

**1a.** Find all critical points of the function  $f(x) = 3x^{2/3} - 2x$ .

$$f'(x) = \frac{2}{3} \cdot 3x^{-1/3} - 2 = 2x^{-1/3} - 2$$

Critical points are where the derivative is zero or undefined.  $f'(0)$  is undefined, so  $x = 0$  is a critical point. We also have:

$$\begin{aligned} f'(x) &= 2x^{-1/3} - 2 = 0 \\ x^{-1/3} &= 1 \\ x &= 1 \end{aligned}$$

Therefore the critical points are  $x = 0, 1$ .

**1b.** Find the absolute maximum and absolute minimum of  $f(x) = 3x^{2/3} - 2x$  for  $-1 \leq x \leq 1$ .

The absolute maximum and minimum occur at the critical points or at the endpoints of the interval.

$$\begin{aligned} f(-1) &= 3(-1)^{2/3} - 2(-1) = 3 + 2 = 5 \\ f(0) &= 3(0)^{2/3} - 2(0) = 0 - 0 = 0 \\ f(1) &= 3(1)^{2/3} - 2(1) = 3 - 2 = 1 \end{aligned}$$

Therefore the absolute maximum is 5 and the absolute minimum is 0.