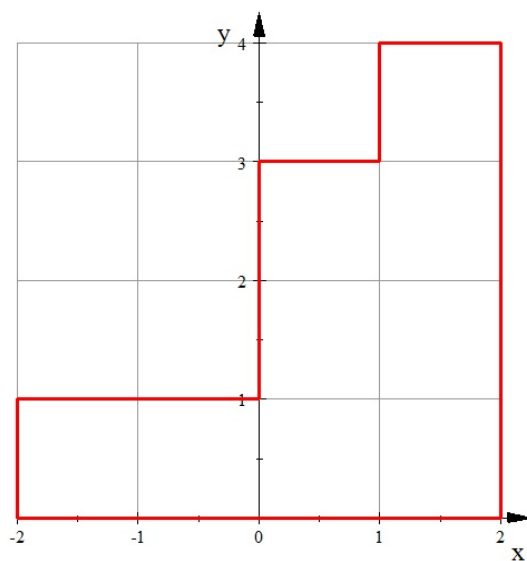


1. Compute the area of the part of the paraboloid $z = x^2 + y^2$ which lies inside the cylinder $x^2 + y^2 = 1$.
2. Let S be the portion of the graph $z = 4 - 2x^2 - 3y^2$ that lies over the region in the xy -plane bounded by $x = 0$, $y = 0$, and $x + y = 1$. Write the integral that computes $\iint_S (x^2 + y^2 + z) \, dS$.
3. Compute $\iint_S \mathbf{F} \cdot d\mathbf{S}$, where $\mathbf{F} = y\mathbf{i} - x\mathbf{j} + z\mathbf{k}$ and S is a surface given by $x = 2u, y = 2v, z = 5 - u^2 - v^2$, where $u^2 + v^2 \leq 1$. S has downward orientation.
4. Compute the flux of the vector field $\mathbf{F} = x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$ over the part of the cylinder $x^2 + y^2 = 4$ that lies between the planes $z = 0$ and $z = 2$ with normal pointing away from the origin. Assume the cylinder is closed (it has a top and a bottom).
5. Let S be the surface defined as $z = 4 - 4x^2 - y^2$ with $z \geq 0$ and oriented upward. Let $\mathbf{F} = \langle x - y, x + y, ze^{xy} \rangle$. Compute $\iint_S \text{curl } \mathbf{F} \cdot d\mathbf{S}$. (*Hint*: use one of the theorems you learned in class.)
6. Evaluate $\int_C (x^4 y^5 - 2y)dx + (3x + x^5 y^4)dy$ where C is the curve below and C is oriented in clockwise direction.



7. Let S be the boundary surface of the region bounded by $z = \sqrt{36 - x^2 - y^2}$ and $z = 0$, with outward orientation. Find $\iint_S \mathbf{F} \cdot d\mathbf{S}$, where $\mathbf{F} = x\mathbf{i} + y^2\mathbf{j} - 2yz\mathbf{k}$.
8. Let C be the boundary curve of the part of the plane $x + y + 2z = 2$ in the first octant. C has counterclockwise orientation when viewing from above. Compute $\int_C \mathbf{F} \cdot d\mathbf{r}$, where $\mathbf{F} = \langle e^{\sin x^2}, z, 3y \rangle$.
9. (*A Challenging Problem*) Evaluate

$$\int_C (y^3 + \cos x)dx + (\sin y + z^2)dy + x dz$$

where C is the closed curve parametrized by $\mathbf{r}(t) = \langle \cos t, \sin t, \sin 2t \rangle$ with counterclockwise direction when viewed from above. (*Hint*: the curve C lies on the surface $z = 2xy$.)