

smai_assignment_2_q_1_2_report

April 8, 2018

0.1 CNN Computations on Cifar-10 Dataset

Load Cifar-10 data Downloading data from <https://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz>
170500096/170498071 [=====] - 16s 0us/step

Training Data

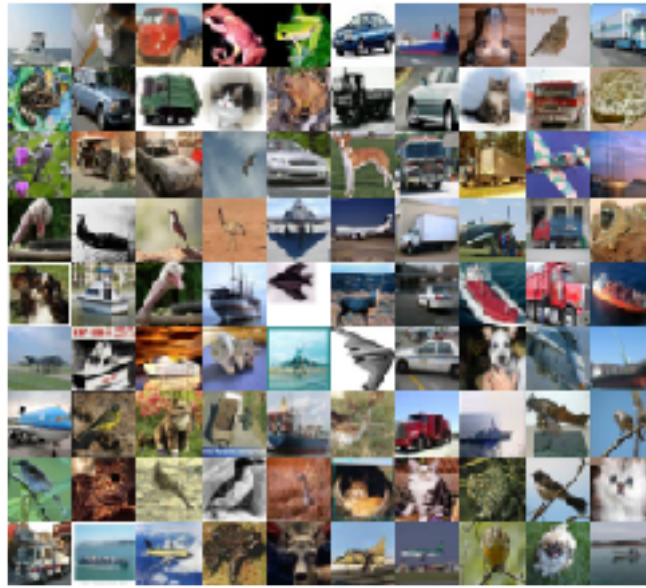
In [3]:

```
Training data:
Number of examples: 50000
Number of channels: 3
Image size: 32 32
```

```
Test data:
Number of examples: 10000
Number of channels: 3
Image size: 32 32
```

Visualize some images from CIFAR-10 dataset. It contains 10 classes namely, airplane, automobile, bird, cat, deer, dog, frog, horse, ship, truck

In [5]:



Normalize the data.

In [4]:

```
mean before normalization: 120.70756512369792
std before normalization: 64.1500758911213
mean after normalization: 4.91799193961621e-17
std after normalization: 0.9999999999999996
```

Training Parameters Training Batch Size (batchSize) = 50
 Number of classes in CIFAR-10 dataset (num_classes) = 10
 Number of epochs for training (num_epochs) = 50
 Learning rate for the network (learningRate) = 0.001
 Learning weight decay. Reduce the learn rate by 0.95 after epoch (lr_weight_decay) = 0.95
 input image dimensions (img_rows, img_cols) = 32, 32

Model Summary

In [7]:

Layer (type)	Output Shape	Param #
conv2d_1 (Conv2D)	(None, 28, 28, 6)	456

```

activation_1 (Activation)      (None, 28, 28, 6)          0
-----
max_pooling2d_1 (MaxPooling2) (None, 14, 14, 6)          0
-----
conv2d_2 (Conv2D)              (None, 10, 10, 16)        2416
-----
activation_2 (Activation)      (None, 10, 10, 16)          0
-----
max_pooling2d_2 (MaxPooling2) (None, 5, 5, 16)          0
-----
flatten_1 (Flatten)           (None, 400)                 0
-----
dense_1 (Dense)                (None, 120)                 48120
-----
activation_3 (Activation)      (None, 120)                 0
-----
dense_2 (Dense)                (None, 84)                 10164
-----
activation_4 (Activation)      (None, 84)                 0
-----
dense_3 (Dense)                (None, 10)                 850
-----
activation_5 (Activation)      (None, 10)                 0
=====
Total params: 62,006
Trainable params: 62,006
Non-trainable params: 0
-----
None

```

Compile and then train the network

In [8]:

Train on 50000 samples, validate on 10000 samples

Epoch 1/50

50000/50000 [=====] - 41s 814us/step - loss: 1.8241 - acc: 0.3356 - va

Epoch 2/50

50000/50000 [=====] - 41s 819us/step - loss: 1.5212 - acc: 0.4504 - va

Epoch 3/50

50000/50000 [=====] - 43s 869us/step - loss: 1.4198 - acc: 0.4907 - va

Epoch 4/50

50000/50000 [=====] - 40s 810us/step - loss: 1.3469 - acc: 0.5191 - va

Epoch 5/50

50000/50000 [=====] - 40s 803us/step - loss: 1.2902 - acc: 0.5398 - va

Epoch 6/50

50000/50000 [=====] - 41s 813us/step - loss: 1.2395 - acc: 0.5626 - va

```

Epoch 7/50
50000/50000 [=====] - 42s 830us/step - loss: 1.2048 - acc: 0.5757 - va
Epoch 8/50
50000/50000 [=====] - 42s 842us/step - loss: 1.1703 - acc: 0.5872 - va
Epoch 9/50
50000/50000 [=====] - 42s 848us/step - loss: 1.1389 - acc: 0.5978 - va
Epoch 10/50
50000/50000 [=====] - 43s 857us/step - loss: 1.1129 - acc: 0.6054 - va
Epoch 11/50
50000/50000 [=====] - 43s 864us/step - loss: 1.0869 - acc: 0.6166 - va
Epoch 12/50
50000/50000 [=====] - 44s 871us/step - loss: 1.0665 - acc: 0.6247 - va
Epoch 13/50
50000/50000 [=====] - 45s 892us/step - loss: 1.0443 - acc: 0.6343 - va
Epoch 14/50
50000/50000 [=====] - 46s 923us/step - loss: 1.0234 - acc: 0.6400 - va
Epoch 15/50
50000/50000 [=====] - 46s 913us/step - loss: 1.0027 - acc: 0.6475 - va
Epoch 16/50
50000/50000 [=====] - 46s 924us/step - loss: 0.9853 - acc: 0.6554 - va
Epoch 17/50
50000/50000 [=====] - 47s 941us/step - loss: 0.9688 - acc: 0.6612 - va
Epoch 18/50
50000/50000 [=====] - 48s 959us/step - loss: 0.9530 - acc: 0.6641 - va
Epoch 19/50
50000/50000 [=====] - 49s 972us/step - loss: 0.9369 - acc: 0.6717 - va
Epoch 20/50
50000/50000 [=====] - 49s 977us/step - loss: 0.9229 - acc: 0.6781 - va
Epoch 21/50
50000/50000 [=====] - 50s 992us/step - loss: 0.9086 - acc: 0.6797 - va
Epoch 22/50
50000/50000 [=====] - 50s 1ms/step - loss: 0.8930 - acc: 0.6855 - val
Epoch 23/50
50000/50000 [=====] - 51s 1ms/step - loss: 0.8828 - acc: 0.6892 - val
Epoch 24/50
50000/50000 [=====] - 51s 1ms/step - loss: 0.8750 - acc: 0.6923 - val
Epoch 25/50
50000/50000 [=====] - 51s 1ms/step - loss: 0.8606 - acc: 0.6968 - val
Epoch 26/50
50000/50000 [=====] - 52s 1ms/step - loss: 0.8555 - acc: 0.6989 - val
Epoch 27/50
50000/50000 [=====] - 52s 1ms/step - loss: 0.8444 - acc: 0.7029 - val
Epoch 28/50
50000/50000 [=====] - 53s 1ms/step - loss: 0.8414 - acc: 0.7043 - val
Epoch 29/50
50000/50000 [=====] - 53s 1ms/step - loss: 0.8588 - acc: 0.6996 - val
Epoch 30/50
50000/50000 [=====] - 53s 1ms/step - loss: 11.0207 - acc: 0.2600 - val

```

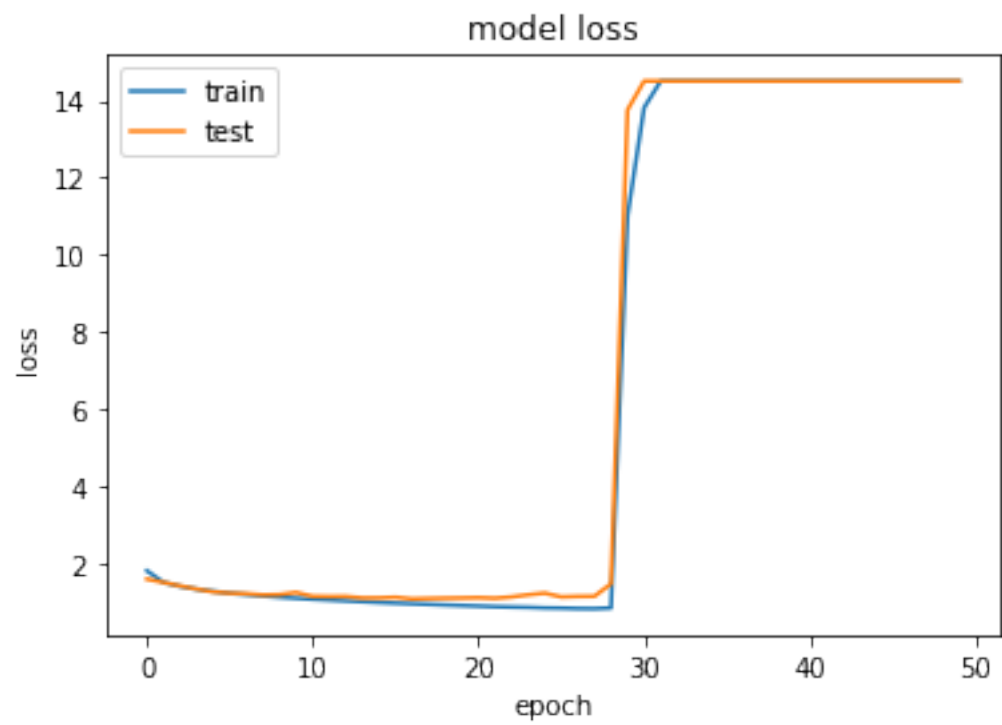
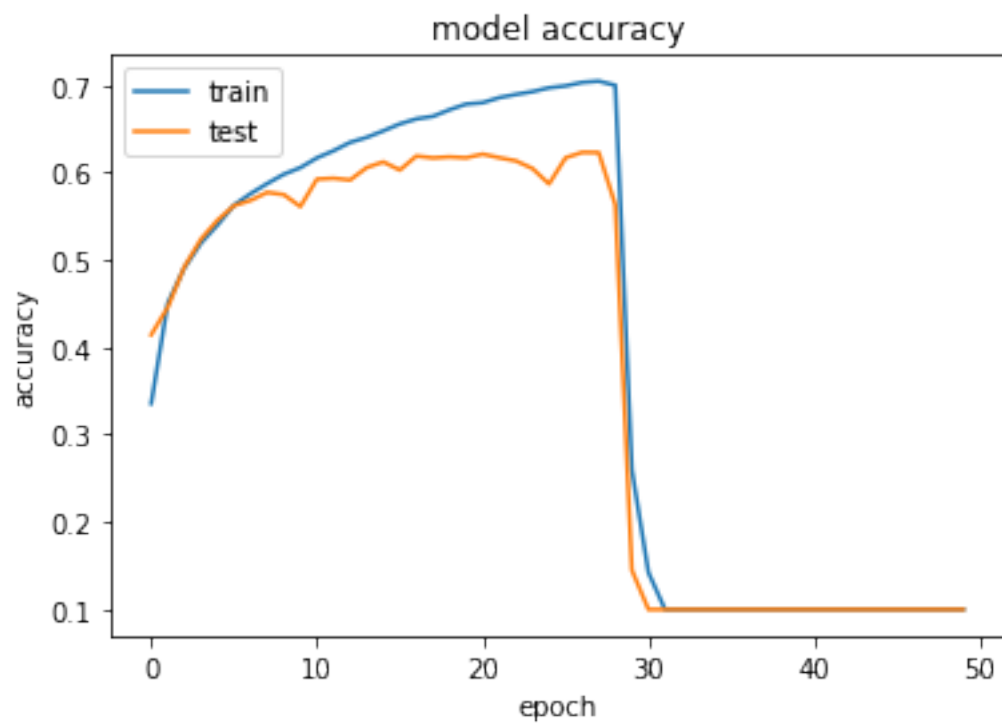
```

Epoch 31/50
50000/50000 [=====] - 53s 1ms/step - loss: 13.8178 - acc: 0.1423 - va
Epoch 32/50
50000/50000 [=====] - 52s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 33/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 34/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 35/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 36/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 37/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 38/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 39/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 40/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 41/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 42/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 43/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 44/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 45/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 46/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 47/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 48/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 49/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va
Epoch 50/50
50000/50000 [=====] - 53s 1ms/step - loss: 14.5056 - acc: 0.1000 - va

```

Print the scores

In [9]:



Test the network

In [10]:

Test score: 14.506285668945312

Test accuracy: 0.1

Q1: [0.5 point]

What are the number of parameters in convolution layers with K filters each of size $3wh$.

A1:

$3 \times w \times h \times K$ weights and K biases

Q2: [0.5 points]

What are the number of parameters in a max pooling operation?

A2:

The max-pooling layers just replace a 2×2 neighborhood by its maximum value. So there are NO parameters needed to be learnt in a pooling layer.

Q3: [0.5 point]

Which of the operations contain most number of parameters? (a) conv (b) pool (c) Fully connected layer (FC) (d) Relu

A3:

The highest number of parameters are learnt in Fully Connected Layer.

Q4: [0.5 point]

Which operation consume most amount of memory? (a) initial convolution layers (b) fully connected layers at the end

A4:

Huge amount of memory is consumed in the initial convolution layers as it has to remember all the images with various of channels.

Q5: [2 points]

Experiment with **learning rate** (learningRate) and notice the behaviour of the learning process. Plot your observations in a graph with brief explanation. Take the values on a log scale. Vary only one parameter at a time.

Observations

1. As the learning rate increases the model takes more time (no of epochs) to converge 2. If the learning rate is very large then the training might not even converge. 3. A careful choice of learning is very important in training neural networks.

Graphs shown below in support of the observations.

In [14]:

Training at Learning Rate = $1e-05$

Layer (type)	Output Shape	Param #
conv2d_9 (Conv2D)	(None, 28, 28, 6)	456
activation_21 (Activation)	(None, 28, 28, 6)	0

max_pooling2d_9 (MaxPooling2)	(None, 14, 14, 6)	0
conv2d_10 (Conv2D)	(None, 10, 10, 16)	2416
activation_22 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_10 (MaxPooling)	(None, 5, 5, 16)	0
flatten_5 (Flatten)	(None, 400)	0
dense_13 (Dense)	(None, 120)	48120
activation_23 (Activation)	(None, 120)	0
dense_14 (Dense)	(None, 84)	10164
activation_24 (Activation)	(None, 84)	0
dense_15 (Dense)	(None, 10)	850
activation_25 (Activation)	(None, 10)	0

=====
Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/35

50000/50000 [=====] - 41s 826us/step - loss: 1.8603 - acc: 0.3150 - va

Epoch 2/35

50000/50000 [=====] - 41s 820us/step - loss: 1.5606 - acc: 0.4359 - va

Epoch 3/35

50000/50000 [=====] - 42s 831us/step - loss: 1.4420 - acc: 0.4817 - va

Epoch 4/35

50000/50000 [=====] - 42s 837us/step - loss: 1.3588 - acc: 0.5144 - va

Epoch 5/35

50000/50000 [=====] - 42s 839us/step - loss: 1.2882 - acc: 0.5411 - va

Epoch 6/35

50000/50000 [=====] - 42s 842us/step - loss: 1.2349 - acc: 0.5627 - va

Epoch 7/35

50000/50000 [=====] - 43s 857us/step - loss: 1.1903 - acc: 0.5791 - va

Epoch 8/35

50000/50000 [=====] - 43s 866us/step - loss: 1.1534 - acc: 0.5941 - va

Epoch 9/35

50000/50000 [=====] - 44s 875us/step - loss: 1.1174 - acc: 0.6060 - va

Epoch 10/35

50000/50000 [=====] - 44s 883us/step - loss: 1.0881 - acc: 0.6215 - va

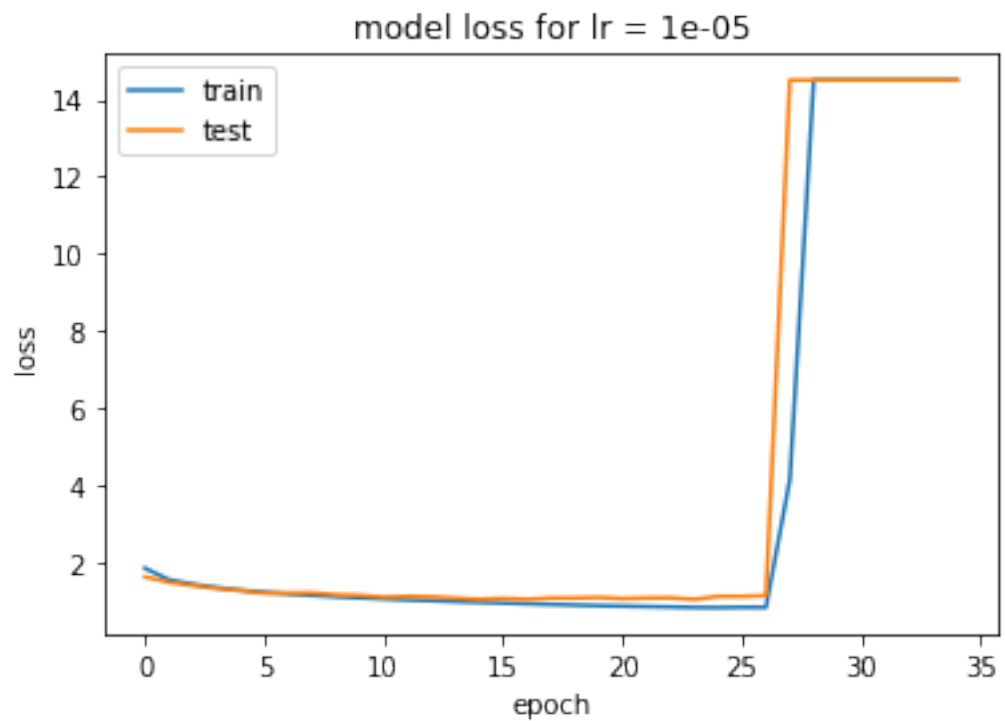
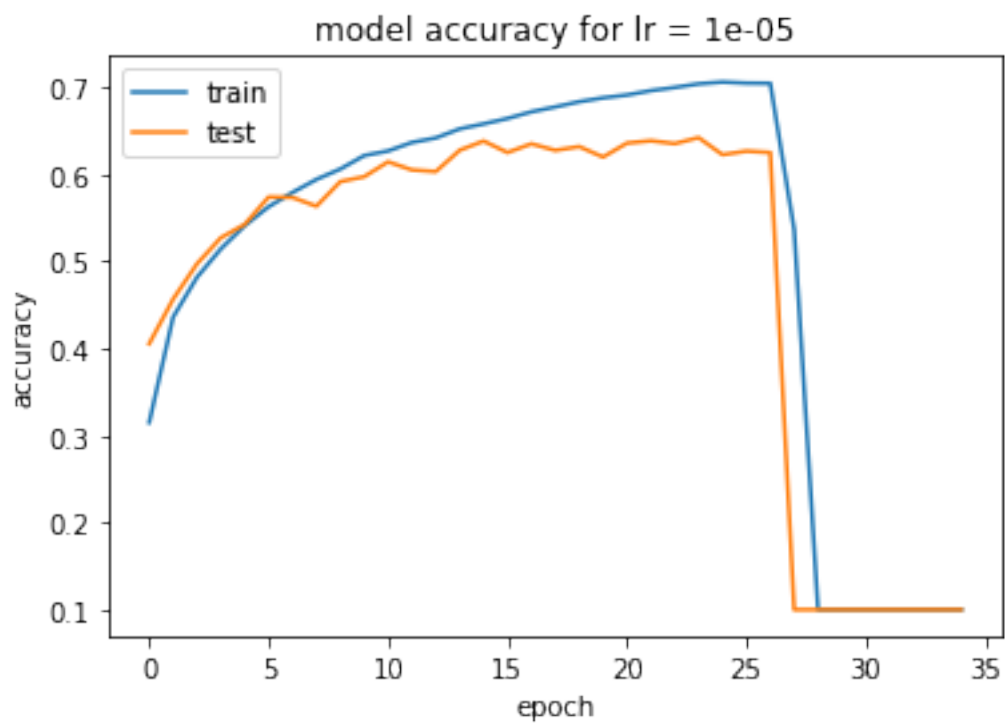

```

Epoch 11/35
50000/50000 [=====] - 44s 890us/step - loss: 1.0616 - acc: 0.6268 - va
Epoch 12/35
50000/50000 [=====] - 45s 902us/step - loss: 1.0354 - acc: 0.6366 - va
Epoch 13/35
50000/50000 [=====] - 46s 916us/step - loss: 1.0175 - acc: 0.6418 - va
Epoch 14/35
50000/50000 [=====] - 46s 930us/step - loss: 0.9938 - acc: 0.6522 - va
Epoch 15/35
50000/50000 [=====] - 45s 900us/step - loss: 0.9738 - acc: 0.6579 - va
Epoch 16/35
50000/50000 [=====] - 44s 887us/step - loss: 0.9542 - acc: 0.6641 - va
Epoch 17/35
50000/50000 [=====] - 45s 896us/step - loss: 0.9353 - acc: 0.6718 - va
Epoch 18/35
50000/50000 [=====] - 45s 910us/step - loss: 0.9191 - acc: 0.6773 - va
Epoch 19/35
50000/50000 [=====] - 46s 926us/step - loss: 0.9032 - acc: 0.6833 - va
Epoch 20/35
50000/50000 [=====] - 46s 927us/step - loss: 0.8869 - acc: 0.6878 - va
Epoch 21/35
50000/50000 [=====] - 47s 934us/step - loss: 0.8757 - acc: 0.6910 - va
Epoch 22/35
50000/50000 [=====] - 47s 947us/step - loss: 0.8639 - acc: 0.6960 - va
Epoch 23/35
50000/50000 [=====] - 48s 956us/step - loss: 0.8535 - acc: 0.6997 - va
Epoch 24/35
50000/50000 [=====] - 48s 962us/step - loss: 0.8407 - acc: 0.7039 - va
Epoch 25/35
50000/50000 [=====] - 48s 969us/step - loss: 0.8355 - acc: 0.7059 - va
Epoch 26/35
50000/50000 [=====] - 49s 972us/step - loss: 0.8444 - acc: 0.7047 - va
Epoch 27/35
50000/50000 [=====] - 49s 977us/step - loss: 0.8418 - acc: 0.7045 - va
Epoch 28/35
50000/50000 [=====] - 50s 993us/step - loss: 4.1497 - acc: 0.5367 - va
Epoch 29/35
50000/50000 [=====] - 50s 1ms/step - loss: 14.5063 - acc: 0.1000 - va
Epoch 30/35
50000/50000 [=====] - 50s 1ms/step - loss: 14.5063 - acc: 0.1000 - va
Epoch 31/35
50000/50000 [=====] - 50s 1ms/step - loss: 14.5063 - acc: 0.1000 - va
Epoch 32/35
50000/50000 [=====] - 50s 998us/step - loss: 14.5063 - acc: 0.1000 - v
Epoch 33/35
50000/50000 [=====] - 50s 1ms/step - loss: 14.5063 - acc: 0.1000 - va
Epoch 34/35
50000/50000 [=====] - 50s 1ms/step - loss: 14.5063 - acc: 0.1000 - va

```

Epoch 35/35

50000/50000 [=====] - 51s 1ms/step - loss: 14.5063 - acc: 0.1000 - val



Training at Learning Rate = 0.0001

Layer (type)	Output Shape	Param #
conv2d_11 (Conv2D)	(None, 28, 28, 6)	456
activation_26 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_11 (MaxPooling)	(None, 14, 14, 6)	0
conv2d_12 (Conv2D)	(None, 10, 10, 16)	2416
activation_27 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_12 (MaxPooling)	(None, 5, 5, 16)	0
flatten_6 (Flatten)	(None, 400)	0
dense_16 (Dense)	(None, 120)	48120
activation_28 (Activation)	(None, 120)	0
dense_17 (Dense)	(None, 84)	10164
activation_29 (Activation)	(None, 84)	0
dense_18 (Dense)	(None, 10)	850
activation_30 (Activation)	(None, 10)	0

Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/35

50000/50000 [=====] - 48s 964us/step - loss: 1.8739 - acc: 0.3162 - val_loss: 1.8739 - val_acc: 0.3162

Epoch 2/35

50000/50000 [=====] - 38s 751us/step - loss: 1.5411 - acc: 0.4415 - val_loss: 1.5411 - val_acc: 0.4415

Epoch 3/35

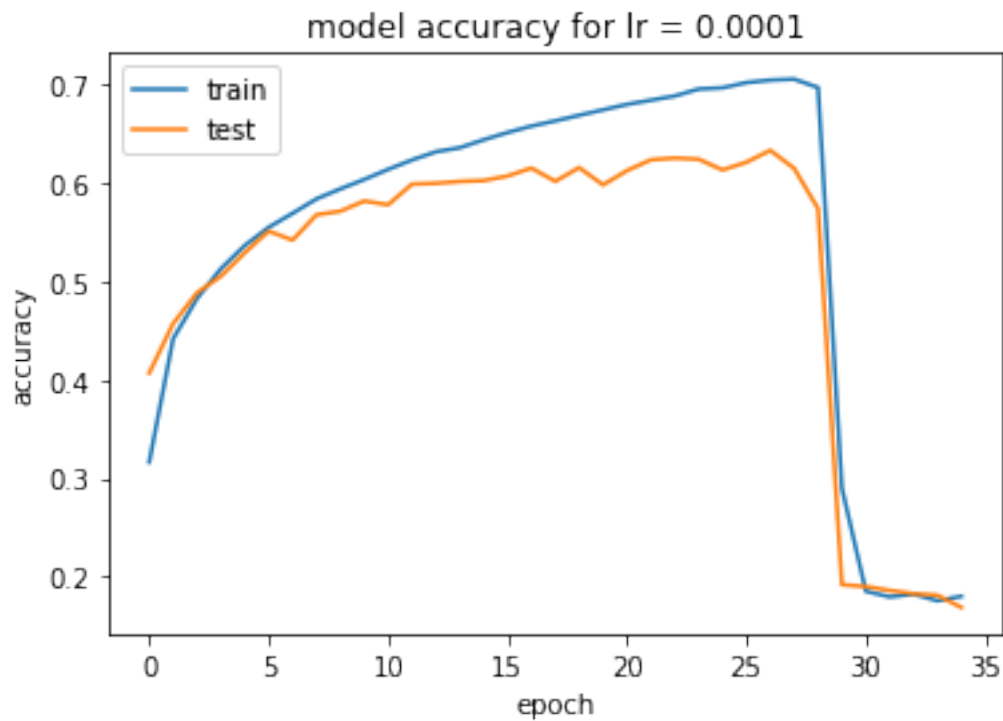
50000/50000 [=====] - 38s 764us/step - loss: 1.4341 - acc: 0.4825 - val_loss: 1.4341 - val_acc: 0.4825

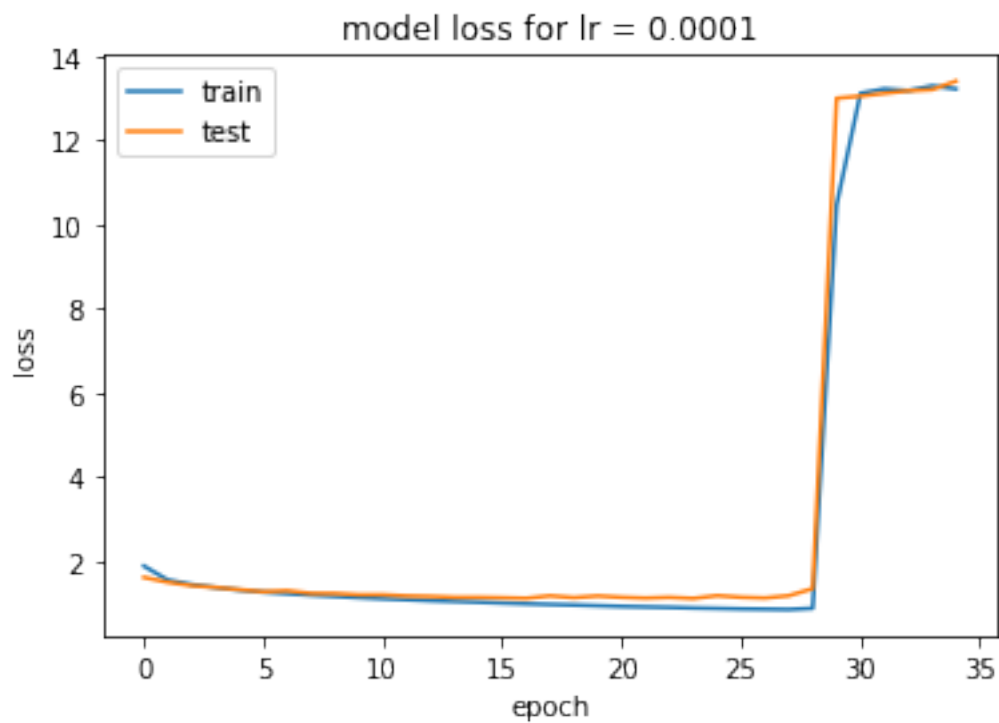
Epoch 4/35

50000/50000 [=====] - 39s 772us/step - loss: 1.3625 - acc: 0.5128 - val_loss: 1.3625 - val_acc: 0.5128

Epoch 5/35
50000/50000 [=====] - 39s 777us/step - loss: 1.3020 - acc: 0.5364 - va
Epoch 6/35
50000/50000 [=====] - 40s 790us/step - loss: 1.2532 - acc: 0.5548 - va
Epoch 7/35
50000/50000 [=====] - 40s 806us/step - loss: 1.2156 - acc: 0.5691 - va
Epoch 8/35
50000/50000 [=====] - 41s 830us/step - loss: 1.1804 - acc: 0.5837 - va
Epoch 9/35
50000/50000 [=====] - 41s 825us/step - loss: 1.1509 - acc: 0.5939 - va
Epoch 10/35
50000/50000 [=====] - 41s 828us/step - loss: 1.1211 - acc: 0.6035 - va
Epoch 11/35
50000/50000 [=====] - 42s 837us/step - loss: 1.0957 - acc: 0.6137 - va
Epoch 12/35
50000/50000 [=====] - 42s 845us/step - loss: 1.0742 - acc: 0.6233 - va
Epoch 13/35
50000/50000 [=====] - 43s 862us/step - loss: 1.0498 - acc: 0.6317 - va
Epoch 14/35
50000/50000 [=====] - 43s 869us/step - loss: 1.0321 - acc: 0.6357 - va
Epoch 15/35
50000/50000 [=====] - 44s 884us/step - loss: 1.0144 - acc: 0.6438 - va
Epoch 16/35
50000/50000 [=====] - 45s 892us/step - loss: 0.9940 - acc: 0.6512 - va
Epoch 17/35
50000/50000 [=====] - 45s 901us/step - loss: 0.9760 - acc: 0.6577 - va
Epoch 18/35
50000/50000 [=====] - 46s 910us/step - loss: 0.9602 - acc: 0.6631 - va
Epoch 19/35
50000/50000 [=====] - 46s 922us/step - loss: 0.9461 - acc: 0.6687 - va
Epoch 20/35
50000/50000 [=====] - 47s 931us/step - loss: 0.9295 - acc: 0.6743 - va
Epoch 21/35
50000/50000 [=====] - 47s 941us/step - loss: 0.9128 - acc: 0.6798 - va
Epoch 22/35
50000/50000 [=====] - 48s 954us/step - loss: 0.9012 - acc: 0.6841 - va
Epoch 23/35
50000/50000 [=====] - 48s 955us/step - loss: 0.8898 - acc: 0.6883 - va
Epoch 24/35
50000/50000 [=====] - 48s 968us/step - loss: 0.8751 - acc: 0.6954 - va
Epoch 25/35
50000/50000 [=====] - 49s 985us/step - loss: 0.8650 - acc: 0.6966 - va
Epoch 26/35
50000/50000 [=====] - 50s 990us/step - loss: 0.8537 - acc: 0.7019 - va
Epoch 27/35
50000/50000 [=====] - 50s 995us/step - loss: 0.8473 - acc: 0.7045 - va
Epoch 28/35
50000/50000 [=====] - 50s 1ms/step - loss: 0.8399 - acc: 0.7054 - val

Epoch 29/35
50000/50000 [=====] - 51s 1ms/step - loss: 0.8678 - acc: 0.6970 - val.
Epoch 30/35
50000/50000 [=====] - 50s 1ms/step - loss: 10.4601 - acc: 0.2898 - va.
Epoch 31/35
50000/50000 [=====] - 51s 1ms/step - loss: 13.1121 - acc: 0.1850 - va.
Epoch 32/35
50000/50000 [=====] - 50s 1ms/step - loss: 13.2172 - acc: 0.1793 - va.
Epoch 33/35
50000/50000 [=====] - 51s 1ms/step - loss: 13.1774 - acc: 0.1821 - va.
Epoch 34/35
50000/50000 [=====] - 50s 1ms/step - loss: 13.2885 - acc: 0.1754 - va.
Epoch 35/35
50000/50000 [=====] - 50s 1ms/step - loss: 13.2175 - acc: 0.1799 - va.





Training at Learning Rate = 0.001

Layer (type)	Output Shape	Param #
conv2d_13 (Conv2D)	(None, 28, 28, 6)	456
activation_31 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_13 (MaxPooling)	(None, 14, 14, 6)	0
conv2d_14 (Conv2D)	(None, 10, 10, 16)	2416
activation_32 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_14 (MaxPooling)	(None, 5, 5, 16)	0
flatten_7 (Flatten)	(None, 400)	0
dense_19 (Dense)	(None, 120)	48120
activation_33 (Activation)	(None, 120)	0
dense_20 (Dense)	(None, 84)	10164

```

-----
activation_34 (Activation)      (None, 84)                0
-----
dense_21 (Dense)                (None, 10)               850
-----
activation_35 (Activation)      (None, 10)                0
=====

```

Total params: 62,006
 Trainable params: 62,006
 Non-trainable params: 0

```

-----
None

```

Train on 50000 samples, validate on 10000 samples

Epoch 1/35

50000/50000 [=====] - 52s 1ms/step - loss: 1.8520 - acc: 0.3267 - val_

Epoch 2/35

50000/50000 [=====] - 40s 807us/step - loss: 1.5452 - acc: 0.4412 - va

Epoch 3/35

50000/50000 [=====] - 38s 768us/step - loss: 1.4234 - acc: 0.4896 - va

Epoch 4/35

50000/50000 [=====] - 39s 775us/step - loss: 1.3506 - acc: 0.5172 - va

Epoch 5/35

50000/50000 [=====] - 39s 786us/step - loss: 1.2903 - acc: 0.5431 - va

Epoch 6/35

50000/50000 [=====] - 40s 795us/step - loss: 1.2406 - acc: 0.5606 - va

Epoch 7/35

50000/50000 [=====] - 41s 812us/step - loss: 1.1974 - acc: 0.5761 - va

Epoch 8/35

50000/50000 [=====] - 41s 820us/step - loss: 1.1613 - acc: 0.5893 - va

Epoch 9/35

50000/50000 [=====] - 42s 835us/step - loss: 1.1273 - acc: 0.6033 - va

Epoch 10/35

50000/50000 [=====] - 42s 831us/step - loss: 1.0981 - acc: 0.6144 - va

Epoch 11/35

50000/50000 [=====] - 42s 843us/step - loss: 1.0689 - acc: 0.6255 - va

Epoch 12/35

50000/50000 [=====] - 43s 853us/step - loss: 1.0446 - acc: 0.6350 - va

Epoch 13/35

50000/50000 [=====] - 43s 868us/step - loss: 1.0196 - acc: 0.6453 - va

Epoch 14/35

50000/50000 [=====] - 44s 877us/step - loss: 0.9973 - acc: 0.6540 - va

Epoch 15/35

50000/50000 [=====] - 44s 888us/step - loss: 0.9779 - acc: 0.6567 - va

Epoch 16/35

50000/50000 [=====] - 45s 899us/step - loss: 0.9601 - acc: 0.6650 - va

Epoch 17/35

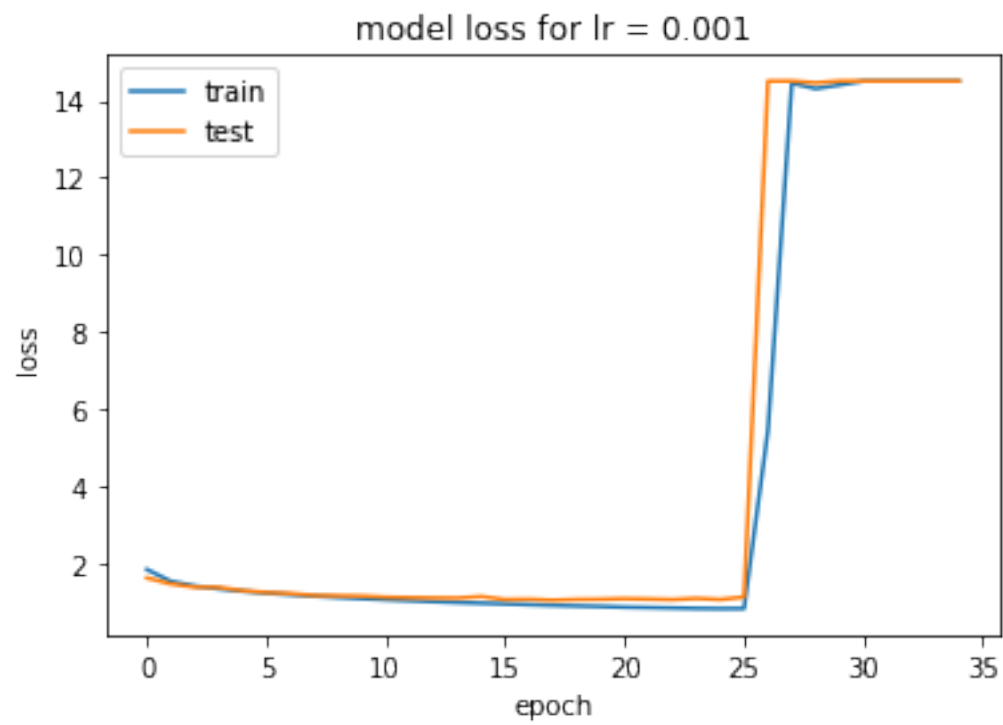
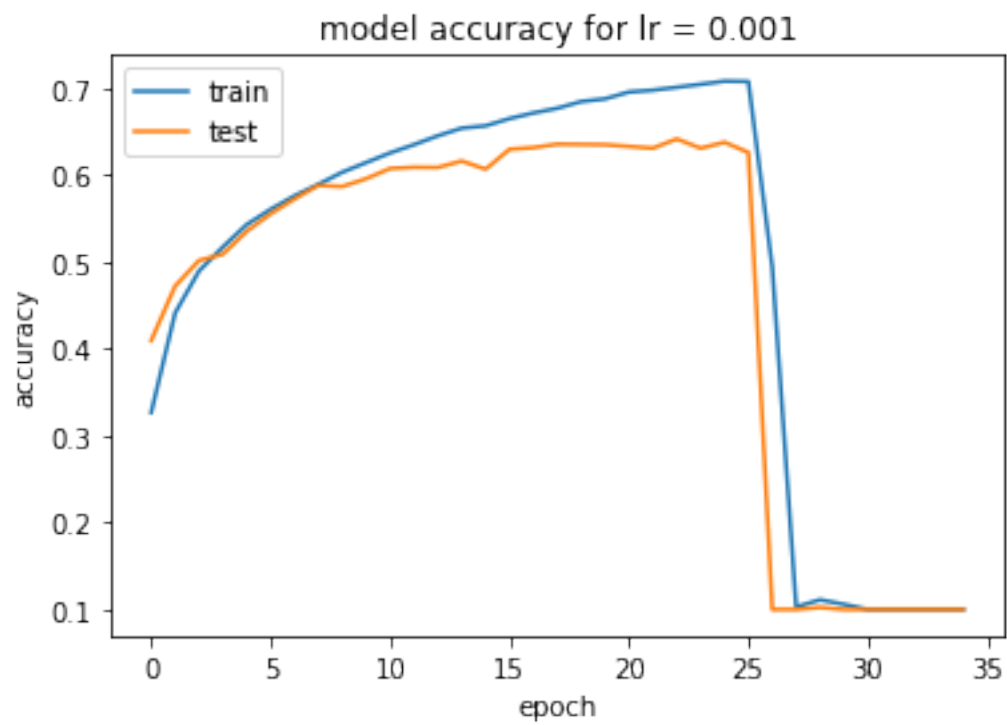
50000/50000 [=====] - 46s 912us/step - loss: 0.9406 - acc: 0.6715 - va

Epoch 18/35

```

50000/50000 [=====] - 46s 924us/step - loss: 0.9228 - acc: 0.6769 - va
Epoch 19/35
50000/50000 [=====] - 46s 926us/step - loss: 0.9070 - acc: 0.6847 - va
Epoch 20/35
50000/50000 [=====] - 47s 944us/step - loss: 0.8927 - acc: 0.6878 - va
Epoch 21/35
50000/50000 [=====] - 47s 949us/step - loss: 0.8751 - acc: 0.6956 - va
Epoch 22/35
50000/50000 [=====] - 48s 963us/step - loss: 0.8642 - acc: 0.6977 - va
Epoch 23/35
50000/50000 [=====] - 49s 983us/step - loss: 0.8535 - acc: 0.7011 - va
Epoch 24/35
50000/50000 [=====] - 49s 986us/step - loss: 0.8427 - acc: 0.7045 - va
Epoch 25/35
50000/50000 [=====] - 50s 998us/step - loss: 0.8365 - acc: 0.7081 - va
Epoch 26/35
50000/50000 [=====] - 50s 1ms/step - loss: 0.8385 - acc: 0.7077 - val
Epoch 27/35
50000/50000 [=====] - 51s 1ms/step - loss: 5.4573 - acc: 0.4938 - val
Epoch 28/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.4534 - acc: 0.1030 - val
Epoch 29/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.3111 - acc: 0.1112 - val
Epoch 30/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.4069 - acc: 0.1059 - val
Epoch 31/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.5063 - acc: 0.1000 - val
Epoch 32/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.5063 - acc: 0.1000 - val
Epoch 33/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.5063 - acc: 0.1000 - val
Epoch 34/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.5063 - acc: 0.1000 - val
Epoch 35/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.5063 - acc: 0.1000 - val

```

Training at Learning Rate = 0.01

Layer (type)	Output Shape	Param #
conv2d_15 (Conv2D)	(None, 28, 28, 6)	456
activation_36 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_15 (MaxPooling)	(None, 14, 14, 6)	0
conv2d_16 (Conv2D)	(None, 10, 10, 16)	2416
activation_37 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_16 (MaxPooling)	(None, 5, 5, 16)	0
flatten_8 (Flatten)	(None, 400)	0
dense_22 (Dense)	(None, 120)	48120
activation_38 (Activation)	(None, 120)	0
dense_23 (Dense)	(None, 84)	10164
activation_39 (Activation)	(None, 84)	0
dense_24 (Dense)	(None, 10)	850
activation_40 (Activation)	(None, 10)	0

Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/35

50000/50000 [=====] - 52s 1ms/step - loss: 1.8252 - acc: 0.3327 - val.

Epoch 2/35

50000/50000 [=====] - 40s 805us/step - loss: 1.5417 - acc: 0.4407 - va

Epoch 3/35

50000/50000 [=====] - 39s 771us/step - loss: 1.4302 - acc: 0.4863 - va

Epoch 4/35

50000/50000 [=====] - 39s 778us/step - loss: 1.3518 - acc: 0.5155 - va

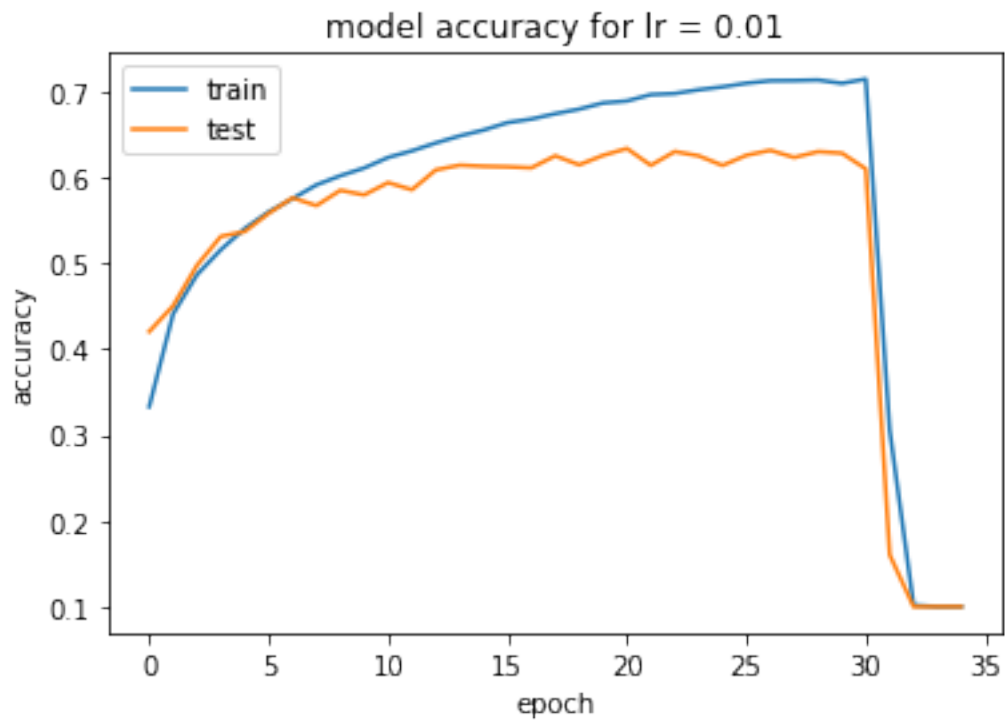
Epoch 5/35

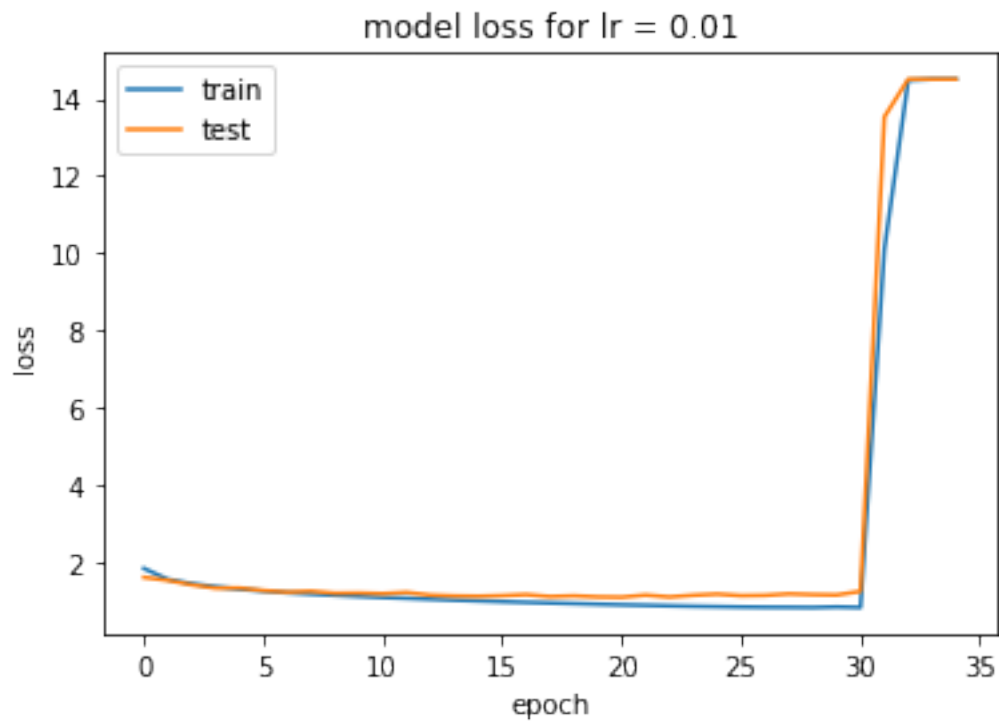
50000/50000 [=====] - 39s 786us/step - loss: 1.2892 - acc: 0.5402 - va

Epoch 6/35

50000/50000 [=====] - 40s 798us/step - loss: 1.2383 - acc: 0.5595 - val
 Epoch 7/35
 50000/50000 [=====] - 41s 815us/step - loss: 1.1951 - acc: 0.5749 - val
 Epoch 8/35
 50000/50000 [=====] - 41s 824us/step - loss: 1.1605 - acc: 0.5909 - val
 Epoch 9/35
 50000/50000 [=====] - 42s 831us/step - loss: 1.1291 - acc: 0.6016 - val
 Epoch 10/35
 50000/50000 [=====] - 42s 837us/step - loss: 1.1007 - acc: 0.6106 - val
 Epoch 11/35
 50000/50000 [=====] - 42s 843us/step - loss: 1.0727 - acc: 0.6229 - val
 Epoch 12/35
 50000/50000 [=====] - 43s 856us/step - loss: 1.0515 - acc: 0.6306 - val
 Epoch 13/35
 50000/50000 [=====] - 43s 869us/step - loss: 1.0272 - acc: 0.6398 - val
 Epoch 14/35
 50000/50000 [=====] - 44s 879us/step - loss: 1.0035 - acc: 0.6480 - val
 Epoch 15/35
 50000/50000 [=====] - 45s 891us/step - loss: 0.9838 - acc: 0.6548 - val
 Epoch 16/35
 50000/50000 [=====] - 45s 900us/step - loss: 0.9639 - acc: 0.6634 - val
 Epoch 17/35
 50000/50000 [=====] - 46s 927us/step - loss: 0.9463 - acc: 0.6676 - val
 Epoch 18/35
 50000/50000 [=====] - 46s 926us/step - loss: 0.9295 - acc: 0.6738 - val
 Epoch 19/35
 50000/50000 [=====] - 47s 939us/step - loss: 0.9140 - acc: 0.6791 - val
 Epoch 20/35
 50000/50000 [=====] - 47s 950us/step - loss: 0.8974 - acc: 0.6863 - val
 Epoch 21/35
 50000/50000 [=====] - 48s 959us/step - loss: 0.8824 - acc: 0.6886 - val
 Epoch 22/35
 50000/50000 [=====] - 49s 981us/step - loss: 0.8693 - acc: 0.6960 - val
 Epoch 23/35
 50000/50000 [=====] - 50s 997us/step - loss: 0.8562 - acc: 0.6973 - val
 Epoch 24/35
 50000/50000 [=====] - 50s 993us/step - loss: 0.8439 - acc: 0.7017 - val
 Epoch 25/35
 50000/50000 [=====] - 50s 994us/step - loss: 0.8347 - acc: 0.7050 - val
 Epoch 26/35
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8255 - acc: 0.7093 - val
 Epoch 27/35
 50000/50000 [=====] - 51s 1ms/step - loss: 0.8194 - acc: 0.7122 - val
 Epoch 28/35
 50000/50000 [=====] - 51s 1ms/step - loss: 0.8169 - acc: 0.7124 - val
 Epoch 29/35
 50000/50000 [=====] - 51s 1ms/step - loss: 0.8126 - acc: 0.7130 - val
 Epoch 30/35

50000/50000 [=====] - 51s 1ms/step - loss: 0.8267 - acc: 0.7092 - val.
Epoch 31/35
50000/50000 [=====] - 51s 1ms/step - loss: 0.8130 - acc: 0.7141 - val.
Epoch 32/35
50000/50000 [=====] - 51s 1ms/step - loss: 10.0942 - acc: 0.3055 - val.
Epoch 33/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.4780 - acc: 0.1017 - val.
Epoch 34/35
50000/50000 [=====] - 51s 1ms/step - loss: 14.5063 - acc: 0.1000 - val.
Epoch 35/35
50000/50000 [=====] - 52s 1ms/step - loss: 14.5063 - acc: 0.1000 - val.





Training at Learning Rate = 0.1

Layer (type)	Output Shape	Param #
conv2d_17 (Conv2D)	(None, 28, 28, 6)	456
activation_41 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_17 (MaxPooling)	(None, 14, 14, 6)	0
conv2d_18 (Conv2D)	(None, 10, 10, 16)	2416
activation_42 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_18 (MaxPooling)	(None, 5, 5, 16)	0
flatten_9 (Flatten)	(None, 400)	0
dense_25 (Dense)	(None, 120)	48120
activation_43 (Activation)	(None, 120)	0
dense_26 (Dense)	(None, 84)	10164

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activation_44 (Activation)      (None, 84)                0
-----
dense_27 (Dense)                (None, 10)               850
-----
activation_45 (Activation)      (None, 10)                0
=====

```

Total params: 62,006
 Trainable params: 62,006
 Non-trainable params: 0

```

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None

```

Train on 50000 samples, validate on 10000 samples

Epoch 1/35

50000/50000 [=====] - 50s 994us/step - loss: 1.8731 - acc: 0.3127 - va

Epoch 2/35

50000/50000 [=====] - 43s 855us/step - loss: 1.5601 - acc: 0.4369 - va

Epoch 3/35

50000/50000 [=====] - 37s 740us/step - loss: 1.4257 - acc: 0.4912 - va

Epoch 4/35

50000/50000 [=====] - 37s 749us/step - loss: 1.3453 - acc: 0.5235 - va

Epoch 5/35

50000/50000 [=====] - 38s 757us/step - loss: 1.2878 - acc: 0.5452 - va

Epoch 6/35

50000/50000 [=====] - 38s 769us/step - loss: 1.2414 - acc: 0.5619 - va

Epoch 7/35

50000/50000 [=====] - 39s 784us/step - loss: 1.1991 - acc: 0.5784 - va

Epoch 8/35

50000/50000 [=====] - 40s 795us/step - loss: 1.1684 - acc: 0.5890 - va

Epoch 9/35

50000/50000 [=====] - 40s 801us/step - loss: 1.1372 - acc: 0.5982 - va

Epoch 10/35

50000/50000 [=====] - 40s 810us/step - loss: 1.1098 - acc: 0.6106 - va

Epoch 11/35

50000/50000 [=====] - 41s 814us/step - loss: 1.0850 - acc: 0.6168 - va

Epoch 12/35

50000/50000 [=====] - 41s 822us/step - loss: 1.0639 - acc: 0.6255 - va

Epoch 13/35

50000/50000 [=====] - 42s 837us/step - loss: 1.0425 - acc: 0.6339 - va

Epoch 14/35

50000/50000 [=====] - 42s 847us/step - loss: 1.0206 - acc: 0.6401 - va

Epoch 15/35

50000/50000 [=====] - 43s 855us/step - loss: 1.0032 - acc: 0.6487 - va

Epoch 16/35

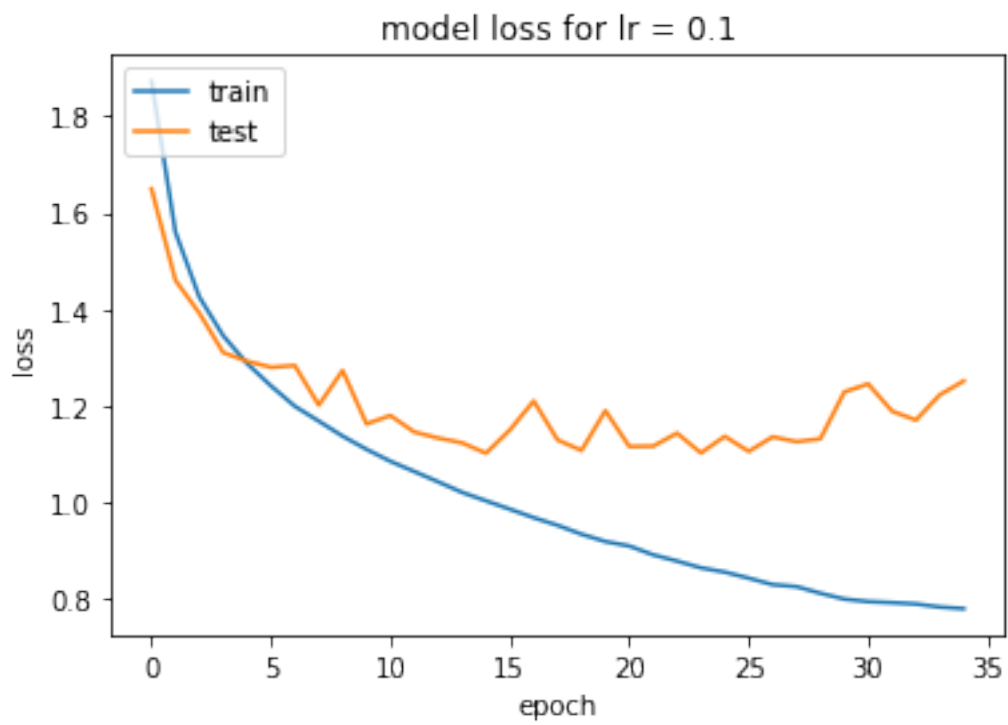
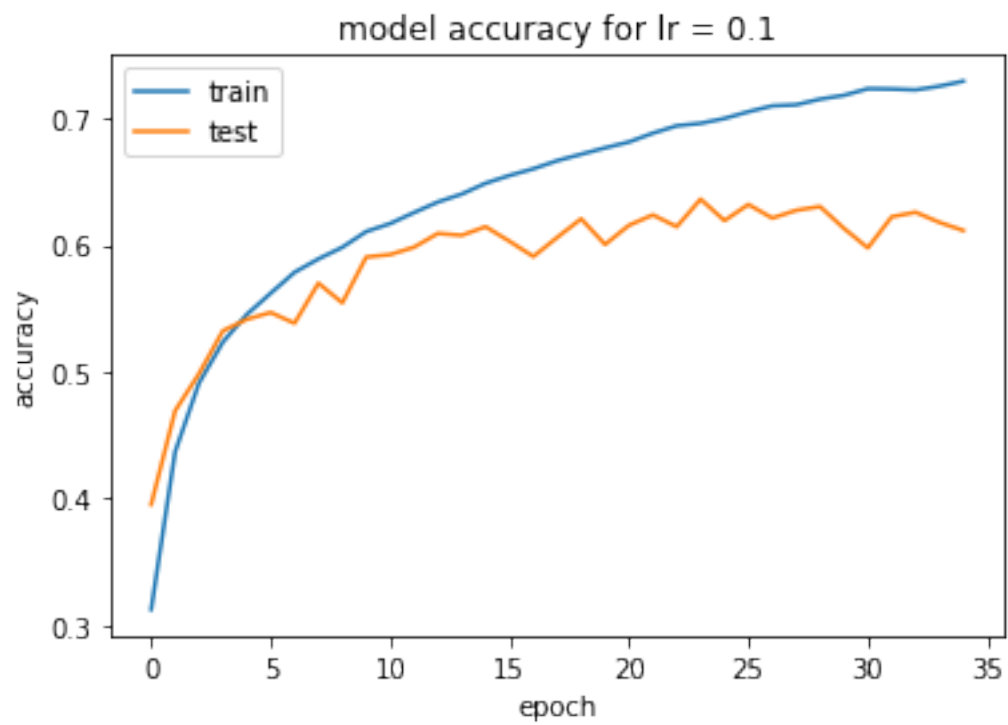
50000/50000 [=====] - 43s 866us/step - loss: 0.9858 - acc: 0.6548 - va

Epoch 17/35

50000/50000 [=====] - 44s 881us/step - loss: 0.9682 - acc: 0.6600 - va

Epoch 18/35

50000/50000 [=====] - 44s 887us/step - loss: 0.9523 - acc: 0.6665 - va
 Epoch 19/35
 50000/50000 [=====] - 45s 899us/step - loss: 0.9339 - acc: 0.6715 - va
 Epoch 20/35
 50000/50000 [=====] - 45s 910us/step - loss: 0.9187 - acc: 0.6765 - va
 Epoch 21/35
 50000/50000 [=====] - 46s 918us/step - loss: 0.9095 - acc: 0.6812 - va
 Epoch 22/35
 50000/50000 [=====] - 47s 930us/step - loss: 0.8912 - acc: 0.6881 - va
 Epoch 23/35
 50000/50000 [=====] - 47s 939us/step - loss: 0.8783 - acc: 0.6939 - va
 Epoch 24/35
 50000/50000 [=====] - 48s 950us/step - loss: 0.8642 - acc: 0.6959 - va
 Epoch 25/35
 50000/50000 [=====] - 48s 953us/step - loss: 0.8554 - acc: 0.6997 - va
 Epoch 26/35
 50000/50000 [=====] - 48s 965us/step - loss: 0.8428 - acc: 0.7050 - va
 Epoch 27/35
 50000/50000 [=====] - 49s 973us/step - loss: 0.8295 - acc: 0.7096 - va
 Epoch 28/35
 50000/50000 [=====] - 49s 984us/step - loss: 0.8253 - acc: 0.7105 - va
 Epoch 29/35
 50000/50000 [=====] - 49s 979us/step - loss: 0.8115 - acc: 0.7149 - va
 Epoch 30/35
 50000/50000 [=====] - 49s 985us/step - loss: 0.7995 - acc: 0.7179 - va
 Epoch 31/35
 50000/50000 [=====] - 49s 990us/step - loss: 0.7943 - acc: 0.7232 - va
 Epoch 32/35
 50000/50000 [=====] - 49s 982us/step - loss: 0.7921 - acc: 0.7229 - va
 Epoch 33/35
 50000/50000 [=====] - 49s 984us/step - loss: 0.7893 - acc: 0.7222 - va
 Epoch 34/35
 50000/50000 [=====] - 49s 978us/step - loss: 0.7830 - acc: 0.7251 - va
 Epoch 35/35
 50000/50000 [=====] - 49s 981us/step - loss: 0.7796 - acc: 0.7291 - va



Training at Learning Rate = 1

Layer (type)	Output Shape	Param #
conv2d_19 (Conv2D)	(None, 28, 28, 6)	456
activation_46 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_19 (MaxPooling)	(None, 14, 14, 6)	0
conv2d_20 (Conv2D)	(None, 10, 10, 16)	2416
activation_47 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_20 (MaxPooling)	(None, 5, 5, 16)	0
flatten_10 (Flatten)	(None, 400)	0
dense_28 (Dense)	(None, 120)	48120
activation_48 (Activation)	(None, 120)	0
dense_29 (Dense)	(None, 84)	10164
activation_49 (Activation)	(None, 84)	0
dense_30 (Dense)	(None, 10)	850
activation_50 (Activation)	(None, 10)	0

Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/35

50000/50000 [=====] - 50s 1ms/step - loss: 1.8582 - acc: 0.3240 - val.

Epoch 2/35

50000/50000 [=====] - 38s 756us/step - loss: 1.5138 - acc: 0.4515 - va

Epoch 3/35

50000/50000 [=====] - 38s 765us/step - loss: 1.4018 - acc: 0.4966 - va

Epoch 4/35

50000/50000 [=====] - 39s 773us/step - loss: 1.3235 - acc: 0.5278 - va

Epoch 5/35

50000/50000 [=====] - 39s 782us/step - loss: 1.2636 - acc: 0.5504 - va

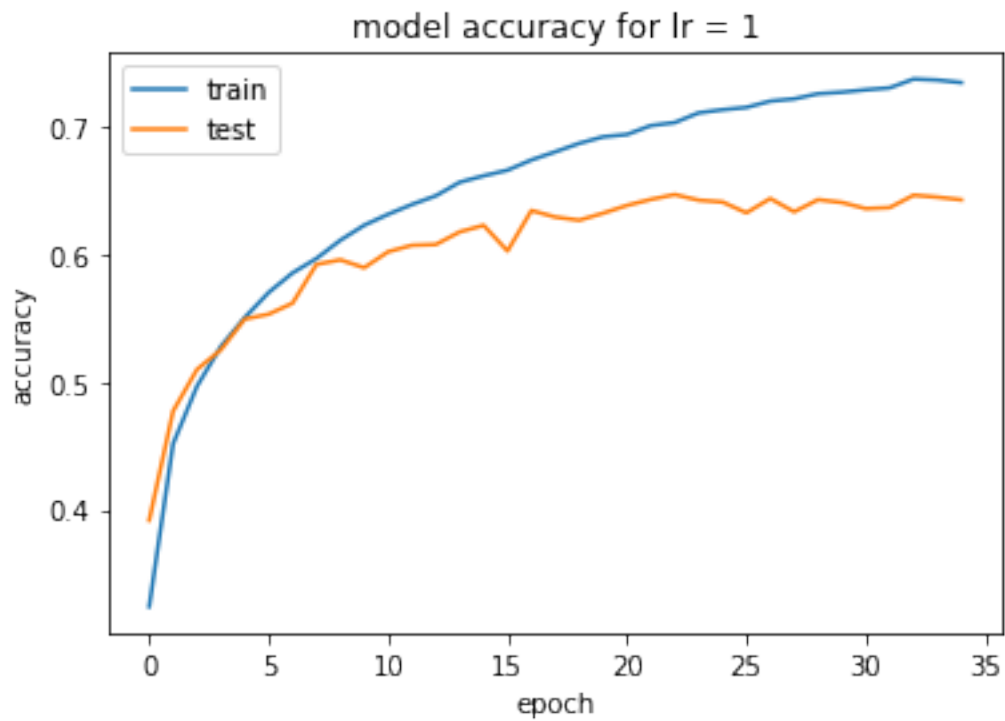
Epoch 6/35

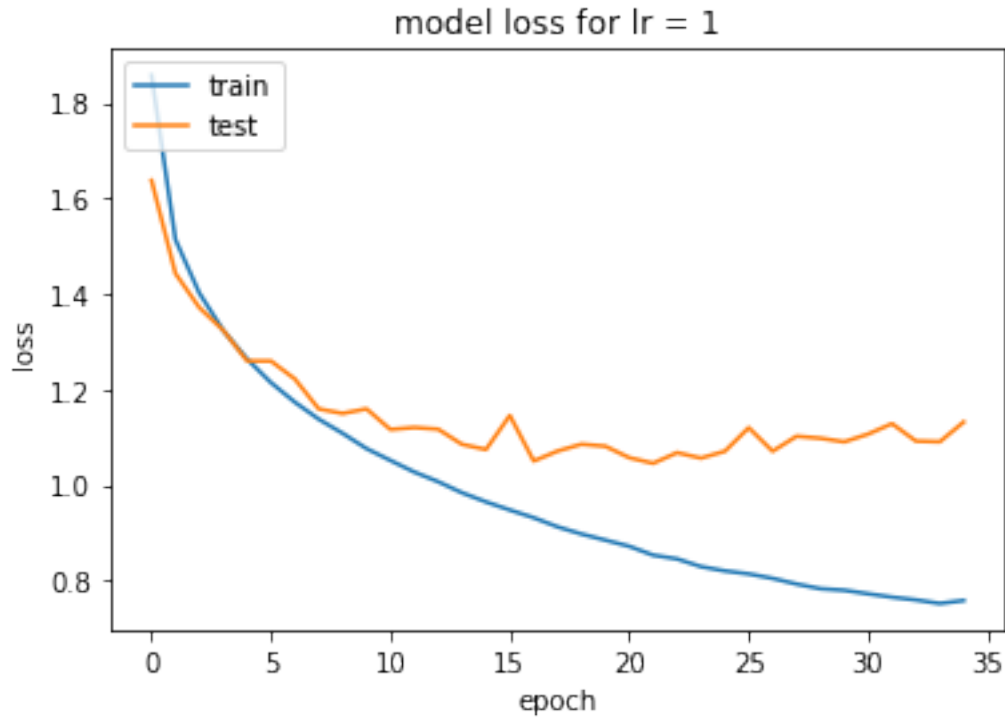
```

50000/50000 [=====] - 40s 791us/step - loss: 1.2141 - acc: 0.5701 - va
Epoch 7/35
50000/50000 [=====] - 40s 810us/step - loss: 1.1731 - acc: 0.5854 - va
Epoch 8/35
50000/50000 [=====] - 41s 816us/step - loss: 1.1375 - acc: 0.5967 - va
Epoch 9/35
50000/50000 [=====] - 41s 824us/step - loss: 1.1079 - acc: 0.6110 - va
Epoch 10/35
50000/50000 [=====] - 42s 832us/step - loss: 1.0759 - acc: 0.6228 - va
Epoch 11/35
50000/50000 [=====] - 42s 836us/step - loss: 1.0511 - acc: 0.6313 - va
Epoch 12/35
50000/50000 [=====] - 43s 852us/step - loss: 1.0267 - acc: 0.6391 - va
Epoch 13/35
50000/50000 [=====] - 44s 872us/step - loss: 1.0065 - acc: 0.6458 - va
Epoch 14/35
50000/50000 [=====] - 44s 882us/step - loss: 0.9833 - acc: 0.6565 - va
Epoch 15/35
50000/50000 [=====] - 45s 894us/step - loss: 0.9643 - acc: 0.6615 - va
Epoch 16/35
50000/50000 [=====] - 45s 908us/step - loss: 0.9472 - acc: 0.6659 - va
Epoch 17/35
50000/50000 [=====] - 46s 919us/step - loss: 0.9310 - acc: 0.6739 - va
Epoch 18/35
50000/50000 [=====] - 47s 943us/step - loss: 0.9119 - acc: 0.6803 - va
Epoch 19/35
50000/50000 [=====] - 48s 960us/step - loss: 0.8968 - acc: 0.6869 - va
Epoch 20/35
50000/50000 [=====] - 48s 959us/step - loss: 0.8841 - acc: 0.6920 - va
Epoch 21/35
50000/50000 [=====] - 49s 973us/step - loss: 0.8712 - acc: 0.6938 - va
Epoch 22/35
50000/50000 [=====] - 50s 990us/step - loss: 0.8526 - acc: 0.7008 - va
Epoch 23/35
50000/50000 [=====] - 50s 999us/step - loss: 0.8448 - acc: 0.7032 - va
Epoch 24/35
50000/50000 [=====] - 50s 999us/step - loss: 0.8286 - acc: 0.7108 - va
Epoch 25/35
50000/50000 [=====] - 51s 1ms/step - loss: 0.8196 - acc: 0.7133 - val
Epoch 26/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.8133 - acc: 0.7150 - val
Epoch 27/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.8040 - acc: 0.7200 - val
Epoch 28/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.7921 - acc: 0.7218 - val
Epoch 29/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.7823 - acc: 0.7258 - val
Epoch 30/35

```

50000/50000 [=====] - 52s 1ms/step - loss: 0.7791 - acc: 0.7270 - val.
Epoch 31/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.7716 - acc: 0.7289 - val.
Epoch 32/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.7646 - acc: 0.7304 - val.
Epoch 33/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.7588 - acc: 0.7373 - val.
Epoch 34/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.7514 - acc: 0.7365 - val.
Epoch 35/35
50000/50000 [=====] - 52s 1ms/step - loss: 0.7576 - acc: 0.7345 - val.





**** Q6: [2 points] ****

Currently, the **batch-size** is 50. Notice the training loss curve if batch size is changed to 1. Is it smooth or fluctating? Show the effect of batch-size on the learning curves in a plot. Take the values on a log scale. Vary only one parameter at a time.

**** A6: ****

Observations

1. When the batch-size is 1 then the loss-curve is fluctuating and not stable.
2. As the batch-size increases the training loss curve starts smoothening.

See the graphs below in support of the observations.

In []:

Training with Batch Size = 1

Layer (type)	Output Shape	Param #
conv2d_1 (Conv2D)	(None, 28, 28, 6)	456
activation_1 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_1 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_2 (Conv2D)	(None, 10, 10, 16)	2416

activation_2 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_2 (MaxPooling2)	(None, 5, 5, 16)	0
flatten_1 (Flatten)	(None, 400)	0
dense_1 (Dense)	(None, 120)	48120
activation_3 (Activation)	(None, 120)	0
dense_2 (Dense)	(None, 84)	10164
activation_4 (Activation)	(None, 84)	0
dense_3 (Dense)	(None, 10)	850
activation_5 (Activation)	(None, 10)	0

Total params: 62,006
 Trainable params: 62,006
 Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 134s 3ms/step - loss: 1.7958 - acc: 0.3402 - va

Epoch 2/30

50000/50000 [=====] - 134s 3ms/step - loss: 1.6776 - acc: 0.3908 - va

Epoch 3/30

50000/50000 [=====] - 134s 3ms/step - loss: 1.6576 - acc: 0.4045 - va

Epoch 4/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6520 - acc: 0.4129 - va

Epoch 5/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6711 - acc: 0.4108 - va

Epoch 6/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6727 - acc: 0.4123 - va

Epoch 7/30

50000/50000 [=====] - 134s 3ms/step - loss: 1.6643 - acc: 0.4155 - va

Epoch 8/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6763 - acc: 0.4141 - va

Epoch 9/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6711 - acc: 0.4174 - va

Epoch 10/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6762 - acc: 0.4178 - va

Epoch 11/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6930 - acc: 0.4118 - va

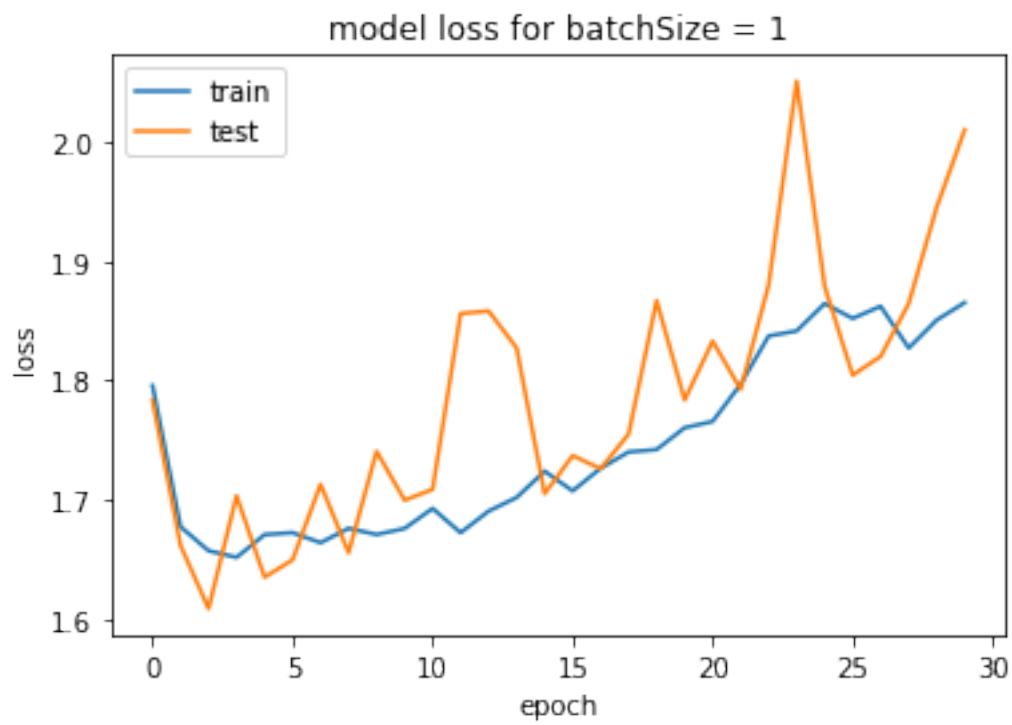
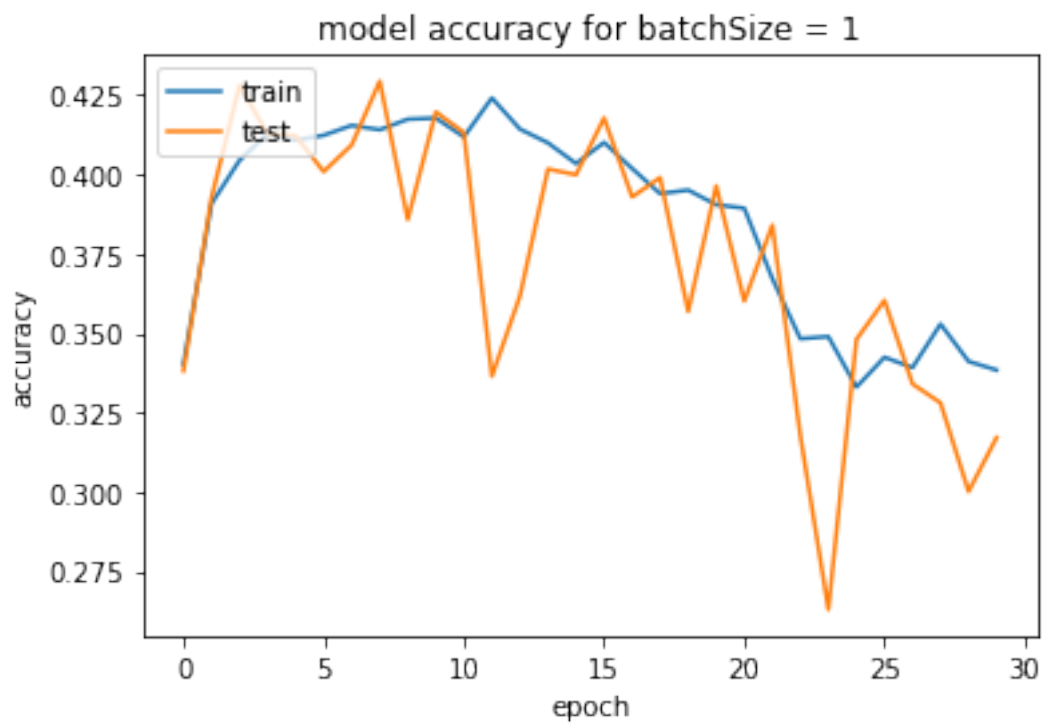
Epoch 12/30

50000/50000 [=====] - 133s 3ms/step - loss: 1.6727 - acc: 0.4241 - va

```

Epoch 13/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.6908 - acc: 0.4143 - va
Epoch 14/30
50000/50000 [=====] - 132s 3ms/step - loss: 1.7022 - acc: 0.4100 - va
Epoch 15/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.7242 - acc: 0.4034 - va
Epoch 16/30
50000/50000 [=====] - 132s 3ms/step - loss: 1.7077 - acc: 0.4101 - va
Epoch 17/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.7266 - acc: 0.4019 - va
Epoch 18/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.7403 - acc: 0.3940 - va
Epoch 19/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.7422 - acc: 0.3951 - va
Epoch 20/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.7605 - acc: 0.3905 - va
Epoch 21/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.7658 - acc: 0.3894 - va
Epoch 22/30
50000/50000 [=====] - 132s 3ms/step - loss: 1.7969 - acc: 0.3672 - va
Epoch 23/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.8373 - acc: 0.3482 - va
Epoch 24/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.8415 - acc: 0.3489 - va
Epoch 25/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.8644 - acc: 0.3330 - va
Epoch 26/30
50000/50000 [=====] - 132s 3ms/step - loss: 1.8520 - acc: 0.3424 - va
Epoch 27/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.8621 - acc: 0.3391 - va
Epoch 28/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.8272 - acc: 0.3529 - va
Epoch 29/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.8506 - acc: 0.3411 - va
Epoch 30/30
50000/50000 [=====] - 133s 3ms/step - loss: 1.8652 - acc: 0.3384 - va

```



Training with Batch Size = 8

Layer (type)	Output Shape	Param #
conv2d_3 (Conv2D)	(None, 28, 28, 6)	456
activation_6 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_3 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_4 (Conv2D)	(None, 10, 10, 16)	2416
activation_7 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_4 (MaxPooling2D)	(None, 5, 5, 16)	0
flatten_2 (Flatten)	(None, 400)	0
dense_4 (Dense)	(None, 120)	48120
activation_8 (Activation)	(None, 120)	0
dense_5 (Dense)	(None, 84)	10164
activation_9 (Activation)	(None, 84)	0
dense_6 (Dense)	(None, 10)	850
activation_10 (Activation)	(None, 10)	0

Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 61s 1ms/step - loss: 1.6404 - acc: 0.4031 - val.

Epoch 2/30

50000/50000 [=====] - 61s 1ms/step - loss: 1.3423 - acc: 0.5211 - val.

Epoch 3/30

50000/50000 [=====] - 60s 1ms/step - loss: 1.2141 - acc: 0.5700 - val.

Epoch 4/30

50000/50000 [=====] - 60s 1ms/step - loss: 1.1330 - acc: 0.5996 - val.

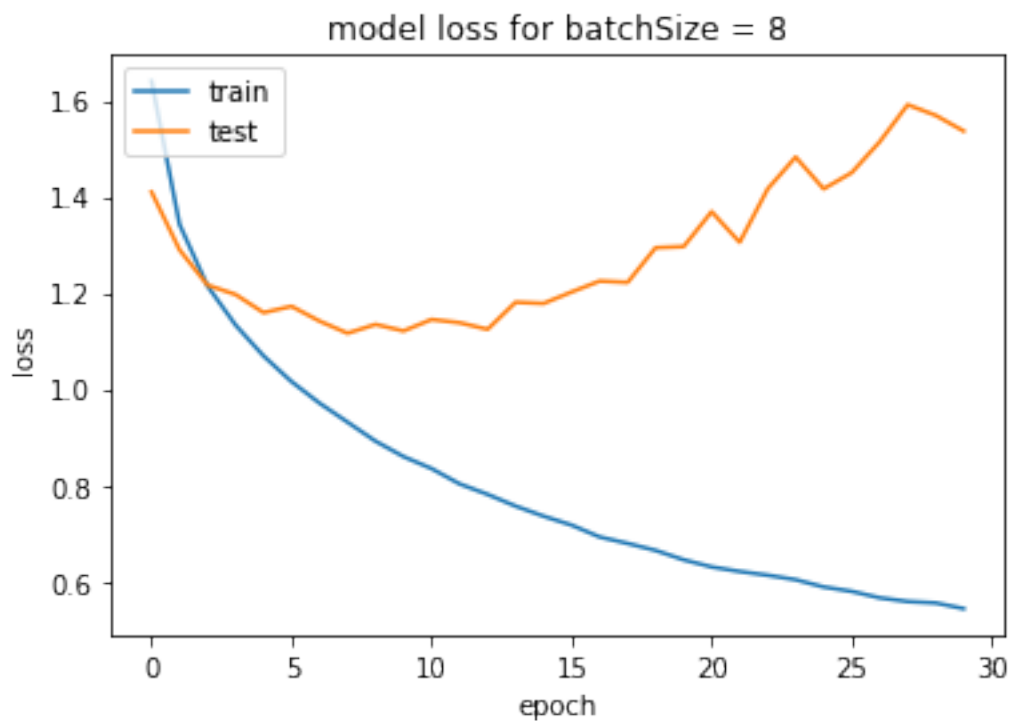
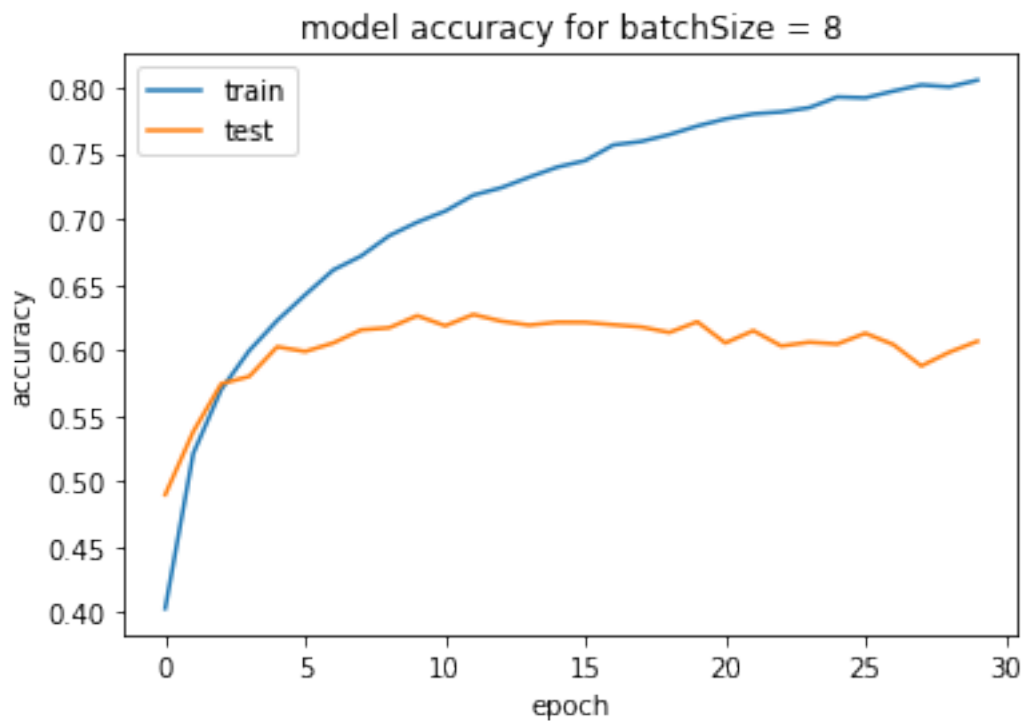
Epoch 5/30

50000/50000 [=====] - 60s 1ms/step - loss: 1.0688 - acc: 0.6225 - val.

Epoch 6/30

50000/50000 [=====] - 61s 1ms/step - loss: 1.0154 - acc: 0.6421 - val.
 Epoch 7/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.9706 - acc: 0.6610 - val.
 Epoch 8/30
 50000/50000 [=====] - 61s 1ms/step - loss: 0.9311 - acc: 0.6717 - val.
 Epoch 9/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.8915 - acc: 0.6872 - val.
 Epoch 10/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.8595 - acc: 0.6974 - val.
 Epoch 11/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.8346 - acc: 0.7059 - val.
 Epoch 12/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.8027 - acc: 0.7180 - val.
 Epoch 13/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.7810 - acc: 0.7237 - val.
 Epoch 14/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.7566 - acc: 0.7318 - val.
 Epoch 15/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.7356 - acc: 0.7394 - val.
 Epoch 16/30
 50000/50000 [=====] - 61s 1ms/step - loss: 0.7171 - acc: 0.7444 - val.
 Epoch 17/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6924 - acc: 0.7563 - val.
 Epoch 18/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6790 - acc: 0.7590 - val.
 Epoch 19/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6645 - acc: 0.7642 - val.
 Epoch 20/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6449 - acc: 0.7707 - val.
 Epoch 21/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6301 - acc: 0.7761 - val.
 Epoch 22/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6206 - acc: 0.7799 - val.
 Epoch 23/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6128 - acc: 0.7815 - val.
 Epoch 24/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.6036 - acc: 0.7847 - val.
 Epoch 25/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.5885 - acc: 0.7928 - val.
 Epoch 26/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.5793 - acc: 0.7922 - val.
 Epoch 27/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.5659 - acc: 0.7973 - val.
 Epoch 28/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.5582 - acc: 0.8020 - val.
 Epoch 29/30
 50000/50000 [=====] - 60s 1ms/step - loss: 0.5552 - acc: 0.8006 - val.
 Epoch 30/30

50000/50000 [=====] - 60s 1ms/step - loss: 0.5434 - acc: 0.8056 - val.



Training with Batch Size = 16

Layer (type)	Output Shape	Param #
conv2d_5 (Conv2D)	(None, 28, 28, 6)	456
activation_11 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_5 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_6 (Conv2D)	(None, 10, 10, 16)	2416
activation_12 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_6 (MaxPooling2D)	(None, 5, 5, 16)	0
flatten_3 (Flatten)	(None, 400)	0
dense_7 (Dense)	(None, 120)	48120
activation_13 (Activation)	(None, 120)	0
dense_8 (Dense)	(None, 84)	10164
activation_14 (Activation)	(None, 84)	0
dense_9 (Dense)	(None, 10)	850
activation_15 (Activation)	(None, 10)	0

=====
Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 57s 1ms/step - loss: 1.7070 - acc: 0.3786 - val.

Epoch 2/30

50000/50000 [=====] - 57s 1ms/step - loss: 1.3816 - acc: 0.5063 - val.

Epoch 3/30

50000/50000 [=====] - 56s 1ms/step - loss: 1.2652 - acc: 0.5516 - val.

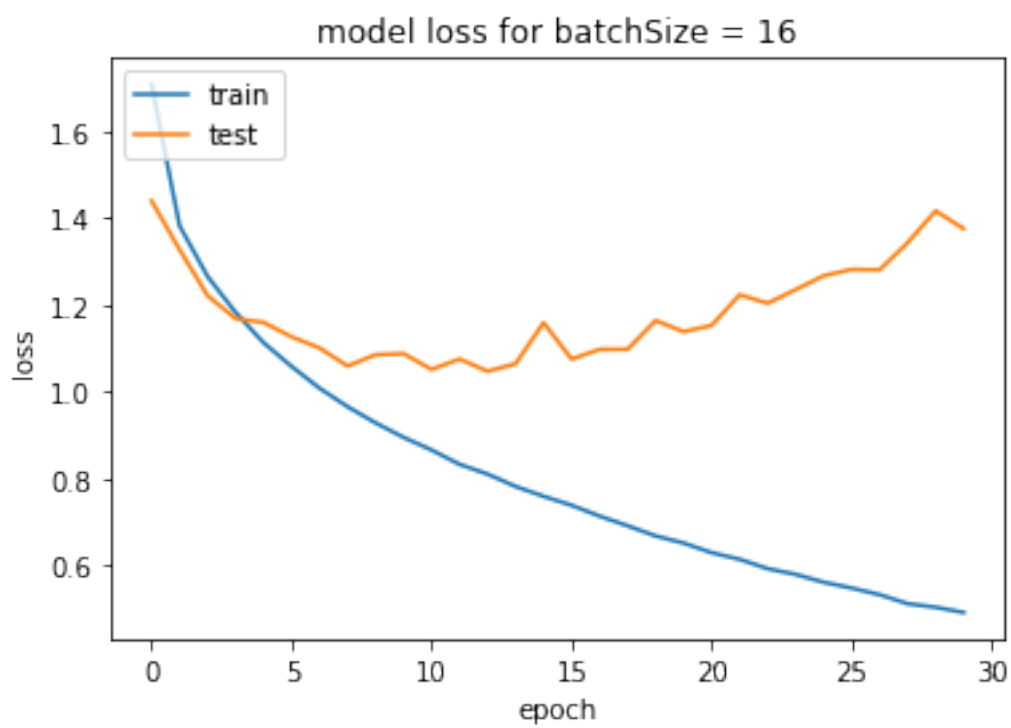
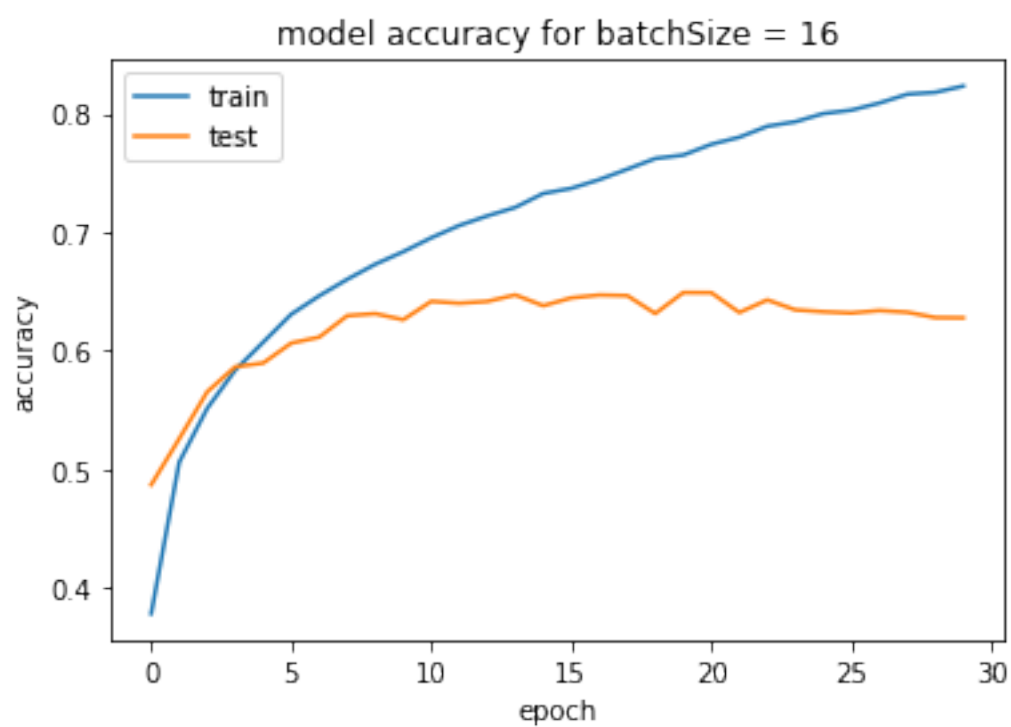
Epoch 4/30

50000/50000 [=====] - 56s 1ms/step - loss: 1.1824 - acc: 0.5839 - val.

```

Epoch 5/30
50000/50000 [=====] - 57s 1ms/step - loss: 1.1127 - acc: 0.6074 - val.
Epoch 6/30
50000/50000 [=====] - 56s 1ms/step - loss: 1.0582 - acc: 0.6309 - val.
Epoch 7/30
50000/50000 [=====] - 56s 1ms/step - loss: 1.0080 - acc: 0.6464 - val.
Epoch 8/30
50000/50000 [=====] - 57s 1ms/step - loss: 0.9655 - acc: 0.6603 - val.
Epoch 9/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.8660 - acc: 0.6953 - val.
Epoch 12/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.8330 - acc: 0.7057 - val.
Epoch 13/30
50000/50000 [=====] - 57s 1ms/step - loss: 0.8106 - acc: 0.7138 - val.
Epoch 14/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.7822 - acc: 0.7209 - val.
Epoch 15/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.7595 - acc: 0.7327 - val.
Epoch 16/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.7389 - acc: 0.7370 - val.
Epoch 17/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.7140 - acc: 0.7443 - val.
Epoch 18/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.6918 - acc: 0.7531 - val.
Epoch 19/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.6684 - acc: 0.7621 - val.
Epoch 20/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.6521 - acc: 0.7650 - val.
Epoch 21/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.6299 - acc: 0.7741 - val.
Epoch 22/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.6147 - acc: 0.7801 - val.
Epoch 23/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.5931 - acc: 0.7893 - val.
Epoch 24/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.5800 - acc: 0.7931 - val.
Epoch 25/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.5619 - acc: 0.8000 - val.
Epoch 26/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.5486 - acc: 0.8029 - val.
Epoch 27/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.5333 - acc: 0.8088 - val.
Epoch 28/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.5126 - acc: 0.8163 - val.
Epoch 29/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.5043 - acc: 0.8179 - val.
Epoch 30/30
50000/50000 [=====] - 56s 1ms/step - loss: 0.4924 - acc: 0.8232 - val.

```



Training with Batch Size = 64

Layer (type)	Output Shape	Param #
conv2d_7 (Conv2D)	(None, 28, 28, 6)	456
activation_16 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_7 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_8 (Conv2D)	(None, 10, 10, 16)	2416
activation_17 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_8 (MaxPooling2D)	(None, 5, 5, 16)	0
flatten_4 (Flatten)	(None, 400)	0
dense_10 (Dense)	(None, 120)	48120
activation_18 (Activation)	(None, 120)	0
dense_11 (Dense)	(None, 84)	10164
activation_19 (Activation)	(None, 84)	0
dense_12 (Dense)	(None, 10)	850
activation_20 (Activation)	(None, 10)	0

Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 50s 1ms/step - loss: 1.8737 - acc: 0.3202 - val.

Epoch 2/30

50000/50000 [=====] - 50s 1ms/step - loss: 1.5591 - acc: 0.4381 - val.

Epoch 3/30

50000/50000 [=====] - 50s 1ms/step - loss: 1.4394 - acc: 0.4828 - val.

Epoch 4/30

50000/50000 [=====] - 50s 1ms/step - loss: 1.3640 - acc: 0.5126 - val.

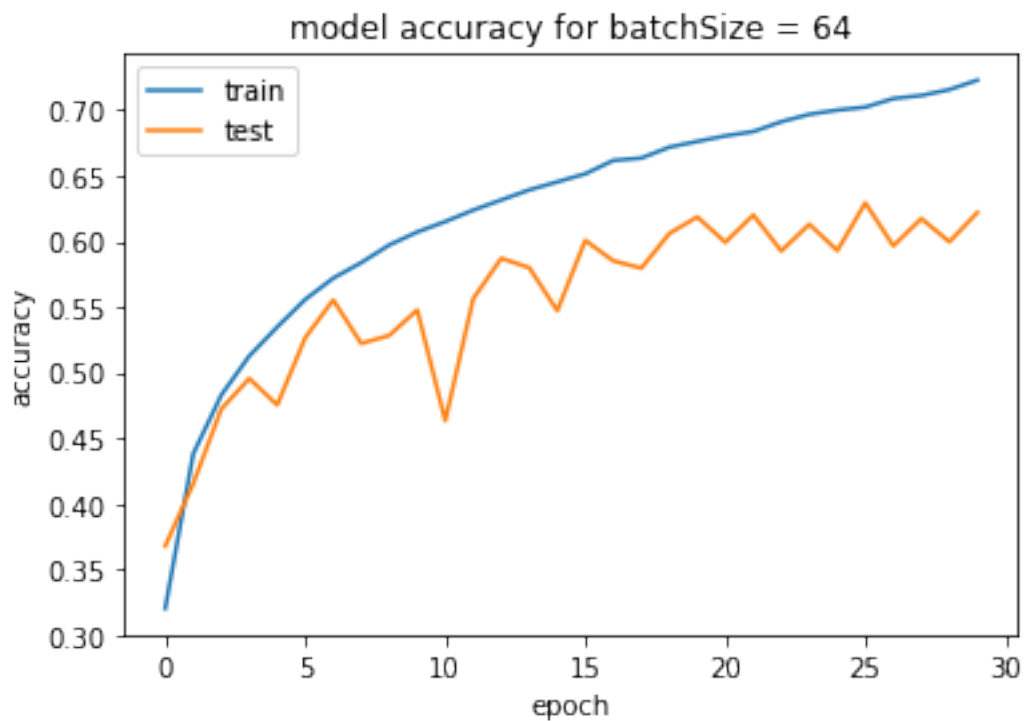
Epoch 5/30

50000/50000 [=====] - 50s 1ms/step - loss: 1.3029 - acc: 0.5348 - val.

Epoch 6/30

50000/50000 [=====] - 50s 1ms/step - loss: 1.2534 - acc: 0.5558 - val.
 Epoch 7/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.2118 - acc: 0.5720 - val.
 Epoch 8/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.1768 - acc: 0.5838 - val.
 Epoch 9/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.1456 - acc: 0.5973 - val.
 Epoch 10/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.1176 - acc: 0.6072 - val.
 Epoch 11/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.0933 - acc: 0.6151 - val.
 Epoch 12/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.0699 - acc: 0.6239 - val.
 Epoch 13/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.0494 - acc: 0.6316 - val.
 Epoch 14/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.0280 - acc: 0.6393 - val.
 Epoch 15/30
 50000/50000 [=====] - 50s 1ms/step - loss: 1.0104 - acc: 0.6454 - val.
 Epoch 16/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.9926 - acc: 0.6515 - val.
 Epoch 17/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.9726 - acc: 0.6617 - val.
 Epoch 18/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.9590 - acc: 0.6635 - val.
 Epoch 19/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.9388 - acc: 0.6718 - val.
 Epoch 20/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.9278 - acc: 0.6762 - val.
 Epoch 21/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.9126 - acc: 0.6804 - val.
 Epoch 22/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8999 - acc: 0.6837 - val.
 Epoch 23/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8865 - acc: 0.6913 - val.
 Epoch 24/30
 50000/50000 [=====] - 51s 1ms/step - loss: 0.8701 - acc: 0.6969 - val.
 Epoch 25/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8574 - acc: 0.7001 - val.
 Epoch 26/30
 50000/50000 [=====] - 51s 1ms/step - loss: 0.8465 - acc: 0.7024 - val.
 Epoch 27/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8321 - acc: 0.7089 - val.
 Epoch 28/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8207 - acc: 0.7112 - val.
 Epoch 29/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8076 - acc: 0.7157 - val.
 Epoch 30/30

50000/50000 [=====] - 50s 1ms/step - loss: 0.7942 - acc: 0.7229 - val.



Training with Batch Size = 128

Layer (type)	Output Shape	Param #
conv2d_9 (Conv2D)	(None, 28, 28, 6)	456
activation_21 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_9 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_10 (Conv2D)	(None, 10, 10, 16)	2416
activation_22 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_10 (MaxPooling2D)	(None, 5, 5, 16)	0
flatten_5 (Flatten)	(None, 400)	0
dense_13 (Dense)	(None, 120)	48120
activation_23 (Activation)	(None, 120)	0
dense_14 (Dense)	(None, 84)	10164
activation_24 (Activation)	(None, 84)	0
dense_15 (Dense)	(None, 10)	850
activation_25 (Activation)	(None, 10)	0

Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 48s 968us/step - loss: 2.1028 - acc: 0.2148 - val_loss: 2.1028 - val_acc: 0.2148

Epoch 2/30

50000/50000 [=====] - 48s 966us/step - loss: 1.7425 - acc: 0.3640 - val_loss: 1.7425 - val_acc: 0.3640

Epoch 3/30

50000/50000 [=====] - 48s 966us/step - loss: 1.5926 - acc: 0.4214 - val_loss: 1.5926 - val_acc: 0.4214

Epoch 4/30

50000/50000 [=====] - 48s 967us/step - loss: 1.5049 - acc: 0.4585 - val_loss: 1.5049 - val_acc: 0.4585

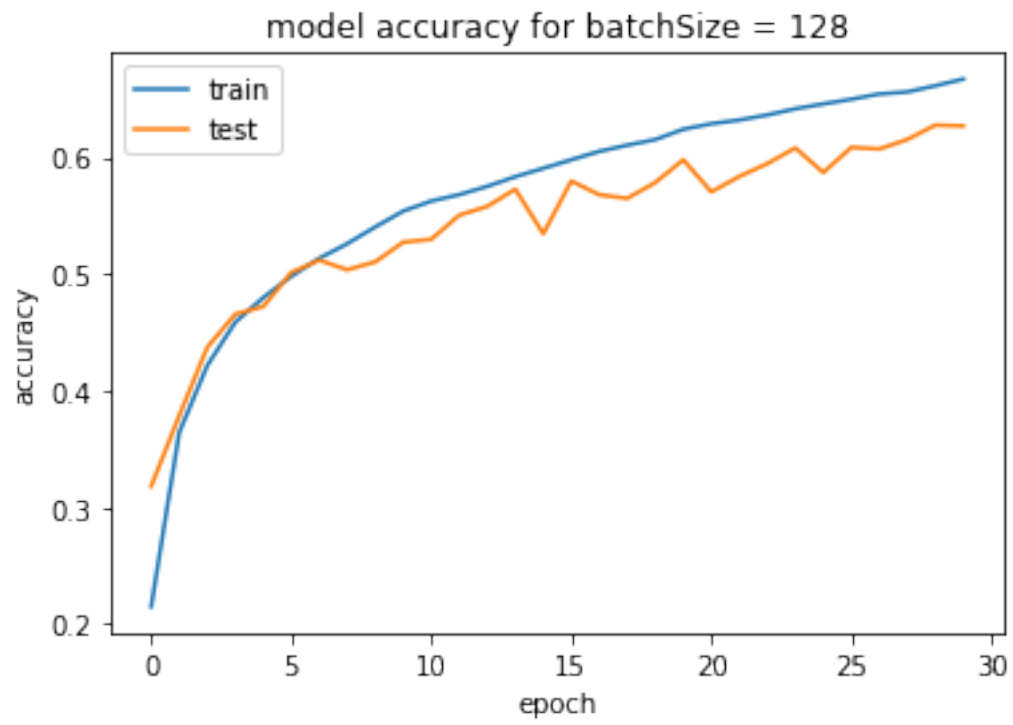
Epoch 5/30
50000/50000 [=====] - 48s 965us/step - loss: 1.4477 - acc: 0.4796 - va
Epoch 6/30
50000/50000 [=====] - 48s 966us/step - loss: 1.3993 - acc: 0.4979 - va
Epoch 7/30
50000/50000 [=====] - 48s 967us/step - loss: 1.3613 - acc: 0.5133 - va
Epoch 8/30
50000/50000 [=====] - 48s 967us/step - loss: 1.3294 - acc: 0.5259 - va
Epoch 9/30
50000/50000 [=====] - 48s 966us/step - loss: 1.2973 - acc: 0.5402 - va
Epoch 10/30
50000/50000 [=====] - 48s 965us/step - loss: 1.2703 - acc: 0.5538 - va
Epoch 11/30
50000/50000 [=====] - 48s 966us/step - loss: 1.2481 - acc: 0.5624 - va
Epoch 12/30
50000/50000 [=====] - 48s 965us/step - loss: 1.2248 - acc: 0.5679 - va
Epoch 13/30
50000/50000 [=====] - 48s 966us/step - loss: 1.2040 - acc: 0.5750 - va
Epoch 14/30
50000/50000 [=====] - 48s 966us/step - loss: 1.1866 - acc: 0.5833 - va
Epoch 15/30
50000/50000 [=====] - 48s 967us/step - loss: 1.1652 - acc: 0.5905 - va
Epoch 16/30
50000/50000 [=====] - 48s 965us/step - loss: 1.1471 - acc: 0.5978 - va
Epoch 17/30
50000/50000 [=====] - 48s 966us/step - loss: 1.1277 - acc: 0.6050 - va
Epoch 18/30
50000/50000 [=====] - 48s 966us/step - loss: 1.1106 - acc: 0.6103 - va
Epoch 19/30
50000/50000 [=====] - 48s 966us/step - loss: 1.0969 - acc: 0.6151 - va
Epoch 20/30
50000/50000 [=====] - 48s 965us/step - loss: 1.0789 - acc: 0.6239 - va
Epoch 21/30
50000/50000 [=====] - 49s 971us/step - loss: 1.0644 - acc: 0.6287 - va
Epoch 22/30
50000/50000 [=====] - 48s 967us/step - loss: 1.0528 - acc: 0.6318 - va
Epoch 23/30
50000/50000 [=====] - 48s 964us/step - loss: 1.0380 - acc: 0.6362 - va
Epoch 24/30
50000/50000 [=====] - 48s 965us/step - loss: 1.0247 - acc: 0.6415 - va
Epoch 25/30
50000/50000 [=====] - 48s 966us/step - loss: 1.0134 - acc: 0.6457 - va
Epoch 26/30
50000/50000 [=====] - 48s 967us/step - loss: 1.0020 - acc: 0.6497 - va
Epoch 27/30
50000/50000 [=====] - 48s 965us/step - loss: 0.9894 - acc: 0.6541 - va
Epoch 28/30
50000/50000 [=====] - 48s 966us/step - loss: 0.9815 - acc: 0.6559 - va

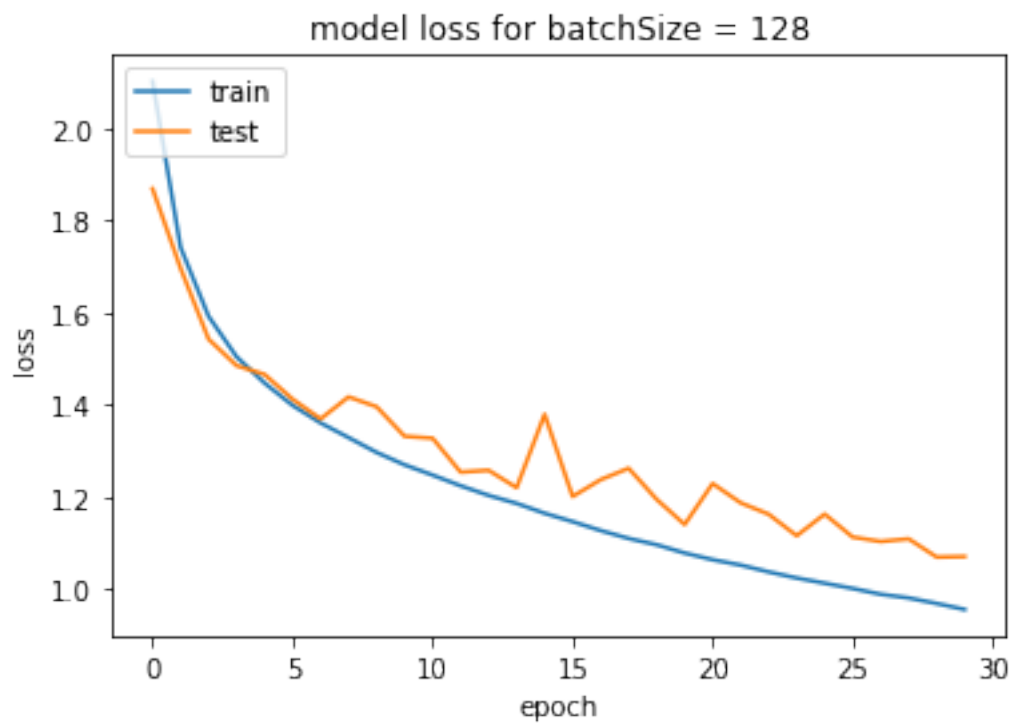
Epoch 29/30

50000/50000 [=====] - 48s 967us/step - loss: 0.9694 - acc: 0.6612 - val

Epoch 30/30

50000/50000 [=====] - 48s 968us/step - loss: 0.9564 - acc: 0.6670 - val





Training with Batch Size = 256

Layer (type)	Output Shape	Param #
conv2d_11 (Conv2D)	(None, 28, 28, 6)	456
activation_26 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_11 (MaxPooling)	(None, 14, 14, 6)	0
conv2d_12 (Conv2D)	(None, 10, 10, 16)	2416
activation_27 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_12 (MaxPooling)	(None, 5, 5, 16)	0
flatten_6 (Flatten)	(None, 400)	0
dense_16 (Dense)	(None, 120)	48120
activation_28 (Activation)	(None, 120)	0
dense_17 (Dense)	(None, 84)	10164

```

-----
activation_29 (Activation)      (None, 84)                0
-----
dense_18 (Dense)                (None, 10)               850
-----
activation_30 (Activation)      (None, 10)                0
=====
Total params: 62,006
Trainable params: 62,006
Non-trainable params: 0
-----
None
Train on 50000 samples, validate on 10000 samples
Epoch 1/30
50000/50000 [=====] - 49s 973us/step - loss: 2.1966 - acc: 0.1856 - va
Epoch 2/30
50000/50000 [=====] - 48s 970us/step - loss: 1.9138 - acc: 0.3078 - va
Epoch 3/30
50000/50000 [=====] - 48s 970us/step - loss: 1.7339 - acc: 0.3706 - va
Epoch 4/30
50000/50000 [=====] - 49s 971us/step - loss: 1.6417 - acc: 0.4034 - va
Epoch 5/30
50000/50000 [=====] - 49s 971us/step - loss: 1.5837 - acc: 0.4256 - va
Epoch 6/30
50000/50000 [=====] - 49s 971us/step - loss: 1.5382 - acc: 0.4416 - va
Epoch 7/30
50000/50000 [=====] - 49s 970us/step - loss: 1.5025 - acc: 0.4561 - va
Epoch 8/30
50000/50000 [=====] - 48s 970us/step - loss: 1.4690 - acc: 0.4685 - va
Epoch 9/30
50000/50000 [=====] - 48s 969us/step - loss: 1.4469 - acc: 0.4799 - va
Epoch 10/30
50000/50000 [=====] - 48s 969us/step - loss: 1.4211 - acc: 0.4886 - va
Epoch 11/30
50000/50000 [=====] - 49s 971us/step - loss: 1.3994 - acc: 0.4959 - va
Epoch 12/30
50000/50000 [=====] - 49s 970us/step - loss: 1.3839 - acc: 0.5061 - va
Epoch 13/30
49920/50000 [=====>.] - ETA: 0s - loss: 1.3683 - acc: 0.5105

```

**** Q7: [2 points] ****

Increase the **number of convolution filters** and experiment. Present your observations using plots and brief explanations. Take the values on a log scale. Vary only one parameter at a time.

**** A7: ****

Observations

1. Increasing the number of convolution filters in the first layer, improves the accuracy upto a certain number of filters as the model is able to learn more sophisticated and even minute features.
2. However, increasing the no of filters beyond a certain limit results in overfitting and leads to

decrease in accuracy of the model.

Graphs shown below in support of the observations.

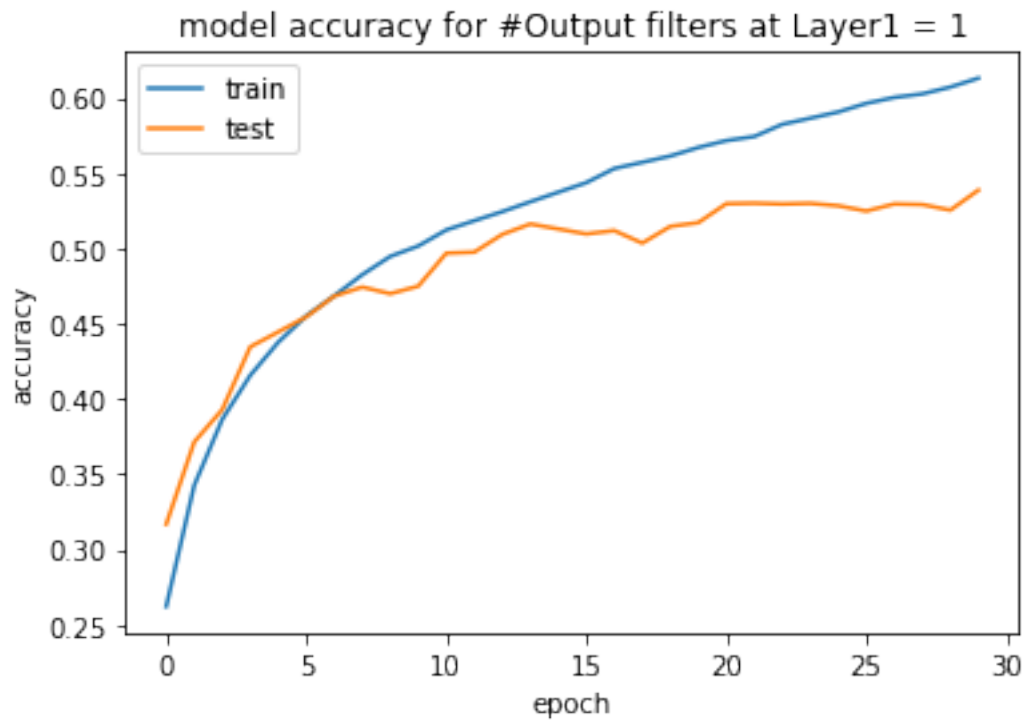
In [9]:

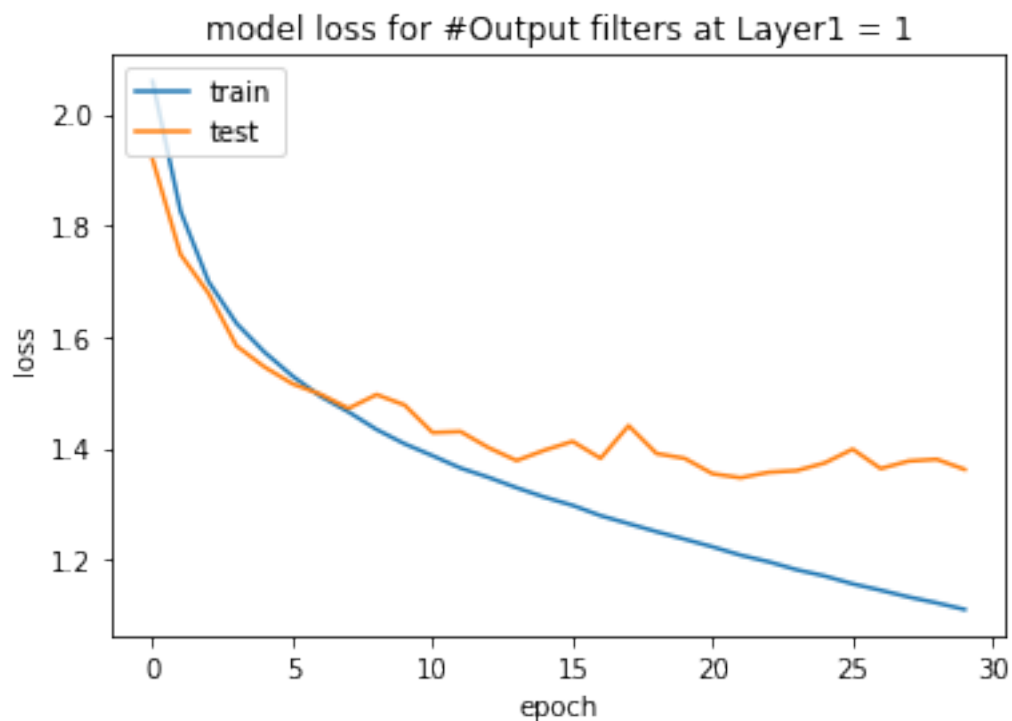
Training with #Output filters at Layer1 = 1

```
-----
Layer (type)                 Output Shape              Param #
-----
conv2d_13 (Conv2D)           (None, 28, 28, 1)         76
-----
activation_31 (Activation)    (None, 28, 28, 1)         0
-----
max_pooling2d_13 (MaxPooling (None, 14, 14, 1)         0
-----
conv2d_14 (Conv2D)           (None, 10, 10, 16)        416
-----
activation_32 (Activation)    (None, 10, 10, 16)        0
-----
max_pooling2d_14 (MaxPooling (None, 5, 5, 16)         0
-----
flatten_7 (Flatten)          (None, 400)               0
-----
dense_19 (Dense)              (None, 120)               48120
-----
activation_33 (Activation)    (None, 120)               0
-----
dense_20 (Dense)              (None, 84)                10164
-----
activation_34 (Activation)    (None, 84)                0
-----
dense_21 (Dense)              (None, 10)               850
-----
activation_35 (Activation)    (None, 10)               0
=====
Total params: 59,626
Trainable params: 59,626
Non-trainable params: 0
-----
None
Train on 50000 samples, validate on 10000 samples
Epoch 1/30
50000/50000 [=====] - 39s 774us/step - loss: 2.0591 - acc: 0.2621 - va
Epoch 2/30
50000/50000 [=====] - 39s 773us/step - loss: 1.8256 - acc: 0.3426 - va
Epoch 3/30
50000/50000 [=====] - 39s 771us/step - loss: 1.6991 - acc: 0.3864 - va
```

Epoch 4/30
50000/50000 [=====] - 38s 769us/step - loss: 1.6240 - acc: 0.4156 - va
Epoch 5/30
50000/50000 [=====] - 39s 775us/step - loss: 1.5724 - acc: 0.4377 - va
Epoch 6/30
50000/50000 [=====] - 39s 771us/step - loss: 1.5295 - acc: 0.4551 - va
Epoch 7/30
50000/50000 [=====] - 39s 771us/step - loss: 1.4931 - acc: 0.4685 - va
Epoch 8/30
50000/50000 [=====] - 39s 775us/step - loss: 1.4651 - acc: 0.4825 - va
Epoch 9/30
50000/50000 [=====] - 39s 771us/step - loss: 1.4336 - acc: 0.4947 - va
Epoch 10/30
50000/50000 [=====] - 39s 771us/step - loss: 1.4079 - acc: 0.5016 - va
Epoch 11/30
50000/50000 [=====] - 39s 771us/step - loss: 1.3865 - acc: 0.5122 - va
Epoch 12/30
50000/50000 [=====] - 39s 772us/step - loss: 1.3643 - acc: 0.5184 - va
Epoch 13/30
50000/50000 [=====] - 39s 771us/step - loss: 1.3476 - acc: 0.5244 - va
Epoch 14/30
50000/50000 [=====] - 39s 771us/step - loss: 1.3290 - acc: 0.5310 - va
Epoch 15/30
50000/50000 [=====] - 39s 774us/step - loss: 1.3120 - acc: 0.5373 - va
Epoch 16/30
50000/50000 [=====] - 39s 771us/step - loss: 1.2973 - acc: 0.5437 - va
Epoch 17/30
50000/50000 [=====] - 38s 769us/step - loss: 1.2788 - acc: 0.5531 - va
Epoch 18/30
50000/50000 [=====] - 39s 773us/step - loss: 1.2645 - acc: 0.5572 - va
Epoch 19/30
50000/50000 [=====] - 38s 769us/step - loss: 1.2500 - acc: 0.5614 - va
Epoch 20/30
50000/50000 [=====] - 38s 769us/step - loss: 1.2366 - acc: 0.5670 - va
Epoch 21/30
50000/50000 [=====] - 39s 772us/step - loss: 1.2228 - acc: 0.5716 - va
Epoch 22/30
50000/50000 [=====] - 38s 768us/step - loss: 1.2079 - acc: 0.5743 - va
Epoch 23/30
50000/50000 [=====] - 38s 768us/step - loss: 1.1960 - acc: 0.5824 - va
Epoch 24/30
50000/50000 [=====] - 39s 774us/step - loss: 1.1817 - acc: 0.5865 - va
Epoch 25/30
50000/50000 [=====] - 39s 771us/step - loss: 1.1705 - acc: 0.5906 - va
Epoch 26/30
50000/50000 [=====] - 38s 766us/step - loss: 1.1563 - acc: 0.5963 - va
Epoch 27/30
50000/50000 [=====] - 38s 769us/step - loss: 1.1449 - acc: 0.6003 - va

Epoch 28/30
50000/50000 [=====] - 38s 769us/step - loss: 1.1327 - acc: 0.6026 - va
Epoch 29/30
50000/50000 [=====] - 38s 764us/step - loss: 1.1221 - acc: 0.6071 - va
Epoch 30/30
50000/50000 [=====] - 38s 766us/step - loss: 1.1103 - acc: 0.6131 - va





Training with #Output filters at Layer1 = 10

Layer (type)	Output Shape	Param #
conv2d_15 (Conv2D)	(None, 28, 28, 10)	760
activation_36 (Activation)	(None, 28, 28, 10)	0
max_pooling2d_15 (MaxPooling)	(None, 14, 14, 10)	0
conv2d_16 (Conv2D)	(None, 10, 10, 16)	4016
activation_37 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_16 (MaxPooling)	(None, 5, 5, 16)	0
flatten_8 (Flatten)	(None, 400)	0
dense_22 (Dense)	(None, 120)	48120
activation_38 (Activation)	(None, 120)	0
dense_23 (Dense)	(None, 84)	10164

```

-----
activation_39 (Activation)      (None, 84)                0
-----
dense_24 (Dense)               (None, 10)               850
-----
activation_40 (Activation)      (None, 10)                0
=====

```

```

Total params: 63,910
Trainable params: 63,910
Non-trainable params: 0

```

```

-----
None

```

```

Train on 50000 samples, validate on 10000 samples

```

```

Epoch 1/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.8218 - acc: 0.3343 - val.

```

```

Epoch 2/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.4842 - acc: 0.4653 - val.

```

```

Epoch 3/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.3666 - acc: 0.5092 - val.

```

```

Epoch 4/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.2887 - acc: 0.5373 - val.

```

```

Epoch 5/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.2313 - acc: 0.5604 - val.

```

```

Epoch 6/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.1827 - acc: 0.5807 - val.

```

```

Epoch 7/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.1405 - acc: 0.5962 - val.

```

```

Epoch 8/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.1049 - acc: 0.6089 - val.

```

```

Epoch 9/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.0741 - acc: 0.6195 - val.

```

```

Epoch 10/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.0438 - acc: 0.6302 - val.

```

```

Epoch 11/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 1.0128 - acc: 0.6432 - val.

```

```

Epoch 12/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 0.9916 - acc: 0.6510 - val.

```

```

Epoch 13/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 0.9638 - acc: 0.6615 - val.

```

```

Epoch 14/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 0.9437 - acc: 0.6672 - val.

```

```

Epoch 15/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 0.9197 - acc: 0.6766 - val.

```

```

Epoch 16/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 0.9033 - acc: 0.6825 - val.

```

```

Epoch 17/30

```

```

50000/50000 [=====] - 60s 1ms/step - loss: 0.8810 - acc: 0.6902 - val.

```

```

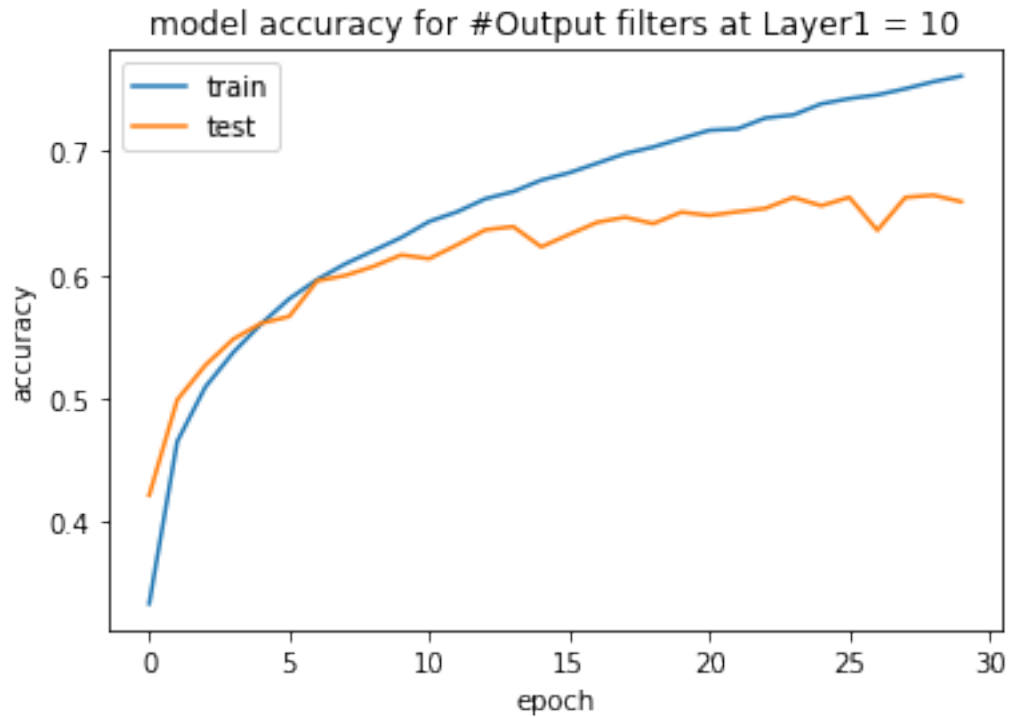
Epoch 18/30

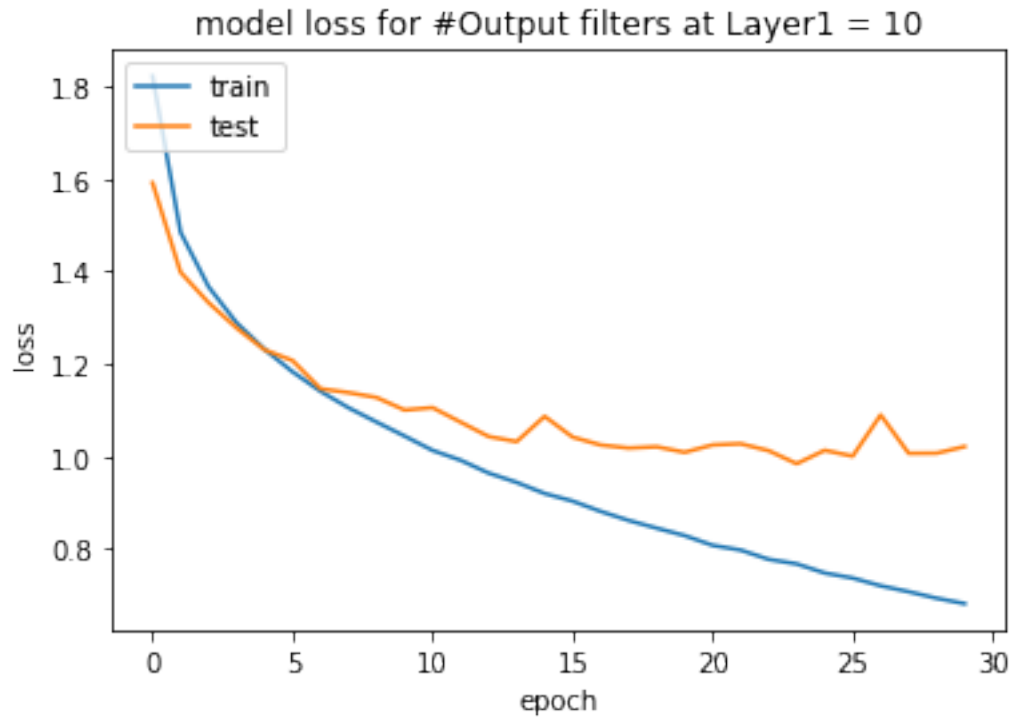
```

```

50000/50000 [=====] - 60s 1ms/step - loss: 0.8615 - acc: 0.6981 - val.
Epoch 19/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.8448 - acc: 0.7033 - val.
Epoch 20/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.8287 - acc: 0.7102 - val.
Epoch 21/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.8076 - acc: 0.7168 - val.
Epoch 22/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.7974 - acc: 0.7180 - val.
Epoch 23/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.7773 - acc: 0.7268 - val.
Epoch 24/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.7676 - acc: 0.7293 - val.
Epoch 25/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.7478 - acc: 0.7382 - val.
Epoch 26/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.7370 - acc: 0.7425 - val.
Epoch 27/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.7202 - acc: 0.7455 - val.
Epoch 28/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.7074 - acc: 0.7504 - val.
Epoch 29/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.6933 - acc: 0.7561 - val.
Epoch 30/30
50000/50000 [=====] - 60s 1ms/step - loss: 0.6816 - acc: 0.7607 - val.

```





Training with #Output filters at Layer1 = 25

Layer (type)	Output Shape	Param #
conv2d_17 (Conv2D)	(None, 28, 28, 25)	1900
activation_41 (Activation)	(None, 28, 28, 25)	0
max_pooling2d_17 (MaxPooling)	(None, 14, 14, 25)	0
conv2d_18 (Conv2D)	(None, 10, 10, 16)	10016
activation_42 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_18 (MaxPooling)	(None, 5, 5, 16)	0
flatten_9 (Flatten)	(None, 400)	0
dense_25 (Dense)	(None, 120)	48120

activation_43 (Activation)	(None, 120)	0

dense_26 (Dense)	(None, 84)	10164

activation_44 (Activation)	(None, 84)	0

dense_27 (Dense)	(None, 10)	850

activation_45 (Activation)	(None, 10)	0
=====		

Total params: 71,050

Trainable params: 71,050

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 93s 2ms/step - loss: 1.7594 - acc: 0.3597 - val.

Epoch 2/30

50000/50000 [=====] - 93s 2ms/step - loss: 1.4482 - acc: 0.4802 - val.

Epoch 3/30

50000/50000 [=====] - 92s 2ms/step - loss: 1.3272 - acc: 0.5270 - val.

Epoch 4/30

50000/50000 [=====] - 92s 2ms/step - loss: 1.2308 - acc: 0.5637 - val.

Epoch 5/30

50000/50000 [=====] - 92s 2ms/step - loss: 1.1603 - acc: 0.5907 - val.

Epoch 6/30

50000/50000 [=====] - 92s 2ms/step - loss: 1.1028 - acc: 0.6128 - val.

Epoch 7/30

50000/50000 [=====] - 92s 2ms/step - loss: 1.0528 - acc: 0.6304 - val.

Epoch 8/30

50000/50000 [=====] - 92s 2ms/step - loss: 1.0127 - acc: 0.6446 - val.

Epoch 9/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.9756 - acc: 0.6573 - val.

Epoch 10/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.9430 - acc: 0.6694 - val.

Epoch 11/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.9135 - acc: 0.6782 - val.

Epoch 12/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.8887 - acc: 0.6870 - val.

Epoch 13/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.8608 - acc: 0.6976 - val.

Epoch 14/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.8355 - acc: 0.7068 - val.

Epoch 15/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.8115 - acc: 0.7168 - val.

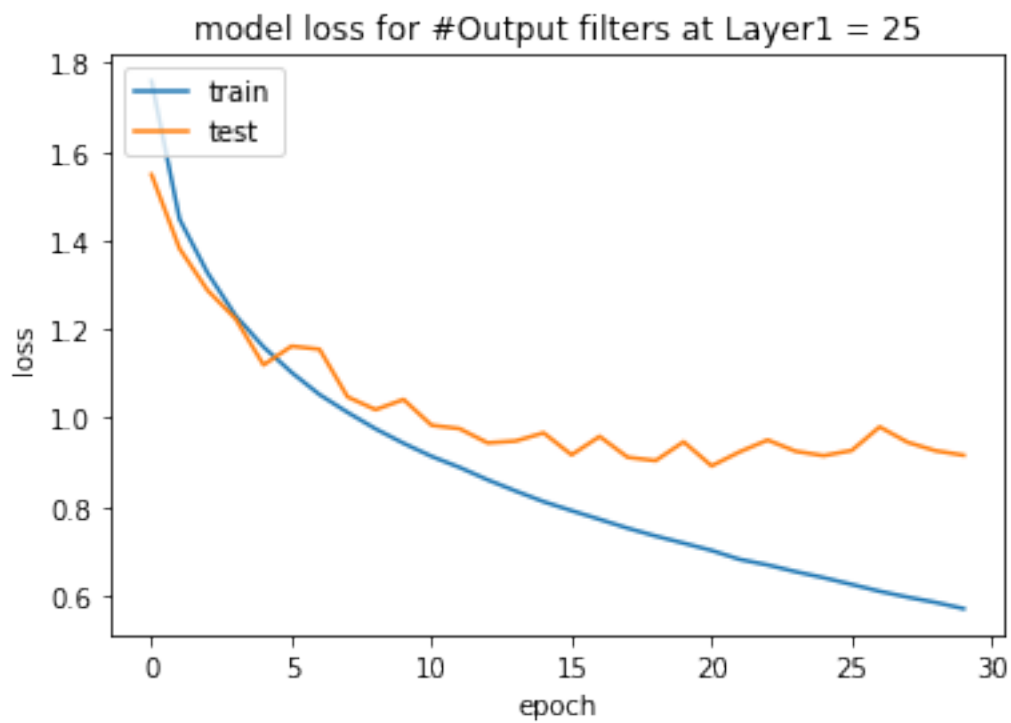
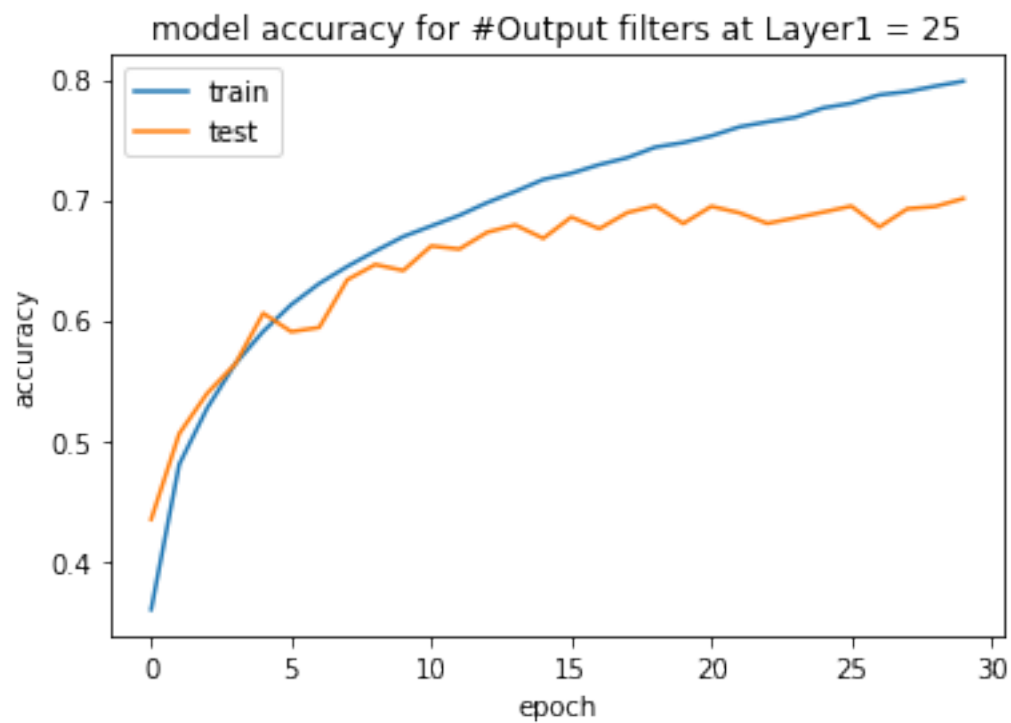
Epoch 16/30

50000/50000 [=====] - 92s 2ms/step - loss: 0.7912 - acc: 0.7219 - val.

```

Epoch 17/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.7716 - acc: 0.7291 - val.
Epoch 18/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.7517 - acc: 0.7349 - val.
Epoch 19/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.7340 - acc: 0.7437 - val.
Epoch 20/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.7180 - acc: 0.7474 - val.
Epoch 21/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.7015 - acc: 0.7530 - val.
Epoch 22/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.6814 - acc: 0.7605 - val.
Epoch 23/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.6688 - acc: 0.7647 - val.
Epoch 24/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.6537 - acc: 0.7684 - val.
Epoch 25/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.6401 - acc: 0.7763 - val.
Epoch 26/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.6249 - acc: 0.7801 - val.
Epoch 27/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.6095 - acc: 0.7871 - val.
Epoch 28/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.5962 - acc: 0.7898 - val.
Epoch 29/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.5844 - acc: 0.7943 - val.
Epoch 30/30
50000/50000 [=====] - 92s 2ms/step - loss: 0.5703 - acc: 0.7985 - val.

```



Training with #Output filters at Layer1 = 50

Layer (type)	Output Shape	Param #
conv2d_19 (Conv2D)	(None, 28, 28, 50)	3800
activation_46 (Activation)	(None, 28, 28, 50)	0
max_pooling2d_19 (MaxPooling)	(None, 14, 14, 50)	0
conv2d_20 (Conv2D)	(None, 10, 10, 16)	20016
activation_47 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_20 (MaxPooling)	(None, 5, 5, 16)	0
flatten_10 (Flatten)	(None, 400)	0
dense_28 (Dense)	(None, 120)	48120
activation_48 (Activation)	(None, 120)	0
dense_29 (Dense)	(None, 84)	10164
activation_49 (Activation)	(None, 84)	0
dense_30 (Dense)	(None, 10)	850
activation_50 (Activation)	(None, 10)	0

Total params: 82,950

Trainable params: 82,950

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 148s 3ms/step - loss: 1.7639 - acc: 0.3557 - va

Epoch 2/30

50000/50000 [=====] - 148s 3ms/step - loss: 1.4333 - acc: 0.4840 - va

Epoch 3/30

50000/50000 [=====] - 147s 3ms/step - loss: 1.3063 - acc: 0.5317 - va

Epoch 4/30

50000/50000 [=====] - 147s 3ms/step - loss: 1.2032 - acc: 0.5702 - va

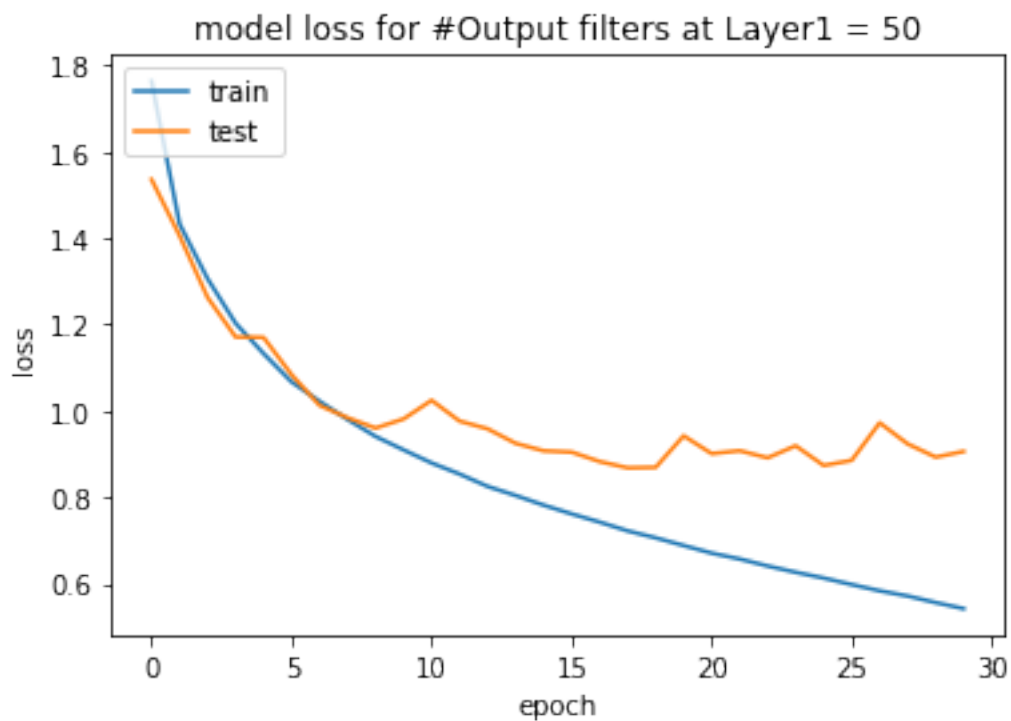
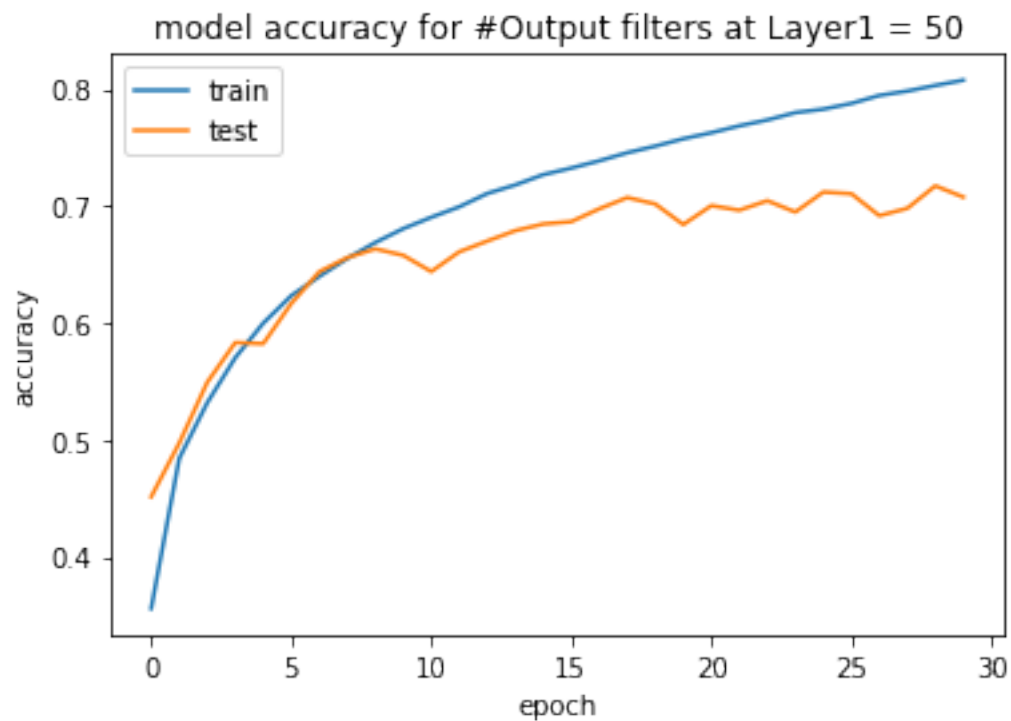
Epoch 5/30

50000/50000 [=====] - 147s 3ms/step - loss: 1.1328 - acc: 0.5998 - va

Epoch 6/30

50000/50000 [=====] - 147s 3ms/step - loss: 1.0673 - acc: 0.6233 - va.
 Epoch 7/30
 50000/50000 [=====] - 147s 3ms/step - loss: 1.0222 - acc: 0.6398 - va.
 Epoch 8/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.9802 - acc: 0.6551 - va.
 Epoch 9/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.9409 - acc: 0.6688 - va.
 Epoch 10/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.9098 - acc: 0.6807 - va.
 Epoch 11/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.8795 - acc: 0.6904 - va.
 Epoch 12/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.8538 - acc: 0.6994 - va.
 Epoch 13/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.8252 - acc: 0.7108 - va.
 Epoch 14/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.8042 - acc: 0.7181 - va.
 Epoch 15/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.7819 - acc: 0.7269 - va.
 Epoch 16/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.7616 - acc: 0.7325 - va.
 Epoch 17/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.7426 - acc: 0.7388 - va.
 Epoch 18/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.7222 - acc: 0.7457 - va.
 Epoch 19/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.7062 - acc: 0.7513 - va.
 Epoch 20/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.6883 - acc: 0.7576 - va.
 Epoch 21/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.6707 - acc: 0.7628 - va.
 Epoch 22/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.6572 - acc: 0.7687 - va.
 Epoch 23/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.6409 - acc: 0.7737 - va.
 Epoch 24/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.6264 - acc: 0.7800 - va.
 Epoch 25/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.6130 - acc: 0.7829 - va.
 Epoch 26/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.5979 - acc: 0.7878 - va.
 Epoch 27/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.5835 - acc: 0.7947 - va.
 Epoch 28/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.5714 - acc: 0.7984 - va.
 Epoch 29/30
 50000/50000 [=====] - 147s 3ms/step - loss: 0.5562 - acc: 0.8032 - va.
 Epoch 30/30

50000/50000 [=====] - 147s 3ms/step - loss: 0.5421 - acc: 0.8077 - va



Training with #Output filters at Layer1 = 100

Layer (type)	Output Shape	Param #
conv2d_21 (Conv2D)	(None, 28, 28, 100)	7600
activation_51 (Activation)	(None, 28, 28, 100)	0
max_pooling2d_21 (MaxPooling)	(None, 14, 14, 100)	0
conv2d_22 (Conv2D)	(None, 10, 10, 16)	40016
activation_52 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_22 (MaxPooling)	(None, 5, 5, 16)	0
flatten_11 (Flatten)	(None, 400)	0
dense_31 (Dense)	(None, 120)	48120
activation_53 (Activation)	(None, 120)	0
dense_32 (Dense)	(None, 84)	10164
activation_54 (Activation)	(None, 84)	0
dense_33 (Dense)	(None, 10)	850
activation_55 (Activation)	(None, 10)	0

Total params: 106,750

Trainable params: 106,750

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 234s 5ms/step - loss: 1.7726 - acc: 0.3588 - va

Epoch 2/30

50000/50000 [=====] - 233s 5ms/step - loss: 1.4308 - acc: 0.4865 - va

Epoch 3/30

50000/50000 [=====] - 234s 5ms/step - loss: 1.2990 - acc: 0.5380 - va

Epoch 4/30

50000/50000 [=====] - 234s 5ms/step - loss: 1.2048 - acc: 0.5741 - va

```

Epoch 5/30
50000/50000 [=====] - 233s 5ms/step - loss: 1.1277 - acc: 0.6050 - va
Epoch 6/30
50000/50000 [=====] - 233s 5ms/step - loss: 1.0682 - acc: 0.6275 - va
Epoch 7/30
50000/50000 [=====] - 234s 5ms/step - loss: 1.0204 - acc: 0.6426 - va
Epoch 8/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.9807 - acc: 0.6559 - va
Epoch 9/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.9423 - acc: 0.6693 - va
Epoch 10/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.9104 - acc: 0.6811 - va
Epoch 11/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.8790 - acc: 0.6930 - va
Epoch 12/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.8511 - acc: 0.7035 - va
Epoch 13/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.8289 - acc: 0.7109 - va
Epoch 14/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.8054 - acc: 0.7176 - va
Epoch 15/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.7822 - acc: 0.7265 - va
Epoch 16/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.7633 - acc: 0.7322 - va
Epoch 17/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.7400 - acc: 0.7416 - va
Epoch 18/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.7220 - acc: 0.7490 - va
Epoch 19/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.7050 - acc: 0.7539 - va
Epoch 20/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.6879 - acc: 0.7588 - va
Epoch 21/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.6714 - acc: 0.7646 - va
Epoch 22/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.6521 - acc: 0.7699 - va
Epoch 23/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.6381 - acc: 0.7778 - va
Epoch 24/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.6220 - acc: 0.7813 - va
Epoch 25/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.6101 - acc: 0.7867 - va
Epoch 26/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.5946 - acc: 0.7902 - va
Epoch 27/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.5822 - acc: 0.7943 - va
Epoch 28/30
50000/50000 [=====] - 233s 5ms/step - loss: 0.5709 - acc: 0.7993 - va

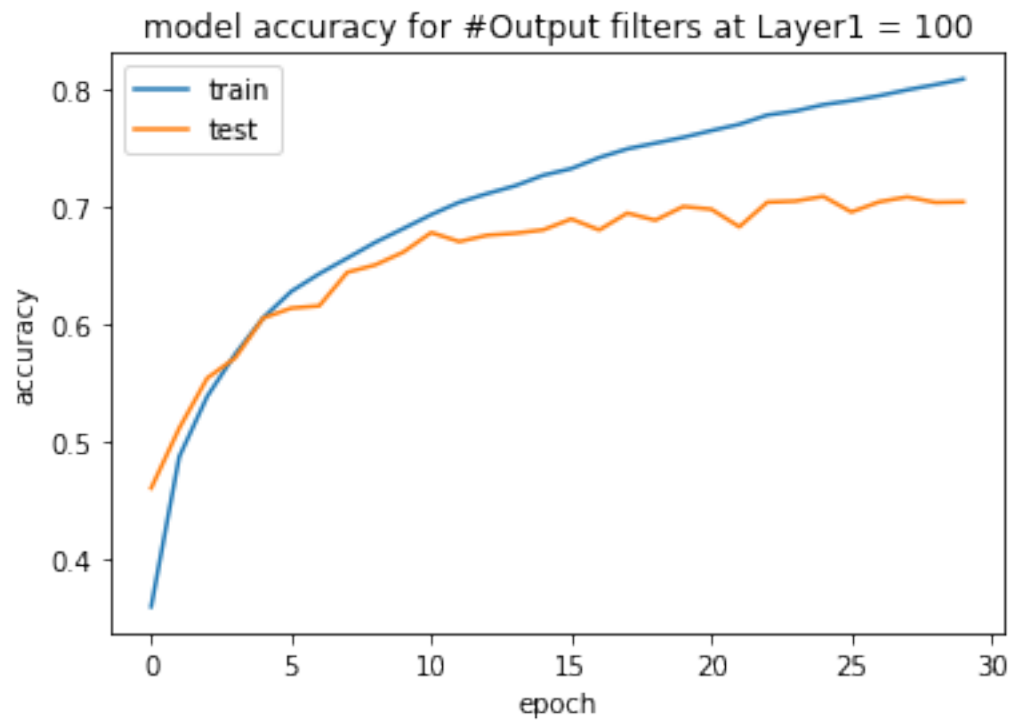
```

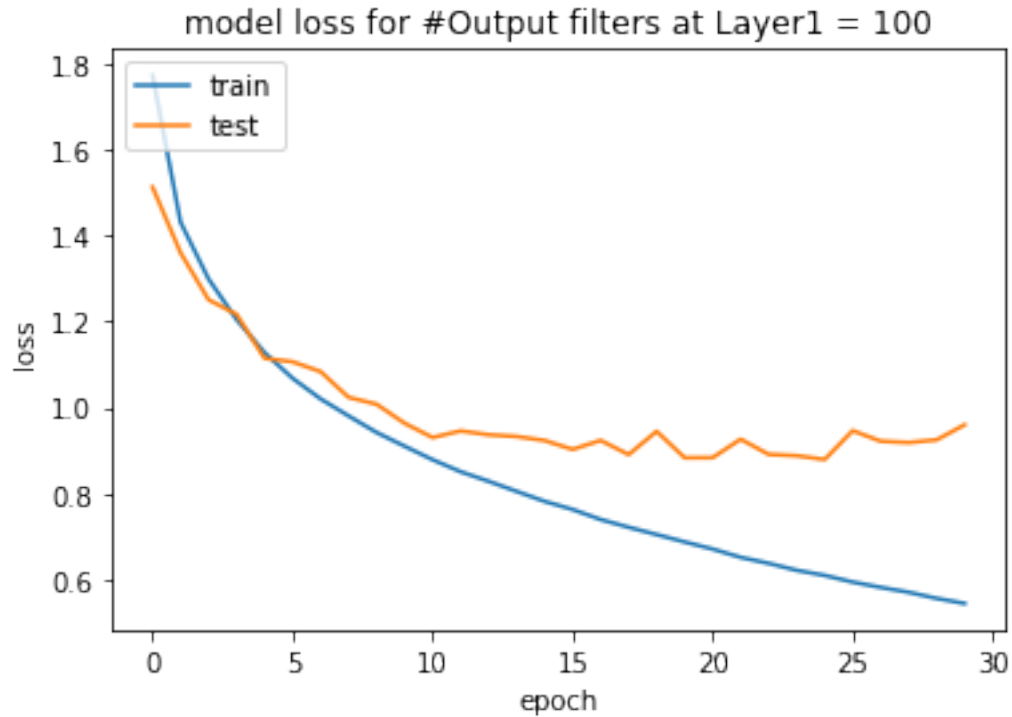
Epoch 29/30

50000/50000 [=====] - 233s 5ms/step - loss: 0.5567 - acc: 0.8037 - va

Epoch 30/30

50000/50000 [=====] - 233s 5ms/step - loss: 0.5449 - acc: 0.8085 - va





**** Q8: [2 points] ****

What do you observe if you increase the **number of layers** (depth of the network) ? Present your observations using plots and brief explanations.

**** A8: ****

Observations

1. If the Neural Network is wider and deeper the back-propagation and hyper-parameters becomes very complicated. However increasing the number of hidden layers increases the accuracy and also fit even most complex non-linear classifiers.

Graph below in support of the observations.

In [10]:

Layer (type)	Output Shape	Param #
conv2d_12 (Conv2D)	(None, 32, 32, 6)	456
activation_14 (Activation)	(None, 32, 32, 6)	0
max_pooling2d_9 (MaxPooling2D)	(None, 16, 16, 6)	0
conv2d_13 (Conv2D)	(None, 16, 16, 16)	2416
activation_15 (Activation)	(None, 16, 16, 16)	0

conv2d_14 (Conv2D)	(None, 16, 16, 32)	12832
activation_16 (Activation)	(None, 16, 16, 32)	0
conv2d_15 (Conv2D)	(None, 12, 12, 64)	51264
activation_17 (Activation)	(None, 12, 12, 64)	0
max_pooling2d_10 (MaxPooling)	(None, 6, 6, 64)	0
flatten_2 (Flatten)	(None, 2304)	0
dense_4 (Dense)	(None, 120)	276600
activation_18 (Activation)	(None, 120)	0
dense_5 (Dense)	(None, 84)	10164
activation_19 (Activation)	(None, 84)	0
dense_6 (Dense)	(None, 10)	850
activation_20 (Activation)	(None, 10)	0

=====
Total params: 354,582

Trainable params: 354,582

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 274s 5ms/step - loss: 1.8120 - acc: 0.3415 - va

Epoch 2/30

50000/50000 [=====] - 273s 5ms/step - loss: 1.4712 - acc: 0.4712 - va

Epoch 3/30

50000/50000 [=====] - 273s 5ms/step - loss: 1.3195 - acc: 0.5278 - va

Epoch 4/30

50000/50000 [=====] - 273s 5ms/step - loss: 1.1932 - acc: 0.5741 - va

Epoch 5/30

50000/50000 [=====] - 273s 5ms/step - loss: 1.0969 - acc: 0.6125 - va

Epoch 6/30

50000/50000 [=====] - 273s 5ms/step - loss: 1.0121 - acc: 0.6443 - va

Epoch 7/30

50000/50000 [=====] - 273s 5ms/step - loss: 0.9453 - acc: 0.6667 - va

Epoch 8/30

50000/50000 [=====] - 273s 5ms/step - loss: 0.8846 - acc: 0.6884 - va

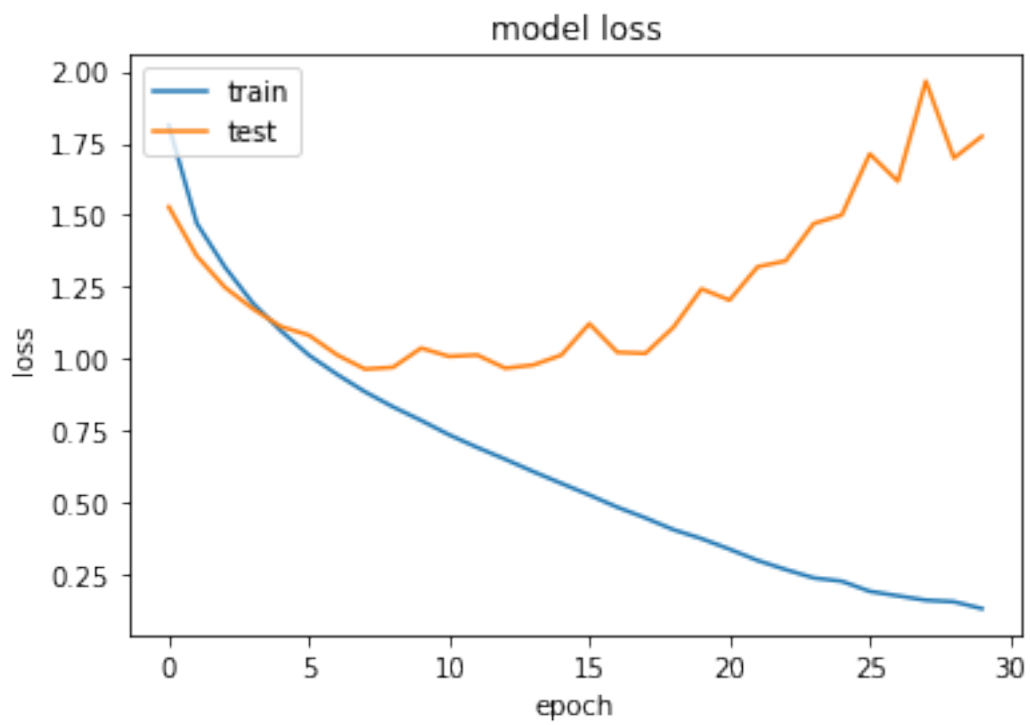
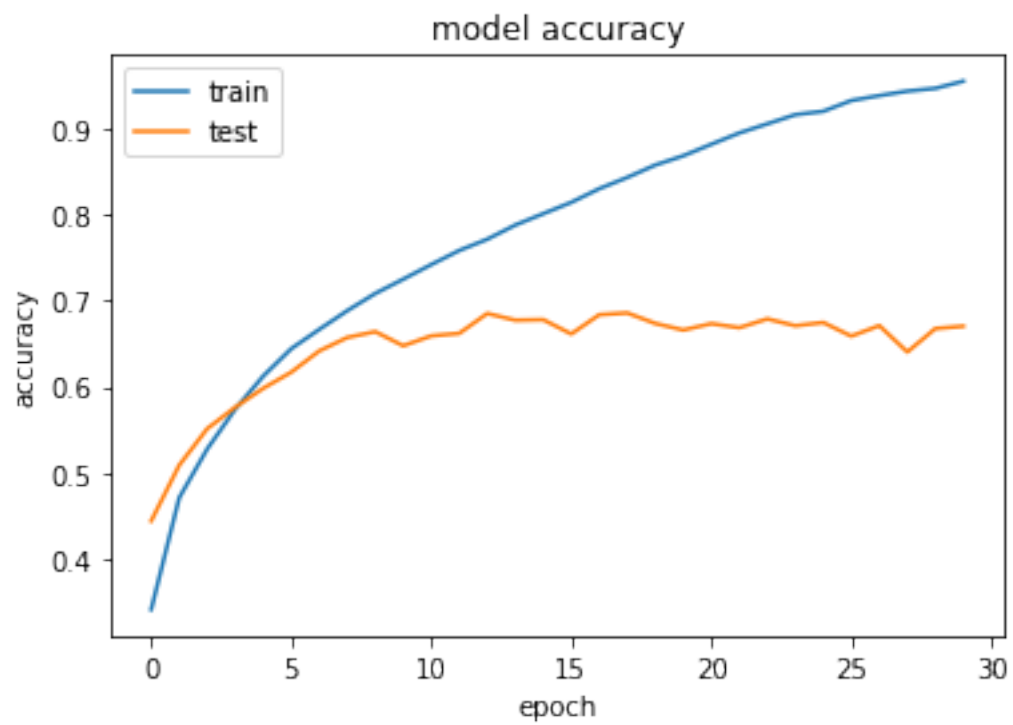
Epoch 9/30

50000/50000 [=====] - 273s 5ms/step - loss: 0.8321 - acc: 0.7084 - va

```

Epoch 10/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.7850 - acc: 0.7251 - va
Epoch 11/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.7349 - acc: 0.7420 - va
Epoch 12/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.6909 - acc: 0.7584 - va
Epoch 13/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.6498 - acc: 0.7714 - va
Epoch 14/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.6068 - acc: 0.7879 - va
Epoch 15/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.5658 - acc: 0.8011 - va
Epoch 16/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.5254 - acc: 0.8143 - va
Epoch 17/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.4827 - acc: 0.8301 - va
Epoch 18/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.4455 - acc: 0.8432 - va
Epoch 19/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.4044 - acc: 0.8576 - va
Epoch 20/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.3734 - acc: 0.8683 - va
Epoch 21/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.3366 - acc: 0.8817 - va
Epoch 22/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.2973 - acc: 0.8948 - va
Epoch 23/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.2657 - acc: 0.9054 - va
Epoch 24/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.2364 - acc: 0.9161 - va
Epoch 25/30
50000/50000 [=====] - 274s 5ms/step - loss: 0.2251 - acc: 0.9200 - va
Epoch 26/30
50000/50000 [=====] - 274s 5ms/step - loss: 0.1898 - acc: 0.9325 - va
Epoch 27/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.1743 - acc: 0.9382 - va
Epoch 28/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.1589 - acc: 0.9434 - va
Epoch 29/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.1537 - acc: 0.9466 - va
Epoch 30/30
50000/50000 [=====] - 273s 5ms/step - loss: 0.1296 - acc: 0.9550 - va

```

**** Q9: [2 points] ****

What do you observe if you increase the **activation functions** (tanh, relu, sigmoid) ? Present your observations using plots and brief explanations.

**** A9: ****

Observations .

1. The Rectified Linear Unit (ReLU) activation function gives the best accuracy in comparison with the other activation functions. It is because it eases the gradient computation.

See the graphs below to support the observations.

In [7]:

Training with Activation Function = tanh

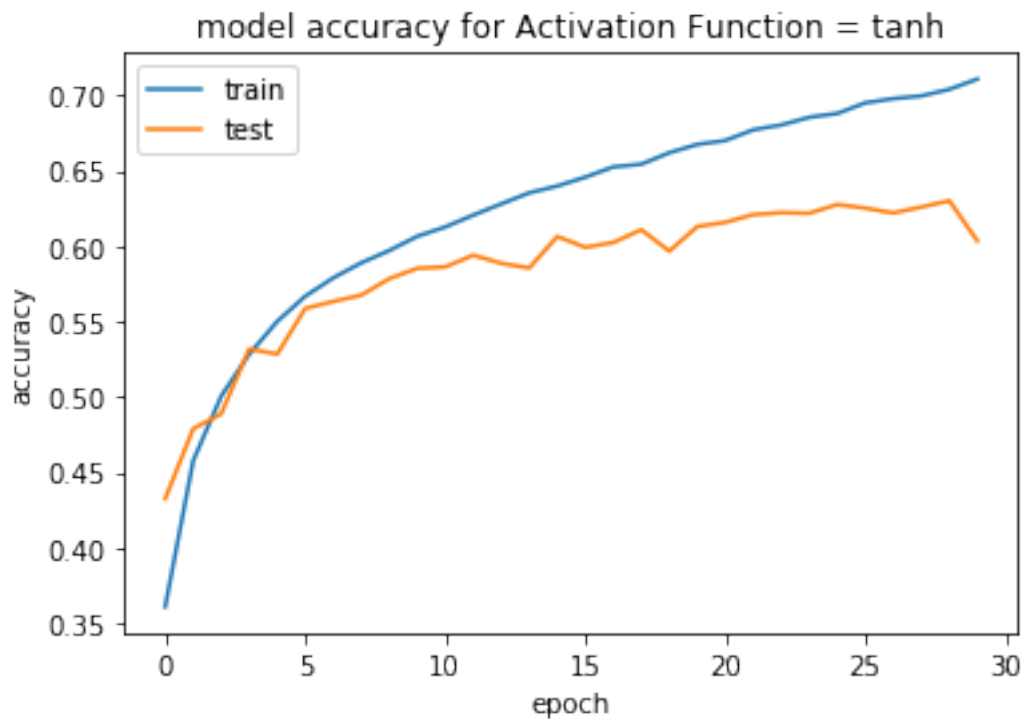
Layer (type)	Output Shape	Param #
conv2d_1 (Conv2D)	(None, 28, 28, 6)	456
activation_1 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_1 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_2 (Conv2D)	(None, 10, 10, 16)	2416
activation_2 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_2 (MaxPooling2D)	(None, 5, 5, 16)	0
flatten_1 (Flatten)	(None, 400)	0
dense_1 (Dense)	(None, 120)	48120
activation_3 (Activation)	(None, 120)	0
dense_2 (Dense)	(None, 84)	10164
activation_4 (Activation)	(None, 84)	0
dense_3 (Dense)	(None, 10)	850
activation_5 (Activation)	(None, 10)	0
Total params: 62,006		
Trainable params: 62,006		
Non-trainable params: 0		

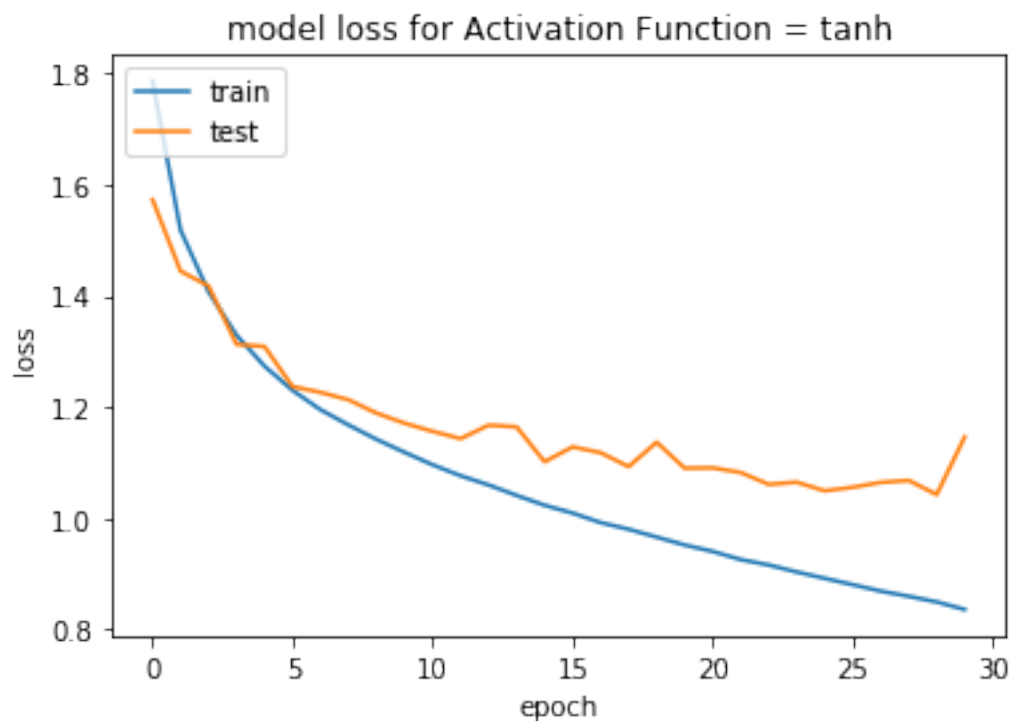
None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30
50000/50000 [=====] - 41s 822us/step - loss: 1.7864 - acc: 0.3608 - va
Epoch 2/30
50000/50000 [=====] - 40s 806us/step - loss: 1.5183 - acc: 0.4577 - va
Epoch 3/30
50000/50000 [=====] - 41s 815us/step - loss: 1.4075 - acc: 0.5004 - va
Epoch 4/30
50000/50000 [=====] - 41s 819us/step - loss: 1.3293 - acc: 0.5282 - va
Epoch 5/30
50000/50000 [=====] - 41s 823us/step - loss: 1.2736 - acc: 0.5500 - va
Epoch 6/30
50000/50000 [=====] - 41s 828us/step - loss: 1.2302 - acc: 0.5667 - va
Epoch 7/30
50000/50000 [=====] - 42s 849us/step - loss: 1.1952 - acc: 0.5788 - va
Epoch 8/30
50000/50000 [=====] - 43s 867us/step - loss: 1.1678 - acc: 0.5888 - va
Epoch 9/30
50000/50000 [=====] - 44s 873us/step - loss: 1.1419 - acc: 0.5970 - va
Epoch 10/30
50000/50000 [=====] - 44s 880us/step - loss: 1.1186 - acc: 0.6064 - va
Epoch 11/30
50000/50000 [=====] - 44s 889us/step - loss: 1.0963 - acc: 0.6126 - va
Epoch 12/30
50000/50000 [=====] - 45s 900us/step - loss: 1.0765 - acc: 0.6205 - va
Epoch 13/30
50000/50000 [=====] - 46s 920us/step - loss: 1.0600 - acc: 0.6279 - va
Epoch 14/30
50000/50000 [=====] - 46s 926us/step - loss: 1.0411 - acc: 0.6352 - va
Epoch 15/30
50000/50000 [=====] - 45s 900us/step - loss: 1.0234 - acc: 0.6398 - va
Epoch 16/30
50000/50000 [=====] - 44s 889us/step - loss: 1.0093 - acc: 0.6456 - va
Epoch 17/30
50000/50000 [=====] - 45s 908us/step - loss: 0.9922 - acc: 0.6525 - va
Epoch 18/30
50000/50000 [=====] - 46s 913us/step - loss: 0.9803 - acc: 0.6542 - va
Epoch 19/30
50000/50000 [=====] - 46s 922us/step - loss: 0.9661 - acc: 0.6618 - va
Epoch 20/30
50000/50000 [=====] - 47s 932us/step - loss: 0.9520 - acc: 0.6674 - va
Epoch 21/30
50000/50000 [=====] - 47s 933us/step - loss: 0.9404 - acc: 0.6699 - va
Epoch 22/30
50000/50000 [=====] - 47s 946us/step - loss: 0.9257 - acc: 0.6771 - va
Epoch 23/30
50000/50000 [=====] - 48s 958us/step - loss: 0.9160 - acc: 0.6803 - va
Epoch 24/30
50000/50000 [=====] - 49s 970us/step - loss: 0.9034 - acc: 0.6853 - va

Epoch 25/30
 50000/50000 [=====] - 49s 974us/step - loss: 0.8919 - acc: 0.6879 - val.
 Epoch 26/30
 50000/50000 [=====] - 49s 981us/step - loss: 0.8805 - acc: 0.6949 - val.
 Epoch 27/30
 50000/50000 [=====] - 49s 986us/step - loss: 0.8690 - acc: 0.6977 - val.
 Epoch 28/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8596 - acc: 0.6995 - val.
 Epoch 29/30
 50000/50000 [=====] - 50s 1000us/step - loss: 0.8495 - acc: 0.7039 - val.
 Epoch 30/30
 50000/50000 [=====] - 50s 1ms/step - loss: 0.8359 - acc: 0.7107 - val.





Training with Activation Function = relu

Layer (type)	Output Shape	Param #
conv2d_3 (Conv2D)	(None, 28, 28, 6)	456
activation_6 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_3 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_4 (Conv2D)	(None, 10, 10, 16)	2416
activation_7 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_4 (MaxPooling2D)	(None, 5, 5, 16)	0
flatten_2 (Flatten)	(None, 400)	0
dense_4 (Dense)	(None, 120)	48120
activation_8 (Activation)	(None, 120)	0
dense_5 (Dense)	(None, 84)	10164

```

-----
activation_9 (Activation)      (None, 84)                0
-----
dense_6 (Dense)                (None, 10)               850
-----
activation_10 (Activation)     (None, 10)                0
=====

```

Total params: 62,006
Trainable params: 62,006
Non-trainable params: 0

```
-----
None
```

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 38s 755us/step - loss: 1.7910 - acc: 0.3423 - va

Epoch 2/30

50000/50000 [=====] - 37s 732us/step - loss: 1.4936 - acc: 0.4564 - va

Epoch 3/30

50000/50000 [=====] - 37s 748us/step - loss: 1.3899 - acc: 0.4991 - va

Epoch 4/30

50000/50000 [=====] - 38s 753us/step - loss: 1.3216 - acc: 0.5264 - va

Epoch 5/30

50000/50000 [=====] - 38s 764us/step - loss: 1.2637 - acc: 0.5507 - va

Epoch 6/30

50000/50000 [=====] - 38s 769us/step - loss: 1.2157 - acc: 0.5690 - va

Epoch 7/30

50000/50000 [=====] - 40s 797us/step - loss: 1.1776 - acc: 0.5847 - va

Epoch 8/30

50000/50000 [=====] - 40s 803us/step - loss: 1.1432 - acc: 0.5932 - va

Epoch 9/30

50000/50000 [=====] - 41s 823us/step - loss: 1.1145 - acc: 0.6064 - va

Epoch 10/30

50000/50000 [=====] - 41s 823us/step - loss: 1.0833 - acc: 0.6172 - va

Epoch 11/30

50000/50000 [=====] - 41s 825us/step - loss: 1.0584 - acc: 0.6272 - va

Epoch 12/30

50000/50000 [=====] - 41s 828us/step - loss: 1.0364 - acc: 0.6335 - va

Epoch 13/30

50000/50000 [=====] - 42s 849us/step - loss: 1.0135 - acc: 0.6427 - va

Epoch 14/30

50000/50000 [=====] - 43s 860us/step - loss: 0.9974 - acc: 0.6482 - va

Epoch 15/30

50000/50000 [=====] - 45s 892us/step - loss: 0.9764 - acc: 0.6564 - va

Epoch 16/30

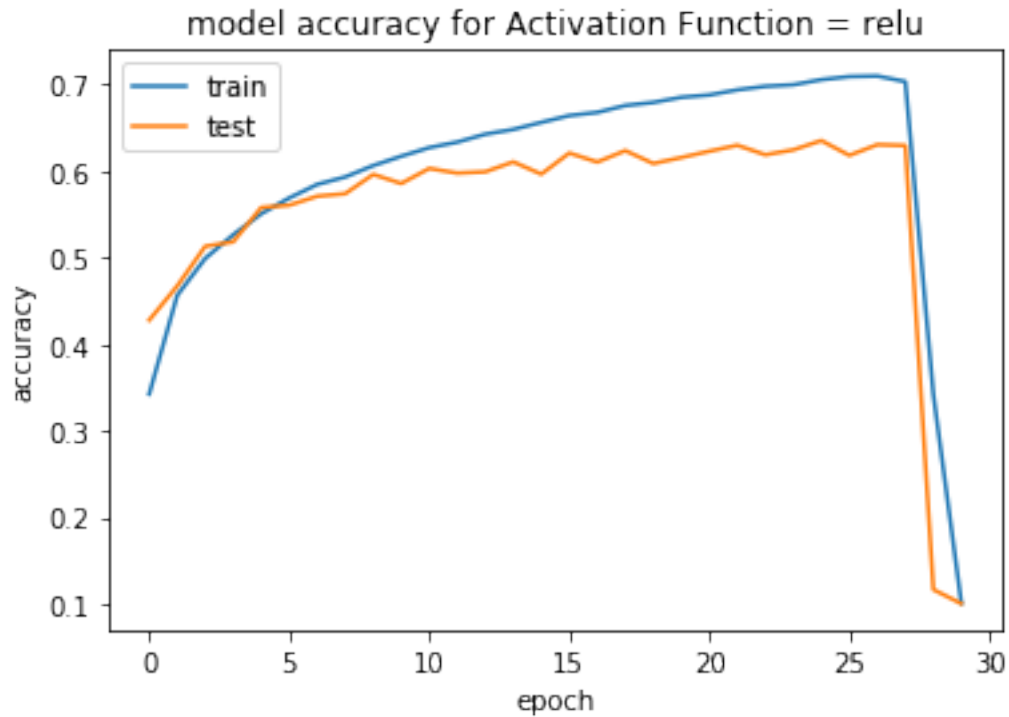
50000/50000 [=====] - 45s 899us/step - loss: 0.9560 - acc: 0.6642 - va

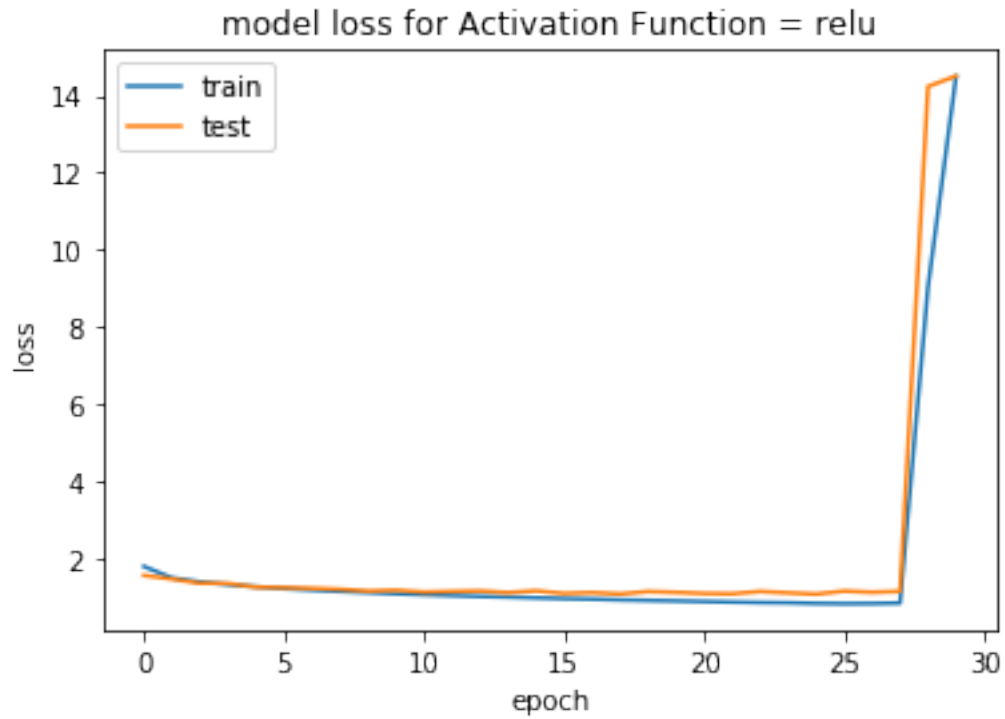
Epoch 17/30

50000/50000 [=====] - 45s 901us/step - loss: 0.9421 - acc: 0.6679 - va

Epoch 18/30

50000/50000 [=====] - 46s 916us/step - loss: 0.9234 - acc: 0.6758 - va
Epoch 19/30
50000/50000 [=====] - 46s 923us/step - loss: 0.9092 - acc: 0.6794 - va
Epoch 20/30
50000/50000 [=====] - 47s 939us/step - loss: 0.8964 - acc: 0.6853 - va
Epoch 21/30
50000/50000 [=====] - 47s 945us/step - loss: 0.8807 - acc: 0.6880 - va
Epoch 22/30
50000/50000 [=====] - 48s 952us/step - loss: 0.8668 - acc: 0.6939 - va
Epoch 23/30
50000/50000 [=====] - 48s 968us/step - loss: 0.8542 - acc: 0.6980 - va
Epoch 24/30
50000/50000 [=====] - 49s 985us/step - loss: 0.8480 - acc: 0.6998 - va
Epoch 25/30
50000/50000 [=====] - 49s 987us/step - loss: 0.8318 - acc: 0.7057 - va
Epoch 26/30
50000/50000 [=====] - 50s 991us/step - loss: 0.8253 - acc: 0.7093 - va
Epoch 27/30
50000/50000 [=====] - 50s 1ms/step - loss: 0.8285 - acc: 0.7099 - val
Epoch 28/30
50000/50000 [=====] - 50s 1ms/step - loss: 0.8405 - acc: 0.7035 - val
Epoch 29/30
50000/50000 [=====] - 50s 1ms/step - loss: 9.0416 - acc: 0.3421 - val
Epoch 30/30
50000/50000 [=====] - 50s 1ms/step - loss: 14.4970 - acc: 0.1006 - val





Training with Activation Function = sigmoid

Layer (type)	Output Shape	Param #
conv2d_5 (Conv2D)	(None, 28, 28, 6)	456
activation_11 (Activation)	(None, 28, 28, 6)	0
max_pooling2d_5 (MaxPooling2D)	(None, 14, 14, 6)	0
conv2d_6 (Conv2D)	(None, 10, 10, 16)	2416
activation_12 (Activation)	(None, 10, 10, 16)	0
max_pooling2d_6 (MaxPooling2D)	(None, 5, 5, 16)	0
flatten_3 (Flatten)	(None, 400)	0
dense_7 (Dense)	(None, 120)	48120

activation_13 (Activation)	(None, 120)	0

dense_8 (Dense)	(None, 84)	10164

activation_14 (Activation)	(None, 84)	0

dense_9 (Dense)	(None, 10)	850

activation_15 (Activation)	(None, 10)	0
=====		

Total params: 62,006

Trainable params: 62,006

Non-trainable params: 0

None

Train on 50000 samples, validate on 10000 samples

Epoch 1/30

50000/50000 [=====] - 38s 754us/step - loss: 2.3108 - acc: 0.1008 - val

Epoch 2/30

50000/50000 [=====] - 38s 758us/step - loss: 2.3034 - acc: 0.1013 - val

Epoch 3/30

50000/50000 [=====] - 38s 762us/step - loss: 2.3030 - acc: 0.1031 - val

Epoch 4/30

50000/50000 [=====] - 38s 759us/step - loss: 2.3023 - acc: 0.1050 - val

Epoch 5/30

50000/50000 [=====] - 38s 767us/step - loss: 2.3013 - acc: 0.1090 - val

Epoch 6/30

50000/50000 [=====] - 39s 776us/step - loss: 2.2997 - acc: 0.1120 - val

Epoch 7/30

50000/50000 [=====] - 45s 893us/step - loss: 2.2963 - acc: 0.1251 - val

Epoch 8/30

50000/50000 [=====] - 45s 904us/step - loss: 2.2877 - acc: 0.1507 - val

Epoch 9/30

50000/50000 [=====] - 45s 906us/step - loss: 2.2623 - acc: 0.1712 - val

Epoch 10/30

50000/50000 [=====] - 46s 917us/step - loss: 2.1963 - acc: 0.1911 - val

Epoch 11/30

50000/50000 [=====] - 46s 927us/step - loss: 2.1079 - acc: 0.2062 - val

Epoch 12/30

50000/50000 [=====] - 48s 960us/step - loss: 2.0681 - acc: 0.2132 - val

Epoch 13/30

50000/50000 [=====] - 49s 986us/step - loss: 2.0546 - acc: 0.2192 - val

Epoch 14/30

50000/50000 [=====] - 50s 996us/step - loss: 2.0454 - acc: 0.2237 - val

Epoch 15/30

50000/50000 [=====] - 50s 1ms/step - loss: 2.0365 - acc: 0.2338 - val

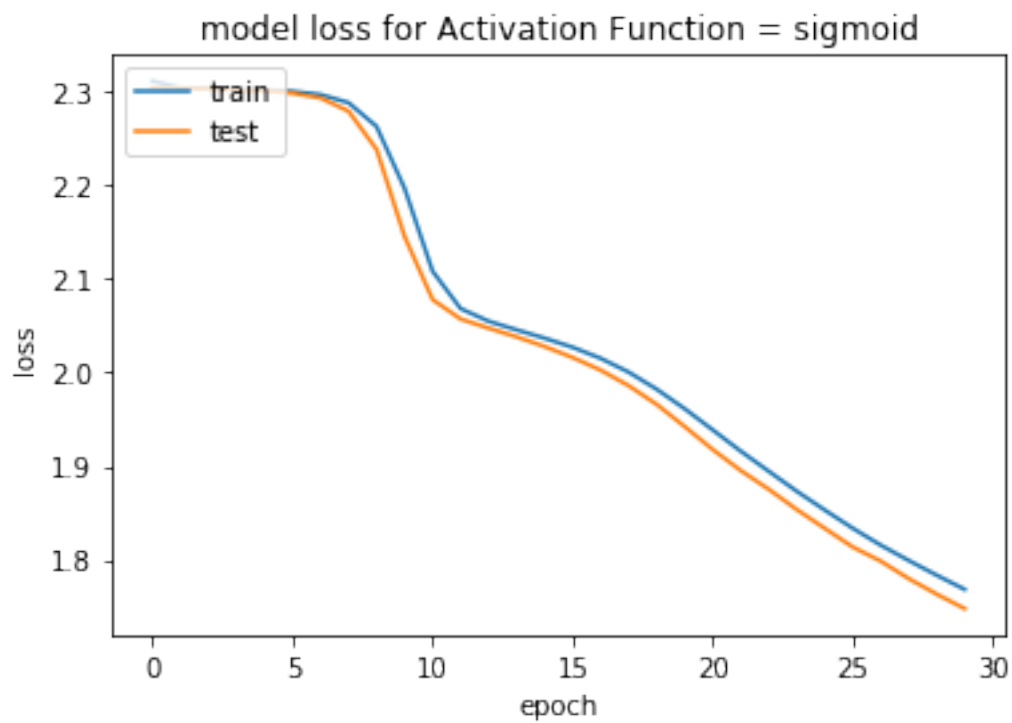
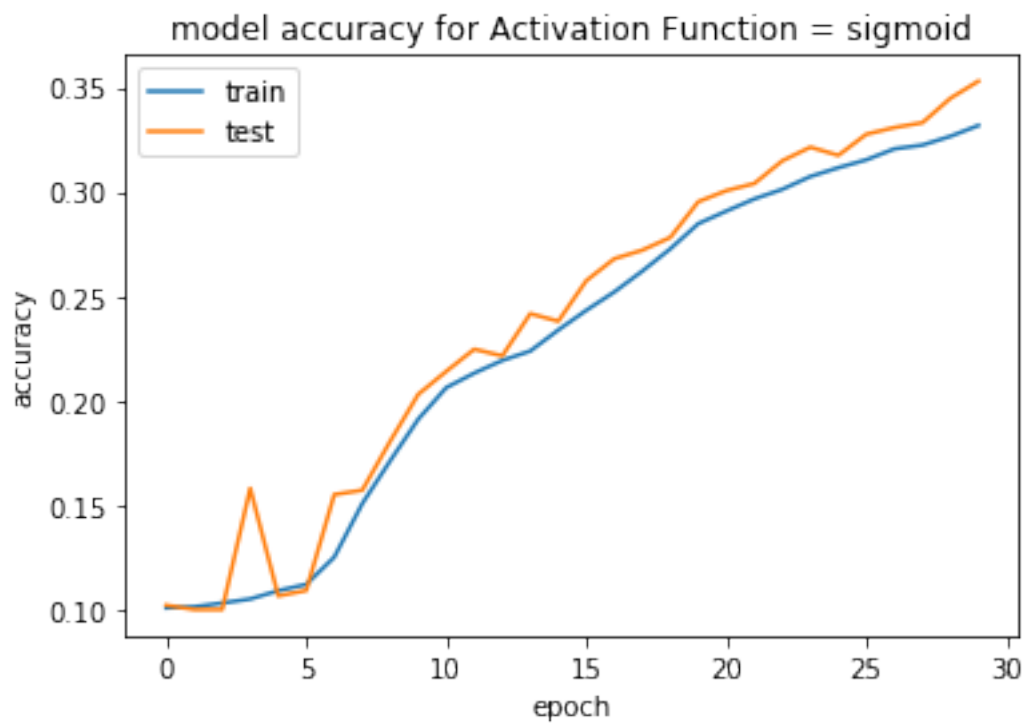
Epoch 16/30

50000/50000 [=====] - 51s 1ms/step - loss: 2.0268 - acc: 0.2432 - val

```

Epoch 17/30
50000/50000 [=====] - 51s 1ms/step - loss: 2.0150 - acc: 0.2520 - val.
Epoch 18/30
50000/50000 [=====] - 51s 1ms/step - loss: 2.0003 - acc: 0.2620 - val.
Epoch 19/30
50000/50000 [=====] - 52s 1ms/step - loss: 1.9821 - acc: 0.2726 - val.
Epoch 20/30
50000/50000 [=====] - 51s 1ms/step - loss: 1.9613 - acc: 0.2847 - val.
Epoch 21/30
50000/50000 [=====] - 51s 1ms/step - loss: 1.9387 - acc: 0.2907 - val.
Epoch 22/30
50000/50000 [=====] - 52s 1ms/step - loss: 1.9160 - acc: 0.2965 - val.
Epoch 23/30
50000/50000 [=====] - 52s 1ms/step - loss: 1.8946 - acc: 0.3011 - val.
Epoch 24/30
50000/50000 [=====] - 53s 1ms/step - loss: 1.8733 - acc: 0.3073 - val.
Epoch 25/30
50000/50000 [=====] - 53s 1ms/step - loss: 1.8532 - acc: 0.3115 - val.
Epoch 26/30
50000/50000 [=====] - 53s 1ms/step - loss: 1.8338 - acc: 0.3153 - val.
Epoch 27/30
50000/50000 [=====] - 53s 1ms/step - loss: 1.8157 - acc: 0.3205 - val.
Epoch 28/30
50000/50000 [=====] - 53s 1ms/step - loss: 1.7994 - acc: 0.3223 - val.
Epoch 29/30
50000/50000 [=====] - 53s 1ms/step - loss: 1.7836 - acc: 0.3265 - val.
Epoch 30/30
50000/50000 [=====] - 54s 1ms/step - loss: 1.7685 - acc: 0.3317 - val.

```



**** Q10: [1 points] ****

CNN training requires lot of training data. In the absence of large training data, a common practice is to use synthetic data using operations such as flipping, scaling, etc. Can you think of any other two operations techniques that can help to increase the training set? Demonstrate these effects with sufficient explanation.

**** A10: ****

To increase the training data we can use techniques like 1. Rotating the images - clockwise and anti clockwise. 2. Taking mirror images about horizontal and vertical axes (increases the training set x4 times) 3. Adding a little white noise.

Using Caffe, mirroring and random cropping are possible without changing actual DB.