

Amstrong's Axioms

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- 1. Reflexivity if $Y \subseteq X$ then $X \rightarrow Y$
- 2. Augmentation if $X \rightarrow Y$ then $XZ \rightarrow Y$ and /or $XZ \rightarrow YZ$
- 3. Transitivity if $X \rightarrow Y$ and $Y \rightarrow Z$ then $X \rightarrow Z$
- 4. Psuedo transitivity if $X \rightarrow Y$ and $YW \rightarrow Z$ then $XW \rightarrow Z$
- 5. Union $X \rightarrow Y$ and $X \rightarrow Z$ then $X \rightarrow YZ$
- 6. Decomposition If $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$

1. Reflexivity if $Y \subseteq X$
then $X \rightarrow Y$

1. Since $A \subseteq AB$,
 $AB \rightarrow A$

2. Since $B \subseteq AB$
then $AB \rightarrow B$

3. Since $AB \subseteq AB$,
Then $AB \rightarrow AB$

A	B	C	D	E
a1	b1	c1	d1	e1
a2	b2	c2	d2	e2
a1	b2	c3	d2	e3
a3	b3	c4	d2	e4
a4	b4	c5	d4	e5

2. Augmentation if $X \rightarrow Y$ then $XZ \rightarrow Y$ and /or $XZ \rightarrow YZ$

1. IF $C \rightarrow A$ THEN
 $CB \rightarrow A$
AND $CB \rightarrow AB$

A	B	C	D	E
a1	b1	c1	d1	e1
a2	b2	c2	d2	e2
a1	b2	c3	d2	e3
a3	b3	c4	d2	e4
a4	b4	c5	d4	e5

4. Psuedo transitivity if $X \rightarrow Y$ and $YW \rightarrow Z$ then $XW \rightarrow Z$

If $C \rightarrow B$ AND
 $BA \rightarrow D$
then
 $CA \rightarrow D$

A	B	C	D	E
a1	b1	c1	d1	e1
a2	b2	c2	d2	e2
a1	b2	c3	d2	e3
a3	b3	c4	d2	e4
a4	b4	c5	d4	e5

5. Union $X \rightarrow Y$ and
 $X \rightarrow Z$ then $X \rightarrow YZ$

1. IF $C \rightarrow A$ AND
 $C \rightarrow B$ THEN

$C \rightarrow AB$

A	B	C	D	E
a1	b1	c1	d1	e1
a2	b2	c2	d2	e2
a1	b2	c3	d2	e3
a3	b3	c4	d2	e4
a4	b4	c5	d4	e5

6. Decomposition If
 $X \rightarrow YZ$, then $X \rightarrow Y$ and
 $X \rightarrow Z$

1. If $C \rightarrow DE$ then
 $C \rightarrow D$ As well as
 $C \rightarrow E$

A	B	C	D	E
a1	b1	c1	d1	e1
a2	b2	c2	d2	e2
a1	b2	c3	d2	e3
a3	b3	c4	d2	e4
a4	b4	c5	d4	e5

Exercises on Inference rules(Amstrongs axioms)

- Q1. Given the set $F=\{A \rightarrow B, C \rightarrow X, BX \rightarrow Z\}$ Derive $AC \rightarrow Z$

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- Q1. Given the set $F=\{A \rightarrow B, C \rightarrow X, BX \rightarrow Z\}$ Derive $AC \rightarrow Z$

Answer

$$A \rightarrow B \quad (1)$$

$$\underline{BX \rightarrow Z} \quad (2)$$

- $AX \rightarrow Z$ (3) (psuedotransitivity rule (1) and(2))

- $C \rightarrow X \quad (4)$

$$\underline{AX \rightarrow Z} \text{ (5) psuedotransitivity rule (3) and(4))}$$

$$CA \rightarrow Z \quad (6)$$

$$CA \rightarrow Z \text{ means } AC \rightarrow Z$$

Q2. $F = \{A \rightarrow B, C \rightarrow D\}$ With $C \subseteq B$, Derive $A \rightarrow D$

- $A \rightarrow B$ (1)
- $B \rightarrow C$ (2) (GIVEN)
- $A \rightarrow C$ (3) (TRANSITIVITY (1) AND (2))
- $C \rightarrow D$ (4)
- $A \rightarrow D$ (5) (TRANSITIVITY (3) AND (4))

Redundant FDs

- Given a set F of functional dependencies, $A \rightarrow B$ of F is said to be **redundant** with respect to the FDs of F iff $A \rightarrow B$ can be derived from set of FDs $F - \{A \rightarrow B\}$
- $A \rightarrow B$ can be derived from set of functional dependencies **not including $A \rightarrow B$**

Given a set $F=\{X\rightarrow YW, XW\rightarrow Z, Z\rightarrow Y, XY\rightarrow Z\}$. Determine if the functional dependencies $XY\rightarrow Z$ is redundant in F ?

- Step 1: Remove $XY\rightarrow Z$ from F
- New $F_1=\{X\rightarrow YW, XW\rightarrow Z, Z\rightarrow Y\}$
- Step 2, Using F_1 , derive $XY\rightarrow Z$
- $X\rightarrow YW$ (1)
- $XW\rightarrow Z$ (2)
- $Z\rightarrow Y$ (3)
- By Applying decomposition rule on (1) we get
- $X\rightarrow Y$ (4)
- $X\rightarrow W$ (5)

- $X \rightarrow W$ (5)
- $XW \rightarrow Z$ (2)
- $XX \rightarrow Z$ (Pseudotransitivity (5) and (2))
- $X \rightarrow Z$ (6)
- **$XY \rightarrow Z$ (augmentation rule on (6))**