

# SURF

## (SPEEDED UP ROBUST FEATURES)

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# Reference



- Herbert Bay, Tinne Tuytelaars, and Luc Van Gool. SURF: Speeded Up Robust Features. *European Conference on Computer Vision*, May 2006.

# Introduction



- Search for image correspondences
  - ▣ Detection
    - Interest points – corners, blobs, and T-junctions
    - Repeatability
  - ▣ Description
    - Descriptor – represented by a feature vector
    - Distinctive, robust
  - ▣ Matching
    - Based on distance between feature vectors

# Introduction



- Interest Point Detectors

- Harris corner detector
- Harris-Laplace and Hessian-Laplace
- DoG (Difference of Gaussians)

- Feature Descriptors

- SIFT : Histogram of local oriented gradients around the interest point, 128-dimension
- PCA-SIFT : 36-dimension

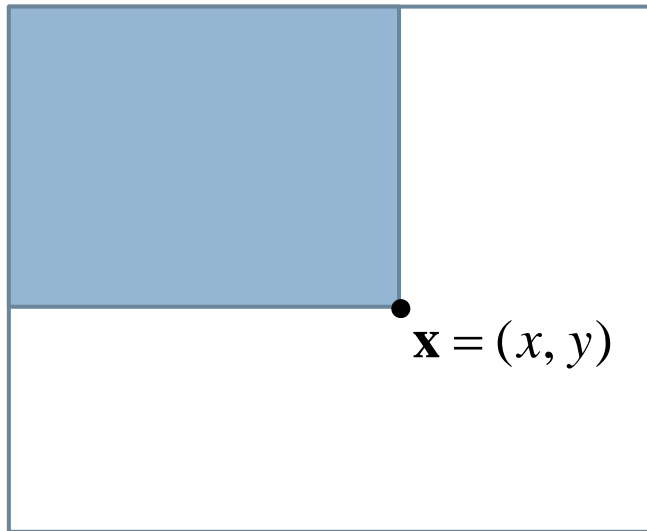
# SURF



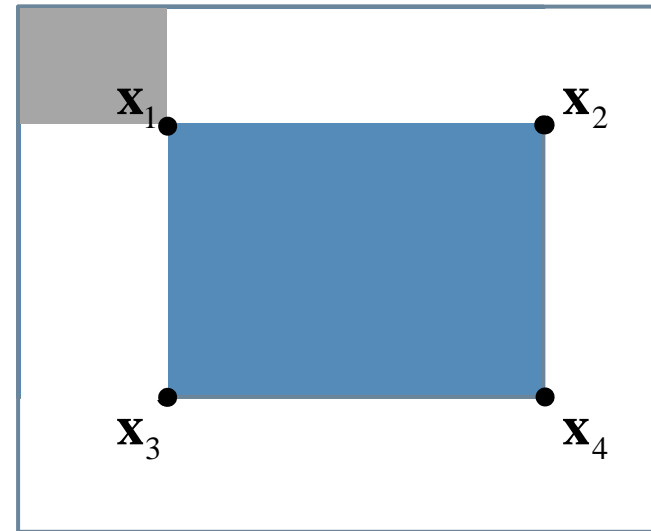
- Integral Image
- Detector
  - ▣ Approximated Hessian-based detector
- Descriptor
  - ▣ Based on distribution of Haar-wavelet responses within the interest point neighborhood
  - ▣ 64 dimensions
- Matching
  - ▣ New indexing step based on the sign of the Laplacian

# SURF

## □ Integral Image



$$I_{\Sigma}(\mathbf{x}) = \sum_{i=0}^{i \leq x} \sum_{j=0}^{j \leq y} I(i, j)$$

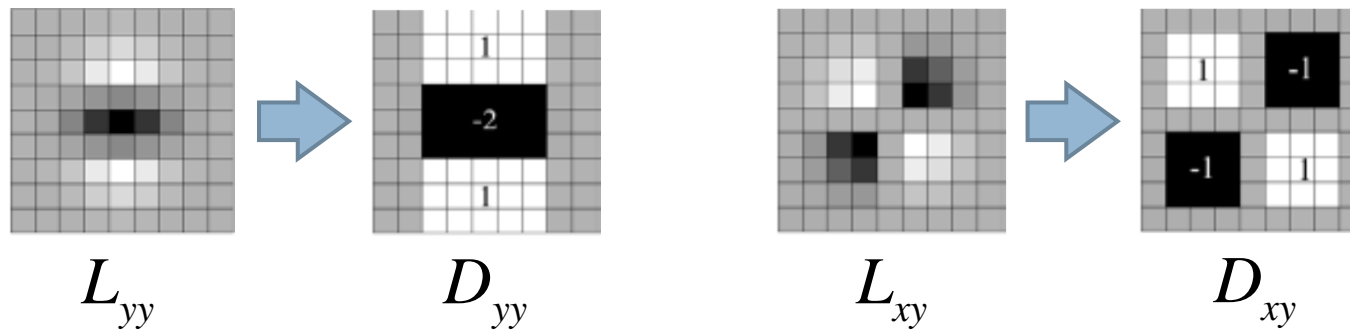


$$I_{\Sigma}(\mathbf{x}_4) - I_{\Sigma}(\mathbf{x}_3) - I_{\Sigma}(\mathbf{x}_2) + I_{\Sigma}(\mathbf{x}_1)$$

# SURF – Detector

## □ Hessian matrix

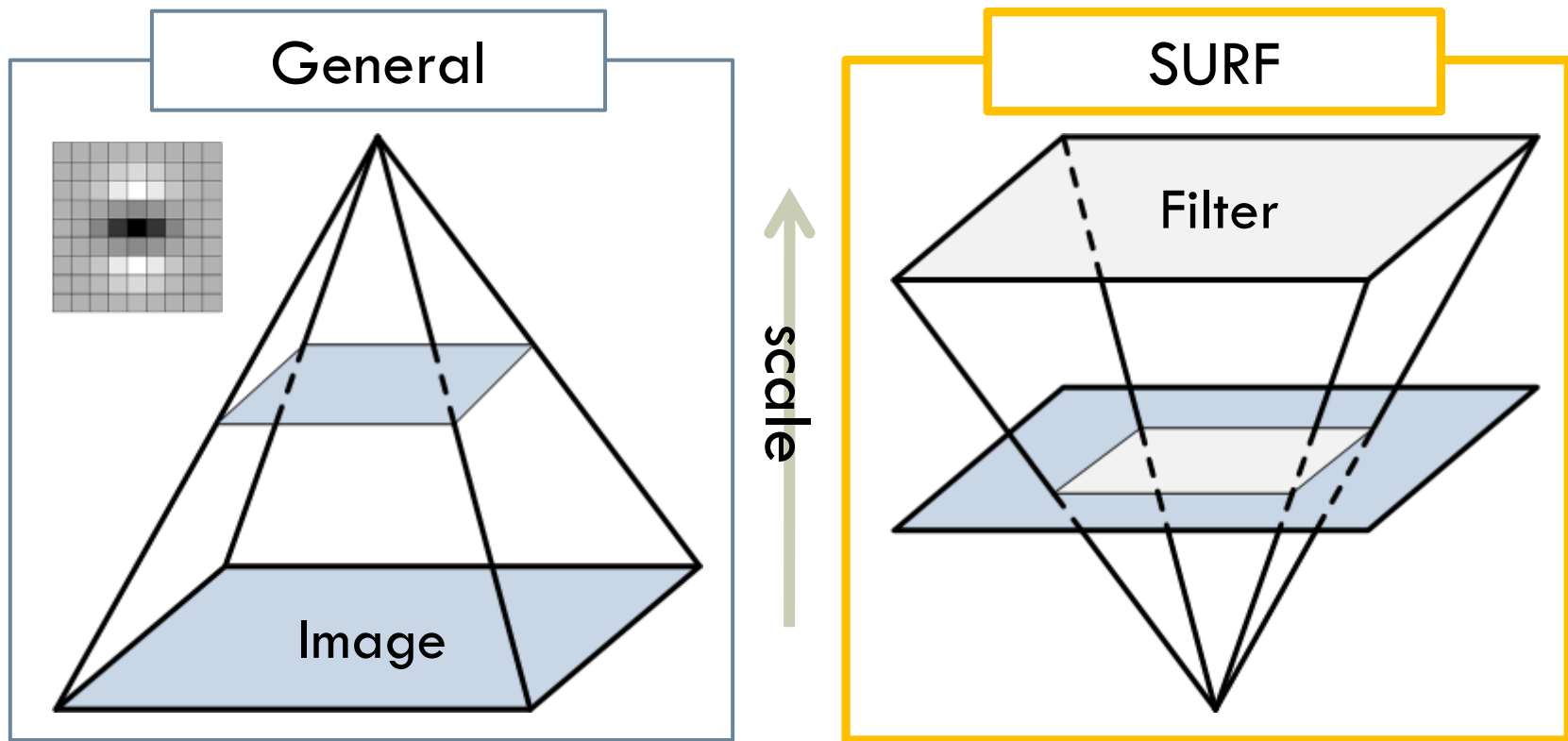
$$\square \quad H(\mathbf{x}, \sigma) = \begin{bmatrix} L_{xx}(\mathbf{x}, \sigma) & L_{xy}(\mathbf{x}, \sigma) \\ L_{xy}(\mathbf{x}, \sigma) & L_{yy}(\mathbf{x}, \sigma) \end{bmatrix}, \quad L_{xx}(\mathbf{x}, \sigma) = \frac{\partial^2}{\partial x^2} g(\sigma)$$



$$\square \quad \det(H_{\text{approx}}) = D_{xx} D_{yy} - (0.9 D_{xy})^2$$

# SURF – Detector

## □ Scale-space



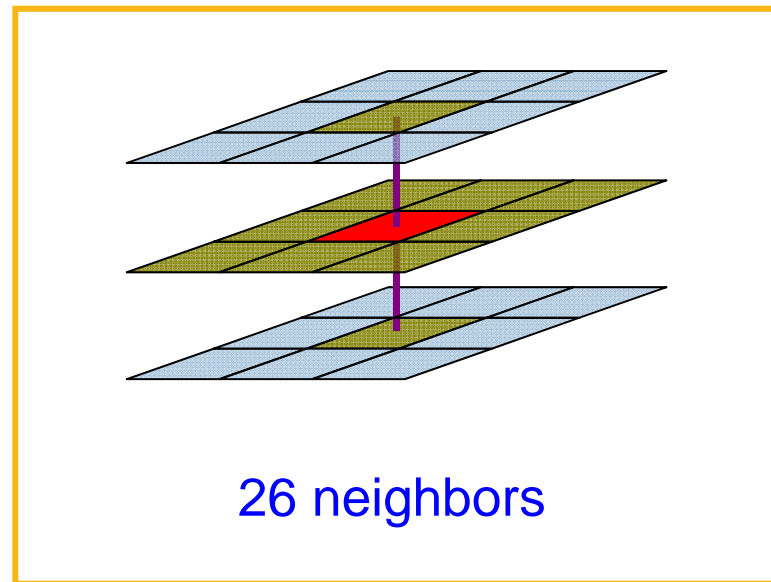
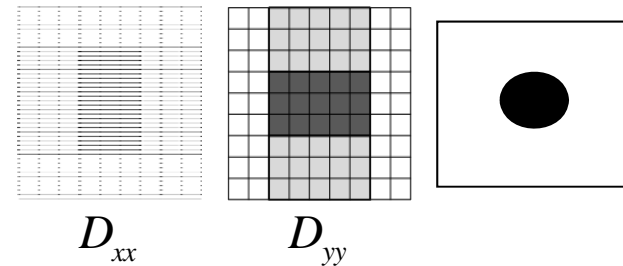


# SURF – Detector

- Local maximum detection

- Blob-like features

- $\det(H_{\text{approx}}) = D_{xx}D_{yy} - (0.9D_{xy})^2$



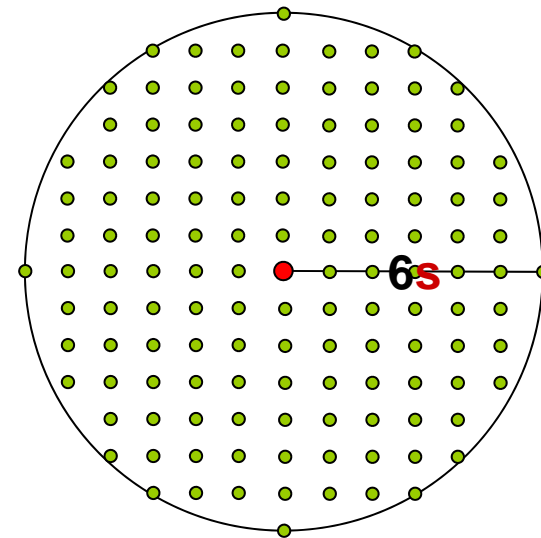
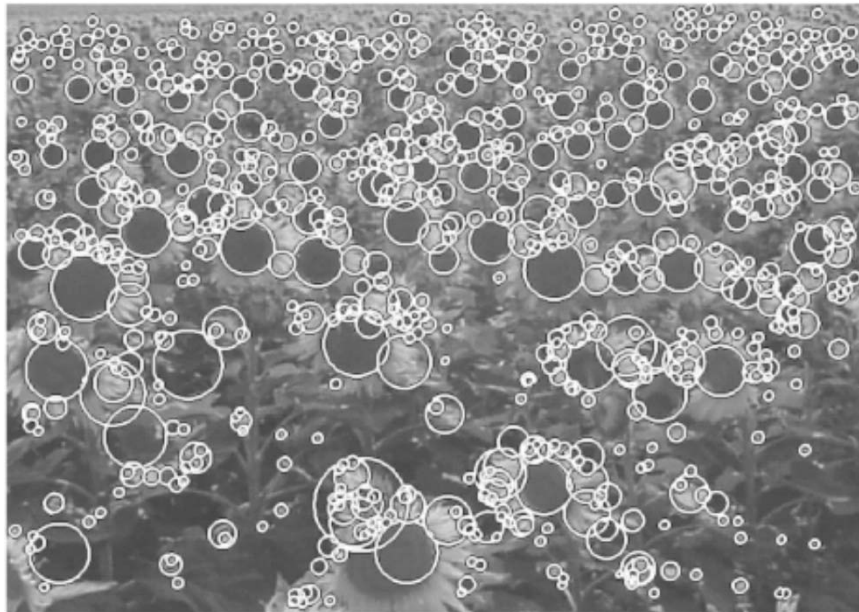
# SURF – Descriptor



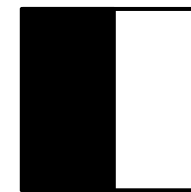
- Two steps
  1. Orientation Assignment
  2. Descriptor Components

# SURF – Descriptor

## □ Orientation Assignment



( $s$  = the scale at which the point was detected)



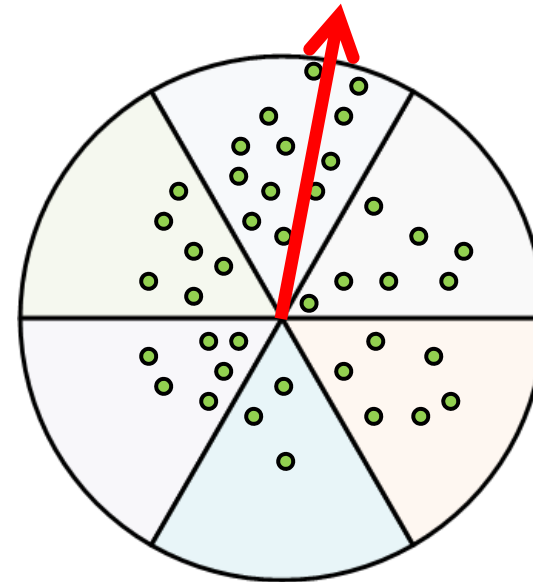
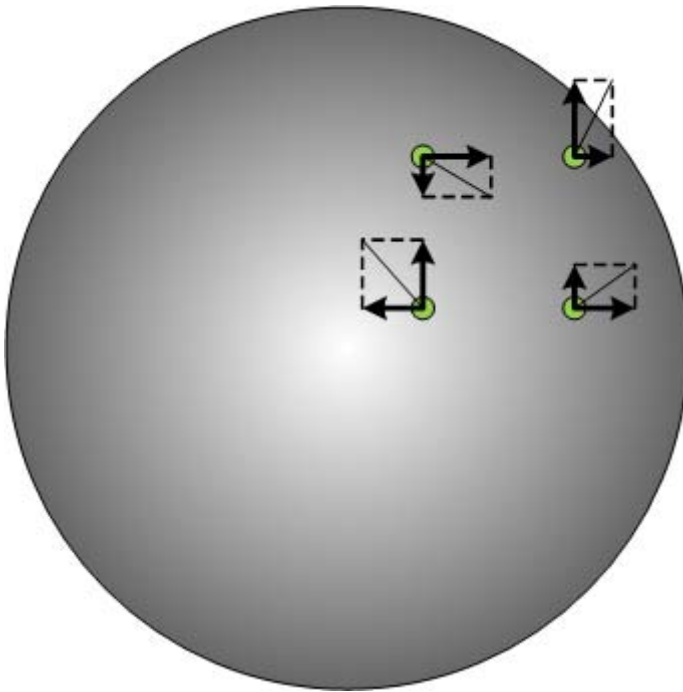
x response



y response

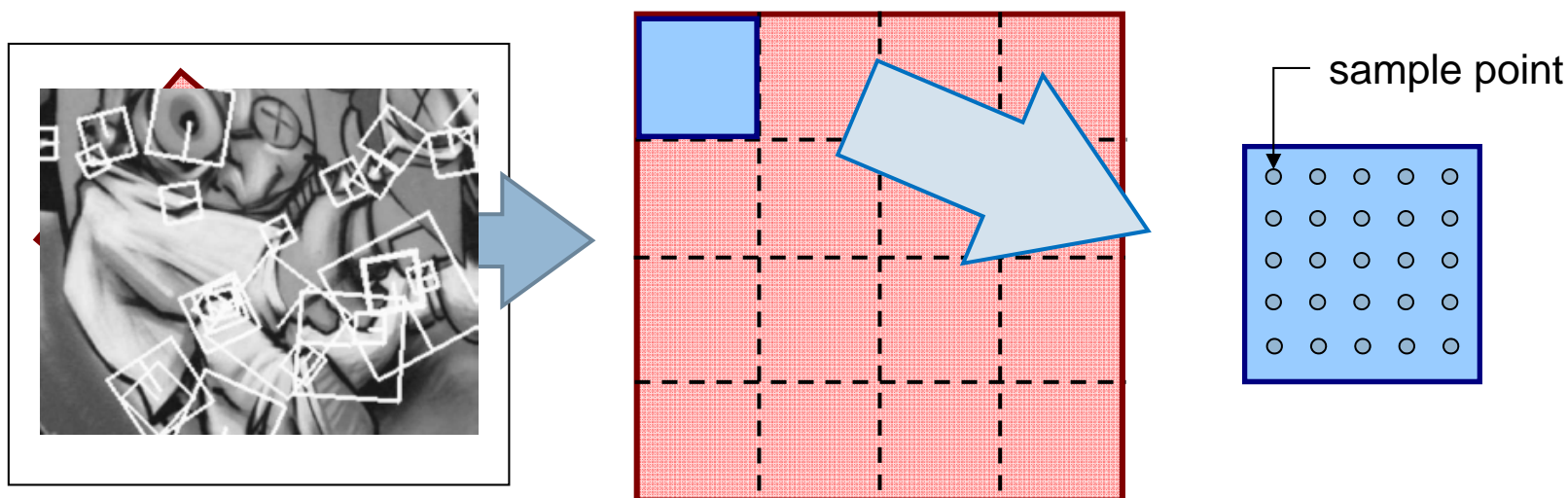
# SURF – Descriptor

## □ Orientation Assignment



# SURF – Descriptor

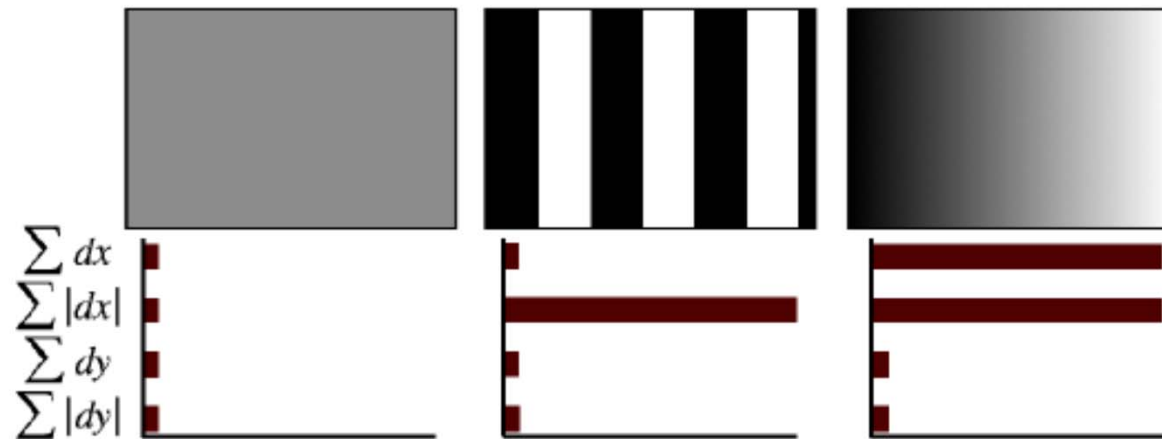
## □ Descriptor Components



- At **sample point**, calculate  $d_x$ ,  $d_y$ ,  $|d_x|$ , and  $|d_y|$
- At **each sub-region**,  $\mathbf{v} = (\sum d_x, \sum d_y, \sum |d_x|, \sum |d_y|)$
- A **descriptor vector** for all 4x4 sub-regions of length 64

# SURF – Descriptor

- Descriptor Components
  - ▣ Properties of the descriptor



# SURF – Matching

- Based on the sign of the Laplacian

- Laplacian

- $|s^2(L_{xx}(\mathbf{x}, s) + L_{yy}(\mathbf{x}, s))|$
    - The trace of the Hessian matrix
    - Computed during the detection phase

- Type



- Compare features if they have the same type

- Euclidean distance

- $\|\mathbf{p}_{1,n} - \mathbf{p}_{2,n'}\| < 0.7 \times \|\mathbf{p}_{1,n} - \mathbf{p}_{2,n''}\|$

# Experimental Results

## □ Environments

- # of octaves : 1

  - No scale variant

- # of layers : 4

  - Sigma : 1.2, 2.0, 2.8, 3.6

- Threshold : 600 (database), 100 or 150 (previous real image)

- Matching constraint

  - $\| \mathbf{p} - \mathbf{p}_{1^{st} \text{ cand.}} \| < 0.5 \| \mathbf{p} - \mathbf{p}_{2^{nd} \text{ cand.}} \|$



# 1<sup>st</sup> Test Image (517 x 374)

□ Threshold : 600

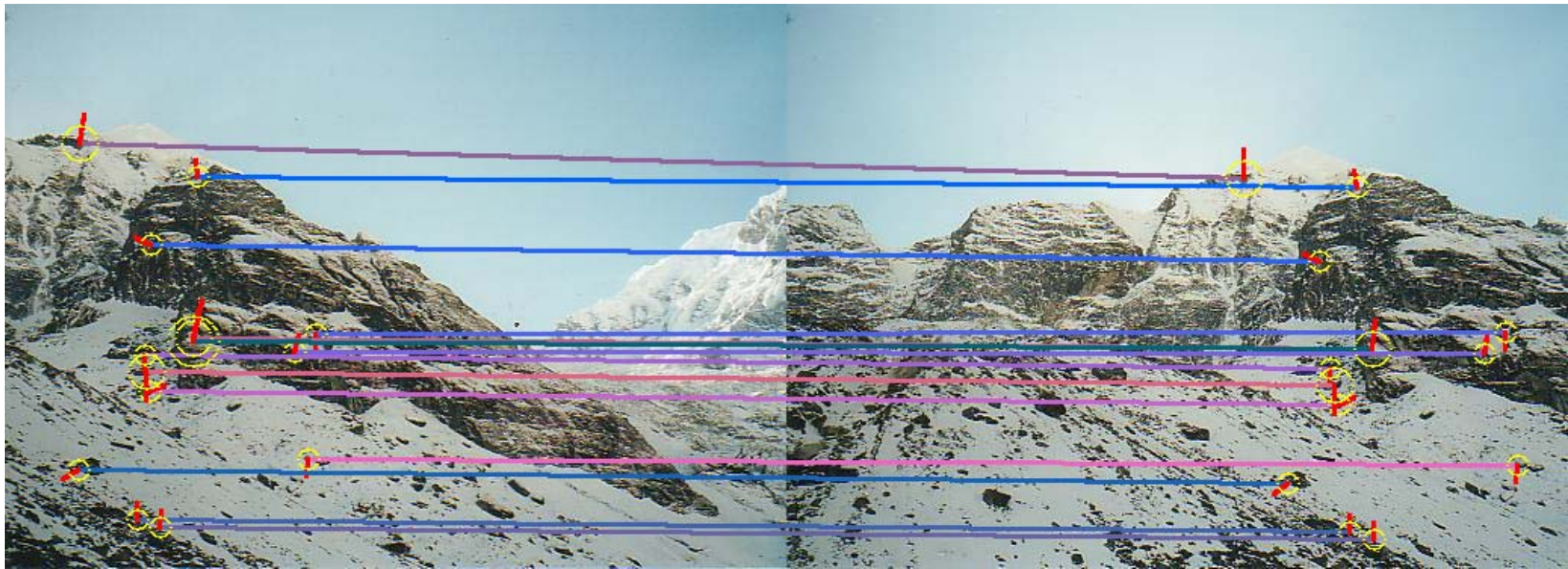


# 1<sup>st</sup> Test Image (517 x 374)





# 1<sup>st</sup> Test Image (517 x 374)



## 2<sup>nd</sup> Test Image (800 x 640)

- Threshold : 600





## 2<sup>nd</sup> Test Image (800 x 640)



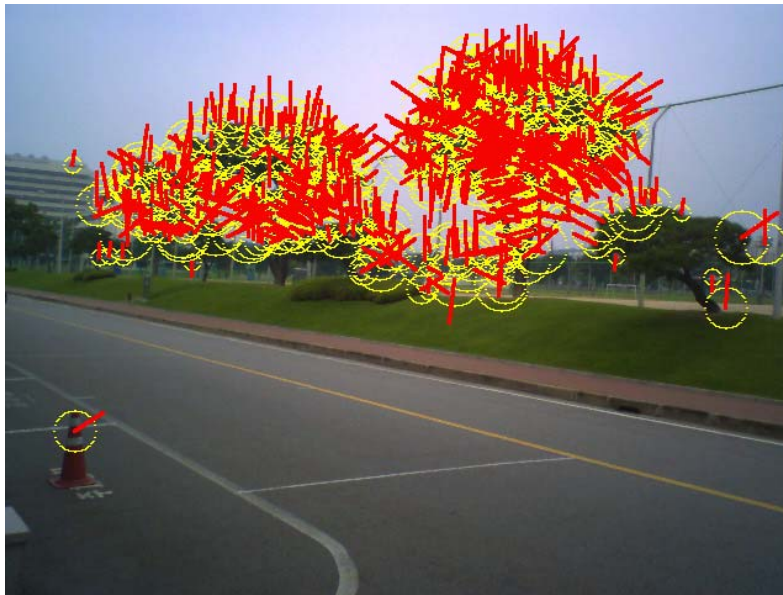
## 2<sup>nd</sup> Test Image (800 x 640)



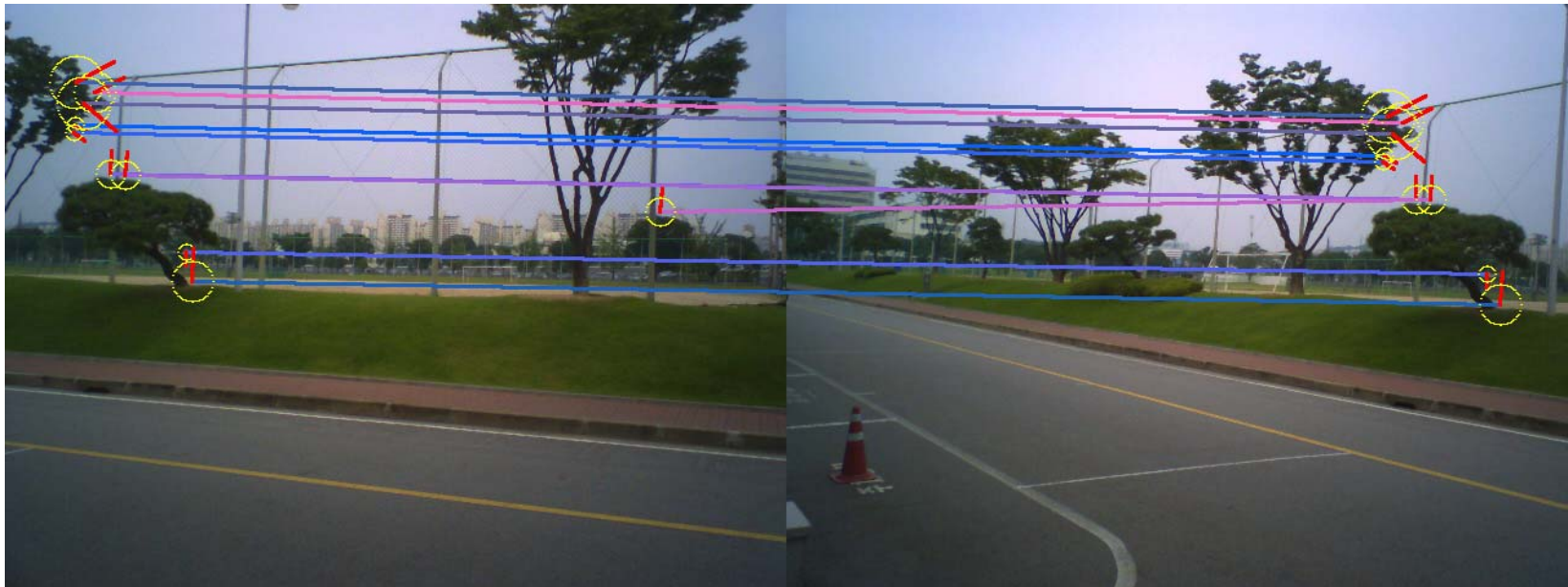


# 3<sup>rd</sup> Test Image (640 x 480)

□ Threshold : 150



# 3<sup>rd</sup> Test Image (640 x 480)

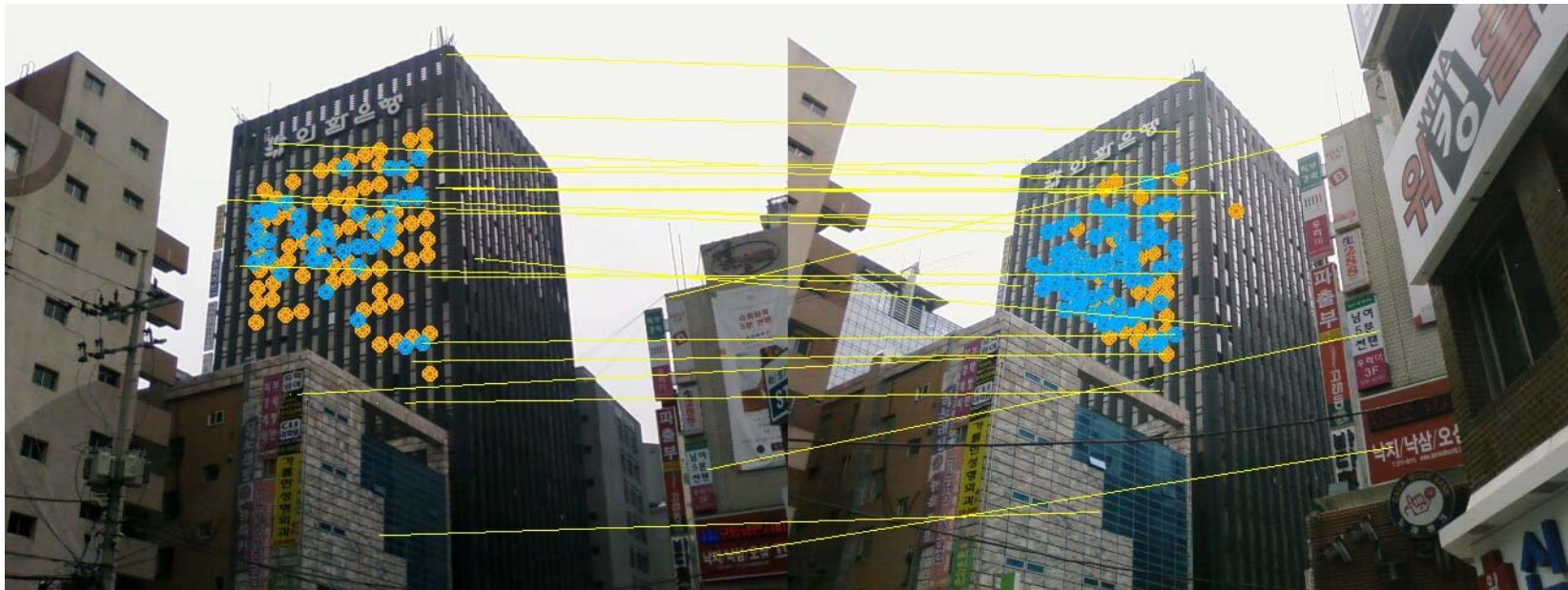




# 4<sup>th</sup> Test Image (640 x 480)

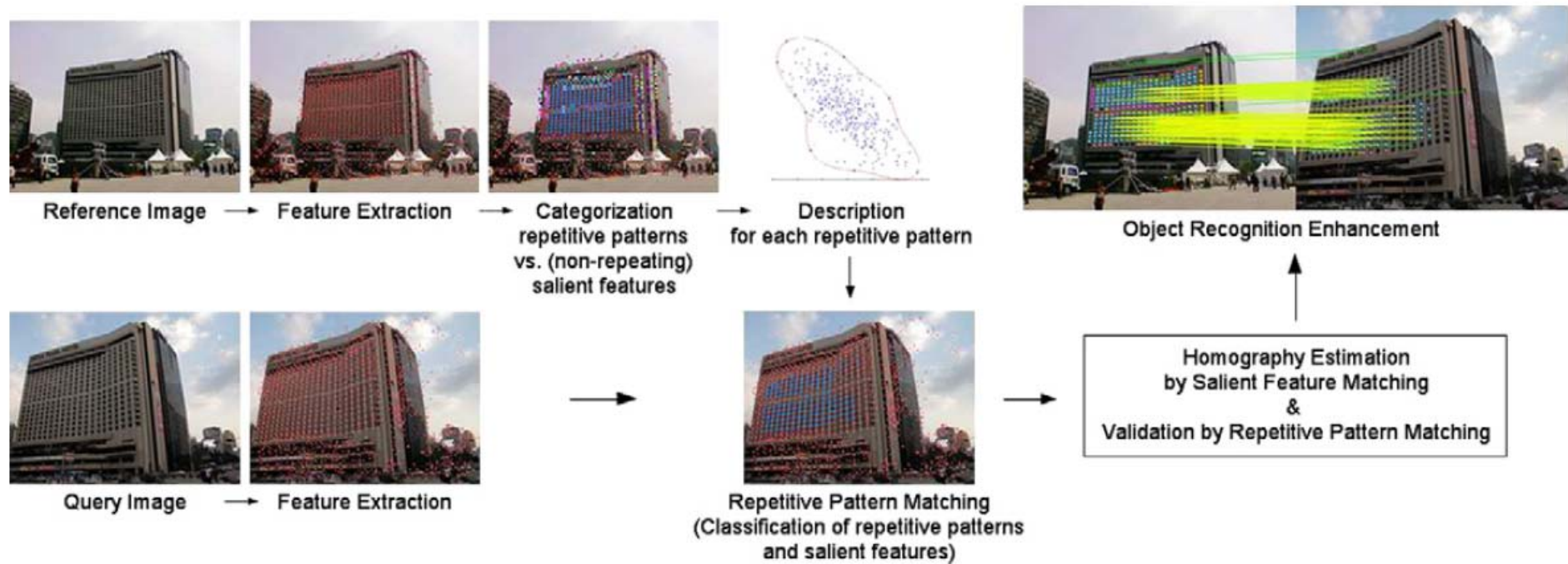


# Problems of Repetitive Pattern (1)



Mismatching results by repetitive pattern in the building image

# Problems of Repetitive Pattern (2)



Grouping the repetitive pattern and recognition