

- 1) For the forward kinematics rotational and translation matrices were used. Parameters  $d_1$  and  $a_2$  were known as 5 and 10.
- 2) For the inverse kinematics we used geometry for all angles.

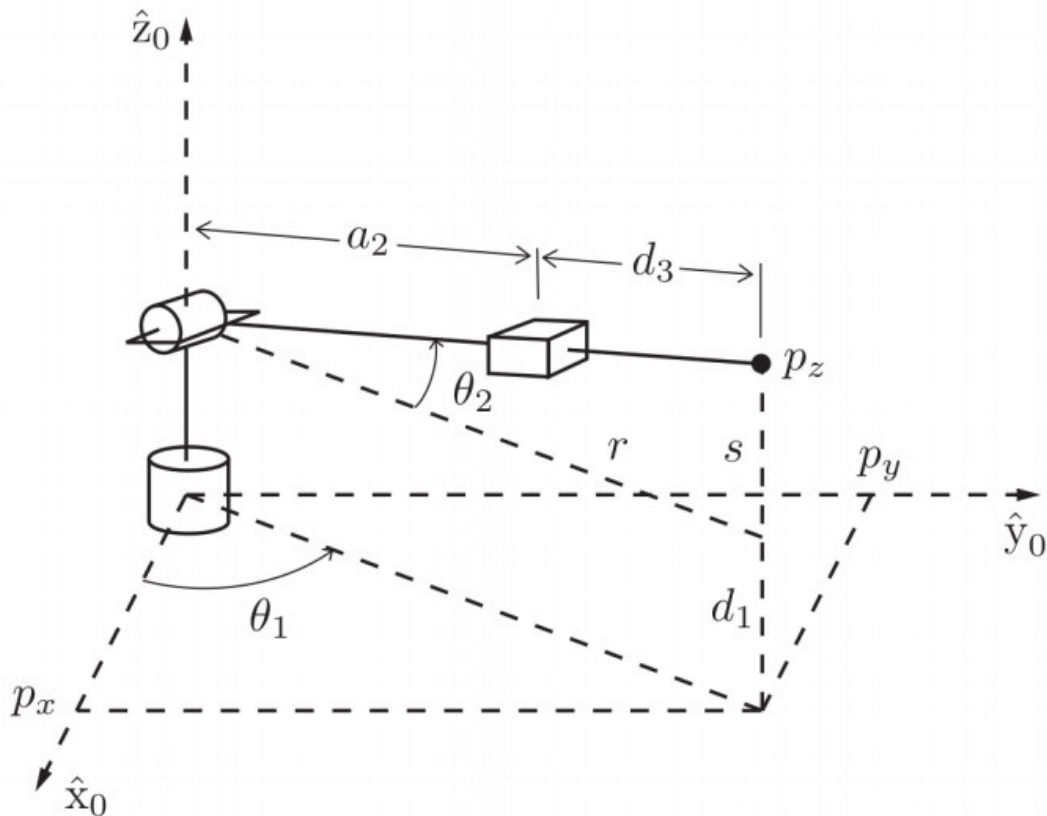


Figure 1 – RRP robot

From figure 1 it is obvious that  $\theta_1$  angle is  $\text{atan}(p_x, p_y)$ , but there may be another solution when  $\theta_1 > \pi$ . So  $\theta_{11}$  solution is when first angle is less than 180 degree, while  $\theta_{12}$  solution is when this angle bigger than 180 degree. The same formulas for the second angle. So we have 4 different solutions  $(\theta_{11}, \theta_{21})$ ;  $(\theta_{12}, \theta_{21})$ ;  $(\theta_{12}, \theta_{22})$ ;  $(\theta_{11}, \theta_{22})$ . Distance  $d_3$  was founded from geometry approach too. Also we have to add singularity if  $x$  and  $y$  coordinates of the end effector are equal to 0, there will be a lot of different solutions for  $\theta_1$  angle.

- 3) Finding Jacobian by **geometric approach**. It is very simple, due to the fact that we have to use the formula  $J_i = \frac{z_{i-1} \times (o_n - o_{i-1})}{z_{i-1}}$ . Where  $o_i$  is a coordinate of the joint I,  $z$  is a rotational part of the R matrix for every joint and  $O_n$  is a coordinate of an end-effector. So in matlab result, J\_geometric is a main formula and J\_geometric\_initial is a numerical result of a Jacobian for given parameters. All operations provided in “main” matlab” file.
- 4) So, there is one singularity, when end-effector intersects z axis.

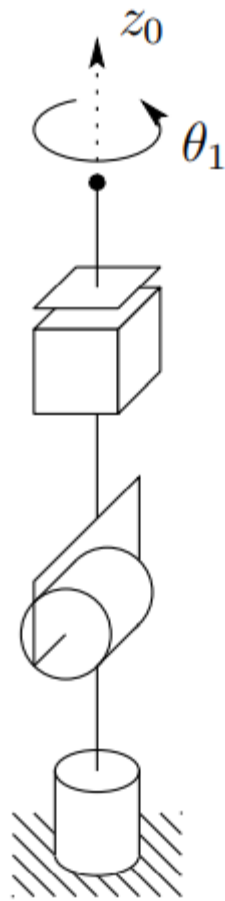


Figure 2 – Singularity

