

DATE:25/07/2025

EXP:03

Autonomous Vehicle Route Planning Using A* Algorithm

AIM:

Problem statement

Develop a simplified smart route planner for an autonomous vehicle navigating a city. The city map is modeled as a weighted undirected graph, where:

- Nodes represent intersections or landmarks
- Edges represent roads connecting intersections
- Weights represent travel time or traffic congestion on each road

Implement the A* search algorithm to compute the optimal (least time-cost) route from a source node to a destination node, considering road weights and using a straight-line heuristic between points.

Objective

- Model the city as a weighted graph with node coordinates.
- Apply A* to find the least-cost path between two nodes.
- Use Euclidean distance as the heuristic.
- Display the computed route, total travel cost, and number of nodes explored.

ALGORITHM:

Algorithm: A* Search

Input:

- Start node start
- Goal node goal
- A heuristic function $h(n)$ that estimates cost from node n to the goal
- Step-cost function $g(n)$ (actual cost so far from start to node n)

Output:

- Optimal path from start to goal (if one exists)

Procedure

1. Initialize an open list (priority queue) and add start with:
 - $g(\text{start}) = 0$
 - $f(\text{start}) = g(\text{start}) + h(\text{start})$
2. Initialize a closed set (visited nodes) as empty.
3. While open list is not empty:
 - a. Remove the node n from open list with the lowest $f(n)$.
 - b. If n is the goal node, return the path from start to goal.
 - c. Add n to the closed set.
 - d. For each successor s of n :
 - Compute $g(s) = g(n) + \text{cost}(n, s)$
 - Compute $f(s) = g(s) + h(s)$
 - If s is already in closed set with a lower $f(s)$, skip it.
 - If s is not in open list (or has better $f(s)$ than before), insert/update it in open list.
4. If open list becomes empty and goal not found \rightarrow Failure (no solution).

CODE:

```
#A*

import heapq

import math

# Coordinates for intersections

coordinates = {

    'A': (0, 0),

    'B': (2, 2),
```

```

'C': (2, 0),
'D': (4, 2),
'E': (5, 0),
'F': (6, 2)
}

# Weighted undirected graph (travel time or congestion)

graph = {
    'A': [('B', 3), ('C', 1)],
    'B': [('A', 3), ('D', 3)],
    'C': [('A', 1), ('D', 4), ('E', 2)],
    'D': [('B', 3), ('C', 4), ('F', 1)],
    'E': [('C', 2), ('F', 5)],
    'F': [('D', 1), ('E', 5)]
}

start = 'A'

goal = 'F'

def heuristic(node1, node2):
    x1, y1 = coordinates[node1]
    x2, y2 = coordinates[node2]
    return math.sqrt((x2 - x1) ** 2 + (y2 - y1) ** 2)

def a_star_verbose(graph, start, goal):
    open_set = []
    heapq.heappush(open_set, (heuristic(start, goal), 0, start, [start]))

```

```

visited = set()

nodes_expanded = 0

step_count = 1

while open_set:

    f, g, current, path = heapq.heappop(open_set)

    if current in visited:

        continue

    visited.add(current)

    nodes_expanded += 1

    # Step-by-step debug output

    print(f"\n Step {step_count}: Visiting Node '{current}'")

    print(f"  g(n) = {g:.2f} (Cost from start)")

    h = heuristic(current, goal)

    print(f"  h(n) = {h:.2f} (Heuristic to goal)")

    print(f"  f(n) = g + h = {g:.2f} + {h:.2f} = {f:.2f}")

    print(f"  Path so far: {' → '.join(path)}")

    # Show current queue status

    print("  📦 Queue Contents:")

    for est, cost, node, p in open_set:

        print(f"    {node}: f={est:.2f}, g={cost}, path={' → '.join(p)}")

    step_count += 1

    if current == goal:

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        print(f'\n Goal '{goal}' reached!')

    return path, g, nodes_expanded

for neighbor, weight in graph[current]:

    if neighbor not in visited:

        g_new = g + weight

        f_new = g_new + heuristic(neighbor, goal)

        heapq.heappush(open_set, (f_new, g_new, neighbor, path + [neighbor]))

return None, float('inf'), nodes_expanded

# Run the A* search with explanation

final_path, total_cost, explored = a_star_verbose(graph, start, goal)

# Final result

print("\n=====")

if final_path:

    print(" Path Found:", " → ".join(final_path))

    print(" Total Travel Time:", total_cost)

    print(" Nodes Expanded:", explored)

else:

    print(" No path found.")

```

OUTPUT:

```
Step 1: Visiting Node 'A'
g(n) = 0.00 (Cost from start)
h(n) = 6.32 (Heuristic to goal)
f(n) = g + h = 0.00 + 6.32 = 6.32
Path so far: A
📁 Queue Contents:

Step 2: Visiting Node 'C'
g(n) = 1.00 (Cost from start)
h(n) = 4.47 (Heuristic to goal)
f(n) = g + h = 1.00 + 4.47 = 5.47
Path so far: A → C
📁 Queue Contents:
  B: f=7.00, g=3, path=A → B

Step 3: Visiting Node 'E'
g(n) = 3.00 (Cost from start)
h(n) = 2.24 (Heuristic to goal)
f(n) = g + h = 3.00 + 2.24 = 5.24
Path so far: A → C → E
📁 Queue Contents:
  B: f=7.00, g=3, path=A → B
  D: f=7.00, g=5, path=A → C → D

Step 4: Visiting Node 'B'
g(n) = 3.00 (Cost from start)
h(n) = 4.00 (Heuristic to goal)
f(n) = g + h = 3.00 + 4.00 = 7.00
Path so far: A → B
📁 Queue Contents:
  D: f=7.00, g=5, path=A → C → D
  F: f=8.00, g=8, path=A → C → E → F
```

```
Step 5: Visiting Node 'D'
g(n) = 5.00 (Cost from start)
h(n) = 2.00 (Heuristic to goal)
f(n) = g + h = 5.00 + 2.00 = 7.00
Path so far: A → C → D
📁 Queue Contents:
  D: f=8.00, g=6, path=A → B → D
  F: f=8.00, g=8, path=A → C → E → F

Step 6: Visiting Node 'F'
g(n) = 6.00 (Cost from start)
h(n) = 0.00 (Heuristic to goal)
f(n) = g + h = 6.00 + 0.00 = 6.00
Path so far: A → C → D → F
📁 Queue Contents:
  D: f=8.00, g=6, path=A → B → D
  F: f=8.00, g=8, path=A → C → E → F

Goal 'F' reached!

=====
Path Found: A → C → D → F
Total Travel Time: 6
Nodes Expanded: 6
```

RESULT:

The programs have been completed and the outputs have been verified.