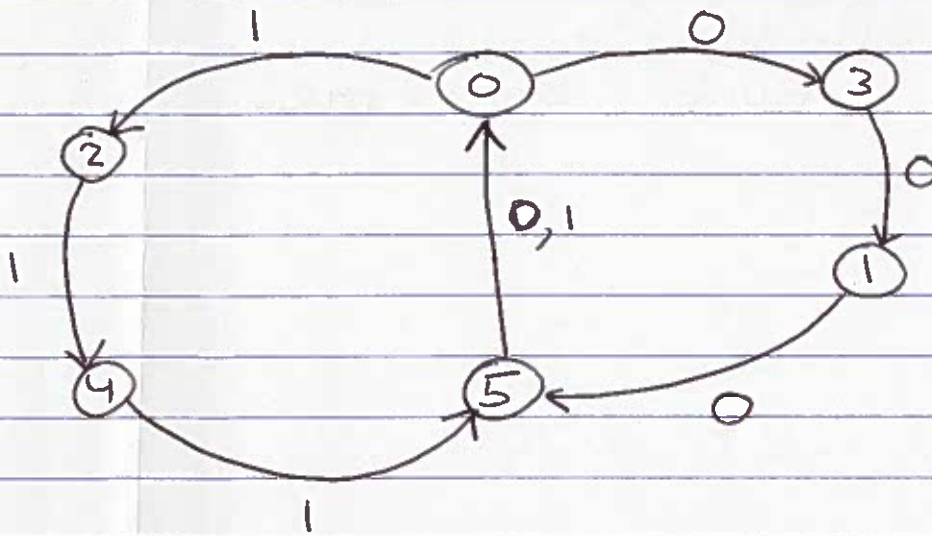


1 a)



b)

| input        | TS           | Q2           | Q1           | Q0           | NS           | D2           | D1           | DO           |
|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| 0            | 0            | 0            | 0            | 0            | 3            | 0            | 1            | 1            |
| 0            | 1            | 0            | 0            | 1            | 5            | 1            | 0            | 1            |
| 0            | 2            | 0            | 1            | 0            | X            | x            | x            | x            |
| 0            | 3            | 0            | 1            | 1            | 1            | 0            | 0            | 1            |
| 0            | 4            | 1            | 0            | 0            | X            | x            | x            | x            |
| 0            | 5            | 1            | 0            | 1            | 0            | 0            | 0            | 0            |
| 0            | X            | x            | x            | x            | x            | x            | x            | x            |
| 0            | X            | x            | x            | x            | x            | x            | x            | x            |
| 1            | 0            | 0            | 0            | 0            | 2            | 0            | 1            | 0            |
| 1            | 1            | 0            | 0            | 1            | X            | x            | x            | x            |
| 1            | 2            | 0            | 1            | 0            | 4            | 1            | 0            | 0            |
| 1            | 3            | 0            | 1            | 1            | X            | x            | x            | x            |
| 1            | 5            |              |              |              |              |              |              |              |
| <del>1</del> | <del>X</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> |
| <del>1</del> | <del>X</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> | <del>x</del> |
| 1            | 4            | 1            | 0            | 0            | 5            | 1            | 0            | 1            |
| 1            | 5            | 1            | 0            | 1            | 0            | 0            | 0            | 0            |
| 1            | x            | x            | x            | x            | x            | x            | x            | x            |
| 1            | x            | x            | x            | x            | x            | x            | x            | x            |

c)

D0:

|     |    | Q1 Q0 |    |    |    |
|-----|----|-------|----|----|----|
|     |    | 00    | 01 | 11 | 10 |
| IQ2 | 00 | 1     | 1  | 1  | x  |
|     | 01 | x     | 0  | x  | x  |
|     | 11 | 1     | 0  | x  | x  |
|     | 10 | 0     | x  | x  | 0  |

$$(I' \cdot Q2') + (Q1' \cdot Q0' \cdot Q2)$$

D1:

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 0  | 0  | X  |
| 01 | X  | 0  | X  | X  |
| 11 | 0  | 0  | X  | X  |
| 10 | 1  | X  | X  | 0  |

$$(Q1' \cdot Q0' \cdot Q2')$$

D2:

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 0  | 1  | 0  | x  |
| 01 | x  | 0  | x  | x  |
| 11 | 1  | 0  | x  | x  |
| 10 | 0  | x  | x  | 1  |

$$(Q1 \cdot Q0') + (Q0' \cdot Q2) + (Q2' \cdot Q1' \cdot Q0)$$



d)

| I | Q <sub>2</sub> | Q <sub>1</sub> | Q <sub>0</sub> | D <sub>2</sub> | D <sub>1</sub> | D <sub>0</sub> | Next State |
|---|----------------|----------------|----------------|----------------|----------------|----------------|------------|
| 0 | 0              | 1              | 0              | 1              | 0              | 1              | 5          |
| 0 | 1              | 0              | 0              | 1              | 0              | 1              | 5          |
| 0 | 1              | 1              | 1              | 0              | 0              | 0              | 0          |
| 0 | 1              | 1              | 0              | 1              | 0              | 0              | 4          |
| 1 | 1              | 1              | 1              | 0              | 0              | 0              | 0          |
| 1 | 1              | 1              | 0              | 1              | 0              | 0              | 4          |
| 1 | 0              | 0              | 1              | 1              | 0              | 0              | 4          |
| 1 | 0              | 1              | 1              | 0              | 0              | 0              | 0          |

Does not cause any issues.

e) States are assigned such that number is in binary. LSB indicates whether odd or even

$$Q_1 = D_0$$

$$Q_2 = D_0'$$

2a)

~~b<sub>3</sub>b<sub>2</sub>~~ b<sub>1</sub>b<sub>0</sub>

|                                       | 00 | 01 | 11 | 10           |
|---------------------------------------|----|----|----|--------------|
| <del>b<sub>3</sub>b<sub>2</sub></del> | 00 | 0  | 0  | 0            |
| b <sub>3</sub> b <sub>2</sub>         | 01 | 0  | 0  | 0            |
|                                       | 11 | 1  | 1  | <del>1</del> |
|                                       | 10 | 0  | 0  | <del>1</del> |

$$(b_3 \cdot b_2) + (b_3 \cdot b_1)$$

$$= b_3 \cdot (b_1 + b_2)$$

b) Any results between 10 & 15 inclusive the binary carry is different from the BCD carry.



c)  $4 + 9 = 13$

$$\begin{array}{r} 0100 \\ 1001 + \\ \hline 1101 \end{array} \quad \text{in binary}$$

0001      0011      in BCD

$3 + 8 = 11$

$$\begin{array}{r} 0011 \\ 1000 + \\ \hline 1011 \end{array} \quad \text{in binary}$$

0001      0001      in BCD

$3 + 9 = 12$

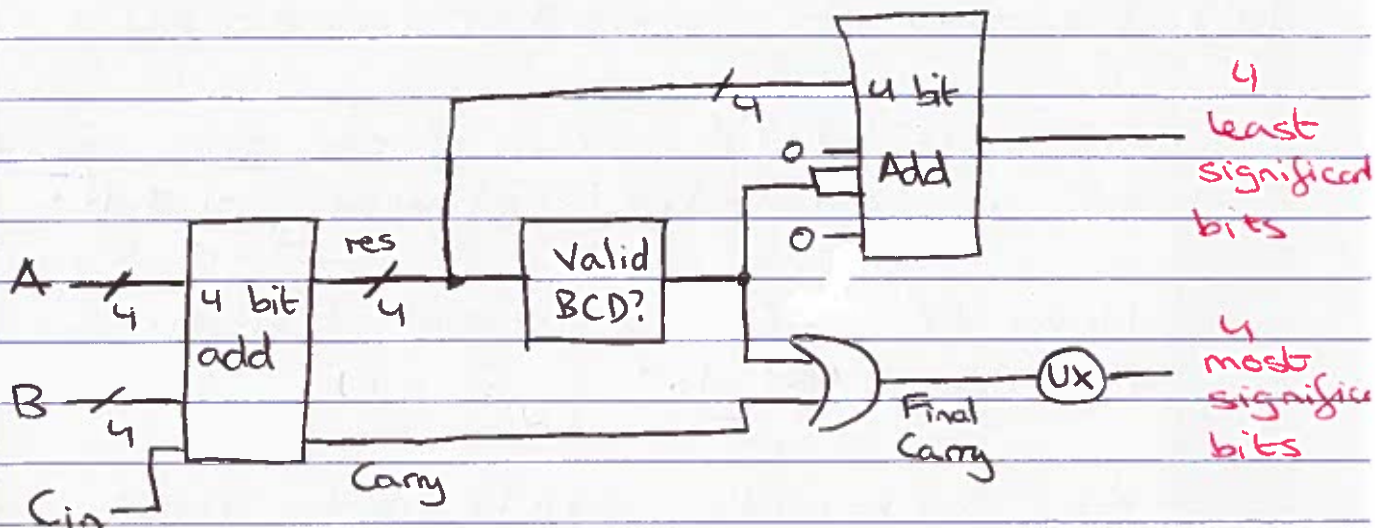
$$\begin{array}{r} 0011 \\ 1001 + \\ \hline 1100 \end{array} \quad \text{in binary}$$

0001      0010      in BCD

Add 0110 to the result if ~~carry~~ is not a valid BCD



d)



e)

