

Notes From Sorting Algorithms:-

- ① Insertion sort / selection sort - $\mathcal{O}(n^2)$ → Concept
- ② Quick sort / Merge sort

Insertion Sort

Steps: Move left to right

- ① if you are at index i , if $A[i] < A[i-1]$ swap.
- ② keep moving down till everything from left is always sorted.
- ③ move to next column.

Code:-

for $i: 1$ to $\text{length}(A)-1$:

$j=1$

while $j > 0$ and $A[j-1] > A[j]$

swap ($A[j]$, $A[j-1]$)

$j=j-1$

Example:-

soot

1 3 5 2 6 4

$A[i]=1$:- All sorted \rightarrow 1 3 5 2 6 4

$A[i]=3$:- $3 > 2$, all sorted \Rightarrow 1 3 5 2 6 4

$A[i]=5$: $5 > 3$, all sorted \Rightarrow 1 3 5 2 6 4

$A[i]=2$:

$2 < 5$ swap 1 3 2 5 6 4

$2 < 3$ swap 1 2 3 5 6 4

$2 > 1 \rightarrow$ OK

$A[i]=6$, $6 > 5$, all ok \rightarrow 1 2 3 5 6 4

$A[i]=4$,

$4 < 6$ swap 1 2 3 5 4 6

$4 < 5$ swap 1 2 3 4 5 6

$4 > 3 \rightarrow$ OK

Sorted Array : 1 2 3 4 5 6

② Selection Sort :-

Idea:- Find minimum \rightarrow put to left side
 - continue,

for $j = 0, j < n - 1, j++$,
 int $iMin = j$;
 for ($i = j + 1, i < n, i++$)
 if $a[i] < a[iMin]$
 $iMin = i$.

if ($iMin \neq j$)
 swap ($a[j], a[iMin]$)

For example \rightarrow Go To Next page

1 3 5 2 6 4
↑
*

Step 1 Find min starting @ 1 _____, replace with 1

New array : 1 3 5 2 6 4

Step 2 Find min starts @ 1 3 5 2 6 4

New array = 1 2 5 3 6 4

Step 3 Find minimum starts @ 1 2 5 3 6 4

New array = 1 2 3 5 6 4

Step 4 Find minimum starts @ 1 2 3 5 6 4

New array : 1 2 3 4 5 6

Step 5 Find min starts @ 1 2 3 4 5 6

New Array : 1 2 3 4 5 6

Step 6 : Repeat for final :-

Ans 1, 2, 3, 4, 5, 6

Quicksort :-

3 1 5 2 6 4

Correct! 1 2 3 4 5 6

No Element in its correct position

Qs: Can we get 1 element in its correct position?

eg : 3 1 5 2 6 4 → ~~Want this in correct posn~~

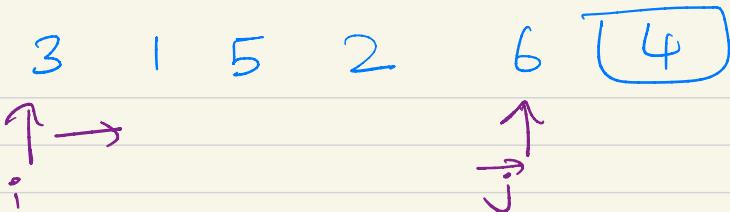
How can I arrange this array so that 4 is in correct position?

3 1 5 2 6 4

Goal



How to do this? \Rightarrow Partition Function



① Move $i \rightarrow, j \leftarrow$

② If $A[i] < 4$, move right

If $A[j] > 4$, move left.

③ Whenever you have $A[i] > 4$ and $A[j] < 4$, swap the 2 places.

④ Keep doing this -

Eg : 3 1 5 2 6 4

i → ← j next

3 1 5 2 6 4 i → j next

3 1 5 2 6 4

i j $A[i] > 4, A[j] < 4$, so swap

3 1 2 5 6 4
i i

Done since $j < i$, now put 4 in mid

3	1	2	4	5	6
---	---	---	---	---	---

\therefore trds array has been partitioned
on the element $\boxed{4}$, $\therefore 4$ is in correct
position.

(partition the array based on the last element)

Partition (Arr, low, high) {

 pivot = Arr[high]

 i = low - 1

 j = high - 1

 while $j > i$:-

 while $Arr[i] \leq pivot$:
 $i++$;

 while $Arr[j] \geq pivot$:

$j--$;

 if $i < j$:

 swap($Arr[i]$, $Arr[j]$)

}

$Arr[high] = Arr[i]$

$Arr[i] = pivot$

 return $i, Arr[:i], Arr[j:]$

This function, can now place the Rightmost element into the correct location.

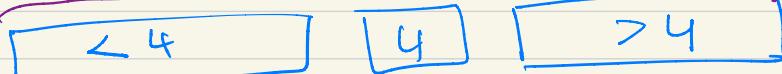
Now can we use this to sort ?

If we know an array has a pivot in correct

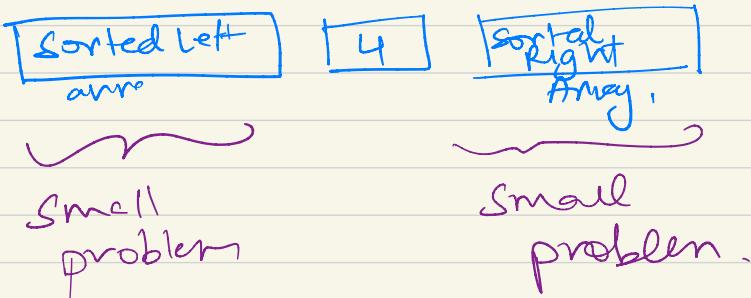
position:

Big Problem

Arr:



Sorted Array :



Quicksort [Arr] :- {

pivot, left Array, Right Array = Partition (Arr)

sorted Left Array = Quicksort [left Arr]

sorted Right Array = Quicksort [Right Array]

return [sorted left Array, pivot, sorted Right Array]

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Look @ uploaded code!

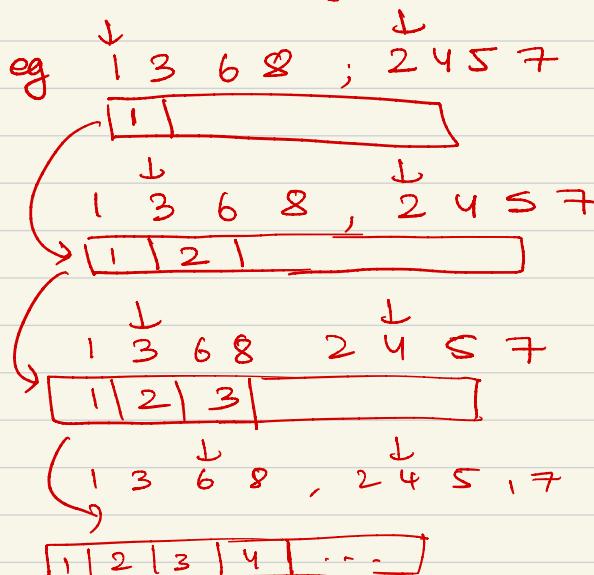
Merge Sort :-

Qs: Can you sort an array which looks like this :

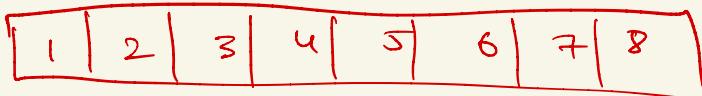
1 3 6 8 2 4 5 7
 Sorted Sorted
 Left Right
Array Array

Easy? 

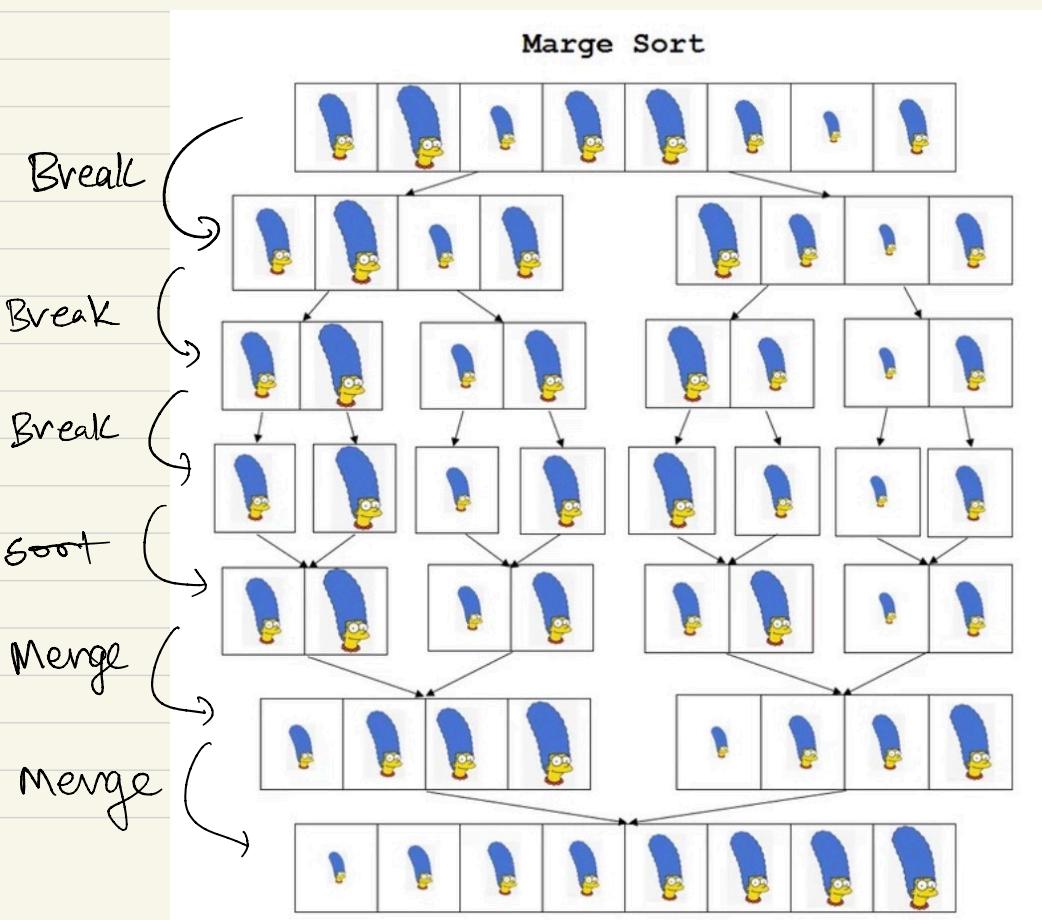
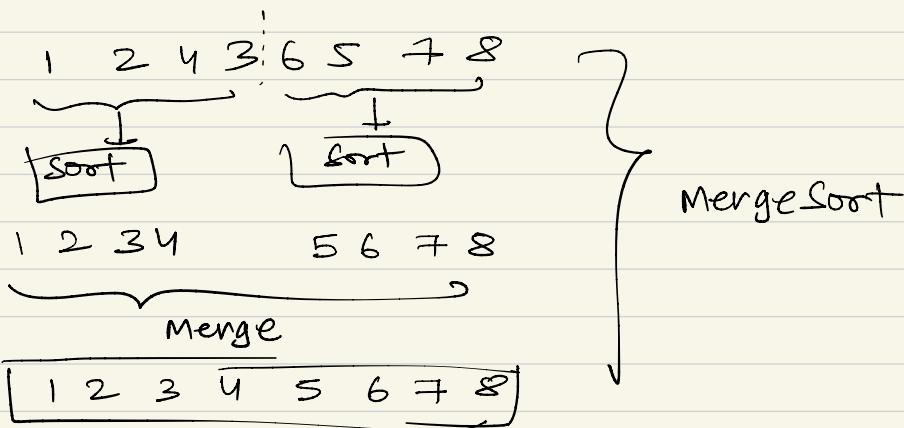
Go left to right on both arrays, add to this empty array whichever is smaller.



so on till you get

 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8

Mergin 2 sorted arr is easy → this is GREAT



Code :-

- ① Define Merge function.
- ② Define

MergeSort [Arr] :

 Array 1 = Arr [0 : len(Arr)]₂

 Array 2 = Arr [$\frac{\text{len}(A)}{2}$ + 1 :]

 return merge (MergeSort(Array1),

 MergeSort(Array2))

Look @ code