alpha-bravo-charlie";  
map.replaceAll(s::replace);
```

Bound Method References (cont.)

```
// <T> the type of the first argument to the  
function
```

```
// <U> the type of the second argument to  
the function
```

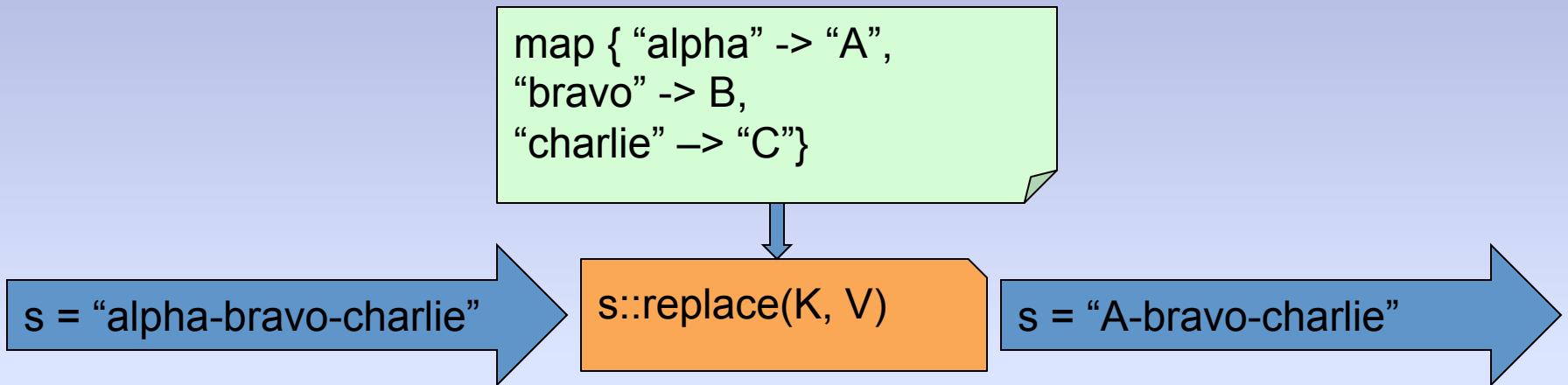
```
// <R> the type of the result of the  
function
```

```
BiFunction<T, U, R> { R apply(T t, U u); }
```

```
void replaceAll(BiFunction<? super K, ?  
super V, ? extends V> function) // (K,V)->V
```

```
String replace(CharSequence target,  
CharSequence replacement)
```

Bound Method References (cont.)



Bound Method References (cont.)

```
s.replace("alpha", "A"); // s ==  
"A-bravo-charlie"  
  
s.replace("bravo", "B"); // s ==  
"alpha-B-charlie"  
  
s.replace("charlie", "C"); // s ==  
"alpha-bravo-C"  
=====  
{alpha=A-bravo-charlie, bravo=alpha-  
B-charlie, charlie=alpha-bravo-C}
```

Unbound Method References

```
Map<String, String> map = new  
TreeMap<>();  
  
map.put("alpha", "A");  
map.put("bravo", "B");  
map.put("charlie", "C");  
  
map.replaceAll(String::concat);
```

No recipient aka closure

Unbound Method References (cont.)

```
String concat(String str) ; =>  
key.concat(value);  
"alpha".concat("A"); // "alphaA"  
"bravo".concat("B"); // "bravoB"  
"charlie".concat("C"); //  
"charlieC"  
=====  
{alpha=alphaA, bravo=bravoB,  
charlie=charlieC}
```

Immutability

- Imperative programming is based on mutability – state change => side effects
- Functional programming is based on immutability – no state change; a new object is created each time
- = sign indicates equation *not* assignment

```
var = 1
```

```
var = var + 1 // Error!!!
```

Currying

- “...the technique of transforming a function that takes multiple arguments (or a tuple of arguments) in such a way that it can be called as a chain of functions, each with a single argument (partial application)”.

- $\text{def } f(\text{args}_1) \dots (\text{args}_{n-1}) (\text{args}_n) = E$
 $\Leftrightarrow \text{def } f = (\text{args}_1 \Rightarrow (\text{args}_2 \Rightarrow \dots (\text{args}_n \Rightarrow E) \dots))$

```
def sum(f: Int => Int)(a: Int, b: Int): Int = if (a > b) 0 else f(a) + sum(f)(a + 1, b)
```

Partial Application

- “...partial application (or partial function application) refers to the process of fixing a number of arguments to a function, producing another function of smaller arity.”
“Arity” means the number of arguments that a function accepts.
- it is a process of binding values to parameters resulting in a function with fewer parameters; it depends on currying
- currying is a process that replaces a single multi-parameter function with a nested set or chain of single-parameter functions

Currying in Java

- Java provides:
 - `Function<T, R>` $T \rightarrow R$
 - `BiFunction<T, U, R>` $(T, U) \rightarrow R$
- But how can we calculate a function that takes >2 arguments?
 - $f(x, y, z) = x * y + z$
 - There is no `TriFunction<T, U, W, R>` $(T, U, W) \rightarrow R$
 - $(A, B, C) \rightarrow D \rightarrow A \rightarrow B \rightarrow C \rightarrow D$
 - $f(2, y, z) = g(y, z) = 2 * y + z \Rightarrow$
 - $g(3, z) = 2 * 3 + z$

Currying in Java

```
List<Integer> list =  
        Arrays.asList(1, 2, 3, 4, 5);  
private Stream<Integer>  
    calculate(Stream<Integer> stream,  
Integer a, Integer b) {  
    return stream.map(  
        ((Function<Integer,>  
            Function<Integer,>  
            Function<Integer, Integer>>>)  
        x -> y -> z -> x + y * z).  
                apply(a).apply(b));  
} // a => x, b => y, stream arg => z  
// [5, 8, 11, 14, 17]  
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```

Currying in Java

```
interface TriIntegerFunction extends  
Function<Integer, Function<Integer,  
Function<Integer, Integer>>> { }
```

```
private Stream<Integer>  
calculate(Stream<Integer> stream,  
Integer a, Integer b) {  
    TriIntegerFunction sline =  
        x -> y -> z -> x + y * z;  
    return  
        stream.map(sline.apply(a).apply(b));  
}
```

Automatic currying in Java

```
public class Functions {  
    public static <A, B, C> Function<A, Function<B,  
C>> curry(final BiFunction<A, B, C> f) {  
        return (A a) -> (B b) -> f.apply(a, b);  
    }  
  
    public static <A, B, C> BiFunction<A, B, C>  
        uncurry(Function<A, Function<B, C>> f) {  
        return (A a, B b) -> f.apply(a).apply(b);  
    }  
}  
Function<Integer, Function<Integer, Integer>> c1 =  
    curry((y, z) -> y * z);  
Function<Integer, Function<Integer, Integer>> c2 =  
    curry((t, x) -> t + x);  
return stream.map(c1.apply(b)).map(c2.apply(a));  
// a => x, b => y, stream arg => z, t  
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```

CHANGE YOUR THINKING

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Expression-based programming

- stop thinking in terms of statement-based programming (imperative)
- start thinking in terms of expression-based programming (functional)
- A statement mutates the current value; does not return anything
- An expression always returns a result or a new value

```
point.moveTo(x1, y1);
```

statement

```
newpoint = point.move(x1, y1);
```

expression

Eager vs lazy evaluation

- In **eager evaluation**, an expression is evaluated as soon as it is bound to a variable.
- The alternative to eager evaluation is **lazy evaluation**, where expressions are only evaluated when evaluating a dependent expression, i.e. until its value is needed
- Java is an “eager” language
- `List<Integer> list = Arrays.asList(1, 2, 3, 4, 5);` is eagerly (strictly) evaluated
- Java 8 streams allow for lazy evaluation

Lazy constructions in Java

- `&&` and `||`
- the ternary operator `? :`
- `if... then...else`
- the `for` loop
- the `while` loop
- the Java 8 Stream
- the Java 8 Optional

Lazy evaluated methods in Java

- Java methods evaluate their arguments eagerly, i.e. before the method is called

```
public static boolean andMethod (boolean  
arg1, boolean arg2) {  
    return arg1 && arg2;  
}
```

- To lazily evaluate its arguments:

```
public static boolean andMethod  
(Supplier<Boolean> arg1,  
Supplier<Boolean> arg2) {  
    return arg1.get() && arg2.get();  
}
```

Start thinking immutable

- Reduce encapsulation by creating associations explicitly as maps
 - Think like relational database architecture, i.e. in terms of tables and relations
 - Identify core types i.e. fields
 - Associate with other types via foreign keys
 - normalize
- Create smaller functions that do just one thing; then combine them together using partial application or function pipelining or composition

Example

```
+ User
└ fields
- final roles: List<String>
- username: String
- emailAddress: String
- passwordHash: byte[]
└ constructors
└ methods
+ addRole(roleName: String): void
+ removeRole(roleName: String): void
+ setPassword(newPassword: String, hashAlgo: MessageDigest): void
+ getUsername(): String
+ setUsername(username: String): void
+ getEmailAddress(): String
+ setEmailAddress(emailAddress: String): void
+ getPasswordHash(): String
```



```
+ UserRoles
└ fields
- final user: User
- final roles: List<UserRole>
└ constructors
+ UserRoles(user: User)
└ methods
+ getUser(): User
+ addRole(roleName: UserRole): void
+ removeRole(roleName: UserRole): void
+ getRoles(): Stream<UserRole>
```



```
+ User
└ fields
- username: String
- emailAddress: String
- passwordHash: byte[]
└ constructors
└ methods
+ setPassword(newPassword: String, hashAlgo: MessageDigest): void
+ getUsername(): String
+ setUsername(username: String): void
+ getEmailAddress(): String
+ setEmailAddress(emailAddress: String): void
+ getPasswordHash(): String
```

```
+ UserRole
└ fields
- final roleName: String
└ constructors
+ UserRole(roleName: String)
└ methods
+ getRoleName(): String
```

Streams

- Find sum of odd numbers:

```
int[] numbers = {1, 2, 3, 4, 5};  
int sumOfOddNumbers =  
    IntStream.of(numbers).  
        filter(x -> x % 2 == 1).sum();
```

Streams

```
/* Create an output list that contains  
 * only the odd-length words, converted  
 * to upper case.  
 */  
  
List<String> result = input.stream()  
    .filter(s -> s.length() % 2 != 0)  
    .map(String::toUpperCase)  
    .collect(Collectors.toList());
```

Filter-map-reduce

Input: **Stream<T>**

method	λ	function	output	eager/lazy
map	$T \rightarrow R$	Function<T, R>	Stream<R>	lazy
flatMap	$T \rightarrow Stream<R>$	Function<T, Stream<R>>	Stream<R>	lazy
filter	$T \rightarrow boolean$	Predicate<T>	Stream<T>	lazy
reduce	$(T, T) \rightarrow T$	BinaryOperator<T>	Optional<T>	eager
collect	$R \rightarrow R$	Supplier<R>	R	eager
forEach	$T \rightarrow void$	Consumer<T>	void	eager

- Streams are evaluated when we apply to them some specific operations called ***terminal (eager)***. This may be done only once. Once a terminal operation is applied to a stream, the stream is no longer usable.

Infinite streams - Lazyness

```
Streams.iterate(seed,  
UnaryOperator)  
.limit(count)  
.collect(Collectors.toList());
```

E.g.

```
Function<Integer, Stream<Integer>>  
f = x -> Stream.iterate(1,  
y -> y + 1).limit(x);
```

Infinite stream example

```
public class Primes {  
    public static boolean isPrime(final int number) {  
        return number > 1 && IntStream.rangeClosed(2,  
(int) Math.sqrt(number)).noneMatch(divisor -> number  
% divisor == 0);  
    }  
  
    private static int nextPrime(final int number) {  
        return isPrime(number + 1) ? number + 1 :  
nextPrime(number + 1);  
    }  
  
    public static List<Integer> primes(final int count)  
    {  
        return Stream.iterate(2, Primes::nextPrime)  
            .limit(count)  
            .collect(Collectors.<Integer>toList());  
    }  
}
```

Terminal Operations

- forEach
- forEachOrdered
- toArray
- reduce
- collect
- min, max
- count
- anyMatch
- allMatch
- noneMatch
- findFirst
- findAny
- iterator
- spliterator

Intermediate Operations

- filter
- map
- mapTo...*
- flatMap
- flatMapTo...*
- Distinct
- sorted
- peek
- limit
- skip
- sequential
- parallel
- unordered
- onClose

* (Int, Long or Double)
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Parallel streams

- Things to consider:
 - size of data
 - do we really want to run the lambda expressions concurrently?
 - the code should be able to run independently without causing any side effects or race conditions
 - the correctness of the solution should not depend on the order of execution of the lambda expressions that are scheduled to run concurrently

Function pipelining

```
List<String> result =  
input.stream()  
.filter(s -> s.length() % 2 != 0)  
.map(String::toUpperCase)  
.collect(Collectors.toList());
```

- stream | filter | map | collect

Function composition

- The ability to compose functions into a chain of operations
- The lack of mutability reduces the chance of errors and makes it easier to parallelize the code
- We can alter a few links in the chain and easily alter the behavior along the way

Recap

- Favor immutability
- Reduce side-effects
- Prefer expressions over statements
- Expressions can be composed
- Design with higher-order functions

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Continuations

- “[A] continuation represents the remainder of a computation given a point in the computation.”
- the idea is that a function is provided with another function that is invoked with the result of the first function’s computation
- Java 8 provides `CompletableFuture<T>` and `CompletableFuture<T>` (a stage of a possibly asynchronous computation, that performs an action or computes a value when another `CompletionStage` completes)
- `CompletableFuture<T>` is functional, monadic, asynchronous and event-driven

Continuations in Java 8

```
public void processOrder(String custId) {  
    return CompletableFuture  
        .supplyAsync(() -> getFromDB(custId))  
        .thenApplyAsync(c -> getOrder(c.getCustId()))  
        .thenAccept(System.out::println);  
}  
  
private Customer getFromDB(String custID) {  
    // TODO get customer from database  
}  
private Order getOrder(String custID) {  
    // TODO get order ...  
}
```

Continuation Frameworks

- Javaflow ([Play](#) framework uses Javaflow)
- RIFE
- JauVM implements tail call / continuation
- Scala 2.8
- Cocoon
- Rhino
- Jetty retry request.
- Coroutines
- Jconts
- jyield
- Kilim
- ATCT

Start thinking immutable - recursion

- Use recursion to avoid mutability
- Example of **recursion**:

```
public int fact(int n) {  
    return n == 0 ? 1 : n * fact(n-1);  
}
```

No need for an
accumulator

- Biggest problem with recursion is *stack overflow*.
- If a function calls itself as its last action, the function's stack frame can be reused. This is called **tail recursion**. This resolves stack overflow.
- If the last action of a function consists of calling a function (which may be the same), one stack frame would be sufficient for both functions. Such calls are called **tail-calls**.

Start thinking immutable - recursion

- Convert loops to tail recursion
- Tail recursion example:

```
public static int foo(int a, int b) {  
    int x = ...; int y = ...;  
    return foo(x, y);  
}
```

Start thinking immutable - recursion

- Example: calculate the sum of:

```
public static int sum(IntUnaryOperator  
func, int a, int b) {  
    if (a > b) return 0;  
    else return function.apply(a) +  
            sum(function, a + 1, b);  
}
```

This is not tail recursive; why!!!

Fibonacci numbers

- Standard fibonacci function is **not** tail-recursive:

$$f(n) = f(n - 1) + f(n - 2)$$

- Why?

Tail recursive fibonacci function

```
public static BigInteger fibTailRec(int x) {  
    return fibTailRecHelper(BigInteger.ONE,  
                           BigInteger.ZERO, BigInteger.valueOf(x));  
}  
  
public static BigInteger  
fibTailRecHelper(BigInteger acc1, BigInteger acc2,  
BigInteger x) {  
    if (x.equals(BigInteger.ZERO)) {  
        return BigInteger.ONE;  
    } else if (x.equals(BigInteger.ONE)) {  
        return acc1.add(acc2);  
    } else {  
        return fibTailRecHelper(acc2,  
                               acc1.add(acc2), x.subtract(BigInteger.ONE));  
    }  
}  
fibTailRec(9813); // Java 1.5=> stack overflow 62
```



Tail recursive factorial function

```
public static BigInteger factTailRec(int number) {  
    return factTailRecHelper(BigInteger.ONE,  
        BigInteger.valueOf(number));  
}  
  
public static BigInteger factTailRecHelper(BigInteger  
factorial, BigInteger number) {  
    if (number.equals(BigInteger.ZERO)) {  
        return BigInteger.ONE;  
    } else if (number.equals(BigInteger.ONE)) {  
        return factorial.multiply(number);  
    } else {  
        return factTailRecHelper(  
            factorial.multiply(number), number.subtract(BigInteger.ONE));  
    }  
}  
  
factTailRec(11799); // 11800 => stack overflow
```



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Tail Recursion Optimisation (TCO)

- We need a way for the last operation to be a (delayed/lazy) call to itself, and no further computation to carry out on the result upon return.

```
@FunctionalInterface
```

```
public interface RecCall<T> {
```

```
    RecCall<T> next();
```

```
    default boolean isDone() { return false; }
```

```
    default T getValue() { throw new
```

```
IllegalStateException(); }
```

```
    default T apply() {
```

```
        return Stream.iterate(this, RecCall::next)
                     .filter(RecCall::isDone)
                     .findFirst()
                     .get()
                     .getValue();
    }
```

```
// ...
```

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Tail Recursion Optimisation (TCO)

```
static <T> RecCall<T> call(final RecCall<T> nextCall) {  
    return nextCall;  
}  
  
static <T> RecCall<T> done(final T value) {  
    return new RecCall<T>() {  
        @Override  
        public boolean isDone() {  
            return true;  
        }  
        @Override  
        public T getValue() {  
            return value;  
        }  
        @Override  
        public RecCall<T> next() {  
            throw new IllegalStateException();  
        }  
    };  
}
```

TCO fibonacci function

```
public static BigInteger fibTailRec(int x) {  
    return fibTailRecHelper(BigInteger.ONE,  
                           BigInteger.ZERO, BigInteger.valueOf(x).apply());  
}
```

```
public static BigInteger fibTailRecHelper(BigInteger acc1,  
                                         BigInteger acc2, BigInteger x) {  
    if (x.equals(BigInteger.ZERO)) {  
        return Recall.done(BigInteger.ONE);  
    } else if (x.equals(BigInteger.ONE)) {  
        return Recall.done(acc1.add(acc2));  
    } else {  
        return Recall.call(() -> fibTailRecHelper(acc2,  
                                                   acc1.add(acc2), x.subtract(BigInteger.ONE)));  
    }  
}
```

Tail recursive lazily executed

TCO factorial function

```
public static BigInteger factTailRec(int number) {  
    return factTailRecHelper(BigInteger.ONE,  
        BigInteger.valueOf(number).apply());  
}  
  
public static RecCall<BigInteger>  
factTailRecHelper(BigInteger factorial, BigInteger number) {  
    if (number.equals(BigInteger.ZERO)) {  
        return Recall.done(factTailRec);  
    } else if (number.equals(BigInteger.ONE)) {  
        return Recall.done(factorial.multiply(number));  
    } else {  
        return Recall.call(() -> factTailRecHelper(  
            factorial.multiply(number),  
            number.subtract(BigInteger.ONE)));  
    }  
}  
factTailRec(500_000);
```



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Tuples

- ordered collections of values of different types of fixed size, e.g.
`(person, "John", 42, 1.78)`
- Java supports tuples:

- Implicitly, e.g.:

```
int sum2(int a, int b) {  
    return a+b; }  
  
(int a, int b) -> a + b;
```

Single argument
function!!!!

but we cannot use them for a function's
return values

Tuples

- Explicitly, e.g.

```
/** A Tuple: double -> (int, double) for integer and  
decimal parts */  
public class Tuple {  
    public final int integerPart;  
    public final double decimalPart;  
  
    public Tuple(int integerPart, double decimalPart) {  
        super();  
        this.integerPart = integerPart;  
        this.decimalPart = decimalPart;  
    }  
  
    @Override  
    public String toString() {  
        return String.format("(%, %s)", integerPart,  
decimalPart);  
    }  
}
```

Tuples

```
private static Tuple  
split(double x) {  
    int integerPart = (int) x;  
    return new Tuple(integerPart,  
x - integerPart);  
}  
System.out.println(split(3.14));  
→ (3, 0.1400000000000012)
```

Fibonacci function with tuples

- 1, 1, 2, 3, 5, 8, 13, 21, ...
- (1, 1), (1, 2), (2, 3), (3, 5), (5, 8),
(8, 13), (13, 21), ...

```
Tuple2<BigInteger, BigInteger> seed = new  
Tuple2<>(BigInteger.ONE, BigInteger.ONE);  
UnaryOperator<Tuple2<BigInteger,  
BigInteger>> fbc = x -> new  
Tuple2<>(x.elem2, x.elem1.add(x.elem2));
```

```
BigInteger fibCoRecursive=  
Stream.iterate(seed, fbc)  
.map(x -> x.elem1)  
.limit(1_000_000).reduce(  
a, b) -> b).get();
```

Memoization

- Memoization means caching the results of functions in order to speed them up when they are called several times with the same argument.
- The first call implies computing and storing the result in memory before returning it.
- Subsequent calls with the same parameter imply only fetching (lookup) the previously stored value and returning it.
- Memoizing is about maintaining state between function calls.
- A memoized function is a function which behavior is dependent upon the current state.

Memoization Example

```
public class Cache {  
    private static final Map<Integer,  
    Integer> cache = new  
    ConcurrentHashMap<>();  
  
    public static Integer  
    square(Integer x) { return  
    cache.computeIfAbsent(x, y -> y * y);  
    }  
}  
  
int sq3 = Cache.square(3);
```

Memoization Example (cont.)

```
public class Cache {  
    private static final Map<Integer,  
    Integer> cache = new  
    ConcurrentHashMap<>();  
  
    public static Function<Integer,  
    Integer> square = x ->  
    cache.computeIfAbsent(x, y -> y * y);  
}  
}  
  
int sq3 = Cache.square.apply(3);
```

We have to repeat this modification for all functions.

Memoizer

```
Function<Integer, Integer> f = x -> x  
* x;
```

```
Function<Integer, Integer> g =  
Memoizer.memoize(f); // reference to  
the function to be memoized
```

```
int sq3 = g.apply(3);
```

- All values returned by function `g` will be calculated through the original function `f` the first time, and returned from the cache for all subsequent accesses.

Memoizer (cont.)

```
public class Memoizer {  
    private Memoizer() {}  
  
    public static <T, U> Function<T, U>  
memoize(final Function<T, U> function) {  
    final Map<T, U> cache = new  
ConcurrentHashMap<>();  
    return input ->  
cache.computeIfAbsent(input,  
function::apply);  
}  
}
```

What about functions with >1 arguments?

- i.e. functions of *tuples* that may also return *tuples*
- More difficult to store multiple values to a Map
- For 2 arguments, f can be a
`BiFunction<T, U, R>:`

```
BiFunction<Integer, Integer,  
Integer> h = (x, y) -> x*x + y*y;
```

- Or use *currying* for ≥ 2 arguments:

```
Function<Integer, Function<Integer,  
Integer>> hc = x -> y -> x*x + y*y;
```

Memoizer with a parameter

```
public class Memoizer2 {  
    private Memoizer2() {}  
  
    public static <T, R> R memoize(final  
        BiFunction<Function<T, R>, T, R> function, final T  
        input) {  
        final Map<T, R> cache = new  
        ConcurrentHashMap<>();  
        Function<T, R> memoized = new Function<T, R>() {  
            @Override  
            public R apply(final T input) {  
                return cache.computeIfAbsent(input, key ->  
                    function.apply(this, key));  
            }  
        };  
        return memoized.apply(input);  
    }  
}
```

Memoizer with currying

```
Function<Integer, Function<Integer, Integer>> f2m =  
    Memoizer.memoize(x ->  
        Memoizer.memoize(y -> x*x + y*y));  
-----  
f2m.apply(2).apply(3);  
-----  
Function<Integer, Function<Integer,  
Function<Integer, Integer>>> f3 =  
    x -> y -> z -> x*x + y*y + z*z;  
Function<Integer, Function<Integer,  
Function<Integer, Integer>>> f3m =  
    Memoizer.memoize(x -> Memoizer.memoize(y ->  
        Memoizer.memoize(z -> x*x + y*y + z*z)));  
-----  
f3m.apply(2).apply(3).apply(-1);
```

Memoizer with tuples (cont.)

```
private static final  
Function<Tuple3<Integer, Integer,  
Integer>, Integer> ft = t ->  
t.elem1*t.elem1 + t.elem2*t.elem2 +  
t.elem3*t.elem3;
```

```
private static final  
Function<Tuple3<Integer, Integer,  
Integer>, Integer> ftm =  
Memoizer.memoize(ft);  
  
-----  
ftm.apply(new Tuple3<>(2, 3, 4));
```

Memoizer with tuples (cont.)

```
public class Tuple3<T, U, V> {  
    public final T elem1;  
    public final U elem2;  
    public final V elem3;  
    public Tuple3(T t, U u, V v) {  
        elem1 = Objects.requireNonNull(t);  
        elem2 = Objects.requireNonNull(u);  
        elem3 = Objects.requireNonNull(v);  
    }  
    @Override  
    public boolean equals(Object o) {  
        if (!(o instanceof Tuple3)) return false;  
        else {  
            Tuple3 that = (Tuple3) o;  
            return elem1.equals(that.elem1) &&  
                elem2.equals(that.elem2) && elem3.equals(that.elem3);  
        }  
    }  
    @Override  
    public int hashCode() {  
        return elem1.hashCode() + elem2.hashCode() + elem3.hashCode();  
    }  
}
```

Monads (Computation expressions)

- A **monad** is a structure that represents computations defined as sequences of steps
- Monads can be chained together in order to build pipelines that process data in steps
- One of the uses for a monad is retain state without resorting to mutable variables
- Monads are a great way to create *workflows* where you have to manage data, control logic, and state (side effects)
- Continuations are a key aspect of computational expressions

Simple Monad example

```
int a = 5, b = 6;  
int c = a + b;
```

```
int pipeFunc(int x, IntUnaryOperator  
f) {  
    return f.applyAsInt(x);  
}  
int result = pipeFunc(5,  
    a -> pipeFunc(6,  
        b -> pipeFunc(a+b, c -> c)) );
```

Monads

- Formally, a monad consists of a *type constructor* M and two operations, *bind* and *return* (where *return* is often also called *unit*):
- The *return* operation takes a value from a plain type and puts it into a monadic container using the constructor, creating a monadic value.
- The *bind* operation takes as its arguments a monadic value and a function from a plain type to a monadic value, and returns a new monadic value.

Monads

- A monad is a set of three things:
 - A parameterized type $M<T>$
 - A *unit* or *return* function $T \rightarrow M<T>$
 - A *bind* operation
$$M<T> \text{ bind } T \rightarrow M<U> = M<U>$$
- Java supports monads, e.g.: `Optional<T>`
 - Parameterized type: `Optional<T>`
 - `unit`: `Optional.of()`
 - `bind`: `Optional.flatMap()`

java.util.Optional<T>

E.g.

```
// unit
```

```
Optional<Integer> maybeInteger =  
Optional.of(1);
```

```
// bind
```

```
Optional<Integer> maybePlusOne =  
maybeInteger.flatMap(  
    n -> Optional.of(n + 1));
```

Other monads in Java 8

- Streams
- CompletableFuture<T>
- Better-Java-Monads by Jason Goodwin
 - Try
 - Futures
 - $\text{List} < \text{CompletableFuture} < T > \rightarrow \text{CompletableFuture} < \text{List} < T >$

Monads

- Maybe or Try
- I/O
- Identity
- State
- Continuation
- ...

State Monad in Java 8

- a state monad allows to attach state information of any type to a calculation
- a state monad maintains state within a specific *workflow*.
- a state monad is basically a function from a state to a pair (state,content).
- Parameterized type: $\langle T, S \rangle$:
 - unit: $t \rightarrow (t, s)$
 - bind: $x \rightarrow (y, s)$
- See ref[9].

Conclusion

OO style

- Abstraction
- Encapsulation
- Polymorphism
- Inheritance
- Statements
- imperative

Functional style

- Higher order functions
- Function composition
- Immutability
- Expressions
- declarative

Conclusion

- Java 8 is not a fully functional programming language
- Allows you to combine imperative with functional style
- Thinking functionally can help you become a better coder
- Think of immutability
- Think of (small) functions (lambdas)
- Think of Streams

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