

# Module IV

Closure of an FD

# Closure of an attribute

- Closure of an attribute  $X$  is represented as  $X^+$  is the set of attributes that can be derived using inference axioms.
- $F = \{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$
- Find  $A^+$
- Step 1:  $A^+ = \{A\}$
- consider left hand side of FD

- $F = \{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$
- Step 1:  $A^+ = \{A\}$
- consider  $A \rightarrow B$
- $A^+ = \{AB\}$
- Consider  $B \rightarrow C$
- $A^+ = \{ABC\}$
- Consider  $C \rightarrow D$
- $A^+ = \{ABCD\}$
- Since no more FDs has to consider,  $A^+ = \{ABCD\}$

# Algorithm

❑ **Algorithm:** Determining  $X^+$ , the Closure of : the set of attribute  $X$  under  $F$

$X^+ = X;$

repeat

$\text{old}X^+ = X^+;$

    for each functional dependency  $Y \rightarrow Z$  in  $F$  do

        If  $X^+ \supset Y$  then  $X^+ = X^+ \cup Z;$

until  $(X^+ = \text{old}X^+);$

- Given  $F = \{A \rightarrow B, B \rightarrow D, AD \rightarrow F, F \rightarrow C\}$
- Find
- 1.  $A^+$
- 2.  $(AB)^+$
- 3.  $(B)^+$



