# Machine Intelligence:: Deep Learning Week 7

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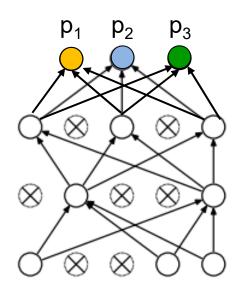
Part I: Preliminary, might change slightly before lecture

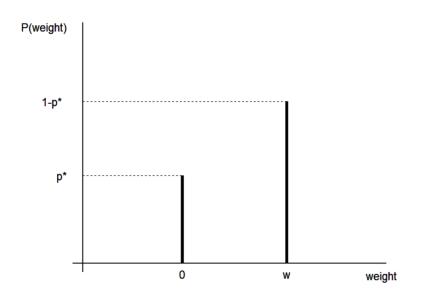
Winterthur, 7. April. 2020

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# Dropout

#### Recall: Classical Dropout only during training

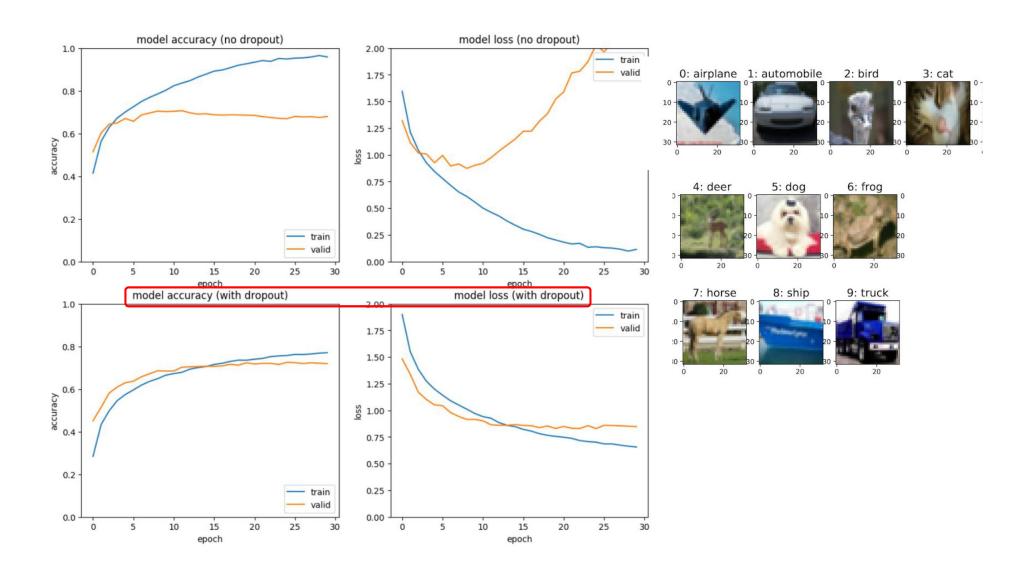




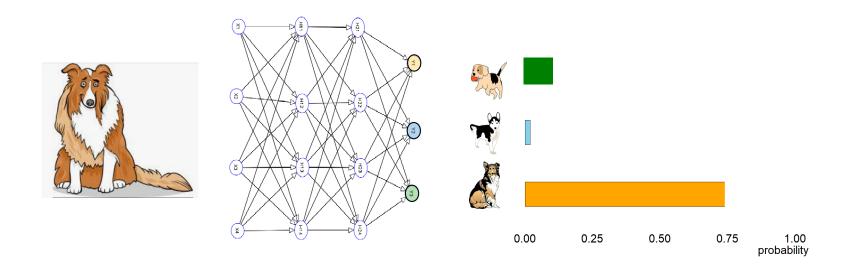
#### Using dropout during training implies:

- In each training step only weights to not-dropped units are updated → we train a sparse sub-model NN
- For non-Bayesian NN we freeze the weights after training to a value  $w \cdot p^*$

#### Recall: Dropout fights overfitting in a CIFAR10 CNN



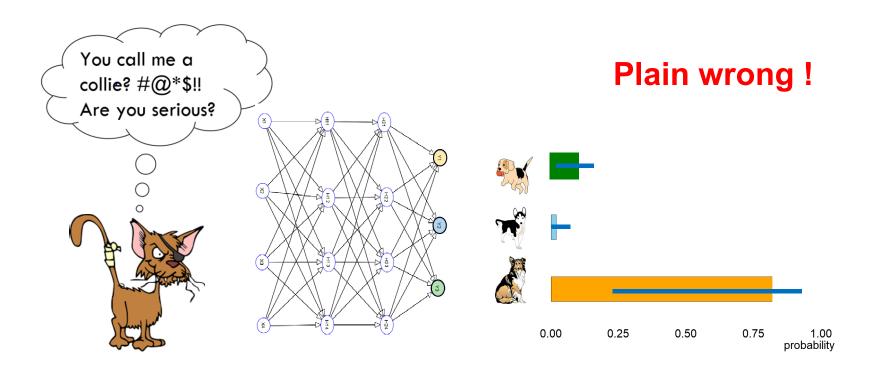
#### Recall: Nice properties of CNNs



CNNs yield high accuracy and calibrated probabilities, but...

### A non-Bayesian NN cannot ring the alarm

What happens if we present a novel class to the CNN?



We need some error bars!

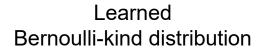
# From Dropout during training to MC Dropout during test time

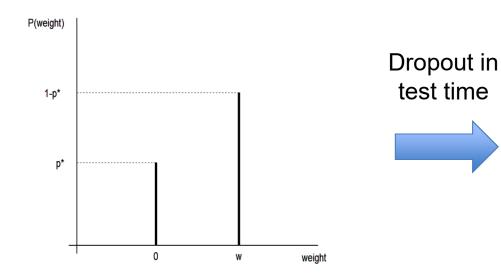
### Bayesian NN via MC Dropout

Yarin Gal et al. (2015):

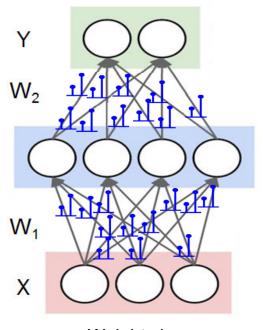
Via Dropout training we learned a whole weight distribution for each connection. We can sample from this Bernoulli-kind distribution by performing dropout during test time and use the dropout-trained NN as Bayesian NN.

Gal showed that doing dropout approximates VI with a Bernoulli-kind variational distribution (instead of a Gaussian).





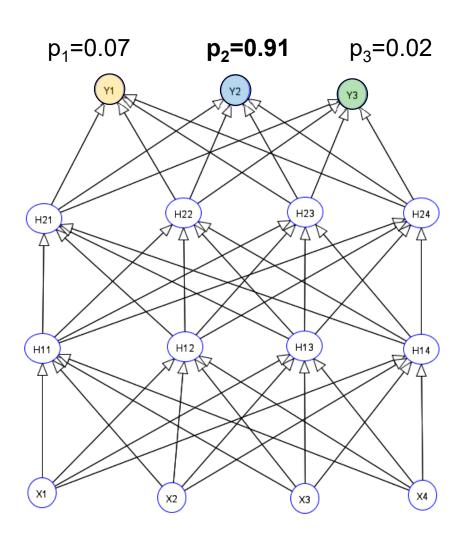
#### MC dropout NN



Weights have Bernoulli-kind distribution

### When using Dropout only during training

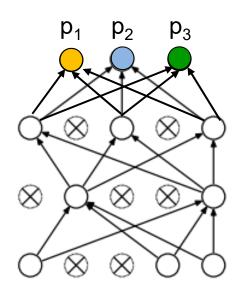
For non-Bayesian NN we freeze the weights after training to a value  $w \cdot p^*$  and use then the trained NN for prediction:

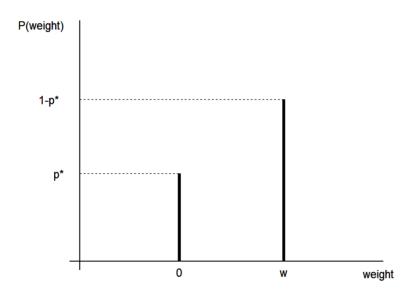


Probability of predicted class: **p**<sub>max</sub>

Input: image pixel values

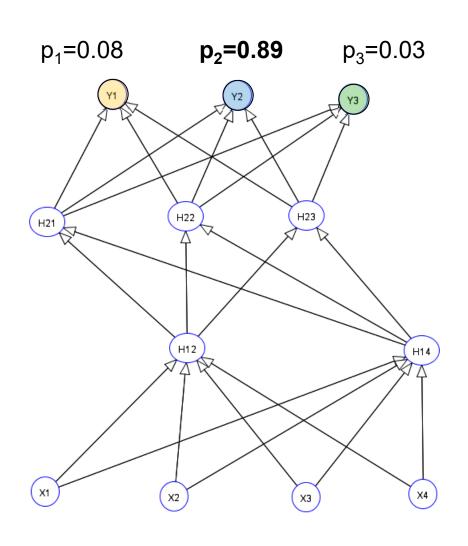
#### Recall: Classical Dropout only during training

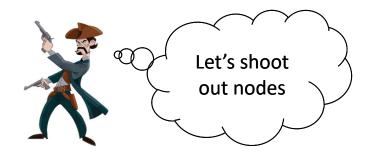




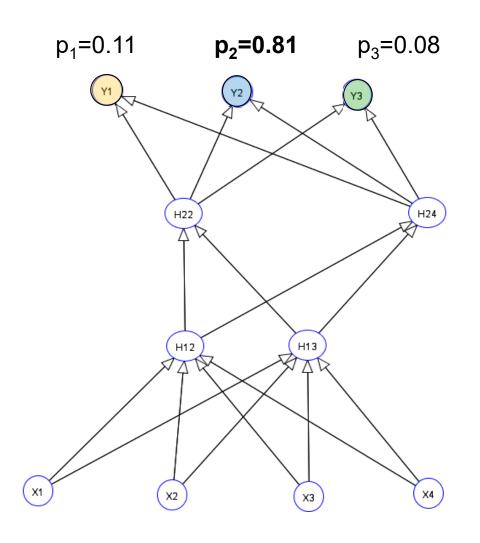
#### Using dropout during training implies:

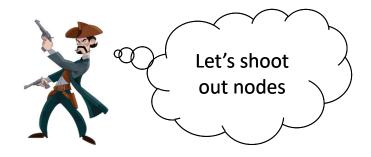
- In each training step only weights to not-dropped units are updated → we train a sparse sub-model NN
- For non-Bayesian NN we freeze the weights after training to a value  $w \cdot p^*$



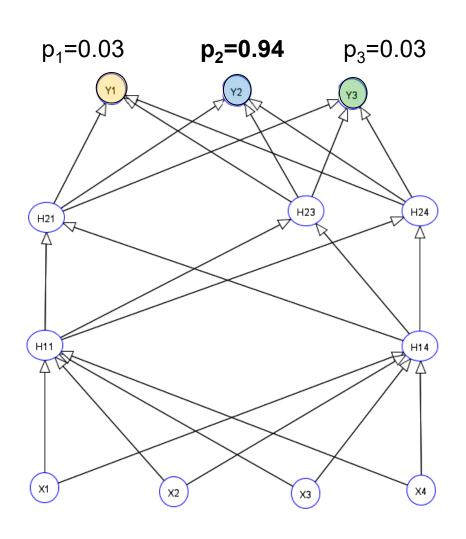


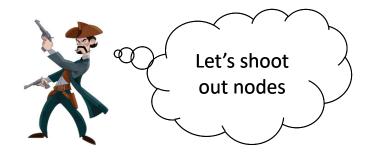
Stochastic dropout of units



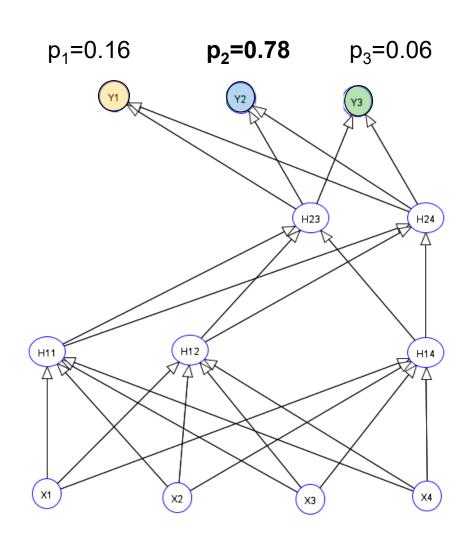


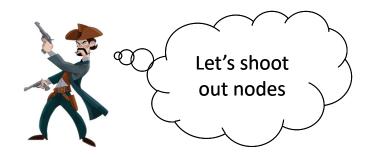
Stochastic dropout of units





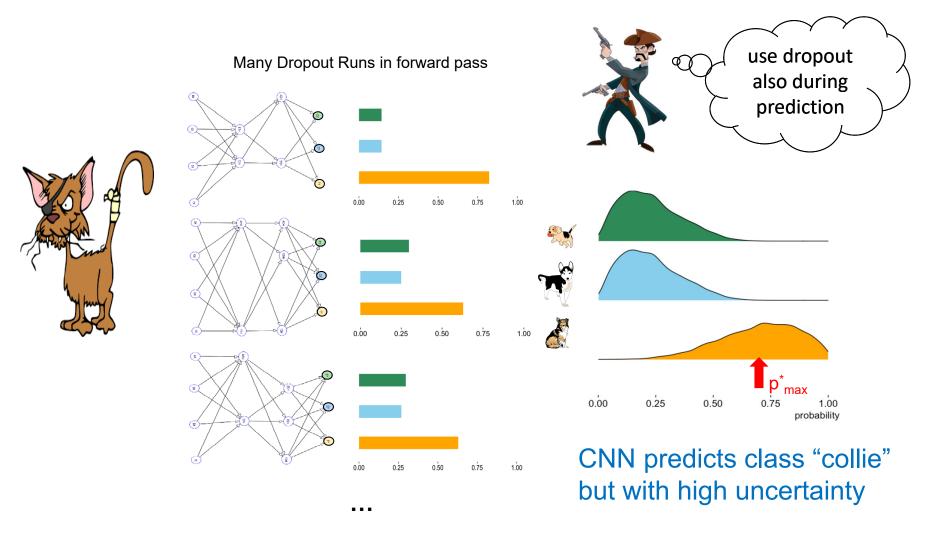
Stochastic dropout of units





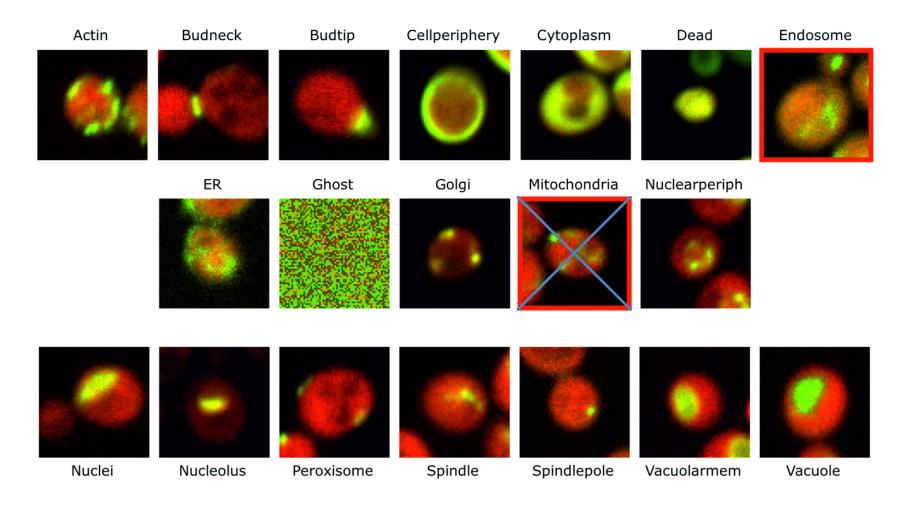
Stochastic dropout of units

# MC Dropout during test time yields a multivariate predictive distribution for the parameters



Remark: Mean of marginal give components of mean in multivariate distribution.

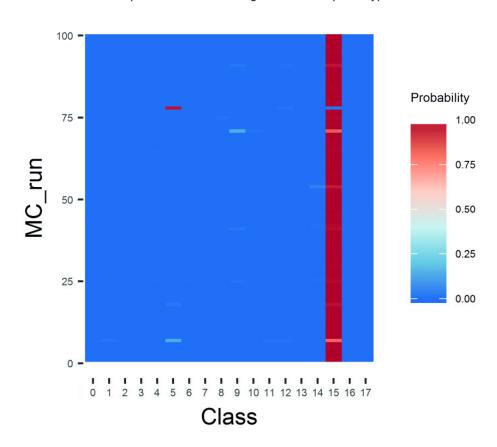
## Experiment with unknown phenotype



## Probability distribution from MC dropout runs

#### Image with known class 15

100 MC predictions for an image with known phenotype 15



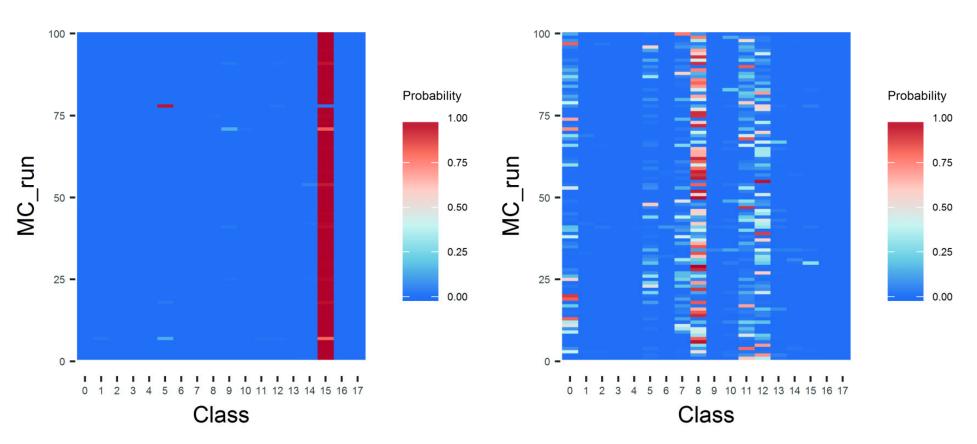
### Probability distribution from MC dropout runs

#### Image with known class 15

100 MC predictions for an image with known phenotype 15

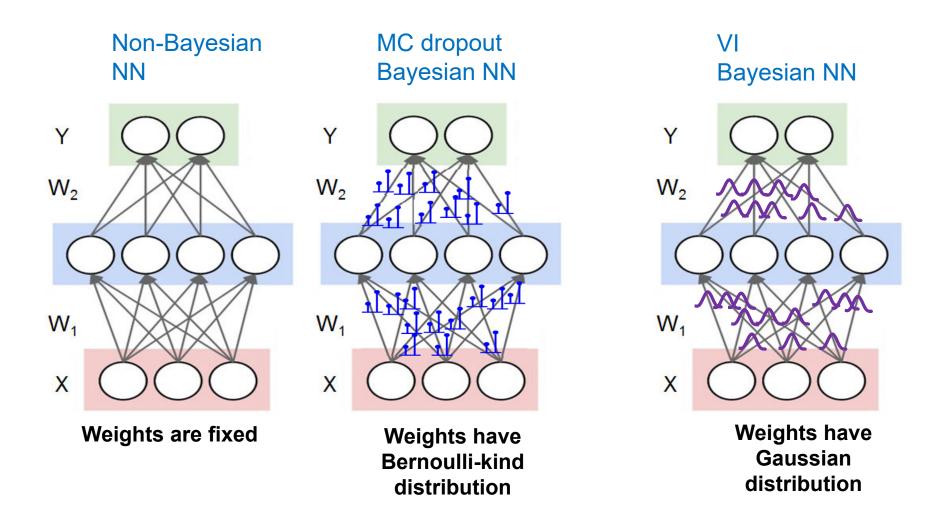
#### Image with unknown class

100 MC predictions for an image with an unknown phenotype

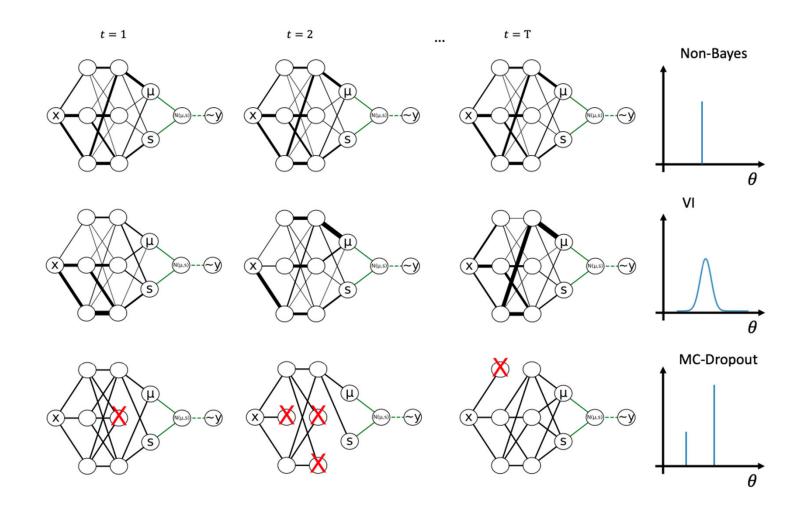


# Comparing non-Bayesian with Bayesian NN

### Non-Bayesian and Bayesian NNs



#### Comparing different Network types

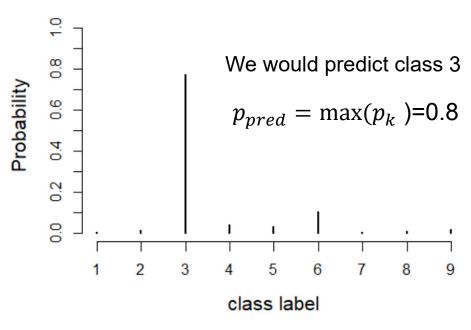


A Non-Baysian NN learns one set of weights: the same input same output A Bayesian NN learns distribution of weights: same input different outputs

# Uncertainty measures in classification

#### Uncertainty in non-Bayesian classification

# Multinomial CPD $MN(p_1(x, w), p_2(x, w), ..., p_9(x, w))$



In a non-Bayesian NN we make for each input x ONE CPD:

Image x
MN(p1(x,w), ..., p9(x,w))

#### **Uncertainty** measures capturing the **aleatoric** uncertainty:

Negative log-Likelihood:  $NLL = -\log(p_{pred})$ 

Entropy:  $H = -\sum_{k=1}^{9} p_k \cdot \log(p_k)$ 

#### Uncertainty in Bayesian classification

In a Bayesian NN we sample T-times from the weight distributions and get each time a slightly different multinomial CPD

predict_no	Image x
1	MN(p1(x,w1),, p9(x,w1))
2	MN(p1(x,w2),, p9(x,w2))
•••	
Т	MN(p1(x,wT),, p9(x,wT))

For each class k  $(k \in \{1,2,...,9\})$  we determine the mean probability:  $p_k^* = \frac{1}{T} \sum_{i=1}^T p_{k_i}$ 

The predicted class has the highest mean probability:  $p_{pred}^* = \max(p_k^*)$ 

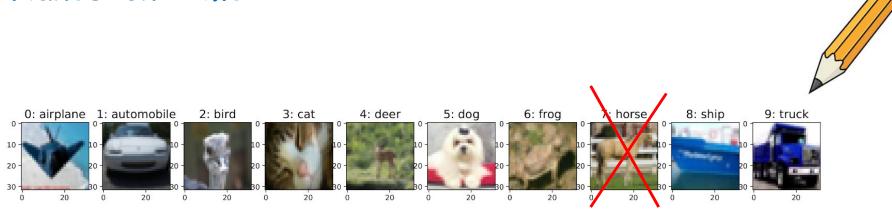
#### Uncertainty measures including aleatoric and epistemic contributions:

Negative log-Likelihood:  $NLL^* = -\log(p_{pred}^*)$ 

Entropy:  $H^* = -\sum_{k=1}^9 p_k^* \cdot \log(p_k^*)$ 

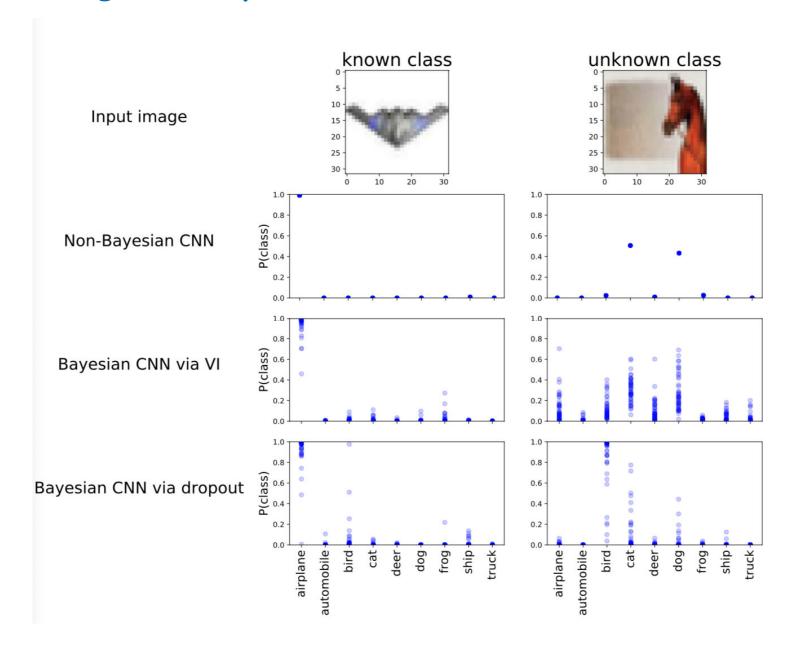
Total variance:  $V_{tot} = \sum_{k=1}^{9} var(p_k) = \sum_{k=1}^{9} \sum_{i=1}^{T} (p_{kt} - p_k^*)^2$ 

#### Hands-on Time

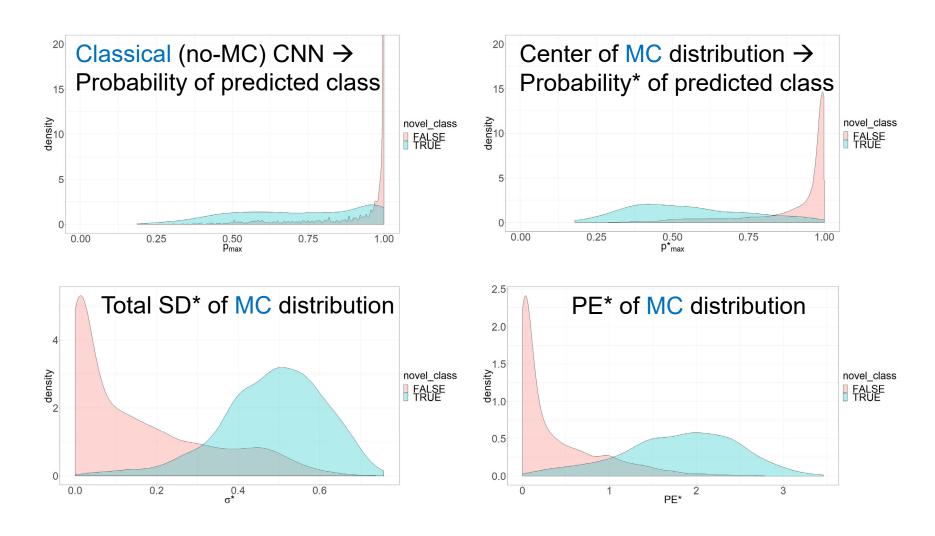


Train a CNN with only 9 of the 10 classes and investigate if the uncertainties are different when predicting images from known or unknown classes.

#### Looking at the predictive distribution!



# Do known/novel classes yield different values for probability and uncertainty measures?

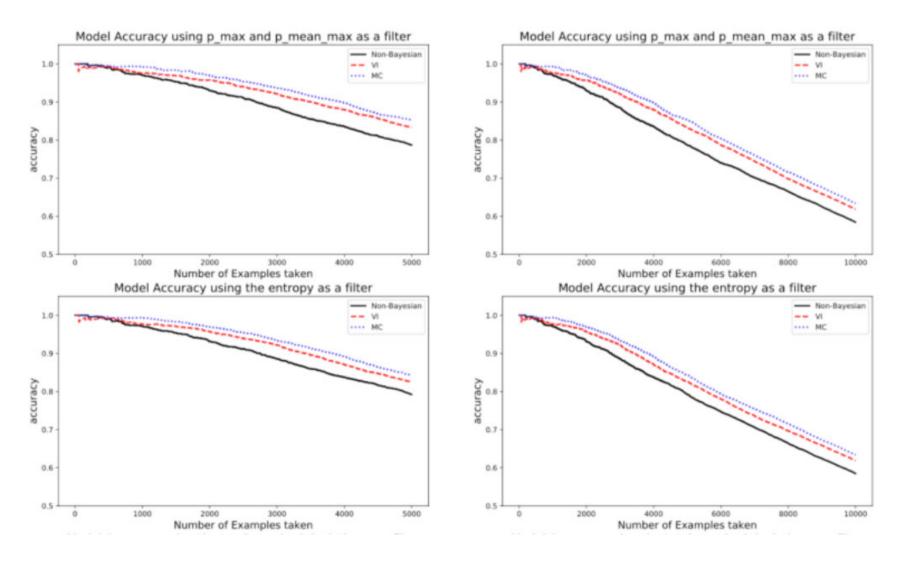


#### Filtering experiment based on uncertainty

Goal: Get higher accuracy by filter only predictions which are quite certainly correct

- Each prediction has an attached uncertainty measure
- Sort predictions according to the uncertainty measures
- The prediction with lowest uncertainty should yield highest prediction performance
- By successively adding predictions with increasing uncertainties should yield an decreasing prediction performance (e.g. accuracy)

#### Filtering experiment to compare uncertainty measures



Uncertainty from non-Bayesian NN is less good in identifying wrong classifications than uncertainty measures from Bayesian variants of the NN.

# Uncertainty measures in regression

#### Uncertainty in non-Bayesian NN

We do predictions for 400 x-values between -10 and 30 yielding for each x a Gaussian CPD.

x1= -10	x2= -9.9		x400= 30		
$N\left(\mu_{x_{1,w}},\sigma_{x_{1,w}}\right)$	$N\left(\mu_{x_{2,w}},\sigma_{x_{2,w}}\right)$		$N\left(\mu_{x_{400,w}},\sigma_{x_{400,w}}\right)$		

#### **Uncertainty** measures capturing the **aleatoric** uncertainty at *x*:

Standard deviation:  $\sigma_x$ 

95% CI:  $\mu_x \pm 1.96 \cdot \sigma_x$ 

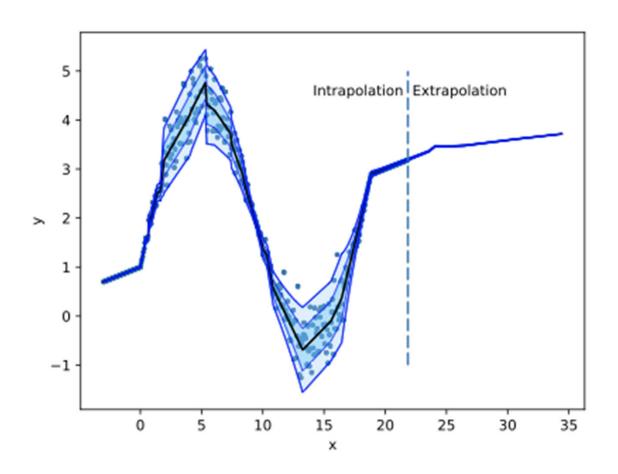
#### Remark:

We could also estimate the 95% CI at position x by sampling several times from the CPD and determine the 0.025 and 0.975 quantiles, yielding :

95% CI:  $[q_{0.025}; q_{0.975}]$ 

#### The problem of non-Bayesian NN

Problem:
A non-Bayesian NN does extrapolation with very small uncertainty



#### Uncertainty in Bayesian regression NN

In a Bayesian NN we sample T-times from the weight distributions and get each time a slightly different CPD. In regression the CPD is often Gaussian.

We do predictions for 400 x-values between -10 and 30 yielding in each of the T runs a different Gaussian CPD at each x-position.

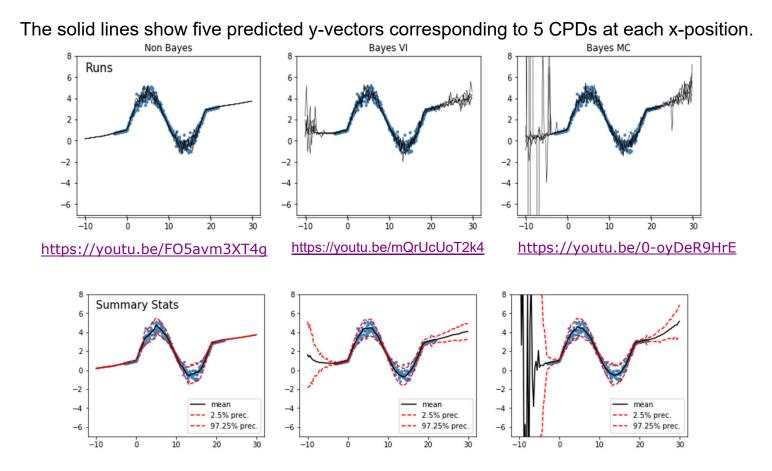
predict_no	x1= -10	x2= -9.9	 x400= 30
1	N(x1,w1,x1,w1)	N(x2,w1,x2,w1)	N(x400,w1,x400,w1)
2	N(x1,w2,x1,w2)	N(x2,w2,x2,w2)	N(x400,w2,x400,w2)
Т	N(x1,wT,x1,wT)	N(x2,wT,x2,wT)	N(x400,wT,x400,wT)

#### Uncertainty measures including aleatoric and epistemic contributions:

To estimate the 95% CI at position x by from each of the T CPDs and determine the 0.025 and 0.975 quantiles, yielding :

95% CI:  $[q_{0.025}; q_{0.975}]$ 

#### How Bayesian NN indicate uncertainty



#### Conclusion

- Standard neural networks (NNs) fail to express their uncertainty (can't talk about the elephant in the room).
- Bayesian neural networks (BNNs) can express their uncertainty.
- BNNs often yield better performance than their non-Bayesian variant.
- Novel classes can be better identified with BNNs, which combine epistemic and aleatoric uncertainties compared to standard NNs.
- Variational inference (VI) and Monte Carlo dropout (MC dropout) are approximation methods that allow you to fit deep BNNs.
- TFP provides easy to use layers for fitting a BNN via VI.
- MC dropout can be used in Keras for fitting BNNs.