

- Derivatives of inverse one-to-one functions: $(f^{-1})'(a) = \frac{1}{f'(f^{-1}(a))}$

- L'Hospital's rule $0/0$ or ∞/∞ case: $\lim \frac{f(x)}{g(x)} = \lim \frac{f'(x)}{g'(x)}$

- Logarithmic and exponential functions. Recall the definition $\ln(x) = \int_1^x \frac{1}{t} dt$

$$\log_b(a) = \frac{\ln(a)}{\ln(b)} \quad \ln(ab) = \ln(a) + \ln(b) \quad \ln(a/b) = \ln(a) - \ln(b) \quad \ln(a^r) = r \ln(a)$$

$$\frac{d}{dx} \ln(x) = \frac{1}{x} \quad \frac{d}{dx} \log_b(x) = \frac{1}{x \ln(b)} \quad \frac{d}{dx} e^x = e^x \quad \frac{d}{dx} a^x = a^x \ln(a)$$

- Compound interest, continuously compounded interest (and exp growth), exp decay:

$$A(t) = A_0 \left(1 + \frac{r}{n}\right)^{nt} \quad A(t) = A_0 e^{rt} \quad A(t) = A_0 e^{-kt}$$

- Trig functions:

$$\begin{aligned} \frac{d}{dx} \sin(x) &= \cos(x) & \frac{d}{dx} \tan(x) &= \sec^2(x) & \frac{d}{dx} \sec(x) &= \sec(x) \tan(x) \\ \frac{d}{dx} \cos(x) &= -\sin(x) & \frac{d}{dx} \cot(x) &= -\csc^2(x) & \frac{d}{dx} \csc(x) &= -\csc(x) \cot(x) \end{aligned}$$

- Inverse trig functions:

$$\begin{aligned} \frac{d}{dx} \sin^{-1}(x) &= \frac{1}{\sqrt{1-x^2}} & \frac{d}{dx} \tan^{-1}(x) &= \frac{1}{1+x^2} & \frac{d}{dx} \sec^{-1}(x) &= \frac{1}{|x|\sqrt{x^2-1}} \\ \frac{d}{dx} \cos^{-1}(x) &= -\frac{1}{\sqrt{1-x^2}} & \frac{d}{dx} \cot^{-1}(x) &= -\frac{1}{1+x^2} & \frac{d}{dx} \csc^{-1}(x) &= -\frac{1}{|x|\sqrt{x^2-1}} \end{aligned}$$

- Integration by parts (in various but equivalent forms), with and without bounds:

$$\begin{aligned} \int uv' &= uv - \int u'v & \int u(x)v'(x)dx &= u(x)v(x) - \int u'(x)v(x)dx \\ \int u dv &= uv - \int v du & \int_a^b u(x)v'(x)dx &= u(x)v(x)|_a^b - \int_a^b u'(x)v(x)dx \end{aligned}$$

- Trig integrals:

$$\begin{aligned} \int \sec(x)dx &= \ln |\sec(x) + \tan(x)| + C & \int \tan(x)dx &= \ln |\sec(x)| + C \\ \int \csc(x)dx &= -\ln |\csc(x) + \cot(x)| + C & \int \cot(x)dx &= -\ln |\csc(x)| + C \end{aligned}$$

- Trig sub identities (choose the appropriate one as needed):

$$\cos^2 \theta = 1 - \sin^2 \theta \quad \tan^2 \theta + 1 = \sec^2 \theta \quad \tan^2 \theta = \sec^2 \theta - 1$$

- May save you time: $\int \ln(x)dx = x \ln(x) - x + C$