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The graph of a relation might not satisfy the vertical line test.

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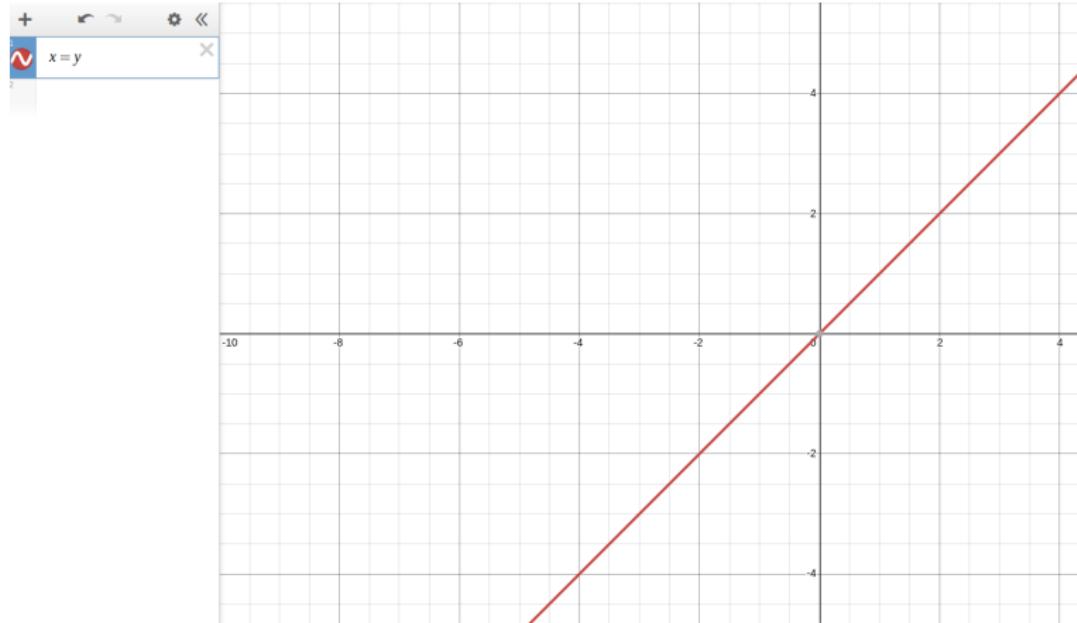
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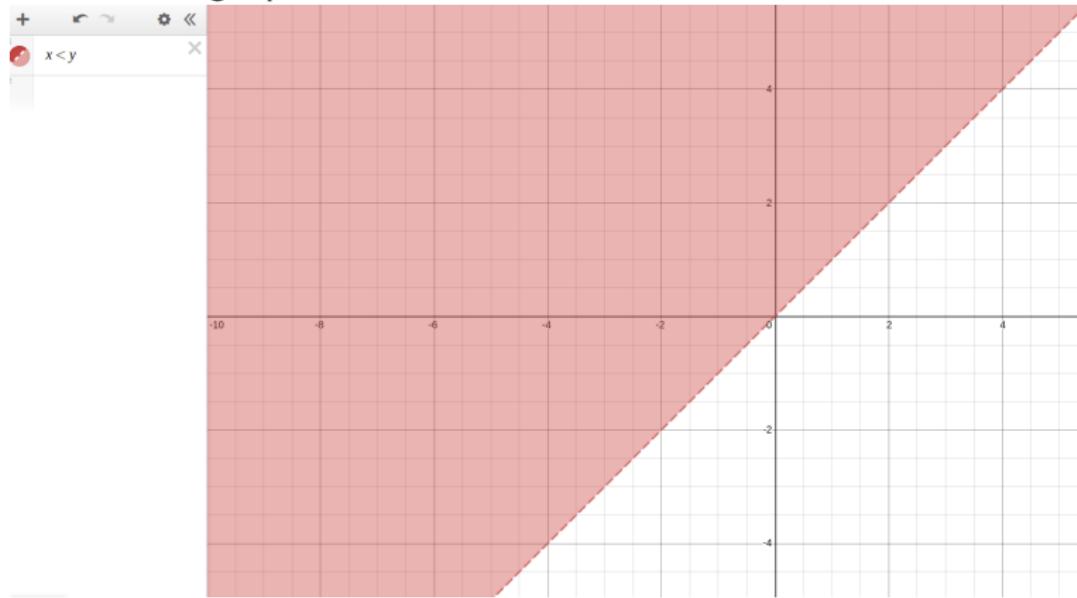
Here’s another question. “Draw the graph of $\sin(x)$ ”. What is the associated predicate?

$<$ and $=$ are binary relations on \mathbb{R} , and hence predicates on \mathbb{R}^2 . Can you draw their graphs?

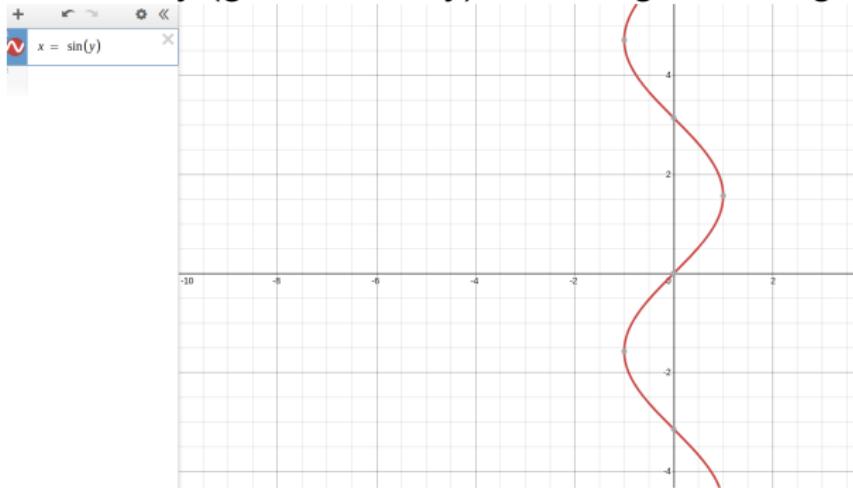
Here's the graph of $=$:



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Last thing: If a function isn't bijective, it doesn't have a two-sided inverse. But you can take the "inverse" of a binary relation by (geometrically) reflecting it in the graph of id_X .



Algebraically, given the predicate $P(x, y)$, we can create the "transpose" predicate $P(y, x)$.