

# Expressing Contract Monitors as Patterns of Communication

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## Abstract

We present a new approach to contract semantics which expresses myriad monitoring strategies using a small core of foundational communication primitives. This approach allows multiple existing contract monitoring approaches, ranging from Findler and Felleisen’s original model of higher-order contracts to semi-eager, parallel, or asynchronous monitors, to be expressed in a single language built on well-understood constructs. We prove that this approach accurately simulates the original semantics of higher-order contracts. A straightforward implementation in Racket demonstrates the practicality of our approach which not only enriches existing Racket monitoring strategies, but also support a new style of monitoring in which collections of contracts collaborate to establish a global invariant.

## 1. Introduction

Since they were introduced by Meyer [25], behavioral contracts have become an integral part of modern programming practice, where they are used to express predicates as pre- and post-conditions on procedures. In a first-order setting, run-time enforcement is well-studied [25, 27, 28]: the pre-condition predicate is applied to the input; the function is run if the precondition holds; and the post-condition is checked on the result.

However, when the setting changes from first-order to higher-order functions, effectful operations, large data structures, or even lazy languages, contract checking becomes more complex. With higher-order functions, contracts must be delayed [16]. With large data structures, programmers wish to avoid checking more than needed. With lazy languages, contracts can force excess evaluation. Fortunately, all of these issues have been tackled, with researchers proposing solid theoretical foundations [4, 15, 16], language integration accommodating existing semantics [6, 11, 19, 22], and new forms of contracts [1, 11, 18, 20, 32]. Contracts are now available in a broad range of production systems.

Even for the specific task of monitoring functions and primitive values, there are a broad number of approaches to contract monitoring presented in the literature, from eager contracts à la Findler and Felleisen [16] to future contracts as presented by Dimoulas et al. [10], and even broader shapes such as the temporal approach presented by Disney et al. [13]. There are, in fact, so many approaches to contract monitoring that Degen et al. [7, 8] and Dimoulas and Felleisen [9] have presented surveys of different approaches, discussing their similarities and differences.

Despite appearances, this cornucopia of monitoring strategies share a common core. Going back to first principles, checking that a given code fragment satisfies a contract clearly requires executing some “assertion” code, and the execution of this assertion code is conceptually distinct from the execution of the original code fragment. There is no fundamental reason why either of these modes of execution should be given supremacy. In particular, taking the view that the contract execution is somewhat subservient to the main

thread of execution only restricts and complicates the language; only in the simplest cases does the interaction of the two executions follow a routine master/slave or call/return pattern. In many cases, it is conceptually clearer to view the two executions as proceeding independently, synchronizing at specific points. Prior implementations and semantic foundations for contracts have merged these non-trivial patterns of interaction into the single, fixed evaluation semantics for the host language. This not only restricts the power of contracts but obscures the powerful idea that contract checking is just a separate process of execution that interacts with the underlying program in a variety of communication patterns.

We tackle this problem head-on, giving a unifying account of multiple contract monitoring semantics while exposing their underlying communication patterns. The communication-centric account clarifies the precise differences between monitoring semantics and how they impact the overall flow of program execution.

**Outline.** This paper presents a new model for interpreting and expressing contract monitoring semantics as models of communication that facilitate coexistence and semantic interoperability in the presence of contracts. This paper proceeds as follows: we outline our approach through examples of contract monitoring (§2). Next we present a calculus with CML-style concurrency operations, demonstrating how these operations, combined with exceptions and delaying mechanisms, may recover varied methods of contract monitoring, including eager, semi-eager, future, and asynchronous monitoring [7, 8, 10, 16, 18] (§3–4). Then we prove that our model accurately simulates the original semantics of Findler and Felleisen [16] (§6). Next we present a thread-based implementation of our framework in Racket and use this system to create

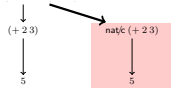
a structural contract sketched by Findler et al. [18], but with improved algorithmic bounds and performance results (§7). Finally we outline how to embed a number of additional monitoring approaches into our semantic model, including lazy, temporal, and statistical monitors (§8), discuss related work (§9), and conclude.

## 2. Background & Examples

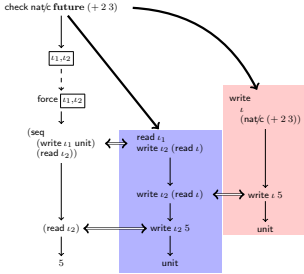
In the conventional study of software contracts, a language designer extends a core calculus with monitoring facilities that adhere to a specific *monitoring strategy*, describing how monitors may interact with the underlying program evaluator and the precise semantics of the monitor itself. This semantic decision is a permanent fixture of the language, often lacking facilities to extend or alter the strategy.

In this section we start to address this problem, abstracting away from this “one-strategy” approach in favor of a many-strategy user language. This language abstracts over how contracts may interact with the underlying evaluator, parameterizing contract monitors with monitoring strategies which indicate precisely how and when a given contract may interact with the user program. This moves the decision of how contracts should be monitored into the programmer’s hands, allowing users to naturally describe contract behavior on a program-by-program basis.

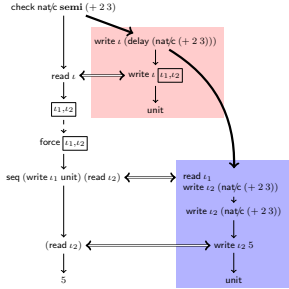
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*Future Monitoring*



*Semi-Eager Monitoring*



**Figure 1.** Communication patterns for eager, semi-eager, future, and asynchronous contract monitoring.

**Eager Predicate Contracts.** Our first example is a predicate contract that verifies its input is a natural number:

$$\text{nat}/c \triangleq \text{pred}/c (\lambda x. x \geq 0)$$

This contract can now be used to construct a monitored subexpression inside a larger expression:

$$1 + \text{check nat}/c \text{ eager } 5$$

When the evaluation of this expression encounters the check parameterized by the **eager** strategy, the user computation is suspended and the monitor assumes control of the evaluation. Eager monitors completely verify their contract at assertion time: if the input value is valid, the monitor terminates with that value result, and if the input does not satisfy the contract, the monitor terminates at assertion time with an exception<sup>1</sup>. In either case, the user

evaluation is resumed with the monitor's result.

This interaction corresponds to *Eager Monitoring* in Figure 1: the check form constructs a monitoring expression (colored red) to verify the contract, pausing the user evaluation until it is complete. The bold line indicates evaluator construction, the double-arrow indicates evaluator synchronization, and the normal arrows indicate evaluation.

***Eager Pair Contracts.*** Eager monitors produce contract violation even if the program does not rely on the value for its final result, and thus unused values may produce contract violations. To demonstrate this quality, consider a second contract combinator over pairs, written *pair/c*. Structural contracts require subcomponents that describe how the substructures should be monitored, and thus pair contracts accept a subcontract and strategy for each of the first and

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<sup>1</sup> We omit blame in this section for simplicity.

second elements of the pair:

$$\text{nat/pcE} \quad \triangleq \quad \text{pair/c} \quad \begin{array}{l} \text{nat/c eager} \\ \text{nat/c eager} \end{array}$$

This pair contract can itself be eagerly enforced, which will eagerly enforce *nat/c* on each of the elements of the pair, regardless of their usage in the program:

$$\begin{array}{ll} \text{fst (check nat/pcE eager (5, 6))} & \Rightarrow 5 \\ \text{fst (check nat/pcE eager (5, -1))} & \Rightarrow \text{exn} \end{array}$$

**The Cost of Eager Contracts.** The strict enforcement strategy of eager contracts is not always a perfect-fit solution. For example, an eagerly-monitored contract that verifies its input is a prime number may require immense computational effort while the user evaluation is suspended:

check prime/c **eager**  $(2 * 37^{63} + 567)$

While such enforcement may be ideal (or even necessary) in many situations, this approach may range from computationally intensive to impossible for large or infinite structures (such as streams). If this is the only monitoring strategy available, programmers will find it too expensive to validate many rich properties.

**Asynchronous Contracts.** Instead of suspending the user evaluator during contract verification, other approaches allow the user evaluator to proceed while the contract is concurrently enforced [10, 13]. In the simplest variant of the idea, the monitor is concurrently enforced, halting the computation with an error if the contract is violation, but the user process is otherwise unimpeded.

This approach corresponds to *Asynchronous Monitoring* in Figure 1: the check form constructs a monitored expression (colored

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**red**) to verify the contract, continuing the user evaluation in parallel. If the monitor verifies the contract, it silently ends its execution. If an error is detected, however, the entire computation might halt with the error. For example, we may asynchronously enforce nat/c in a number of expressions by changing **eager** to **async**:

check nat/c <b>async</b> 5	⇒	5
(λx. x + 5) (check nat/c <b>async</b> -1)	⇒	4 or exn

We use “or” in the second example because asynchronous monitoring induces a third option for contract monitoring: the monitor may not complete before the user evaluator. Asynchronous monitoring only guarantees “best-effort checking”: if a contract is too large or complex to verify during the program’s execution, and the program otherwise terminates correctly, then the remaining verification work is discarded. As a result, asynchronous contract enforcement is often “too weak”, precisely because we the two evaluators are completely disjoint. It may be preferable to facilitate a synchronization between the two evaluators at the user program’s request.

***Future Contracts.*** In their original presentation [10], *future contracts* track a master (user) process and a slave (monitoring) process, synchronizing during I/O events to enforce pending contracts. We take a more traditional approach to future monitors, providing the initiating process with a *promise*—a reference to the monitor result à la computational futures [3, 21]. When the initiating evaluator forces the promise, the expression retrieves the contract result, yielding either the original value or an error. This style of contract monitoring allows the user program to control *when* the program will wait for a contract result by forcing the promise.

check nat/c <b>future</b> 5	⇒	ref
force (check nat/c <b>future</b> -1)	⇒	exn
force (check nat/c <b>future</b> 5)	⇒	5
force (check nat/c <b>future</b> -1)	⇒	exn

This series of interactions correspond to *Future Monitoring* in Figure 1: the check form constructs a monitored expression (colored red) to verify the contract and a future-fulfillment mechanism (as another process, colored blue) before returning a reference to the future-fulfillment mechanism to the user process. This allows the user evaluator to continue computation until the value is required



while a concurrent process enforces the contract, minimizing the time required in the user evaluator for contract enforcement. To further demonstrate this behavior, consider a revised contract over pairs that checks its sub-contracts using **future**:

$$\text{nat/pcF} \triangleq \text{pair/c nat/c future nat/c future}$$

Now we must explicitly force the subcomponents of the pair:

$$\begin{aligned} \text{fst (force (check nat/pcF future (5, -1)))} &\Rightarrow \text{ref} \\ \text{force (fst (force (check nat/pcF future (5, -1))))} &\Rightarrow 5 \\ \text{force (snd (force (check nat/pcF future (5, -1))))} &\Rightarrow \text{exn} \\ \text{force (fst (check nat/pcF eager (5, -1)))} &\Rightarrow 5 \\ \text{force (check nat/pcE future (5, -1))} &\Rightarrow \text{exn} \end{aligned}$$

The last two examples are of particular interest: each pair contract requires three strategies for each of its first sub-component, second sub-component, and the overall pair. If we use **future** for all three, we receive a promise that, when forced, returns a pair of further promises. Our framework allows the free intermixing of monitoring strategies, however, so we can construct a pair contract that is enforced at assertion time while delaying each of the subcomponent contract, or that is eagerly enforces its subcomponents when forced (as in the last example, which uses **nat/pcE**).

***Semi-Eager Contracts.*** The presentation of future contracts presumes that the contract monitor is too computationally complex to perform while suspending the user evaluator. Delaying the actual contract evaluation, however, is often sufficient: if a structural contract may be checked in layers and pieces as the program traverses the structure, piecewise demand-time contract enforcement

is often sufficient. This suggests a fourth model of contract monitoring which delays the monitor enforcement until the user evaluator forces the expression. Findler and Felleisen first used so-called *semi-eager* evaluation to model contracts across module boundaries, enforcing contracts only when invoked by the client module [16]. Hinze et al. [22] and Degen et al. [7] model this approach by encoding the Findler-Felleisen semantics directly in Haskell, and Chitil [5] builds on this encoding, introducing a number of combinators that exploit this delaying behavior.

Future monitoring closely mirrors semi-eager monitoring: while the former immediately performs contract enforcement but delays evaluator communication, the latter delays contract enforcement and immediately performs communication afterwards. As a result, the two strategies behave identically from the user’s perspective in the absence of effectful operations and computational time:

$$\begin{array}{ll}
\text{check nat/c semi } 5 & \Rightarrow \text{ ref} \\
\text{force (check nat/c semi -1)} & \Rightarrow \text{ exn} \\
(\lambda x. 1 + \text{force } x) (\text{check nat/c semi } 5) & \Rightarrow 6 \\
(\lambda x. 1 + \text{force } x) (\text{check nat/c semi -1}) & \Rightarrow \text{ exn}
\end{array}$$

While the usage looks identical with respect to expected outputs, the underlying semantic differences expose an axis of variation for contract monitors: *where* the delaying mechanism occurs in the monitoring process. This difference is apparent in the pattern presented as *Semi-Eager Monitoring* in Figure 1: we move the delay mechanism creation from the user evaluator to the monitoring evaluator, and thus expose a natural variance in monitoring semantics.

**Data Structural Contracts.** The contracts we have presented so far omit a large part of the design space for contracts: neither predicates nor pairs readily lend themselves to recursive contracts. Binary-search trees, conversely, provide an interesting venue for

exploring structural contracts in the large, presenting opportunities for contract enforcement that contrast well with the asymptotic and algorithmic obligations of the underlying structure. For example, we might construct a contract to ensure that a given tree is indeed organized in sorted order. We can do this with a dependent tree contract that takes four subcontracts and strategies for each of the leaf, left subtree, node value, and right subtree:

```
fix bst/E lo hi.
  tree/dc (pred/c null?) eager
    ( $\lambda n. \text{bst}/E \text{ lo } n$ ) eager
    ( $\text{pred}/c (\lambda x. \text{lo} \leq x \text{ and } x \leq \text{hi})$ ) eager
    ( $\lambda n. \text{bst}/E \text{ n hi}$ ) eager
```

This contract ensures that each leaf of the tree is a null value and each value that occurs in the tree is within the correct numeric bounds. Under eager monitoring this contract must traverse the entire tree to enforce this constraint, requiring  $O(n)$  time, whereas a insertion algorithm would require  $O(\log n)$  time in a balanced tree. This style of monitoring is often preferable to ensure program safety, but such traversals become problematic as the structure increases in size. We can forgo such a strong guarantee, however, and opt for semi-eager contract enforcement:

```
fix bst/S lo hi.
  tree/dc (pred/c null?) eager
    ( $\lambda n. \text{bst}/S \text{ lo } n$ ) semi
    ( $\text{pred}/c (\lambda x. \text{lo} \leq x \text{ and } x \leq \text{hi})$ ) eager
    ( $\lambda n. \text{bst}/S \text{ n hi}$ ) semi
```

This contract will enforce the invariant on exactly the nodes we visit during the program, which will recover  $O(\log n)$  complexity for insertion into a balanced tree. Even so, we have tied the user evaluator to this contract, relying on the user program's evaluation to enforce the contract. Departing from such a coupling requires a

full separation of the monitoring evaluator from the user evaluator.

Future monitors provides two approaches to such separation. In the first, we construct such a monitor by replacing the two uses of **semi** with **future** in the definition of  $bst/S$ , yielding  $bst/F$ . This third implementation of the binary-search tree invariant yields a unique situation: the future monitors will traverse the entire

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structure of the tree, but the user evaluator only waits on the results that are relevant to the completion of the program. Thus we may complete the user evaluator's computation without enforcing the invariant over the entire tree.

Alternatively, we might enforce  $bst/E$  concurrently under the **future** strategy, demanding the promise at the end of the entire user program. This will allow us to continue with a computation, verifying the contract concurrently and retrieving the final result at the last possible moment. This last alternative for future monitoring may also be constructed with asynchronous monitoring: the monitor will traverse the entire tree and enforce the contract, reporting an error only if and when it is detected.

**Function Contracts.** Monitoring a function contract verifies contracts on a function's input and output values. Like a pair contract, a function contract consists of two sub-contracts and their associated strategies: the first contract, or *pre-condition*, is enforced on function inputs, and the second contract, or *post-condition*, is asserted on the result of the function application. These contracts are constructed with the function contract combinator  $\text{func}/c$ :

$$\begin{array}{lll} \text{fnat}/cE & \triangleq & \text{func}/c \text{ nat}/c \text{ eager nat}/c \text{ eager} \\ \text{fnat}/cS & \triangleq & \text{func}/c \text{ nat}/c \text{ semi nat}/c \text{ semi} \end{array}$$

Function contracts deviate from pair contracts in one important way: while it was possible to write eager pair contracts that might produce inefficiency or diverge, the equivalent approach for function contracts is untenable. For any infinite set of valid inputs or outputs, such as the natural numbers, it is generally impossible to traverse the entire domain and codomain of a procedure to ensure that each adheres to the pre- and post-condition.

To avoid this problem, functional contract enforcement postpones the pre- and post-condition contracts until the function's precise input is available. This delay manifests as a secondary  $\lambda$ -abstraction around the monitored procedure, and thus while a function contract may be monitored under any strategy, that overall strategy only determines *when* the wrapped procedure is constructed [4]. (The literature suggests an alternative method for checking function contracts through statistical verification [12, 14], which we discuss in Sec. 8.) We define two monitored procedures using the contracts above:

$$\begin{aligned} \text{sub1/mE} &\triangleq \text{check fnat/cE } \mathbf{eager} (\lambda x. x - 1) \\ \text{sub1/mS} &\triangleq \text{check fnat/cS } \mathbf{eager} (\lambda x. \text{force } x - 1) \end{aligned}$$

We use **eager** in both cases to avoid delaying the construction of the wrapped procedure. Applications proceed as follows:

$$\begin{array}{llll} \text{sub1/mE } 5 &\Rightarrow 4 & (\text{ef}_1) & \text{sub1/mS } 5 &\Rightarrow \text{ref} & (\text{sf}_1) \\ \text{sub1/mE } -1 &\Rightarrow \text{exn} & (\text{ef}_2) & \text{sub1/mS } -1 &\Rightarrow \text{exn} & (\text{sf}_2) \\ \text{sub1/mE } 0 &\Rightarrow \text{exn} & (\text{ef}_3) & \text{sub1/mS } 0 &\Rightarrow \text{ref} & (\text{sf}_3) \\ & & & \text{force (sub1/mS } 0) &\Rightarrow \text{exn} & (\text{sf}_4) \end{array}$$

The first three examples are as expected: no contract is violated in the first, the pre-condition is violated in the second, and the post-condition is violated in the third. The semi-eager examples are more intricate: example (sf<sub>1</sub>) behaves as expected, returning a reference that will yield 4 when forced, example (sf<sub>2</sub>) produces an

exception when the value monitored by the pre-condition is forced in the body of the function, and examples (sf<sub>3</sub>) and (sf<sub>4</sub>) indicate that the post-condition result must be demanded before usage.

***The Many-Strategy Approach.*** Unfortunately, none of these approaches provide a single “silver bullet” solution to contract monitoring. While Degen et al. [7] conclude that “faithfulness is better than laziness”, we assert that each strategy is an ideal fit in a number of situations, and so fixing the contract evaluator with a single strategy is a poor fit for programmer flexibility.

Furthermore, there is evidence that some useful contracts cannot be expressed with any of the strategies or combinators we have introduced so far [18]. For example, consider checking the fullness

of a binary search tree, which ensures that a tree of height  $n$  has  $2^n$  nodes. This property is easy to verify by traversing the tree, but it poses subtle issues for contract monitoring strategies. We would like to check as much of the tree as possible without forcing additional evaluation, but the *contract* requires traversal and thus we require some mechanism to back-propagate values to waiting contracts as the tree is explored.

As we will see in Sec. 7.2, asynchronous and semi-eager strategies combined with communication allow us to write this back-propagation mechanism, arranging a series of callbacks to verify the tree is full. This contract requires careful construction, but it will allow us to signal an error after we have traversed any unbalanced part of the subtree to its leaves.

The contracts we have examined thus far are all built from the same primitive effects: exceptions, concurrent processes with communication, and delaying and forcing mechanisms. In the next sections we will outline a core calculus with these operations and demonstrate how to construct general, generic, and strategy-agnostic monitoring mechanisms from them.

### 3. An Concurrent Calculus for Contracts

Having demonstrated the core ideas of this new approach to contract monitoring, we turn our attention toward formalizing these features in  $\lambda_{CC}$ , the calculus of concurrent contracts. This calculus combines several standard features, including pure  $\lambda$ -expressions, exceptions, delay and force primitives, and a process model inspired by Concurrent ML [24, 29, 30]. The pure  $\lambda$ -calculus portion of the calculus includes several common forms (the unshaded portion of Figure 3), including if, case, pairs, and recursive bindings. Each of the additional language layers provides a separate level of abstraction in  $\lambda_{CC}$  aimed at a distinct class of clients:

- The  $\lambda$ -calculus with check, raise, strategies  $s$ , blame  $B$ , and force (but not delay), appearing as “white” and red in Figure 3. This language fragment provides a framework for user programs that wish to enforce contracts and interact with delayed contract values. Contract writers also use this calculus to construct contracts and contract combinators that naturally adhere to the standard notions of value propagation for contracts. All of the contract combinators used in Sec. 2 and defined in Figure 6 are written in this language. Furthermore, we track blame following Dimoulas et al. [11]: each blame object contains three

strings, indicating the contract, positive, and negative parties.

- The  $\lambda$ -calculus with the above features and synchronous process facilities `chan`, `read`, and `write`, including the white, red, and purple portions of Figure 3. These primitives allow contract writers to interact with the contract runtime to craft additional patterns of communication between monitoring evaluators to recover new—and sometimes improved—contract evaluation patterns. These three forms are colored purple to indicate their dual nature as contract writing facilities and underlying semantic specification. The only style of contract where we have found this necessary was described in the previous section, using  $\lambda_{CC}$ 's built-in communication facilities to construct contracts in a recursive, dependent structural contract. We show how to express this style of contract in our Racket implementation in Sec. 7.
- The full calculus, including everything in Figure 3 (the white, red, purple, and blue portions), adds the additional features to complete the semantic model of contract monitoring in terms of processes. These effects along with answers  $a$ , channel names  $\iota$ , the special *delay reference* form (Sec. 3.2), process pools  $\mathcal{P}$ , process tags  $\mathcal{T}$ , channel maps  $\mathcal{K}$ , evaluation contexts  $\mathcal{E}$ , and process contexts  $\mathcal{C}$ , provide a basis for the implementation of

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$$\begin{array}{lcl}
 e & ::= & x \mid v \mid e e \mid \text{fix } f x. e \mid \text{if } e \text{ then } e \text{ else } e \mid (e, e) \\
 & & \mid \text{unop } e \mid \text{binop } e e \mid \text{case } (e; \text{inl } x \triangleright e; \text{inr } x \triangleright e) \\
 & & \mid \text{injl } e \mid \text{inj r } e \\
 & & \mid \text{check } e \text{ s e } B \mid \text{force } e \mid \text{raise } e
 \end{array}$$



		read $e$   chan $e$   write $e e$
		spawn $\mathcal{T} e$   delay $e$   catch $e e$
$v$	$:=$	$\lambda x. e$   true   false   inl $v$   inr $v$   $(v, v)$
		unit   $n$   str   $B$
$B$	$:=$	$(str, str, str)$
$s$	$:=$	eager   semi   future   async   ...
		$\iota$   dref $_{\iota_1, \iota_2}$
$\mathcal{E}$	$:=$	$\square$   $\mathcal{E} e$   $v \mathcal{E}$   if $\mathcal{E}$ then $e$ else $e$   $(\mathcal{E}, e)$   $(v, \mathcal{E})$
		unop $\mathcal{E}$   binop $\mathcal{E} e$   binop $v \mathcal{E}$
		case $(\mathcal{E}; \text{inl } x \triangleright e; \text{inr } x \triangleright e)$   injl $\mathcal{E}$   injr $\mathcal{E}$
		check $\square s e B$   force $\mathcal{E}$   raise $\mathcal{E}$
		write $\mathcal{E} e$   write $v \mathcal{E}$   read $\mathcal{E}$
		spawn $\mathcal{T} \mathcal{E}$   catch $\mathcal{E} e$   catch $v \mathcal{E}$
$a$	$:=$	$v$   raise $v$
$\mathcal{P}$	$:=$	$\mathcal{P} + \mathcal{P}$   $\langle n, \mathcal{T} \mid e \rangle$   done $a$
$\mathcal{T}$	$:=$	U   M   A
$\mathcal{K}$	$:=$	$\{\iota_0, \dots, \iota_n\}$
$\mathcal{C}$	$:=$	$\square$   $\langle n, \mathcal{T} \mid \mathcal{E} \rangle$   $\mathcal{C} + \mathcal{P}$

**Figure 2.** Syntax of  $\lambda_{\text{CC}}$ .

check, force, and delay. Furthermore, this calculus serves as a semantic specification for the runtime evaluation of contract monitors, giving an account of the underlying operations of contracts, and it is not intended for use in user programs.

### 3.1 Core Features

We have already introduced the core user language (colored white and red) with canonical  $\lambda$ -calculus forms<sup>2</sup> through a series of ex-

amples, and thus we now focus on the remaining pieces of  $\lambda_{CC}$ : exceptions, processes, check, delay, and force. Exceptions are standard, and each of check, force, and delay are implemented in terms of processes. Therefore we briefly explain exceptions and focus on the concurrent aspects of  $\lambda_{CC}$ , postponing delay and force until Sec. 3.2. The check form is described in Sec. 4, where we provide the semantics for each of **eager**, **async**, **future**, and **semi** monitoring in terms of the underlying process calculus and delay. In the remainder of the paper we use  $\rightarrow$  for a single *local* evaluation rule and  $\mapsto$  for a top-level evaluation step.

**Exceptions** We include the standard exception mechanisms **raise** and **catch** to report and handle contract violations. The last three rules in Figure 3 illustrate their behavior. The **catch**  $h\ e$  form installs a handler  $h$  during the evaluation of  $e$ . If that evaluation terminates with a value  $v$ , the handler is discarded and the entire form evaluates to  $v$ . Otherwise the evaluation of  $e$  may raise an exception value  $v'$ , in which case the intermediate contexts are discarded until either the exception reaches the top level or encounters the closest handler. In the latter case, the handler  $h$  is invoked on  $v'$ .

**Processes and Process Calculus** Runtime configurations in  $\lambda_{CC}$ , written  $\mathcal{K}; \mathcal{P}$ , consist of a collection of channels  $\mathcal{K}$  that scope over concurrent processes  $\mathcal{P}$ . The set of channels  $\mathcal{K}$  grows over the course of evaluation as new channels are constructed for communication with **chan**. The syntax distinguishes three kinds of processes:  $\langle n, \mathcal{T} \mid e \rangle$  represents an individual process made up of a unique process numerical identifier  $n$ , a process tag  $\mathcal{T}$ , explained below and a  $\lambda$ -expression  $e$ ; **done**  $a$ , a halt state which indicates

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<sup>2</sup>The semantic relations for these forms are standard and thus omitted.

*Process Evaluation Rules*

$$\frac{e \mapsto e'}{\mathcal{K}; \mathcal{P} + \langle n, \mathcal{T} \mid e \rangle \Rightarrow \mathcal{K}; \mathcal{P} + \langle n, \mathcal{T} \mid e' \rangle} \quad (\text{STEP})$$

$$\frac{n' \notin \mathcal{C}[\text{spawn } \mathcal{T}' e]}{\mathcal{K}; \mathcal{C}[\text{spawn } \mathcal{T}' e] \Rightarrow \mathcal{K}; \mathcal{C}[\text{unit}] + \langle n', \mathcal{T}' \mid e \rangle} \quad (\text{SPAWN})$$

$$\frac{\iota \notin \mathcal{K}}{\mathcal{K}; \mathcal{C}[\text{chan } v] \Rightarrow \mathcal{K} \cup \{\iota\}; \mathcal{C}[v \iota]} \quad (\text{CHANNEL})$$

$$\frac{\iota \in \mathcal{K}}{\mathcal{K}; \mathcal{C}[\text{read } \iota] + \mathcal{C}'[\text{write } \iota v] \Rightarrow \mathcal{K}; \mathcal{C}[v] + \mathcal{C}'[\text{unit}]} \quad (\text{SYNC})$$

$$\frac{}{\mathcal{K}; \langle n, \mathbf{U} \mid a \rangle + \mathcal{P}_A \Rightarrow \mathcal{K}; \text{done } a} \quad (\text{TERM1})$$

$$\frac{}{\mathcal{K}; \langle n, \mathbf{M} \mid v \rangle + \mathcal{P} \Rightarrow \mathcal{K}; \mathcal{P}} \quad (\text{TERM2})$$

$$\frac{}{\mathcal{K}; \langle n, \mathbf{A} \mid v \rangle + \mathcal{P} \Rightarrow \mathcal{K}; \mathcal{P}} \quad (\text{TERM3})$$

$$\frac{}{\mathcal{K}; \langle n, \mathbf{A} \mid \text{raise } v \rangle + \mathcal{P} \Rightarrow \mathcal{K}; \text{done } (\text{raise } v)} \quad (\text{TERM4})$$

$$\frac{\text{catch } h \square \notin \mathcal{E}}{\mathcal{E}[\text{raise } v'] \rightarrow \text{raise } v'} \quad \frac{}{\text{catch } h v \rightarrow v} \quad \frac{}{\text{catch } h (\text{raise } v') \rightarrow h v'}$$


---

**Figure 3.** Small-step semantics for the effectful forms of  $\lambda_{\text{CC}}$ .

that the computation has terminated with an answer  $a$ ; and  $\mathcal{P} + \mathcal{P}$  is the concurrent computation of processes (or collections of processes). Process contexts  $\mathcal{C}$  decompose process configurations.

The remaining semantics in Figure 3 formalizes the behavior of processes. We use  $\Rightarrow$  to rewrite process configurations, where  $\Rightarrow$  is non-deterministic in the result depending on scheduling choices. The rules implicitly identify configurations that differ in the names of bound variables or in the order or grouping of processes.

The first rule, STEP, describes internal steps taken during process evaluation: if the process body can take a top-level step  $e \mapsto e'$ , then the process may take an internal step under the  $\Rightarrow$  relation. The second rule, SPAWN, describes process creation. We require two arguments to spawn a process: a process tag  $\mathcal{T}$ , signifying the nature of the process, and an expression  $e$  to evaluate in the new process. In a well-formed configuration, there is exactly one process tagged U which represents the “main” computation. Configurations may include any number of monitoring processes, tagged M, as well as asynchronous processes, tagged A. Spawn-

ing a new process allocates a unique process identification number, adds the process to the configuration, the original process receives unit, and evaluation proceeds.

The third rule, CHANNEL, creates new channels for synchronous process communication. This form takes a procedure as input and creates a new channel  $\iota$ , adds it to  $\mathcal{K}$ , and provides the new channel as input to the procedure. The fourth rule, SYNC, describes synchronous communication: if the program configuration includes a process ready to write a value across a channel and

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$$\begin{array}{c}
\text{catchM} \triangleq \lambda x f. \text{case } (x; \text{inl } y \triangleright f y; \text{inr } y \triangleright \text{raise } y) \quad \text{rep/D} \triangleq \text{fix rep/D } i_1 i_2 x. \text{seq } (\text{read } i_1) (\text{write } i_2 x) (\text{rep/D } i_1 i_2 x) \\
\\
\frac{v \neq \text{dref}_{i_1, i_2} \quad \text{force } v \rightarrow v}{\text{force } (\text{dref}_{i_1, i_2}) \rightarrow \text{seq } (\text{write } i_1 \text{ unit}) (\text{catchM } (\text{read } i_2) \text{ id})} \\
\\
\text{delay } e \rightarrow \text{chan } (\lambda i_1 i_2. \text{seq } (\text{spawn } A (\text{seq } (\text{read } i_1) (\text{let } x = \text{catch injr } (\text{injl } e) \text{ in seq } (\text{write } i_2 x) (\text{rep/D } i_1 i_2 x)))) \text{dref}_{i_1, i_2})
\end{array}$$

Figure 4. Small-step semantics for a delaying mechanism in  $\lambda_{\text{cc}}$ .

another ready read from the same channel, these two processes can simultaneously perform the communication step.

The termination behavior of a process is dictated by its *tag*, U, M, or A, described by TERM1–TERM4 in Figure 3. If a process configuration consists solely of a finished user process and asynchronous processes, the configuration may halt non-deterministically with the result of the user process. If any of the asynchronous processes has detected a contract violation, the configuration may also non-deterministically terminate with that contract violation. If a monitoring process halts with an error due to a malformed expression, the entire configuration becomes stuck.

## 3.2 Delay and Force

Some contract monitoring strategies (e.g., semi-eager and future) require fine-grained interaction with the user evaluator in the call-by-value calculus to delay the evaluation of code fragments. One way to express such interactions would be to require user expressions to provide synchronization hooks for the monitoring thread. Taken to its logical extreme, this approach would reduce to manually implementing the call-by-value, call-by-name, and call-by-need  $\lambda$ -calculi [31]. These encodings would allow any pattern of interaction between the user evaluator and the monitor, but they would come at a heavy price: *every*  $\lambda$ -expression would be expressed as a process and each application would encode the desired behavior as a pattern of communication between the procedure and argument processes. The pure  $\lambda$ -calculus sublanguage would evaporate, yielding a process-based calculus.

This extreme approach is incompatible with our goals of explaining, integrating, and implementing existing contract systems into existing languages with our approach. Even a less-extreme approach would require intrusive changes to add synchronous behavior in the user program. Instead we add delay and force facilities to provide “enough” control over the critical portions of evaluation without requiring substantial modification to user programs. Monitoring strategies can use delay to suspend the evaluation of  $\lambda$ -expressions, and user programs must explicitly use force to evaluate these suspended expressions. As we illustrate in Sec. 7, wherein we introduce our Racket implementation and use it to write several contracts, these occurrences of force are not overly intrusive. Furthermore, force may be removed if the language has sufficient support to automatically force values during runtime [21].

The need for force seems to imply greater inconvenience for

programmers, compared to existing contract systems which allow the result of contract monitoring to be used directly. However, this seeming convenience relies in most cases (such as contract systems for Racket or Haskell) on only allowing strategies which fit precisely with the underlying language evaluation semantics. Instead, we allow programmers to choose between strategies without requiring changes to the underlying evaluation semantics. Only when there is a mismatch between the monitoring strategy and the evaluation, as in a call-by-value language with **semi** monitoring, is manual control over evaluation with force needed. Dimoulas et al. [10] present a call-by-value calculus with future monitoring *without* delay and force, but only ever execute

6

flat predicate contracts in parallel. Furthermore, they manually add synchronization—equivalent to force—at effect points. They suggest that this could be implicitly performed by the runtime system, just as implicit forcing could be added.

While integral to the inner workings of **semi** and **future**, delay and force are straightforward to define with the communication and process facilities in  $\lambda_{CC}$  (Figure 4). To evaluate delay  $e$ , we construct a pair of new channels  $\iota_1$  and  $\iota_2$  and a new process that performs a blocking read on  $\iota_1$ . The process that invoked delay receives a *delay reference*, a tagged pair which contains  $\iota_1$  and  $\iota_2$  and represents the delayed expression.

The force operation follows: when force is invoked on a delay reference, the forcing process writes unit to  $\iota_1$  and immediately reads from  $\iota_2$ . The secondary process reads from  $\iota_1$  as a trig-

gering mechanism before evaluating  $e$ —catching any errors—and writing the resulting value to  $\iota_2$ . This process finally replicates itself via  $\text{rep}/D$ , ensuring further forces of the same delay reference produces the same value. The forcing process receives an injected value and invokes  $\text{catchM}$ , defined in Figure 4, on it. The  $\text{catchM}$  definition works as follows: if the forcing process receives a value, we unwrap the value and return it; if the forcing process receives an exception, we re-raise the exception at the forcing site. This recovers the standard approach to encoding delay and force.

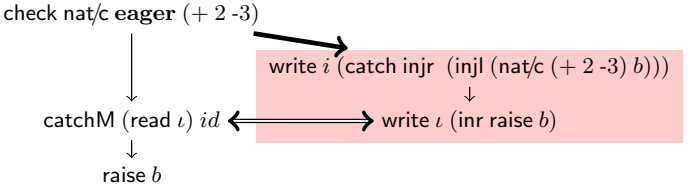
Finally, applying force to any value which is not a delay-reference returns the value unchanged. This operation is a matter of programmer convenience: any program that may interact with a monitored value can freely force the necessary expressions and thus the same procedure will work under eager or delayed monitoring.

## 4. Contract Monitoring with Processes

We now construct the monitoring behaviors characterized in Sec. 2, presenting the underlying semantics for  $\text{check}$  to describe the many-strategy monitoring system for  $\lambda_{\text{CC}}$ . This semantic model, presented in Figure 5, explicitly encodes each monitoring strategy as a pattern of process communication, illustrating their subtle and precise differences.

**Eager Monitors.** The eager approach to contract monitoring closely matches the CPCF calculus described by Dimoulas et al. [11], Findler and Felleisen [16], where every contract is checked at assertion time. These checks are modeled as immediate interactions between processes, as presented in Figure 1. Consider a further diagram where the monitor produces an error:





This behavior is encoded via the process effect operators in  $\lambda_{CC}$  in the eager definition of check (see Figure 5). To demonstrate this interaction, consider the running example of enforcing the contract

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```

check c eager  e b → chan (λi. seq (spawn M (write i (catch injr (injl (c e b)))) (catchM (read i) id))
check c future e b → chan (λi. seq (spawn M (write i (catch injr (injl (c e b)))) (delay (catchM (read i) id))))
check c semi   e b → chan (λi. seq (spawn M (write i (catch injr (injl (delay (c e b)))) (catchM (read i) id))))
check c async  e b → seq (spawn A (c e b))

```

Figure 5. Small-step semantics for the contract monitoring mechanism in  $\lambda_{CC}$ .

nat/c<sup>3</sup>:

$$\begin{aligned}
& \langle 0, U \mid \text{check nat/c eager } v \ b \rangle \\
& \Rightarrow^* \langle 0, U \mid \text{catchM (read } \iota) \ id \rangle \\
& \quad + \langle 1, M \mid \text{write } \iota \ (\text{catch injr (injl (nat/c } v \ b))) \rangle
\end{aligned}$$

When  $v := 5$ , the computation proceeds as:

$$\begin{aligned}
& \Rightarrow^* \langle 0, U \mid \text{catchM (read } \iota) \ id \rangle + \langle 1, M \mid \text{write } \iota \ (\text{inl } 5) \rangle \\
& \Rightarrow^* \langle 0, U \mid \text{catchM (inl } 5) \ id \rangle \\
& \Rightarrow^* \langle 0, U \mid 5 \rangle
\end{aligned}$$

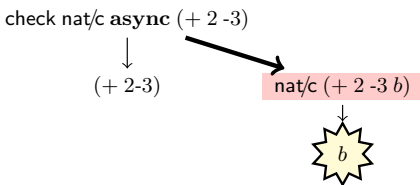
When  $v := -1$ , the computation proceeds as:

$$\begin{aligned}
& \Rightarrow^* \langle 0, U \mid \text{catchM (read } \iota) \ id \rangle + \langle 1, M \mid \text{write } \iota \ (\text{inr } b) \rangle \\
& \Rightarrow^* \langle 0, U \mid \text{catchM (inr } b) \ id \rangle
\end{aligned}$$

$\Rightarrow^* \langle 0, U \mid \text{raise } b \rangle$

Here `check` immediately constructs the communication channel  $\iota$  and the monitoring process. The initiating process performs a blocking read across  $\iota$  while the monitoring process checks the contract with the monitored value. The result of the contract is handled by injecting values to the left and exceptions to the right before writing them to the initiating process. Finally, the initiating evaluator processes the result with `catchM`, continuing with the value or re-throwing the exception.

**Asynchronous Monitors.** The asynchronous approach to contract monitoring consists of stand-alone monitors that perform “best-effort” checking: if the monitor is not finished when the user program is complete, then the entire program produces the user-program answer and discards the incomplete monitor, as presented in Figure 1. Consider a further diagram where the monitor produces an error:



With explicit processes, this monitoring strategy is straightforward, as implemented in Figure 5. When invoked, `check` spawns an asynchronous process to perform the check; there is no additional synchronization except for possible termination of the configuration in the event of an error. When the monitor is complete, the asynchronous process terminates with either a value  $v$  or an exception `raise v`. This lack of synchronization can produce non-deterministic

results for asynchronous monitoring:

$$\begin{aligned}
& \emptyset; \langle 0, U \mid id \text{ (check nat/c \texttt{async} -1 b)} \rangle \\
\Rightarrow^* & \{ \iota \}; \langle 0, U \mid id -1 \rangle + \langle 1, A \mid (\text{nat/c} -1 b) \rangle \\
\Rightarrow^* & \{ \iota \}; \langle 0, U \mid -1 \rangle + \langle 1, A \mid (\text{nat/c} -1 b) \rangle \\
\Rightarrow^* & \{ \iota \}; \text{done} -1 \\
\\
\Rightarrow^* & \{ \iota \}; \langle 0, U \mid id -1 \rangle + \langle 1, A \mid (\text{nat/c} -1 b) \rangle \\
\Rightarrow^* & \{ \iota \}; \langle 0, U \mid \dots \rangle + \langle 1, A \mid \text{raise } b \rangle \\
\Rightarrow^* & \{ \iota \}; \langle 1, A \mid \text{raise } b \rangle \\
\Rightarrow^* & \{ \iota \}; \text{done (raise } b)
\end{aligned}$$

Even with this potential non-determinism, asynchronous contracts can provide a reasonable alternative to completely verifying contracts over large structures.

---

<sup>3</sup> We elide  $\mathcal{K}$  in our examples for simplicity of presentation.

**Future Monitors.** Originally posed by Dimoulas et al. [10], future contracts check contracts concurrently during program execution, synchronizing only when necessary for the program to continue. Dimoulas et al. [10] perform this synchronization at all program side effects; we instead synchronize when the value is demanded. The implementation of future monitoring follows eager monitoring, but delays the receipt of the resulting value until it is needed (Figure 5). The consumer of the contracted value can force the future at any time, at which point the blocking nature of read will halt the current process until contract checking is complete. Returning to our example, evaluation proceeds as follows:

1.  $\langle 0, U \mid \text{force (check nat/c \texttt{future} 5 b)} \rangle$

$$\begin{aligned}
2. & \Rightarrow^* \langle 0, U \mid \text{force} (\text{delay} (\text{catchM} (\text{read } \iota) id)) \rangle + \\
& \quad \langle 1, M \mid \text{write } \iota (\text{catch injr} (\text{injl} (\text{nat/c } 5 b))) \rangle \\
3. & \Rightarrow^* \langle 0, U \mid \text{force dref}_{\iota_2, \iota_3} \rangle + \\
& \quad \langle 1, M \mid \text{write } \iota (\text{catch injr} (\text{injl } 5)) \rangle + \langle 2, A \mid \dots \rangle \\
4. & \Rightarrow^* \langle 0, U \mid \text{catchM} (\text{read } \iota_3) id \rangle + \\
& \quad \langle 1, M \mid \text{write } \iota (\text{inl } 5) \rangle + \langle 2, A \mid \dots \text{read } \iota \dots \rangle \\
5. & \Rightarrow^* \langle 0, U \mid \text{catchM} (\text{read } \iota_3) id \rangle + \langle 2, A \mid \dots \text{write } \iota_3 (\text{inl } 5) \dots \rangle \\
6. & \Rightarrow^* \langle 0, U \mid 5 \rangle + \langle 2, A \mid \dots \rangle
\end{aligned}$$

The derivation corresponds to the enforcement process presented in *Future Monitoring* in Figure 1: the check form constructs two new processes, colored **red** and **blue**, that collectively provide the monitoring future. The third, fourth, and fifth steps correspond to the synchronizations that take place in Figure 1, first between the user and delay processes, then the monitor and delay processes, and finally the user and delay processes again. The derivation ends with the monitoring process removed from the configuration and the user process continuing with the monitor result.

**Semi-Eager Monitoring.** Semi-eager monitoring [5–8, 22] delays contract checking until the checked value is demanded, an approach that appears naturally when Findler-Felleisen-style are recreated in lazy languages such as Haskell [5, 7, 22]. The implementation of semi-eager monitoring mirrors future monitoring, except that the contract expression is delayed instead of the user consumption form (Figure 5). Returning again to our example, evaluation proceeds as follows:

$$\begin{aligned}
& \langle 0, U \mid \text{force} (\text{check nat/c semi } 5 b) \rangle \\
\Rightarrow^* & \langle 0, U \mid \text{force} (\text{catchM} (\text{read } \iota) id) \rangle + \\
& \quad \langle 1, M \mid \text{write } \iota (\text{catch injr} (\text{injl} (\text{delay} (\text{nat/c } 5 b)))) \rangle \\
\Rightarrow^* & \langle 0, U \mid \text{force} (\text{catchM} (\text{read } \iota) id) \rangle + \\
& \quad \langle 1, M \mid \text{write } \iota \text{dref}_{\iota_2, \iota_3} \rangle + \langle 2, A \mid \dots \rangle
\end{aligned}$$

$$\begin{aligned}
&\Rightarrow^* \langle 0, U \mid \text{force dref}_{\iota_2, \iota_3} \rangle + \langle 2, A \mid \text{seq} (\text{read } \iota_1) \dots \rangle \\
&\Rightarrow^* \langle 0, U \mid \text{catchM} (\text{read } \iota_2) \text{ id} \rangle + \\
&\quad \langle 2, A \mid \text{let } x = \text{catch injr} (\text{injl} (\text{nat/c } 5 \ b)) \text{ in } \dots \rangle \\
&\Rightarrow^* \langle 0, U \mid \text{catchM} (\text{read } \iota_2) \text{ id} \rangle + \\
&\quad \langle 2, A \mid \text{seq} (\text{write } \iota_2 (\text{inl } 5)) (\text{rep/D } \iota_1 \ \iota_2 (\text{inl } 5)) \rangle \\
&\Rightarrow^* \langle 0, U \mid 5 \rangle + \langle 1, A \mid \text{rep/D } \iota_1 \ \iota_2 (\text{inl } 5) \rangle
\end{aligned}$$

When the resultant delay reference is forced, the initiating process signals the delay reference to perform the monitoring operation. The delay reference process returns the result of the contract enforcement via the correct injection, facilitating communication between the user evaluator and the delayed monitor.

## 5. Contract Combinators

As we have seen, a contract is a procedure that accepts a value and a blame record and produces a checked version of the value (see also Figure 7), raising the appropriate exception on failure. In a higher-order language, we can abstract over these contracts, pro-

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$$\begin{aligned}
\text{pred/c} &\triangleq \lambda c. \lambda x \ b. \text{if } c \ x \text{ then } x \text{ else raise } b \\
\text{pair/c} &\triangleq \lambda c_1 \ s_1 \ c_2 \ s_2. \\
&\quad \lambda p \ b. (\text{check } c_1 \ s_1 \ (\text{fst } p) \ b, \text{check } c_2 \ s_2 \ (\text{snd } p) \ b) \\
\text{func/c} &\triangleq \lambda c_1 \ s_1 \ c_2 \ s_2. \\
&\quad \lambda f \ b. \lambda x. \text{check } c_2 \ s_2 \ (f \ (\text{check } c_1 \ s_1 \ x \ (\text{inv } b))) \ b \\
\text{func/dc} &\triangleq \lambda c_1 \ s_1 \ g \ s_2. \\
&\quad \lambda f \ b. \\
&\quad \lambda x. \text{check } (g \ (\text{check } c_1 \ s_1 \ x \ (\text{ind } b))) \ s_2
\end{aligned}$$

$$(f \text{ (check } c_1 \ s_1 \ x \ (\text{inv } b))) \ b$$


---

**Figure 6.** Contract combinators for  $\lambda_{CC}$ .

ducing a library of *contract combinators* written with `check` in  $\lambda_{CC}$ . Remarkably,  $\lambda_{CC}$  contracts look syntactically similar, since these abstractions do not need to interact with the low-level communication semantics of `check`. The simplest contract combinator, `pred/c`, simply checks a predicate on the monitored value. More sophisticated contract combinators (see Figure 6) reuse the `check` form to enforce subcontracts on subcomponents of their input.

**Predicate Contracts.** Predicate contracts, constructed with `pred/c`, follow directly from our previous description. The combinator `pred/c` takes a predicate  $c$  as input and produces a contract that expects a value  $x$  and blame tuple  $b$  as input. When this procedure is invoked, we evaluate the expression

$$\text{if } c \ x \text{ then } x \text{ else raise } b$$

Here,  $x$  is the monitored value,  $c$  is the monitoring predicate,  $b$  is the responsible party. This expression is evaluated when the contract is enforced as  $(c \ e \ b)$  in Figure 5, returning the value on success or raising the blame tuple as an exception on failure.

**Pair Contracts.** As discussed in Sec. 2, pairs use two subcontracts with their associated strategies for each of the left and right subcomponents. The pair combinator constructs the contract in terms of its subcontracts, monitoring each on the appropriate subcomponent of the pair with `check` as:

$$(\text{check } c_1 \ s_1 \ (\text{fst } p) \ b, \text{check } c_2 \ s_2 \ (\text{snd } p) \ b)$$

Here  $p$  is the monitored pair,  $c_1$  and  $s_1$  are the contract and strategy for the first element, and  $c_2$  and  $s_2$  are the contract and strategy

for the second element. The contract decomposes the pair into its sub-pieces *when* the monitoring strategy specifies to do so, and construct a new pair via *check*, which is returned to the initiating (or demanding) location.

**Function Contracts.** Function contracts, constructed with *func/c* in Figure 6, take two contracts and strategies which indicate the pre- and post-condition and their strategies. The result is a procedure that expects some function  $f$  and the appropriate blame labels. When invoked, the combinator constructs the function:

$$\lambda x. \text{check } c_2 \ s_2 \ (f \ (\text{check } c_1 \ s_1 \ x \ (\text{inv } b))) \ b$$

Here  $f$  is the monitored function,  $x$  is that function's input,  $c_1$  and  $s_1$  are the contract and strategy for the pre-condition, and  $c_2$  and  $s_2$  are the contract and strategy for the post-condition. We also introduce the blame operator *inv*, which inverts the pre-condition blame labels to ensure correct blame [11]. Dependent functions follow directly<sup>4</sup>, using *ind* to construct the *indy* label structure.

## 6. Metatheory

We briefly sketch out two metatheoretical aspects of our system: the type system and an embedding of the original contract system presented by Findler and Felleisen [16].

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<sup>4</sup>The dependent function combinator uses the same strategy for both enforcements of  $c_1$ , but it is possible to vary this strategy between them.

$$\begin{array}{ll} \tau & ::= \text{int} \mid \text{bool} \mid \text{str} \mid \text{error} \mid () \\ & \mid \tau \rightarrow \tau \mid \tau \times \tau \mid \tau + \tau \mid \text{chan } \tau \mid \text{con } \tau \mid \sigma \\ \sigma & ::= \text{eager} \mid \text{seager} \mid \text{future} \mid \text{async} \end{array}$$

blame	$\Delta$	$\text{str} \times \text{str} \times \text{str}$
con $\tau$	$\Delta$	$\tau \rightarrow \text{blame} \rightarrow \tau$
check	$\Delta$	$\text{con } \tau \rightarrow \sigma \rightarrow \tau \rightarrow \text{blame} \rightarrow \tau$

---

**Figure 7.** Typing grammar for  $\lambda_{\text{CC}}$ .

**Typing the Contract Calculus.** We sketch the type system for  $\lambda_{\text{CC}}$ , using the type grammar in Figure 7. The typing rules are standard: delay  $e$  and force  $e$  share the type of  $e$ . The raise form may be given any type.

We define  $\text{con } \tau$  as an abbreviation for contract types with the shape discussed previously: The contract shorthand enforces the contract shape discussed previously: a contract takes its input and blame labels, returning the original type  $\tau$ . The strategy types  $\sigma$  are as expected: **eager** is typed as **eager** and so forth. The check form takes a contract of type  $\text{con } \tau$ , a strategy of type  $\sigma$ , a monitored expression of type  $\tau$ , and a blame set of type **blame**, returning a value of type  $\tau^5$ .

Communication requires types for channels, which are included in an additional type environment  $\Delta$  over  $\mathcal{K}; \mathcal{P}$ . A process configurations is well-typed up to deadlock if each process term is made up of well-typed subterms, and each process is well-typed if the underlying  $\lambda$ -calculus expression is well-typed.

**Theorem 6.1.** *For any well-typed configuration  $\mathcal{K}; \mathcal{P}$ , either:  $\mathcal{K}; \mathcal{P}$  is in a well-typed halt state; there exists some well-typed configuration  $\mathcal{K}'; \mathcal{P}'$ , well-typed, such that  $\mathcal{K}; \mathcal{P} \Rightarrow \mathcal{K}'; \mathcal{P}'$ ; or  $\mathcal{K}; \mathcal{P}$  is in a stuck state  $\mathcal{S}$ , which include configurations where a monitoring process has raised an exception or is otherwise blocked, or all pro-*



cesses are either blocked on communication that may not be further reduced by SYNC or have delay references in usage positions.

**Correctness of Encoding.** We demonstrate that our semantics faithfully recreates the original semantics provided by Findler and Felleisen’s *Contracts for Higher-Order Functions* [16]. We choose this semantic model for two reasons: first, this semantics has been widely accepted and rigorously verified, and second, the subtleties of less-eager monitoring approaches vary whereas the semantics of eager monitoring is well-accepted. Furthermore, this embedding is one-way: while it may be possible to recover the exact communication structure of every collection of processes [26], it is not worthwhile or insightful. Finally, Findler and Felleisen [16] use *lax* monitoring for dependent monitors (as discussed by Dimoulas et al. [11]), and thus we omit them.

**Theorem 6.2.** *If  $c$  is an expression in  $FF$ , the original semantics presented by Findler and Felleisen [16], then there is some context  $P \in FF$  such that  $c = P[c']$  and a translation function  $T(P, c') : FF \rightarrow \lambda_{CC}$  such that either:*

1. *if  $P[c'] \mapsto^* v$ , then  $T(P, c') \Rightarrow^* \text{done } v$ ;*
2.  *$\forall n$ . if  $P[c'] \mapsto^* \text{exn } p$ , then  $T(P, c') \Rightarrow^* \text{done } (\text{raise } b)$  where  $b = (p, n)$ .*

*Proof.* We assume that Findler and Felleisen’s  $I$  operator has already been run on the input  $c$ , which performs *obligation insertion*, or, more simply, inserts the contracts provided by the outer **val rec** binding form into the main expression. We proceed by “recoloring” the if expressions in  $c$ , indicating whether they were constructed by a contract monitor or not. We also explicitly mark contract forms

<sup>5</sup> Explicitly typing delay references require a type-level metafunction that uses the strategy's type to calculate the final type of a contract (Sec. 4).

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containing values as value forms in the language to ease translation. Monitoring flat contracts will now produce something of the form  $\text{if}_c e_1 e_2 e_3$ . The proof proceeds by induction on the length of  $\mapsto^*$ , where we define a handful of translation functions such that  $T(P, c') = F(g(P), f(c'))$  where

$$\begin{aligned} f(c') &= ((\mathcal{C}, \mathcal{K}), e) \\ g(P) &= ((\mathcal{C}, \mathcal{K}), \mathcal{E}) \end{aligned}$$

such that

$$F(((\mathcal{C}', \mathcal{K}'), \mathcal{E}), ((\mathcal{C}, \mathcal{K}), e)) = \mathcal{K}' \cup \mathcal{K}; \mathcal{C}'[\mathcal{C}[\mathcal{E}[e]]]$$

We only present one case in full:

Case:  $P[V_1^{\text{contract}(V_2), p, n}] \mapsto P[\text{if}_c (V_2 V_1) V_1 (\text{blame } p)]:$

We perform the following translations:

$$\begin{aligned} f(V_1) &= ((\mathcal{C}_{v_1}, \mathcal{K}_{v_1}), v_1) \\ f(V_2) &= ((\mathcal{C}_{v_2}, \mathcal{K}_{v_2}), v_2) \\ c &= \lambda x b. \text{ if } v_2 x \text{ then } x \text{ else raise } b \\ f(\text{contract}(V_2)) &= ((\mathcal{C}_{v_2}, \mathcal{K}_{v_2}), c) \\ f(p) &= ((\mathcal{C}_p, \mathcal{K}_p), p_{cc}) \\ f(n) &= ((\mathcal{C}_n, \mathcal{K}_n), n_{cc}) \\ f_{\text{blame}}(p) &= b \end{aligned}$$

Then  $f(V_1^{\text{contract}(V_2), p, n}) = ((\mathcal{P}_1, \mathcal{K}_1), e_1)$  where:

$$\begin{aligned} e_1 &= \text{check } c \text{ eager } \hat{v}_1 b \\ \mathcal{P}_1 &= \mathcal{C}_{v_1}[\mathcal{C}_{v_2}[\square]] \\ \mathcal{K}_1 &= \mathcal{K}_{v_1} \cup \mathcal{K}_{v_2} \end{aligned}$$

Then let  $\iota_{v_1}$  be a unique channel and  $f(\text{if}_c (V_2 \ V_1) \ V_1 \ (\text{blame } p)) = ((\mathcal{P}_2, \mathcal{K}_2), e_2)$  where:

$$\begin{aligned} e_2 &= \text{catchM} (\text{read } \iota_{v_1}) \text{ id} \\ \mathcal{P}_2 &= \mathcal{C}_{v_1} [\mathcal{C}_{v_2} [\square + \langle n, M \mid \text{write } \iota_{v_1} (\text{catch injr } (\text{injl } (c \ v_1 \ b)))))] \\ \mathcal{K}_2 &= \mathcal{K}_{v_1} \cup \mathcal{K}_{v_2} \cup \{\iota_{v_1}\} \end{aligned}$$

Then we compute  $g(P) = (\mathcal{C}_P, \mathcal{K}_P)$ .

Finally, let  $\mathcal{C} = \mathcal{C}_P [\mathcal{C}_{v_1} [\mathcal{C}_{v_2} [\square]]$  and  $\mathcal{K} = \mathcal{K}_{v_1} \cup \mathcal{K}_{v_2} \cup \mathcal{K}_P$  Therefore:

$$\begin{aligned} & F((\mathcal{C}_P, \mathcal{K}_P), ((\mathcal{P}_1, \mathcal{K}_1), e_1)) \\ &= \mathcal{K}; \mathcal{C}[\text{check } c \ \text{eager } \hat{v}_1 \ b] \\ &\Rightarrow^* \mathcal{K} \cup \{\iota_{v_1}\}; \mathcal{C}[[\text{catchM} (\text{read } \iota_{v_1}) \text{ id}] + \\ &\quad \langle n, M \mid \text{write } \iota_{v_1} (\text{catch injr } (\text{injl } (c_2 \ v_1 \ b))))] \\ & F((\mathcal{C}_P, \mathcal{K}_P), ((\mathcal{P}_2, \mathcal{K}_2), e_2)) \end{aligned}$$

□

## 7. Implementation and Advanced Monitors

In a language (Racket [19]) with the right infrastructure (syntactic extension, processes, exceptions, and communication primitives), our implementation<sup>6</sup> can be realized as a library in less than 100 lines of code. We elide the exact implementation details; they follow directly from the previous semantics. Each strategy is represented by an instance of a Racket structure, the contract combinators and blame facilities are provided as modules, and check is provided as a syntactic transformer:

```
(define-syntax checkCon
  (syntax-rules ()
    [(_ c s e b)
     (cond [(eager-strat? s) ...]
           [(semi-strat? s) ...]
           [(future-strat? s) ...]
           [(async-strat? s) ...])])
```

```
(begin (thread (λ () (c e b))) e))))))
```

We now use this implementation, called `ccon`, to demonstrate the extensibility of our system, from simple contracts to additional contract combinators for structural contracts over trees [18]. We start with small examples:

```
> (checkCon nat/c eager 5 b)
5
> (checkCon nat/c eager -1 b)
```

---

<sup>6</sup> <https://github.com/cgswords/ccon>

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```
Exception: ...
```

```
> (checkCon nat/c semi 5 b)
#<promise ...>
> (force (checkCon nat/c future 5 b))
5
```

These calls are as expected, corresponding to our earlier examples in Sec. 2 and Sec. 4. The result of the third and fourth contract demonstrate the underlying usage of Racket’s `delay` for semi-eager and future strategies. (Here `b` is a blame structure with Server, Contract, and Client labels.)

## 7.1 Tree Contracts in `ccon`

To demonstrate the expressive power of `ccon` (and thus  $\lambda_{CC}$ ), we next construct a tree data structure and define contract combinators for the structure. We define a tree structure as `node` in Figure 8, where a tree is either a null value, `()`, or a node containing a value

and left and right subtrees.

We also define the tree contract combinator `treerec/c`, a recursive combinator which reuses itself on its left and right subtrees. This procedure determines if the current node is a leaf or internal node and then constructs the appropriate monitor. We can use this contract to enforce tree-wide invariants, such as ensuring that every value is a natural number:

```
(define nat-tree-E (tree/c nat/c eager eager nat/c eager))
```

```
> (checkCon nat-tree-E eager (make-node ...) b)
```

We can also use this contract as a pre-condition to a procedure such as `get-root-value`, which returns the root value of any tree `t`:

```
> (get-root-value t)
```

```
5
```

```
> (checkCon (func/c nat-tree-E eager nat/c eager) eager t b)
```

```
5
```

The first invocation inspects the root node of the tree, returning the value. Conversely, the second invocation traverses the entire tree structure, enforcing the precondition contract before extracting the value from the root node. To recover the original complexity, we can use the solution presented by Findler et al. [18], rewriting `nat-tree-E` with semi-eager strategies. However, unlike Findler et al., we have a fine-grained decision to make: shall we eagerly or semi-eagerly enforce the value contract? Eager value checking, `nat-tree-S1` below, ensures that any node we inspect will have a natural number in the value position. Conversely, full semi-eager checking, `nat-tree-S2` below, will only verify that values are natural numbers when the program demands them.

```
(define nat-tree-S1 (tree/c nat/c eager semi nat/c eager))
```

```
(define nat-tree-S2 (tree/c nat/c eager semi nat/c semi))
```

```

> (get-root-val (checkCon nat-tree-S1 eager t b))
5
> (get-root-val (checkCon nat-tree-S2 eager t b))
#<promise ...>

```

Neither of these solutions is “more correct”: both encodings recover the original complexity of `get-root-val`, and the divergence demonstrates the precise power of explicit monitoring strategies. Furthermore, this change is syntactically insignificant: a programmer might try both out to select the most appropriate approach.

## 7.2 Advanced Contracts in `ccon`

There are a family of contracts that cannot benefit from the previous optimization, which include contracts that require *upward value propagation* through monitored structures [18], or more generally, collections of contracts that collaborate to establish global invariants. For example, one may try to ensure that a binary tree is full, i.e., that there are  $2^n$  nodes in the tree if the height of the tree is  $n$ . Implementing this predicate is straightforward, traversing the entire tree, but this once again requires visiting every node.

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```

(struct node (left value right))

(define (treerec/c c1 s1 s2 c3 s3)
  (letrec
    ((treec
      (λ (t b)

```

```

    (match t
      [(node l v r) (let ([nv (checkCon c3 s3 v b)]
                          [nl (checkCon treec s2 l b)]
                          [nr (checkCon treec s2 r b)])
                      (node nl nv nr))]
      [v (checkCon c1 s2 v b)]))
    treec))

(define ((tree/dc c1 s1 c2 s2 c3 s3 c4 s4) t b)
  (match t
    [(node l v r) (let* ([nv (checkCon c3 s3 v b)]
                        [nl (checkCon (c2 nv) s2 l b)]
                        [nr (checkCon (c4 nv) s4 r b)])
                      (node nl nv nr))]
    [v (checkCon c1 s2 v b)]))

```

---

**Figure 8.** Tree contracts in Racket with `ccon`.

```

(define (full/a i)
  (let ([il (make-channel)]
        [ir (make-channel)])
    (treedc
      (pred/c (λ (n) (begin (channel-put i 0) #t))) eager
      (λ (-) (full/a il)) semi
      (pred/c
        (λ (n)
          (let ([hr (sync (choice-evt ir il))]
                [hl (sync (choice-evt ir il))])
            (if (= hl hr)
                (begin (channel-put i (add1 hl)) #t)
                #f))))
      async
      (λ (-) (full/a ir) semi))))

```

---

**Figure 9.** The implementation of full as a callback-based contract.

Alternatively, we might construct a dependent tree contract combinator wherein the left and right subtrees are passed into the value predicate, but Findler et al. [18] observe that these subtrees must be evaluated to verify the contract, and thus recreate the same asymptotic violations. They go on to propose an alternative solution using attributes [19] to track height information on the tree as it is explored, relying on the user evaluator to produce an invasive enforcement mechanism with amortized bounds. This approach is not currently part of the Racket contract system.

We can develop a similar solution in `ccon` using callbacks: we postpone checking any contract until its subcontracts have been checked by using channels within asynchronous contracts. While complex in concept, the only additional facility we require is the ability to create, propagate, and synchronize with new channels of communication, which both  $\lambda_{CC}$  and Racket provide as low-level operations. Thus the adventurous contract writer might implement this callback-oriented approach to fullness as in Figure 9. Furthermore, this solution lives entirely in the contract system: the user is never exposed to it beyond using `force`.

Each invocation of the contract is parameterized by a communication channel `i`, which indicates where to write the current node’s height. At each leaf, the predicate writes 0 to `i` and succeeds. At internal nodes, we create two additional channels, `il` and `ir`, to pass to the left and right subtrees respectively. Next we assert `(full/a il)` and `(full/a ir)` on the appropriate subtrees, utilizing the delaying nature of lambda abstraction to prevent divergence. These contracts



are semi-eagerly monitored, and thus will not be enforced until the subtrees are demanded by the program<sup>7</sup>. Finally, we create an asynchronous monitor for the node's value which performs blocking reads from `il` and `ir`. The results of these reads are the heights of the left and right subtrees, so we verify they are equal, and either write the new height across `i`, triggering the parent node's fullness test, or signal a contract violation. This communication chain allows each contract to propagate values upward from the leaves as the tree is explored, as indicated with upward-pointing arrows in Figure 10.

Such a contract is only possible after full separation of the monitor evaluator from the user evaluator and exposing communication tools to contract writers, facilitating contract enforcement in a custom-crafted traversal of the monitored structure.

## 7.3 Results

We briefly evaluate the performance of `full/a` against the eager fullness contract presented by Findler et al. [18] using a set of microbenchmarks. We use `ccon` to implement `full/a` as in Figure 9, and the eager fullness contract is constructed in Racket's native system as follows:

```
(define full/c (flat-named-contract 'full/c full?))
```

Next we set up the following experiment: for trees of size 1 to  $2^{24}$ , we first enforce one of the contracts on the tree and then perform a single element lookup. This lookup occurs in  $O(\log n)$  time, and so the bulk of the computational work in the Racket-primitive contract will consist of enforcing the fullness contract, while the bulk of the work in enforcing `full/a` occurs in the process and channel construction overhead incurred during execution.

We repeat this test 100 times for each data-point and graph the

arithmetic means in in Figure 11. The  $x$ -axis represents the size of the tree as a function of  $2^n$  and the  $y$ -axis is a logarithmic scale in seconds. The orange line, *Built-In*, indicates that the eager contract run with Racket’s built-in monitoring facilities provides excellent performance for small tree structures but slows down exponentially as the tree increases exponentially in size. Conversely, the blue line, *CCON*, indicates that the full/a implementation in ccon slowly only slightly as longer traversals require increasingly large numbers of processes and channels.

Our results support our initial discussion of performance recovery. Furthermore, the Racket contract system has been heavily optimized for performance [33] and the competitive results of ccon indicate that the process communication model of  $\lambda_{CC}$  is a viable approach to contract monitoring.

## 8. Sketches of Additional Monitoring Strategies

We present sketches of implementations for four strategies that appear in the literature: lazy monitors, temporal monitors, future monitors in the style of Dimoulas et al., and statistical monitors.

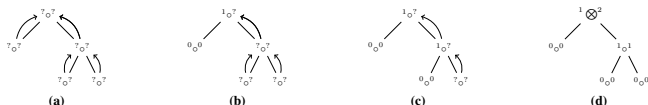
**Lazy Contracts.** Degen et al. [7, 8] introduce the idea of lazy monitors, which entirely avoid any aspect of over-evaluation. For example, checking a predicate on a pair will not force the pair; the monitoring evaluator will wait for the user evaluator to force the pair. If the pair is never used, in full, in the user program, then the monitor will never check it. Modeling lazy monitoring as communication across processes demonstrates its intrusive interaction with the main evaluator.

To facilitate this user-driven monitoring, we must construct a

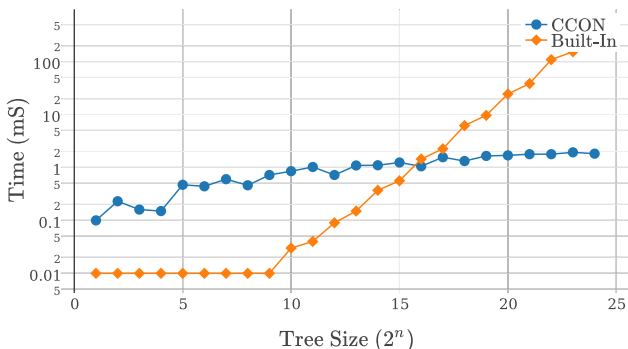
layer of indirection for both evaluators such that the user evaluator may force any expression under a lazy monitor and the lazy monitor will postpone contract enforcement until this forcing occurs. We accomplish this by recursively parsing the input expression  $e$

<sup>7</sup>If we used **eager** in place of **semi**, this contract would revert to an eager,  $O(2^n)$  check at assertion time.

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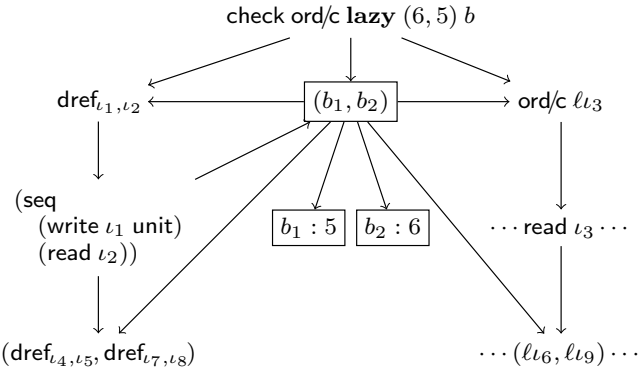


**Figure 10.** Evolution of contract checking during tree traversal for a full binary tree using asynchronous callbacks.



**Figure 11.** Timing results for full tree contract verification in

Racket’s built-in contract system versus our semi-eager approach. Experiments were performed on a MacBook Air with a 1.3 GHz Intel Core i5 and 4GB of RAM.



**Figure 12.** Lazy contract communication [8].

yield two new expression,  $e_d$  and  $e_\ell$ . The first,  $e_d$ , is an expression constructed from delay references wrapped around each component and sub-component in the original expression. Similarly,  $e_\ell$  is constructed identically using *lazy monitor references* of the form  $l_l$ . Each delay reference works in the usual way, except that it will also notify the associated lazy monitor reference when forced. When evaluated, lazy monitor references perform blocking reads, proceeding only when the associated delay reference is forced and provides the appropriate value. The structure of this communica-

tion is presented in Figure 12. This approach closely mirrors the implementation provided by Degen et al. [8], wherein individual call-by-need cells register callbacks for contract monitors.

**Temporal Contracts.** Disney et al. [13] introduce the concept of temporal monitors, which formalize module interactions as a trace of events such as function calls and returns. They formalize this approach by treating each module in the program as a process and

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storing the process trace of sends and receives between these modules as the program proceeds. Finally, the monitoring system verifies that this trace conforms to certain prefix-closed predicates, constraining the behavior of each module and producing an error if this trace violates these predicates. Our approach differs by using individual processes for each monitor. We explicitly enforce predicates on values and control how processes communicate to replicate monitoring strategies, omitting the need to preserve process traces. Such traces, however, may be used to ensure that monitor strategies correctly adhere to their semantic descriptions.

This system may be constructed in  $\lambda_{CC}$  by recreating the original approach, using a mediator process to construct process traces. Any communication events will move through this mediator, which will log the events. Temporal contract assertions will register predicates with this mediator process, which will use these predicates to ensure the process interaction traces adhere to the correct shape. Such a mediator must also provide the outlined by Disney et al. [13], including information capture and correct error propagation.

**Future Contracts à la Dimoulas et al.** Dimoulas et al. [10]

present an alternate model of future contracts that use a master user process and a slave monitoring process, delegating predicate enforcements to the slave process and synchronizing with it when the master performs effects such as reference manipulation and I/O.

This system may be constructed in  $\lambda_{CC}$  using a secondary global process that acts as the slave process. Any monitors with the appropriate strategy are provided to this slave process, which adds the monitor to a list of active checks. To maintain synchronous communication, it may be convenient to establish the slave as two processes: one to receive new monitoring requests and synchronize with the user process during synchronization events, and another “worker” process that polls the synchronization process for a monitor, performs it, and provides the synchronization process with the result before looping. Then, as Dimoulas et al. [10] observe, each effectful operation is wrapped in a proxy procedure that synchronizes with the slave process before executing. This synchronization mechanism would elide the need for force.

***Statistical Software Contracts.*** Dimoulas et al. [12] describe the notion of randomly checked function contracts. In lieu of iterating over the entire input space for a function, it is possible to use a spot checker [14] to obtain partial assurance of a contract by generating and testing a series of inputs. For flat and structural contracts, this approach may randomly verify its contracts: that is, the contract may (or may not) be enforced as evaluation proceeds.

Given a random-generation mechanism and a spot-checker,  $\lambda_{CC}$  may be extended to support this type of soft guarantee: predicate and structural contracts will use a random number generator to decide which, if any, contracts to enforce, and the full spot-checker

will generate sample inputs to contracted functions. This approach induces a secondary extension to  $\lambda_{CC}$ : while statistical guarantees may receive their own strategy, it is more natural to introduce a *strategy combinator* that will take an existing strategy (such as **eager** or **semi**) and modify it to preserve the original enforcement strategy while performing probabilistic contract enforcement.

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## 9. Related Work

Eiffel [25] first popularized software contracts and the idea of writing programs with pervasive contract checking. Eiffel introduces a number of theoretical and semantic concepts that have since induced a large body of research, including the underlying theoretical foundations [4, 15, 16], language integration with existing semantics [1, 6–8, 11, 19, 20, 22]. Degen et al. [7, 8] present descriptions of eager, semi-eager, and lazy monitors; we have characterized the first two precisely and sketched the third in this paper.

Dimoulas and Felleisen [9] address different approaches to monitoring through observational equivalence, relying on these observations to discuss when and how contracts affect the underlying program. They reconstruct contract satisfaction from these principles, and introduce the concept of a *shy* contract, which can evaluate no more than the program would, to discuss the work in laziness by Chitil et al. [6]. Shy contracts are encoded by replacing the arguments to monitored function with weakened arguments that produce exceptions with over-explored, similar in nature to our proposal for expression reconstruction in lazy monitoring.

A variety of alternative semantic models exist, primarily focus-

ing on the original notion of eager contract monitoring [4, 15, 17]. We follow Findler and Felleisen [16] in defining a contract system rather than a model of contract satisfaction.

Multiple approaches to blame assignment, particularly in the case of dependent function contracts, have been proposed [11, 20], resulting in the definition of *complete monitoring* [11]. Since our contract combinators are library functions, we can provide any blame assignment approach (e.g. *lax*, *picky*, and *indy*). Proving complete monitoring in  $\lambda_{CC}$  remains future work.

Behavioral specification for process calculi via *session types* has been explored extensively [23, 34], providing strong type guarantees about process communication patterns. In contrast, we use communication patterns to describe checking of sequential programs. Encoding these communication patterns as session types may further inform the design of contract systems.

## 10. Conclusion and Future Work

We present a unifying perspective on the semantics of contract monitoring, wherein myriad semantic approaches and contract combinators can be characterized by translation into a straightforward process calculus. This approach captures multiple existing approaches to contract monitoring and introduces several new ones. We also present a unified source language in which programmers may select strategies on a per-contract basis, rather than the current status quo where the choice is fixed by the contract system designer. Furthermore, we propose that  $\lambda_{CC}$  is a suitable target for new contract monitoring approaches, providing a extensible interpretation of the interactions between contracts, contract monitors, and user programs. Finally, we demonstrate how the runtime framework can be leveraged to express contracts inexpressible in existing systems, focusing on upward-propagating delayed contracts for binary trees.



In the future we hope to investigate how the formal semantics translates into existing process-oriented languages such as Erlang [2], explore the design space of strategies and strategy combinators, and investigate if proofs of complete monitoring [11] can be carried out in our system.

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